



An Introduction to Deep Learning on Meshes

SIGGRAPH COURSE 2021

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Real world success of deep learning

Reverse image search



Alibaba Pailitao

Facial recognition



Facebook Photo Tags

Speech recognition / Language processing



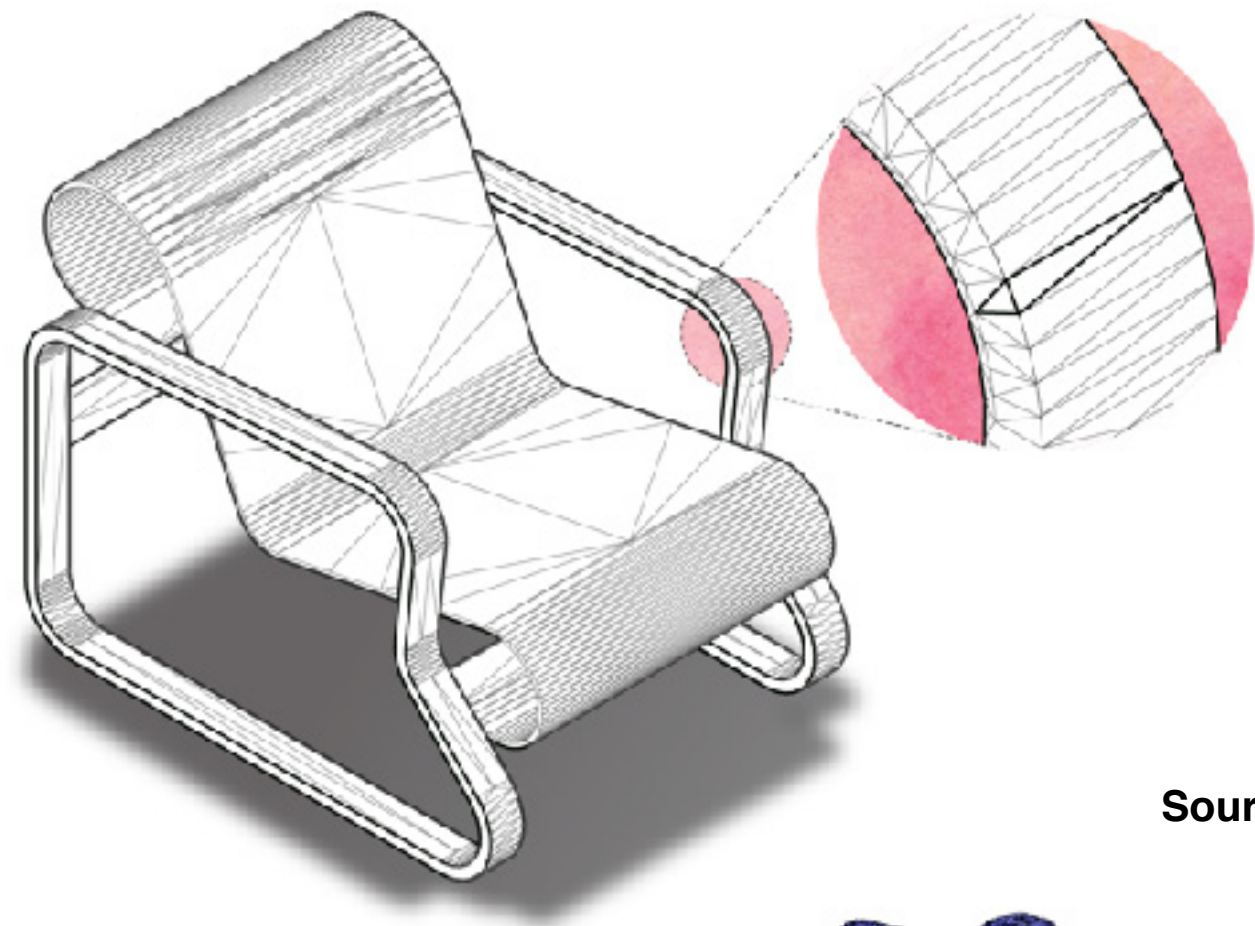
Apple Siri

machine translation

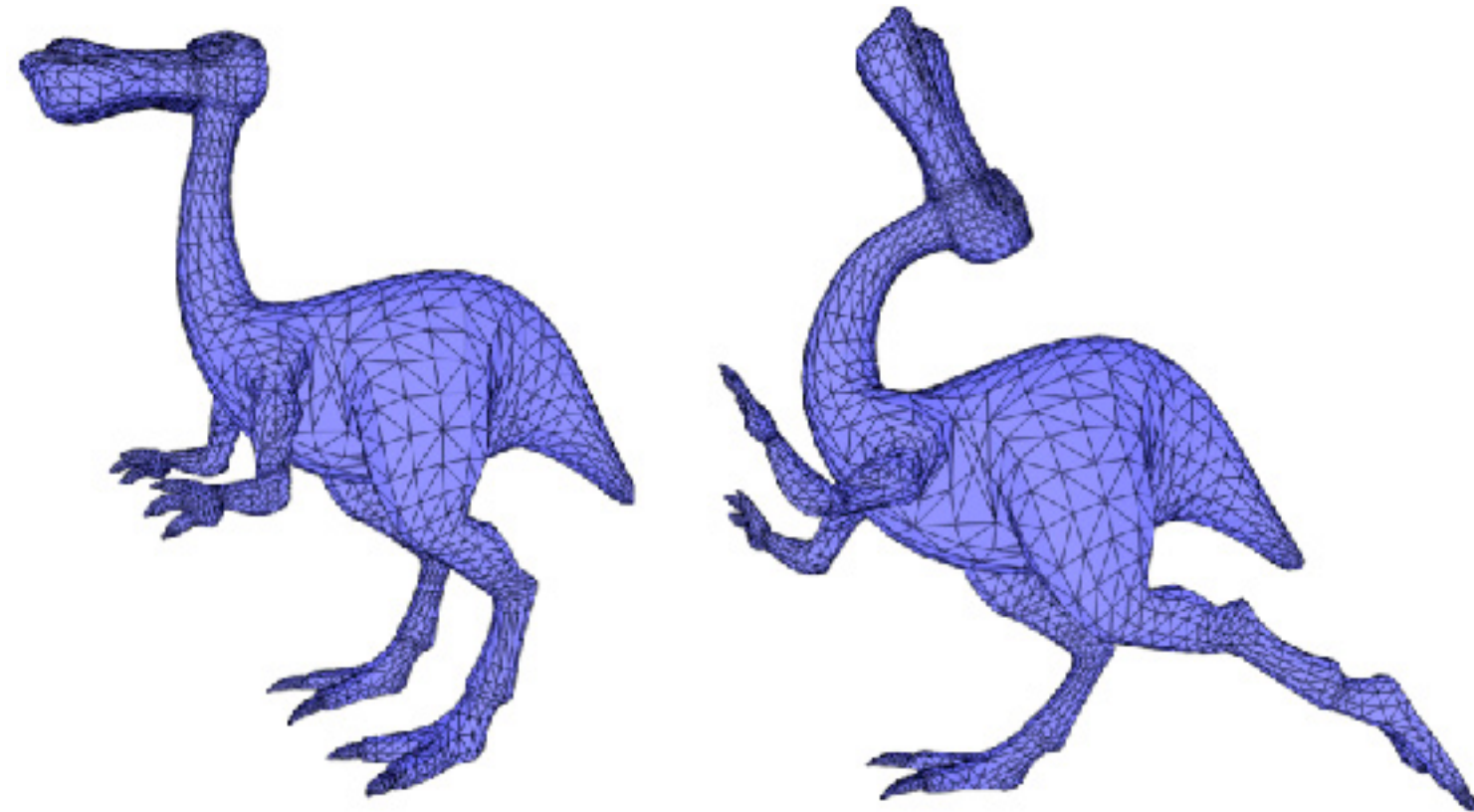


Google translate

Meshes are popular in computer graphics



Source: Sorkine & Alexa 2007



Source: Sawhney & Crane 2017



Source: Li et. al 2020



fast to render

adaptive

efficient to texture

intuitively deformable

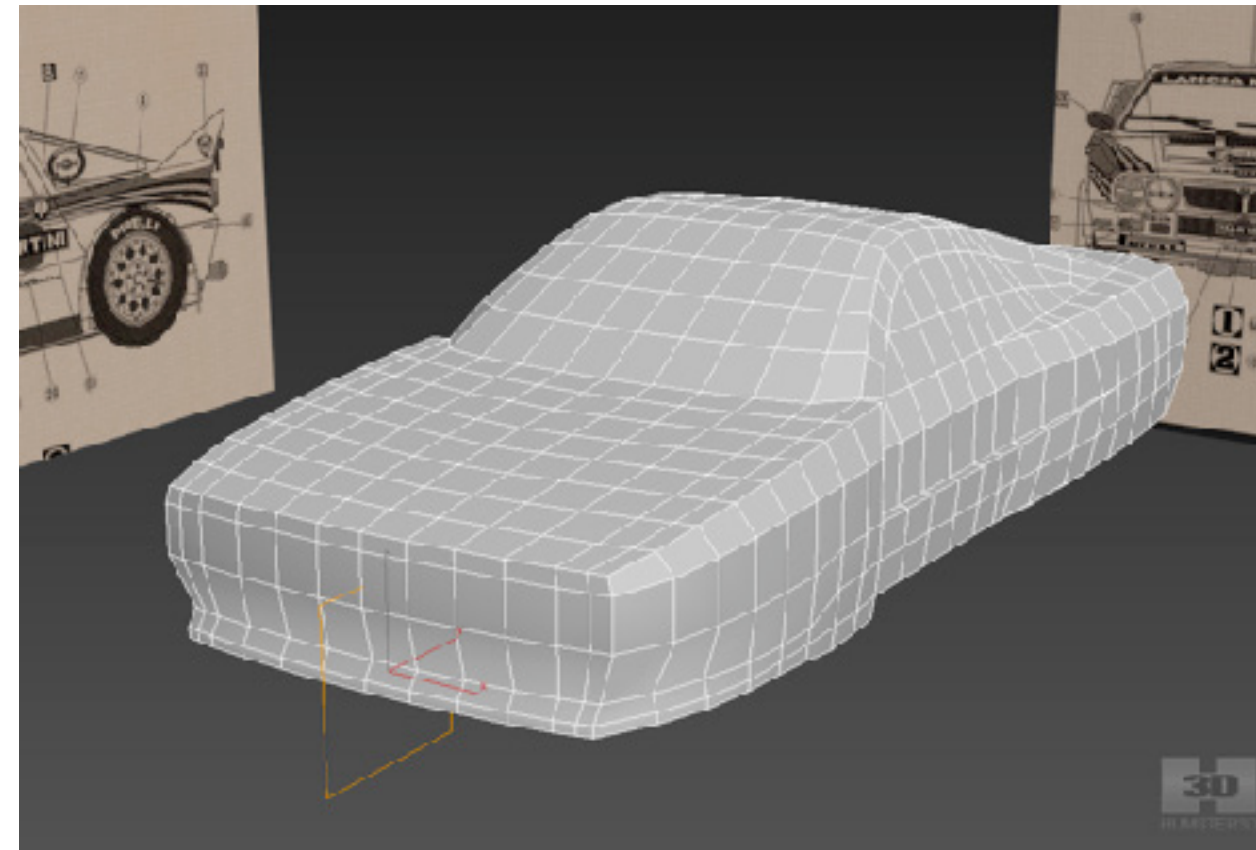
physics simulation

Combining the power of deep learning & meshes

for many applications in geometry processing



Modeling



Editing



Reconstruction



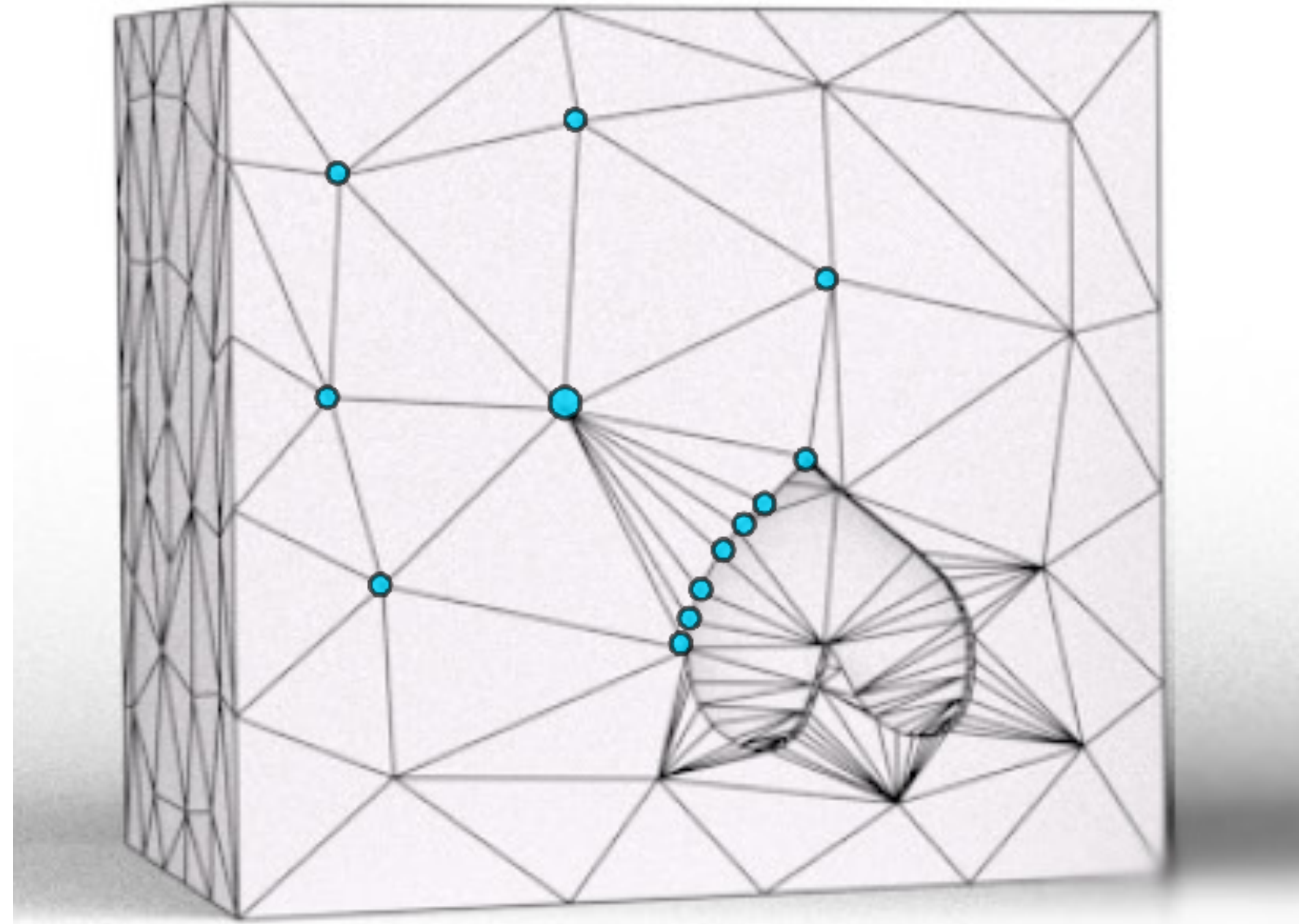
Shape Analysis

Challenges for deep learning on meshes

Representation

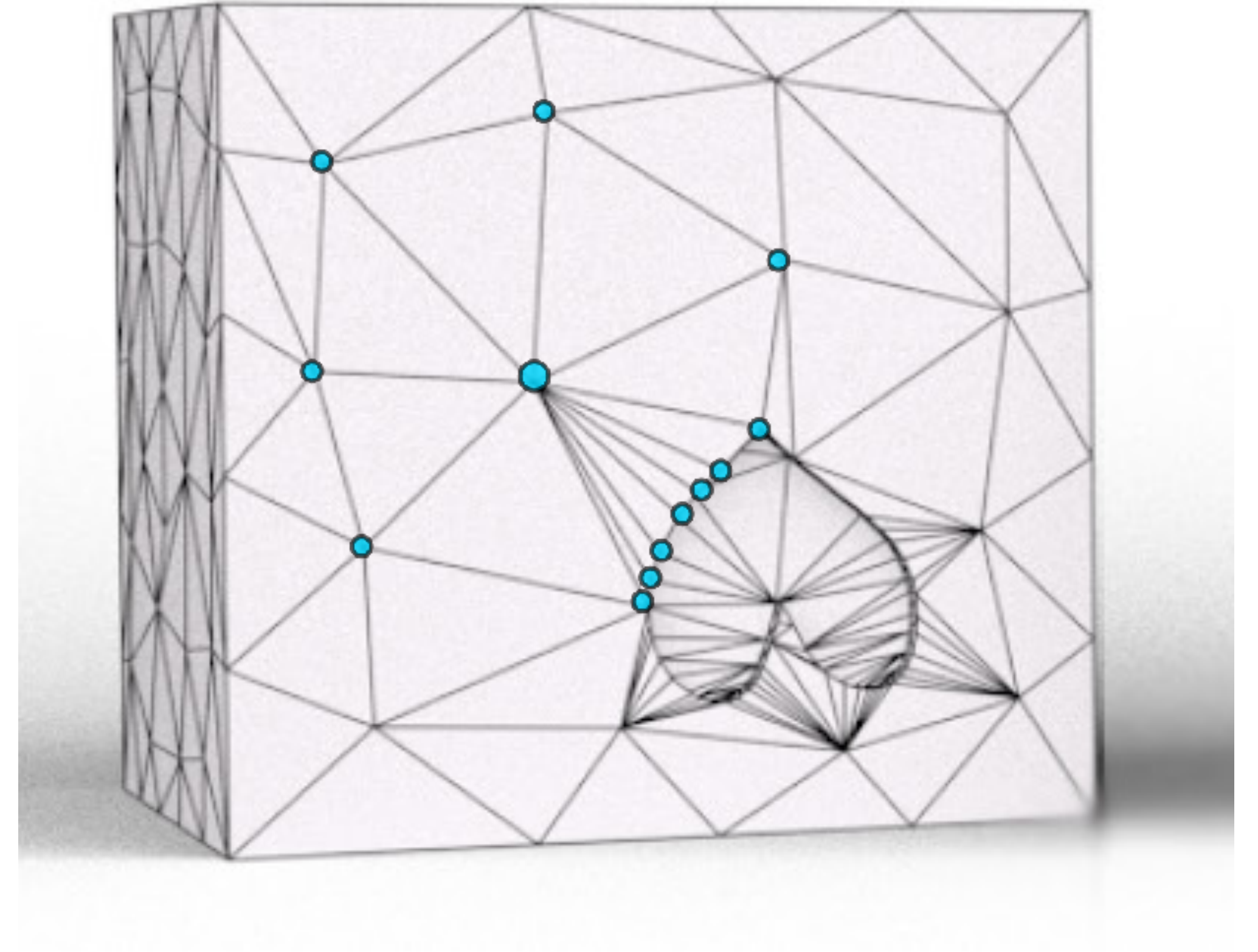
Data Accessibility

Irregular

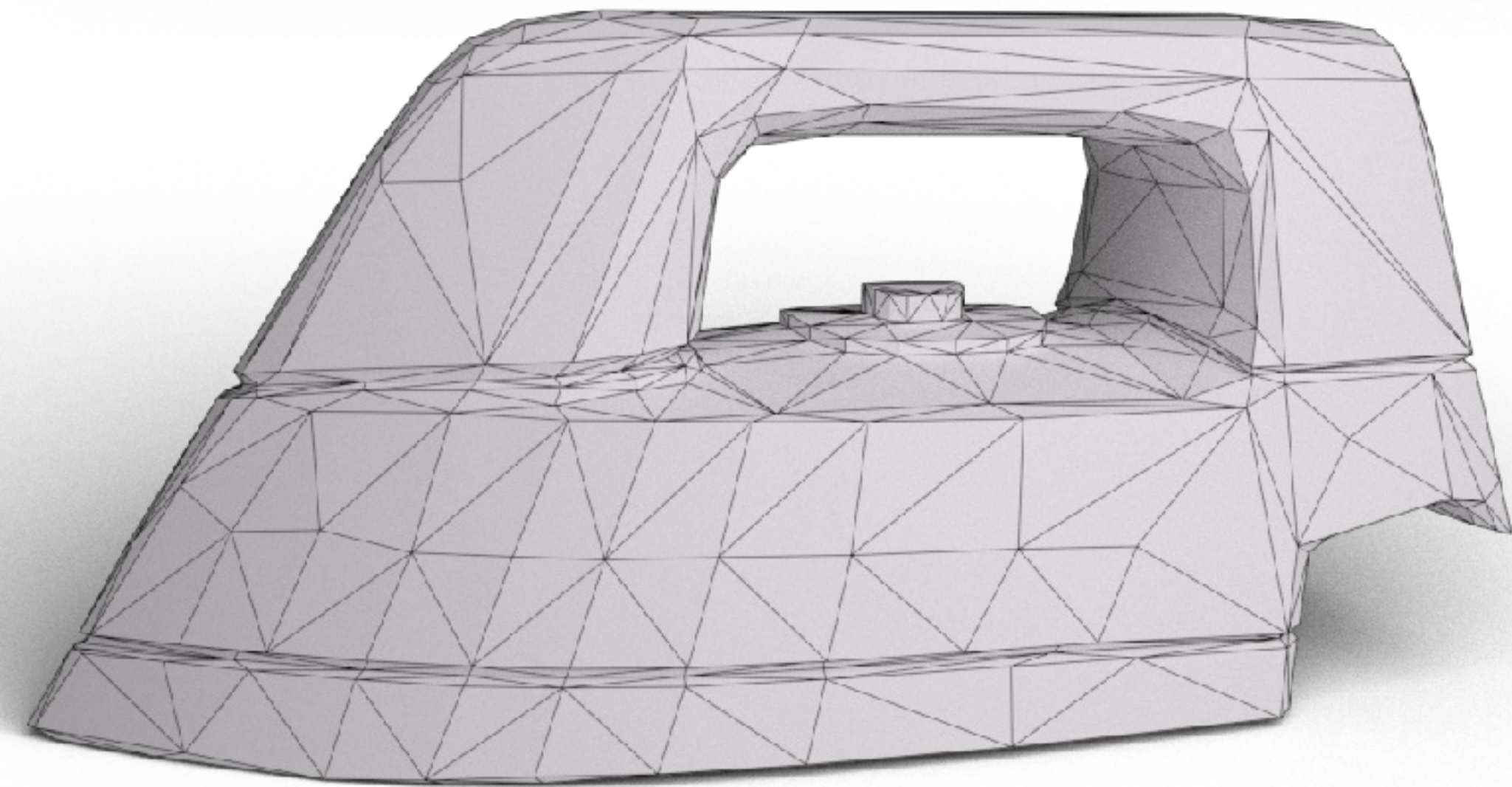
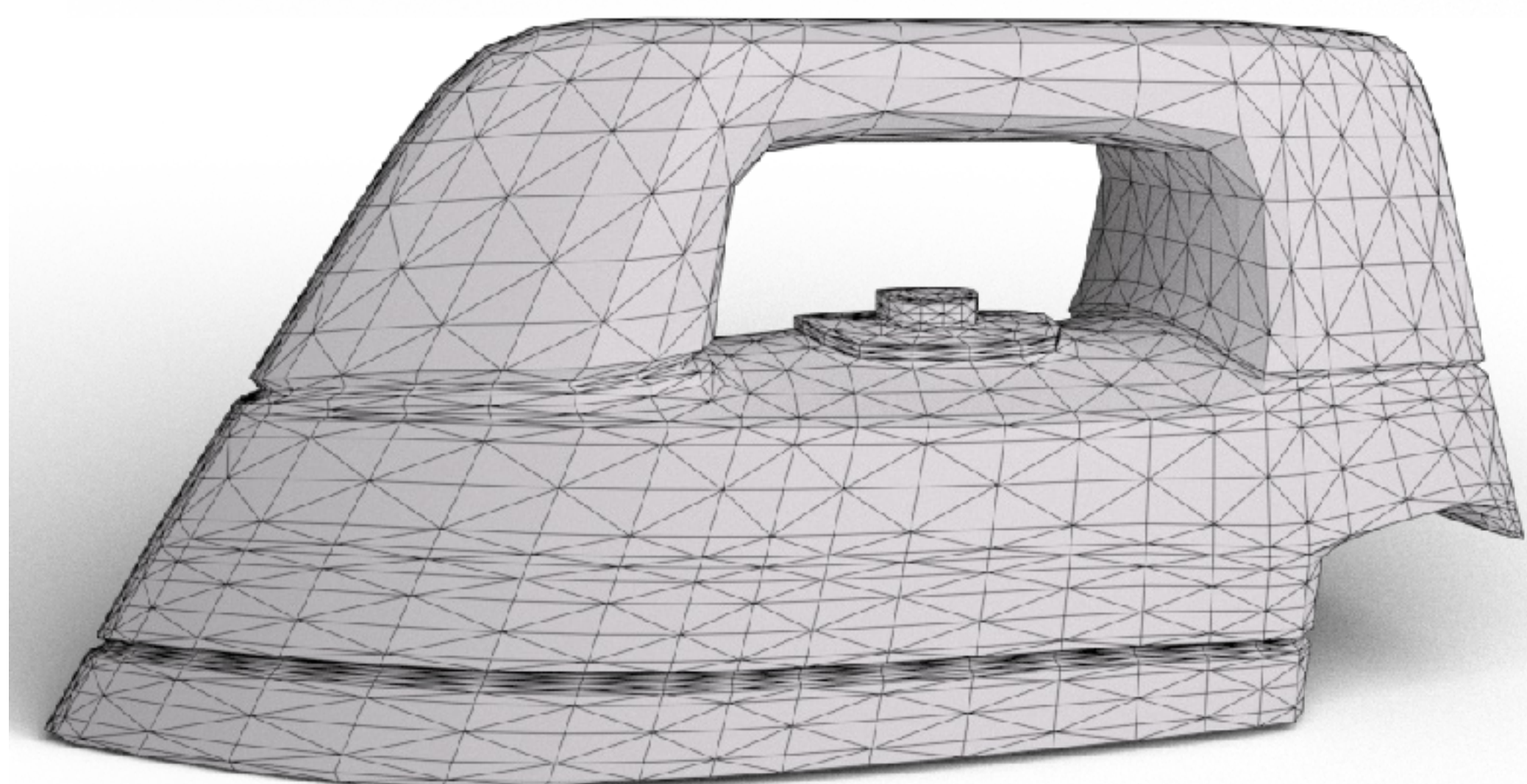
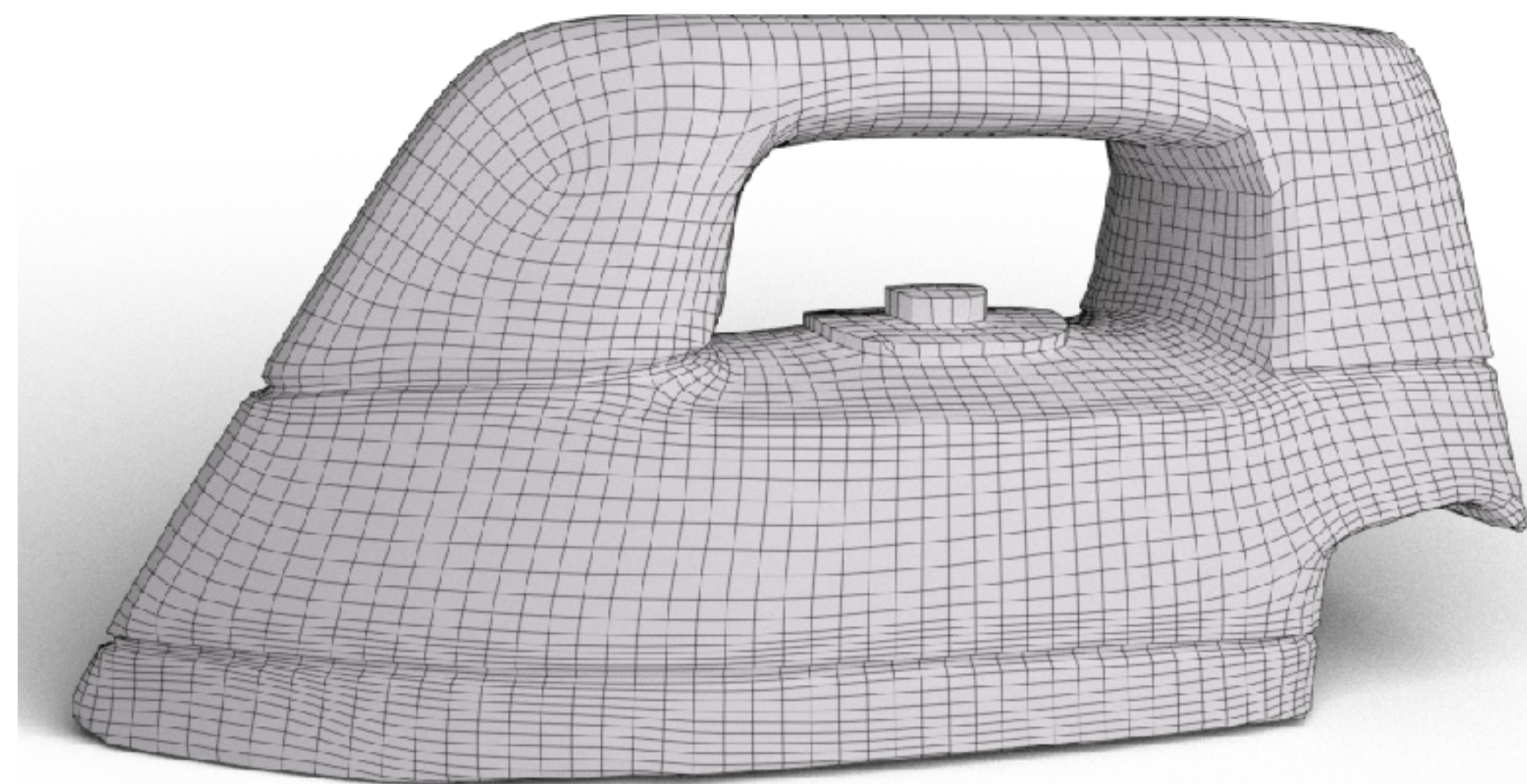
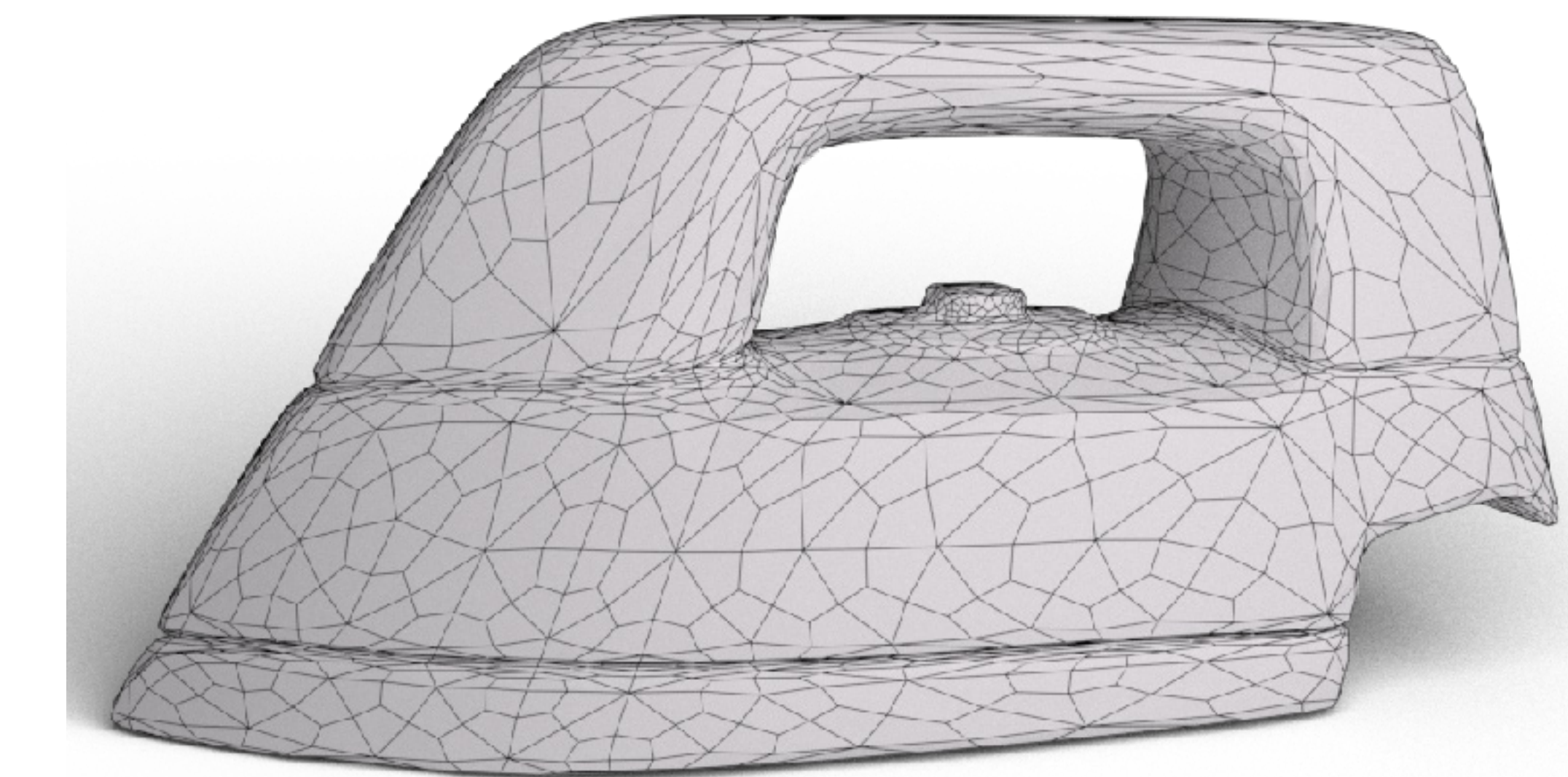


Unordered

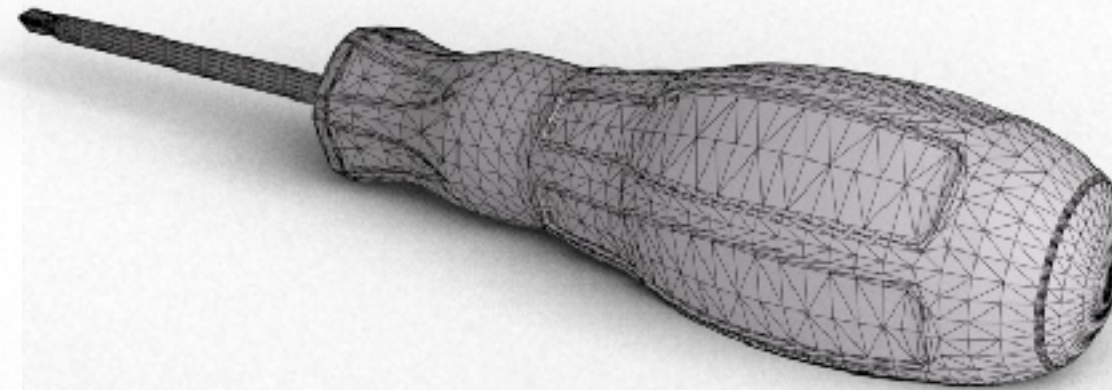
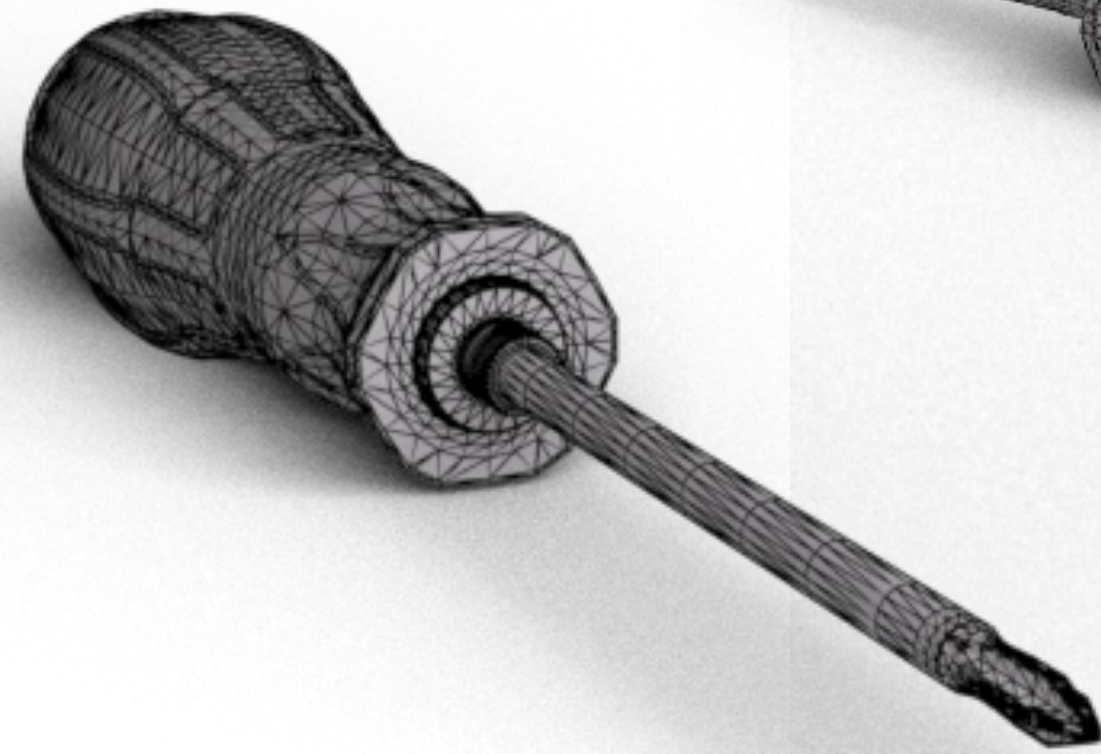
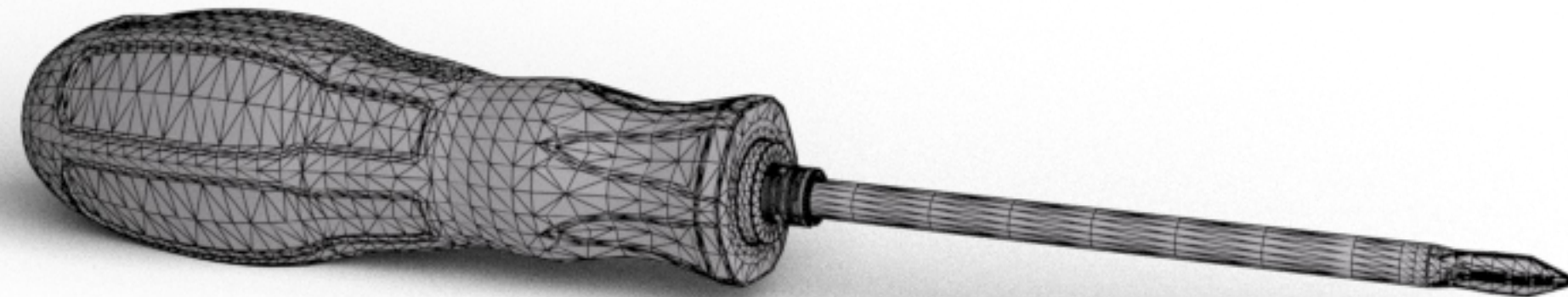
<x, y, z>
<1.2, 3.1, -0.7>
<1.2, 3.4, -0.8>
<1.5, 3.4, -0.6>
<1.5, 3.1, -0.7>
<1.5, 3.7, -0.7>
<1.7, 3.4, -0.7>



Inconsistent



Unoriented

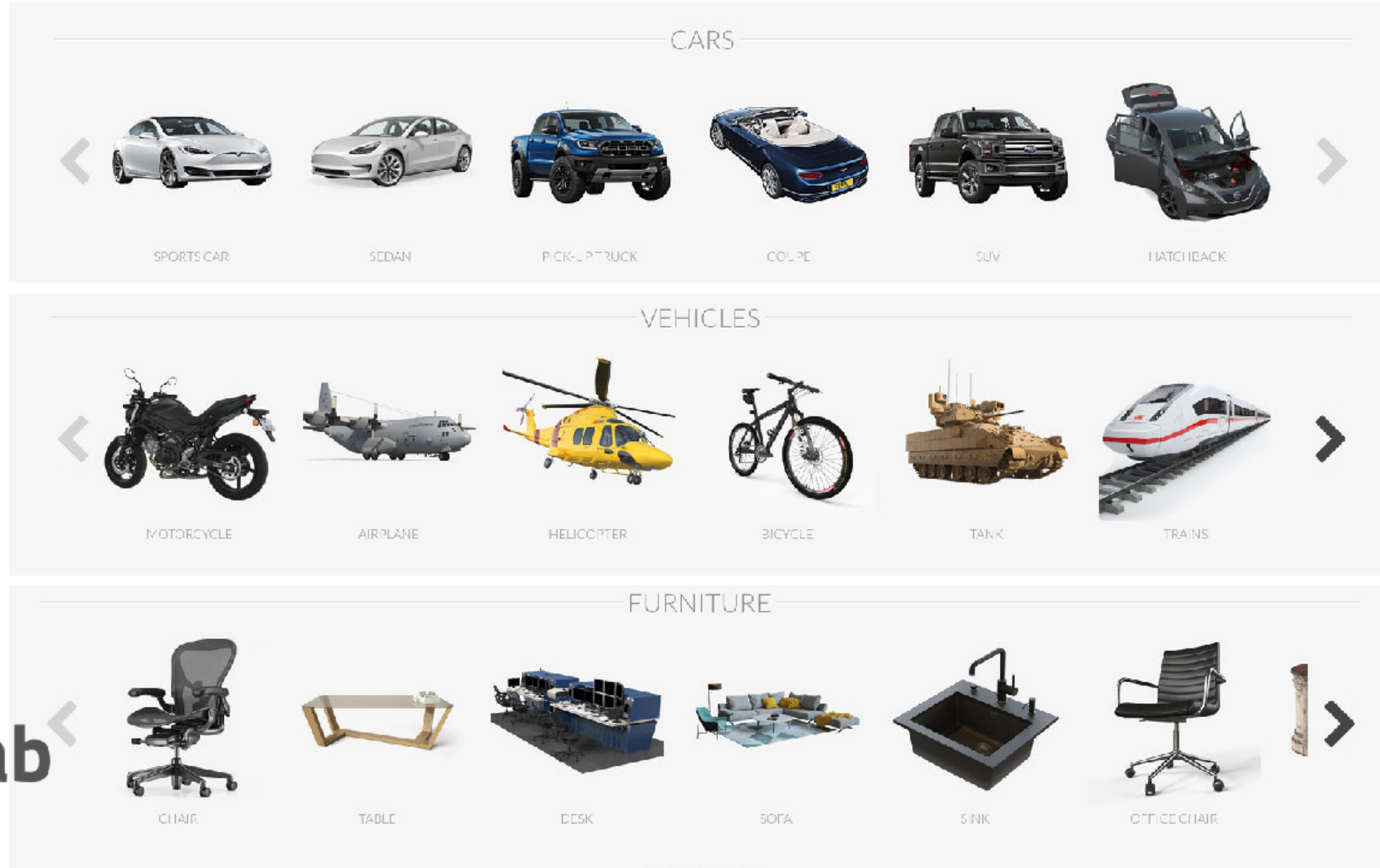
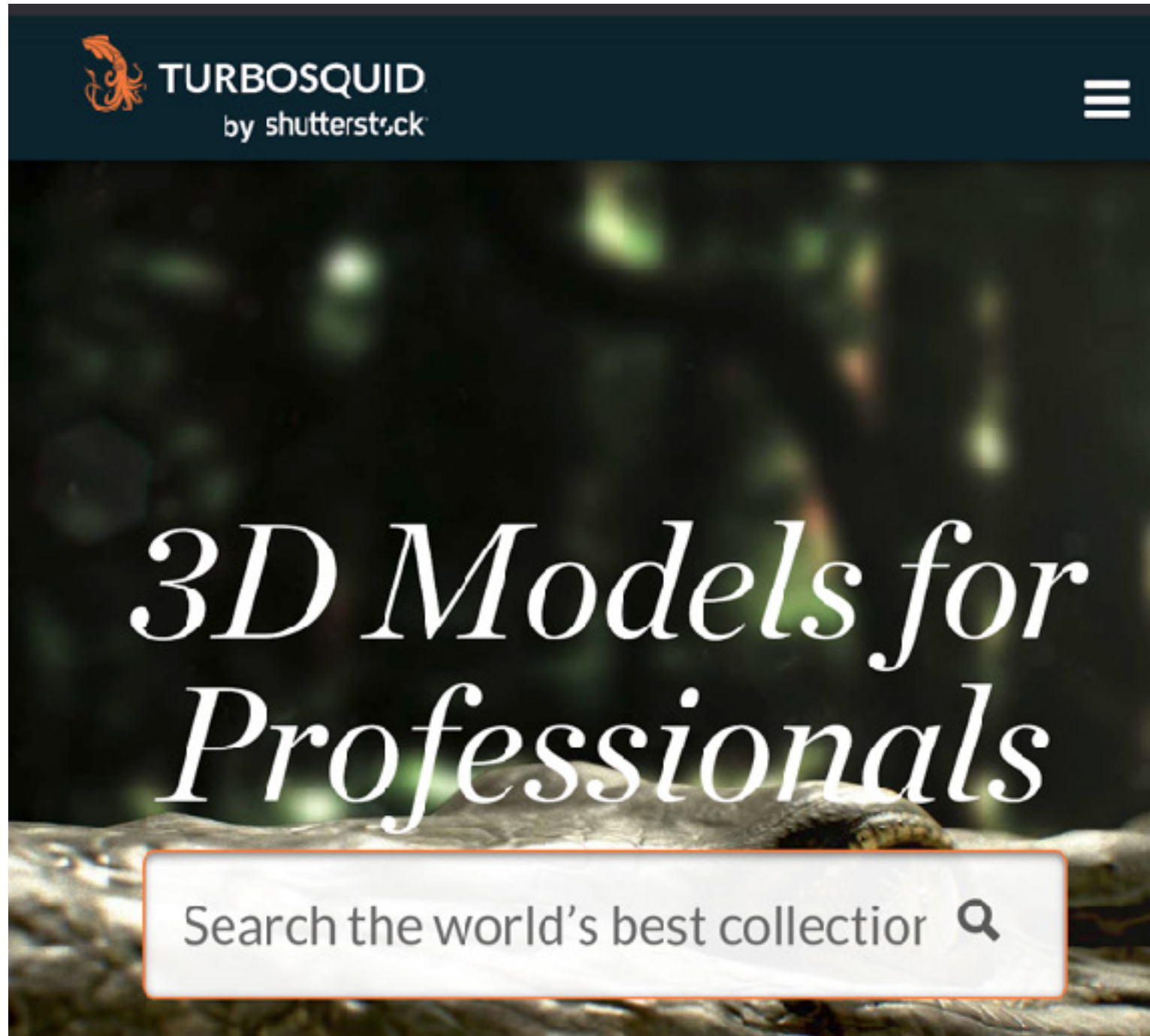


Challenges for deep learning on meshes

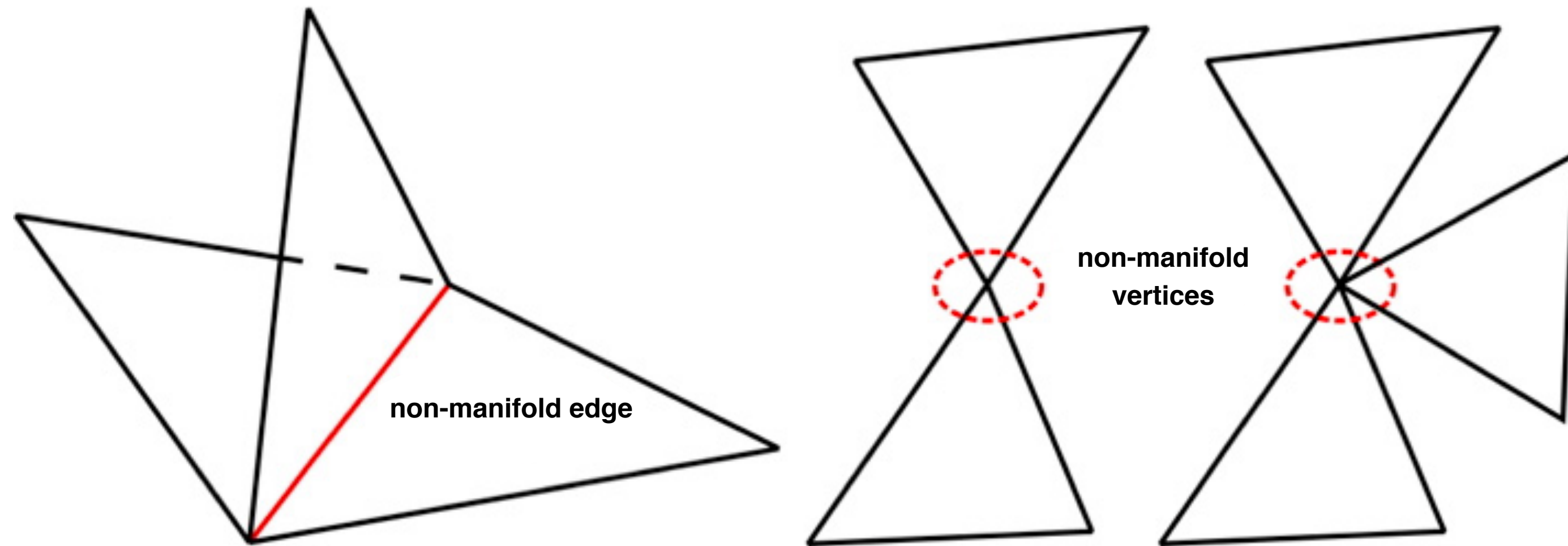
Representation

Data Accessibility

Large Warehouses of 3D Mesh Data

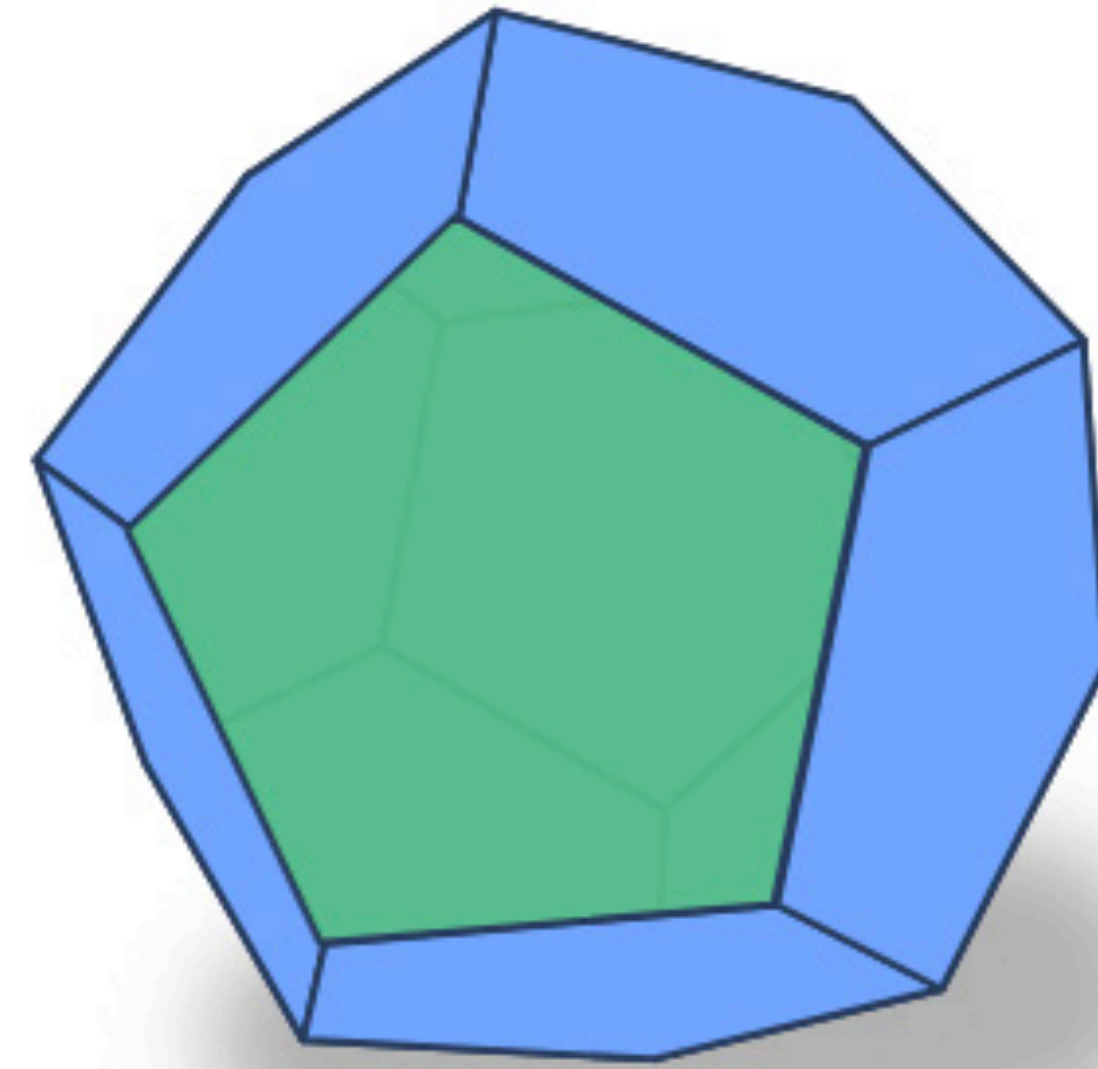
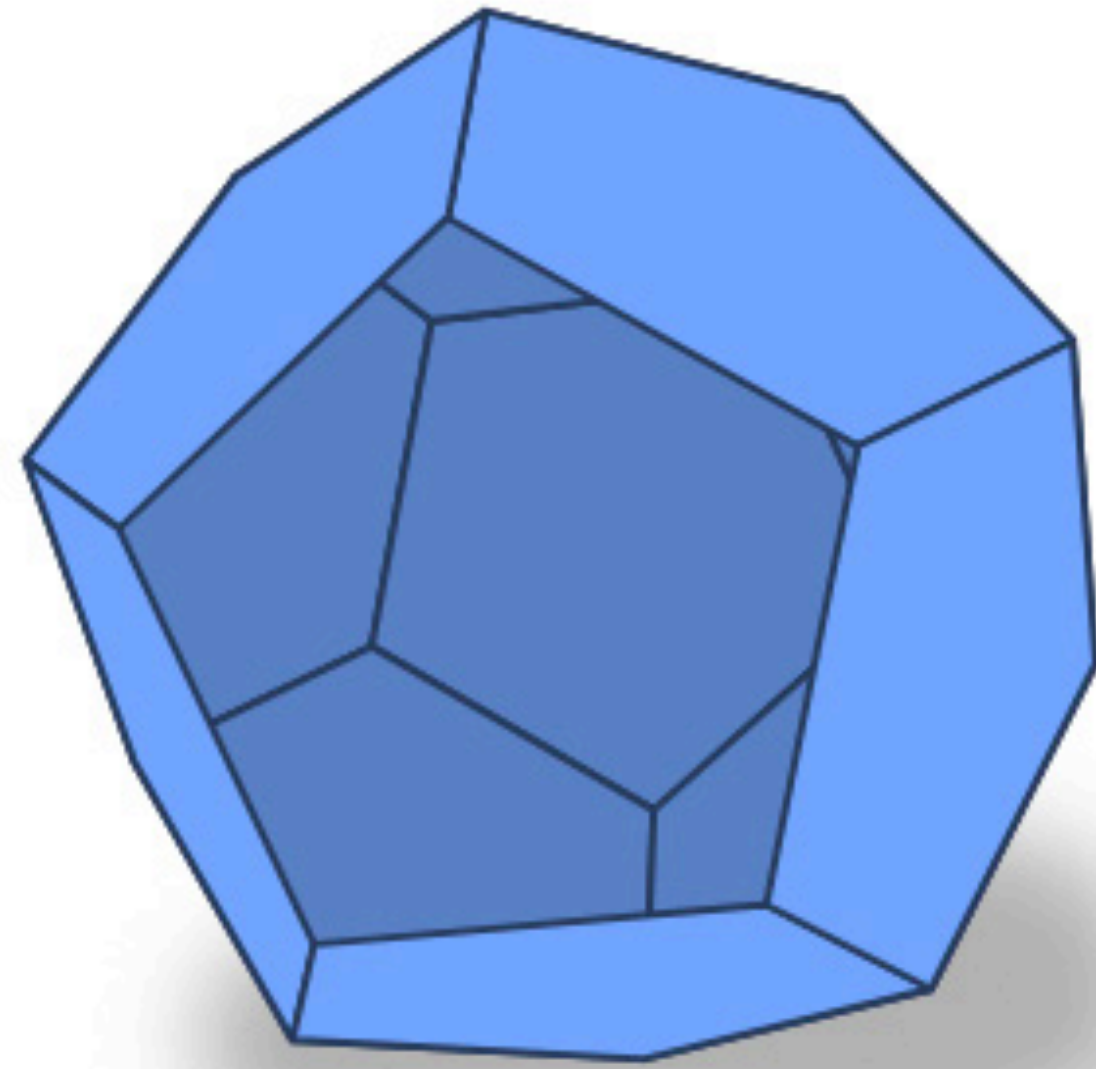


High bar for geometric computation



non-manifold

High bar for geometric computation

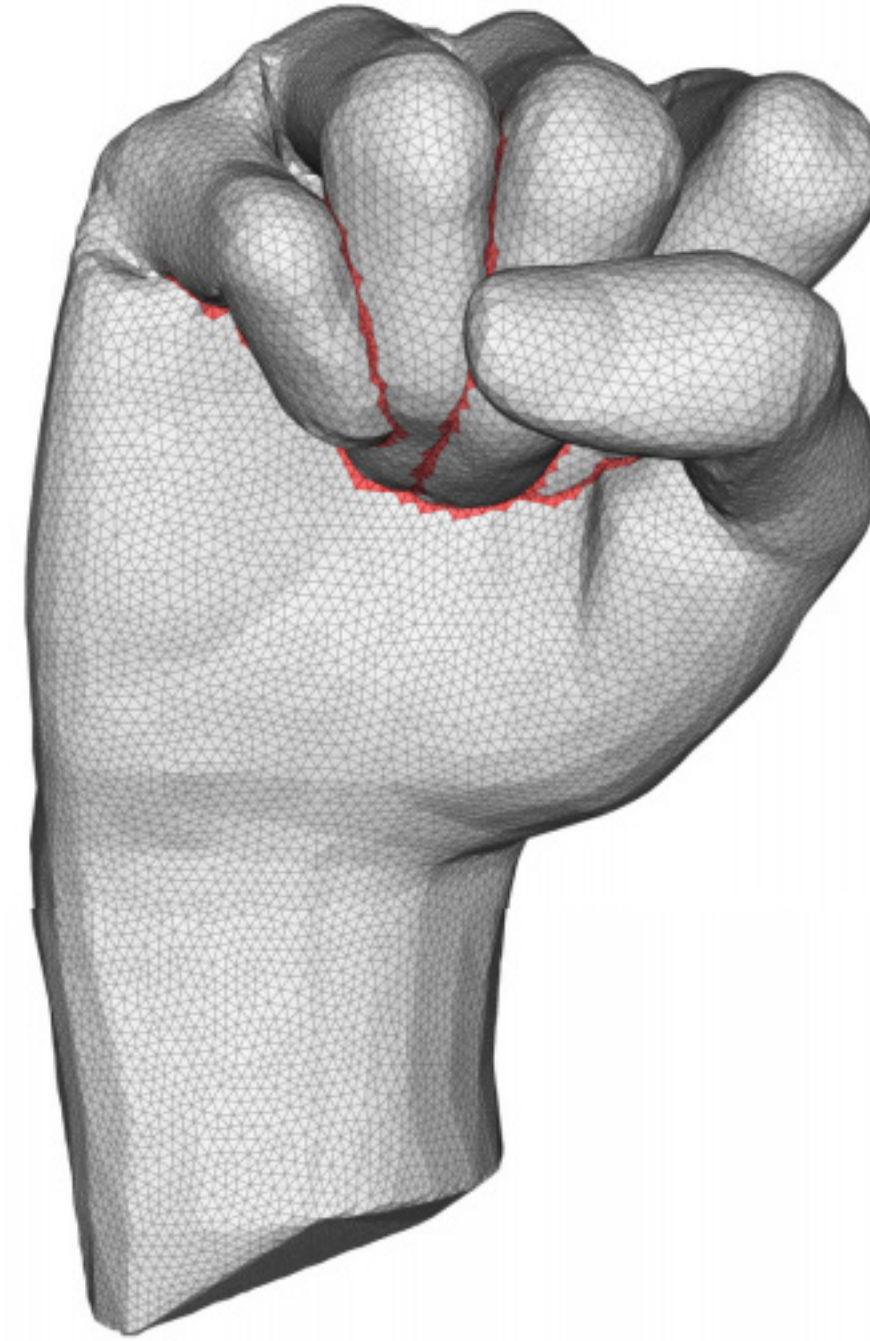


Source: geometry central

non-manifold

not watertight

High bar for geometric computation



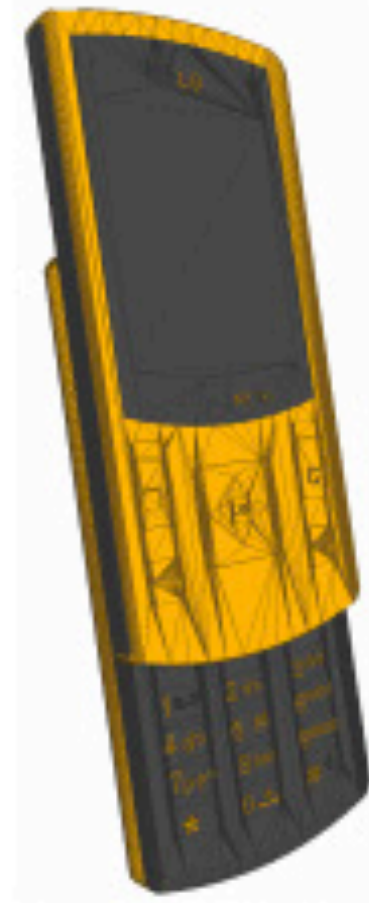
Source: Sacht et. al 2013

non-manifold

not watertight

intersections

High bar for geometric computation



Source: Takayama et. al 2014

non-manifold

not watertight

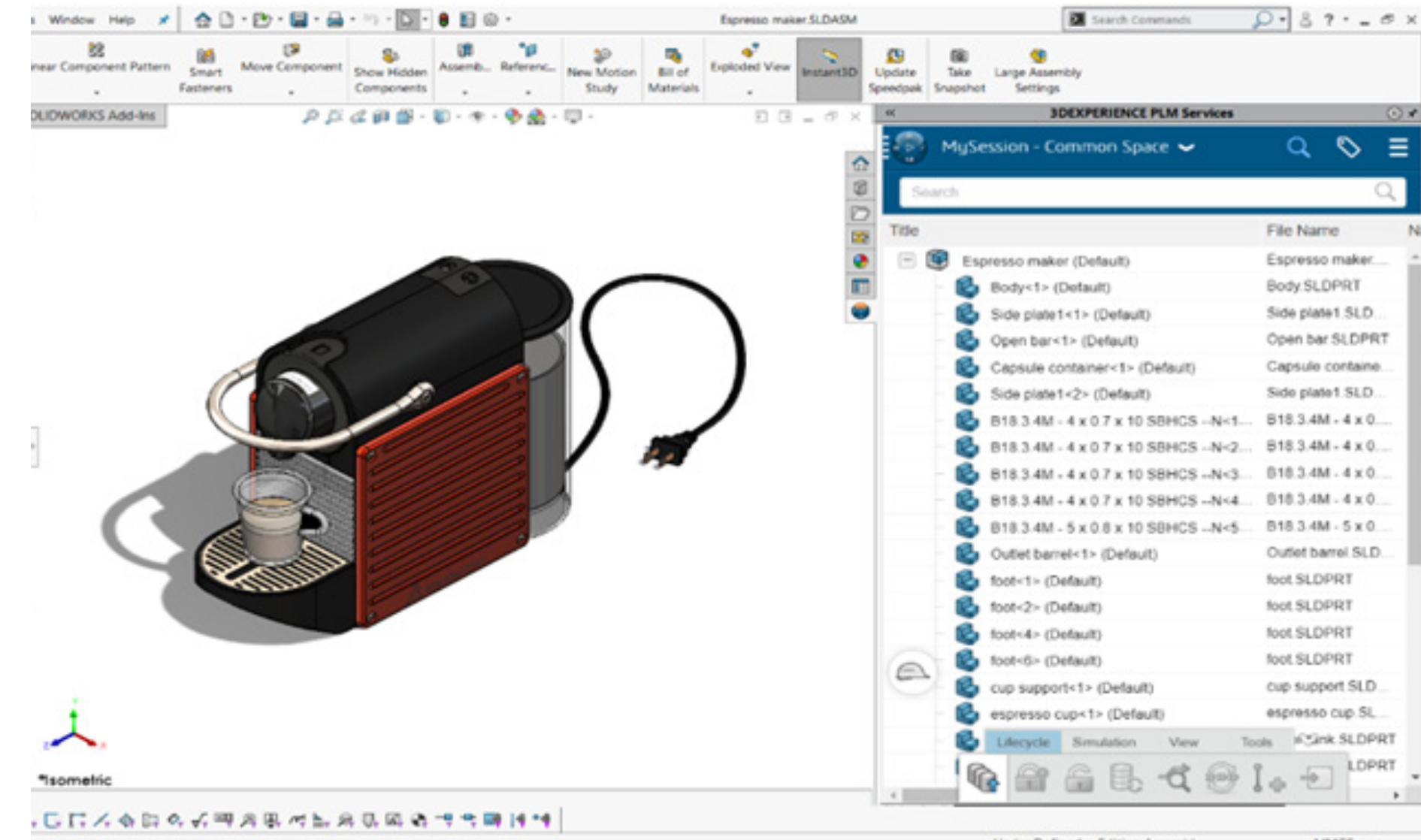
intersections

face orientation

Hard to Create 3D Data

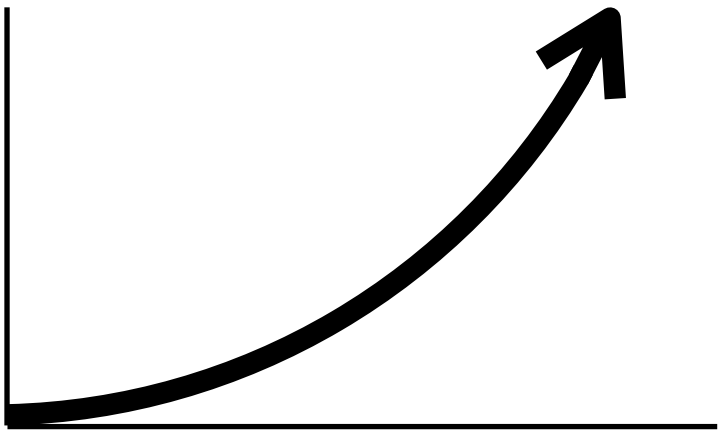
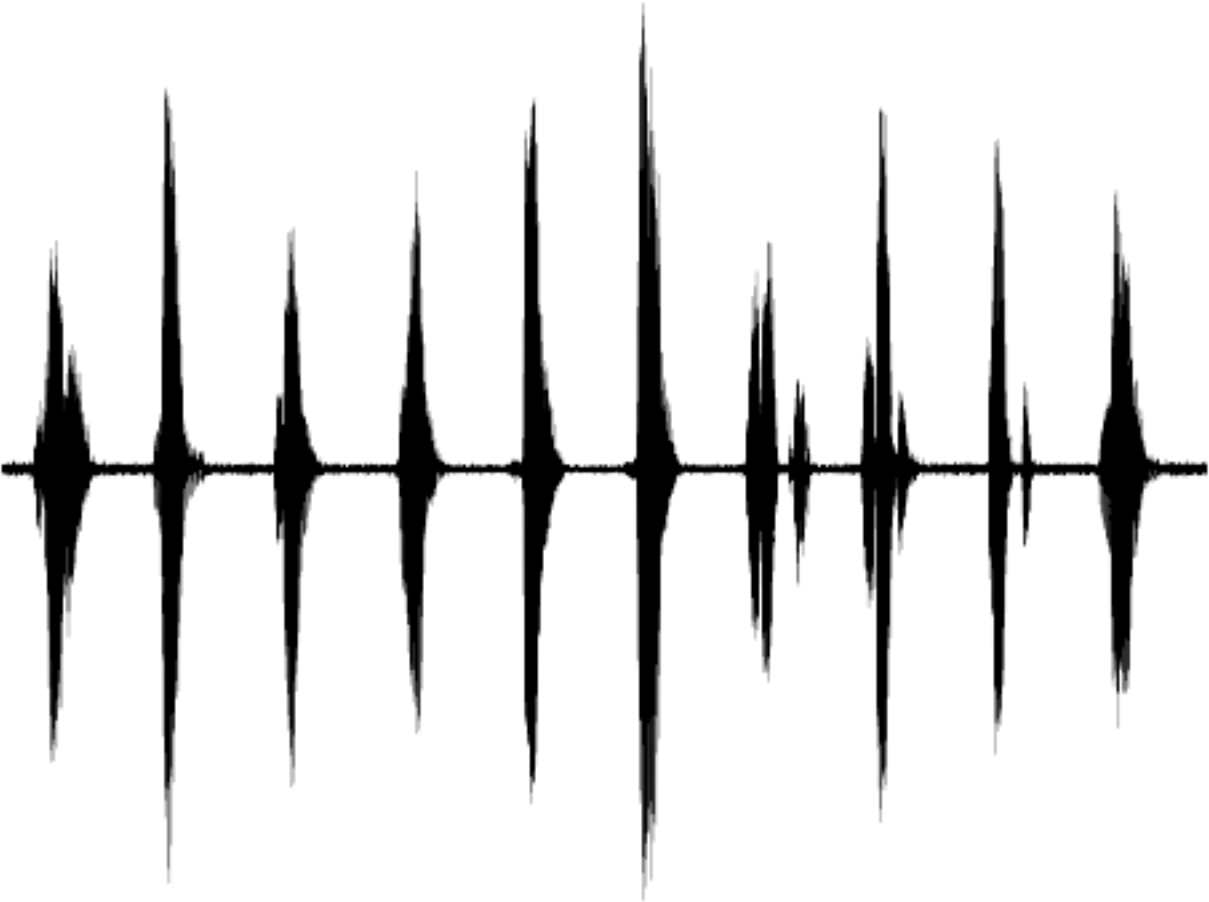


Blender

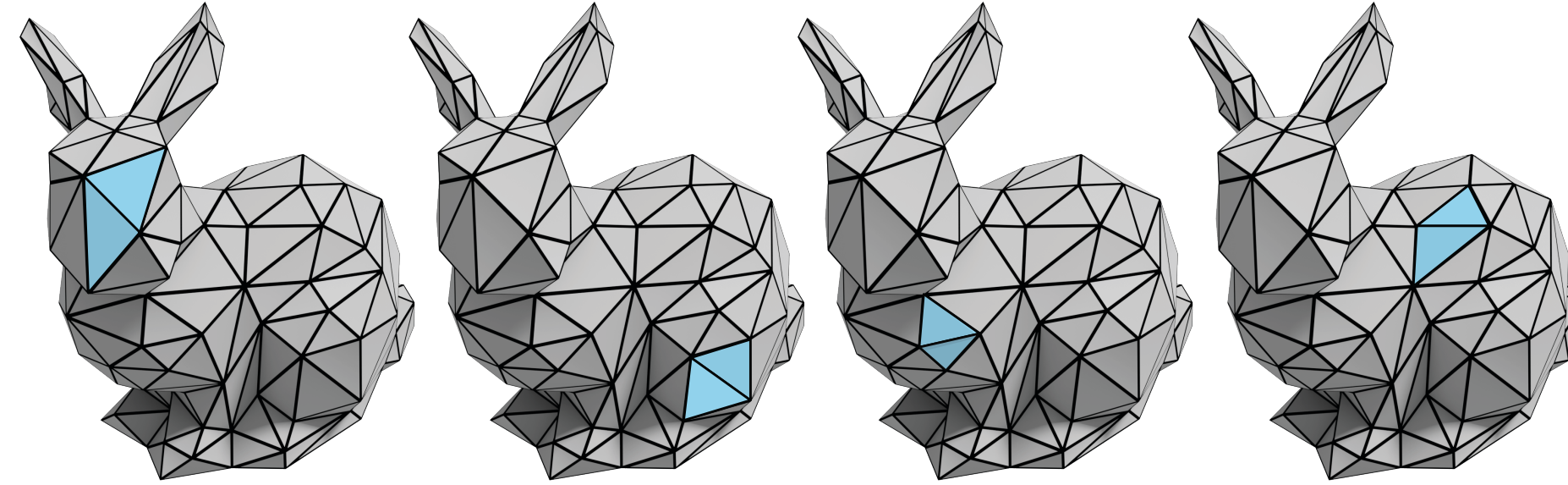


SolidWorks

Curse of dimensionality



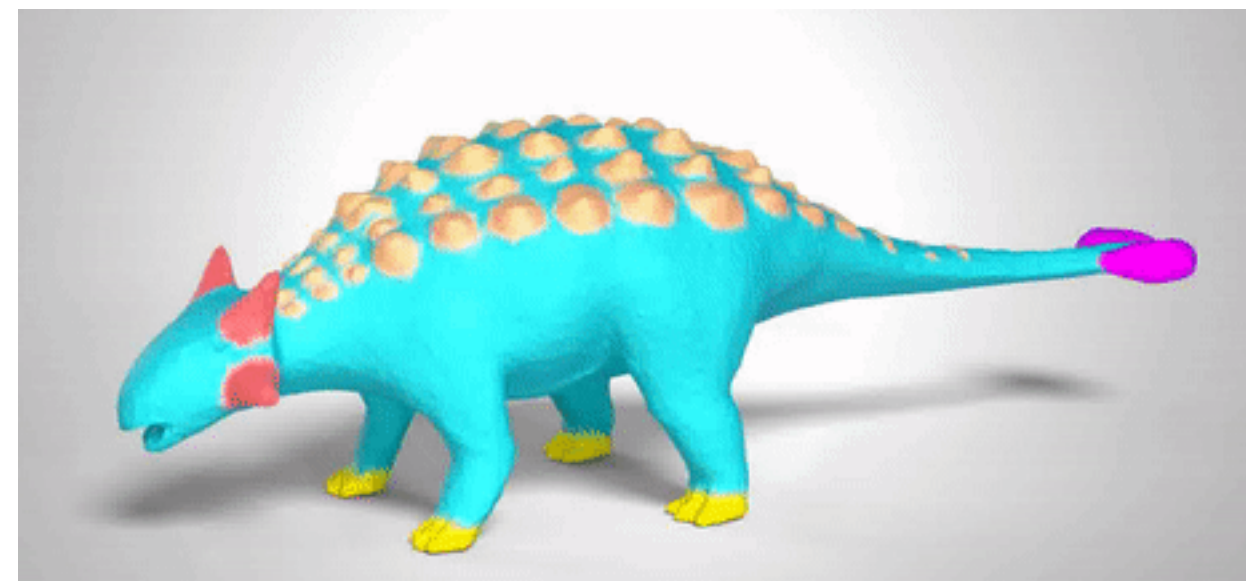
Mesh Convolutional Neural Networks



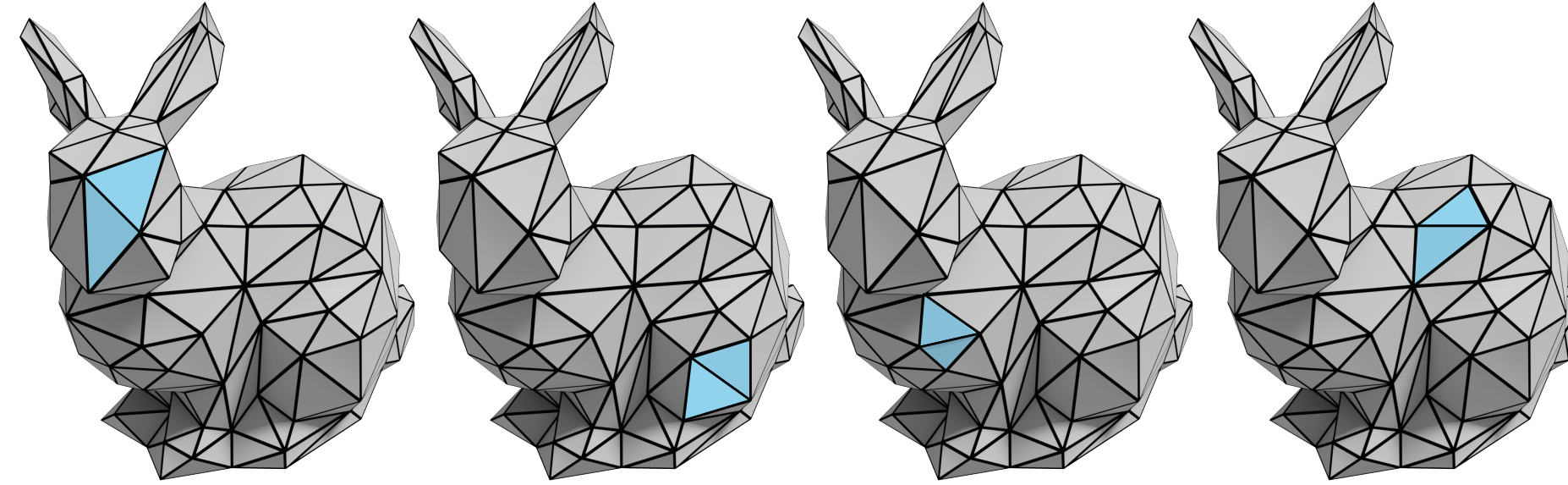
Machine Learning & Geometry Processing



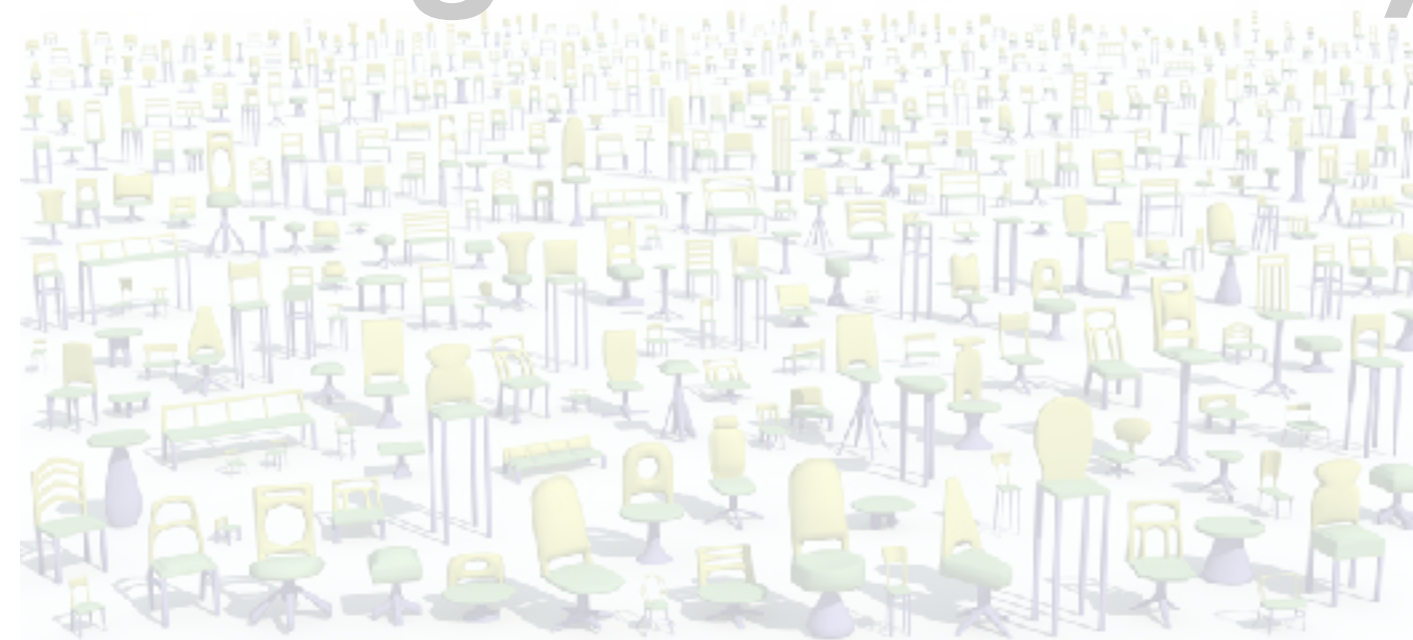
Learning from a Single Mesh



Mesh Convolutional Neural Networks



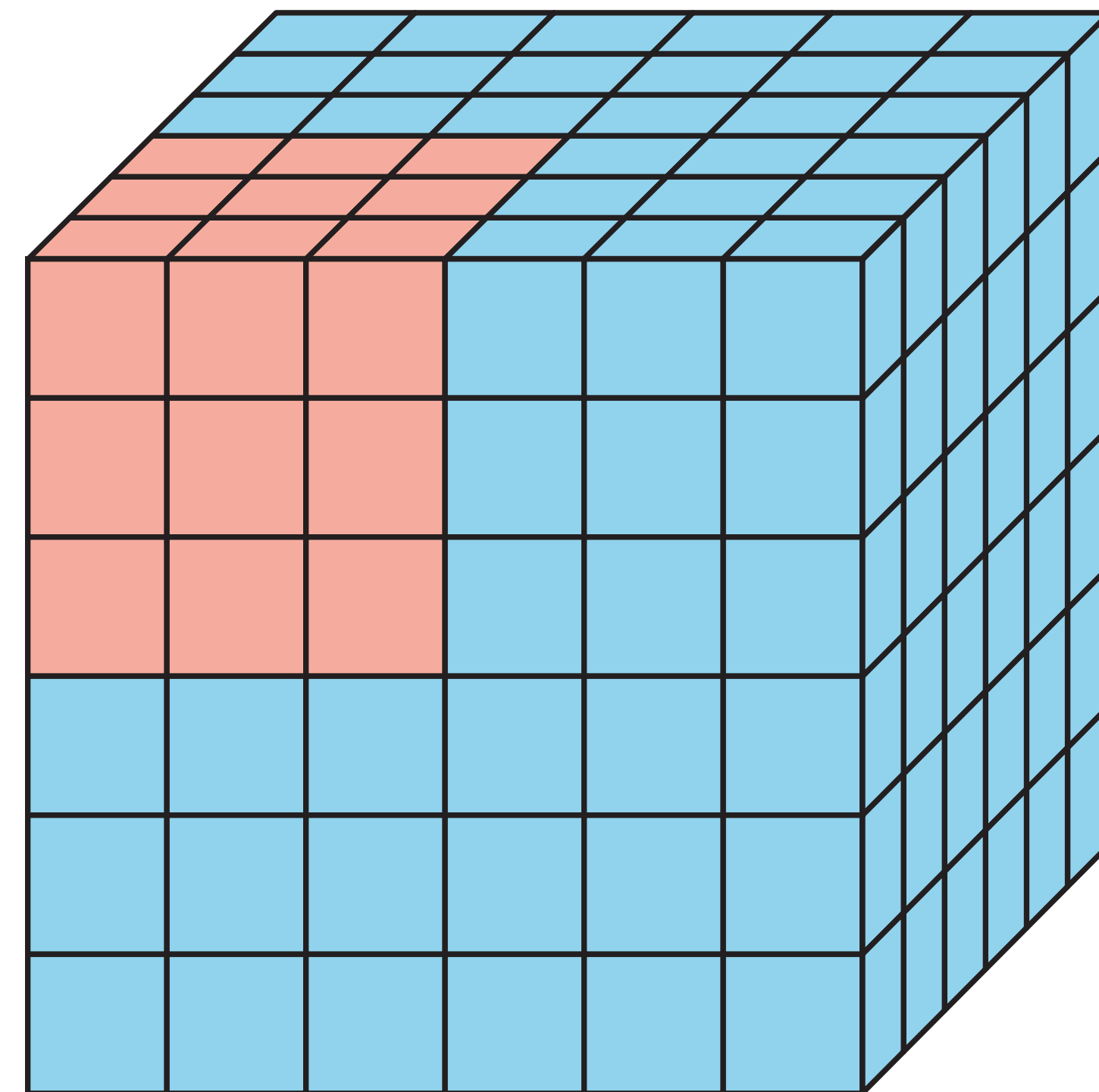
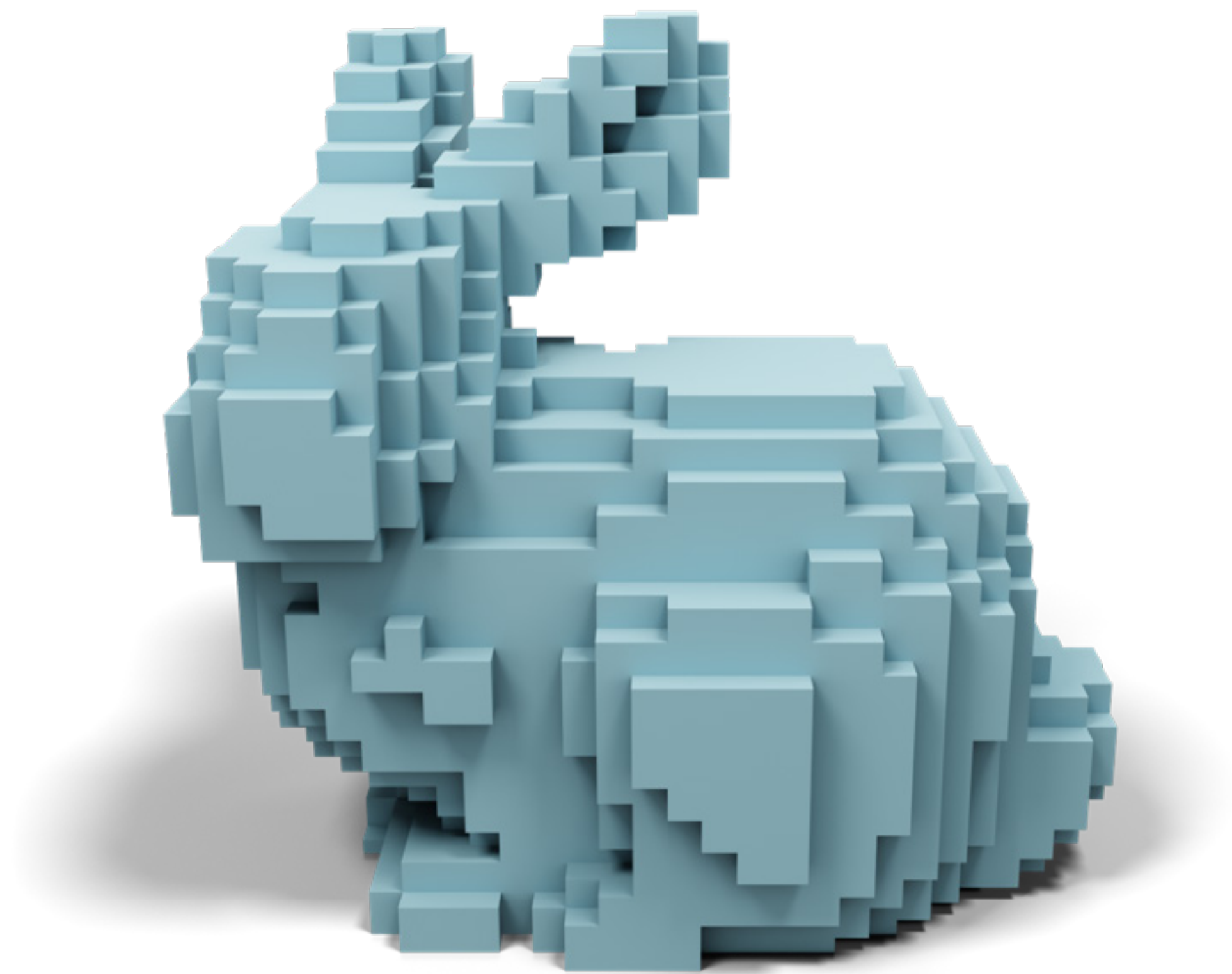
Machine Learning & Geometry Processing



Learning from a Single Mesh

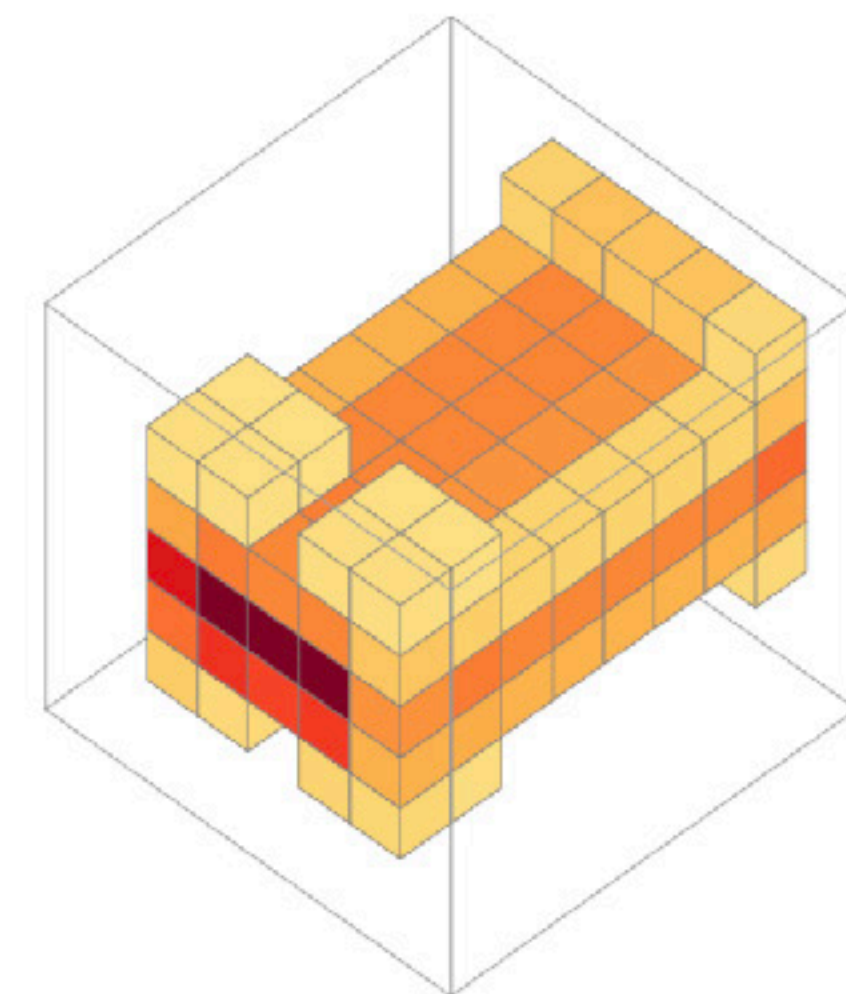
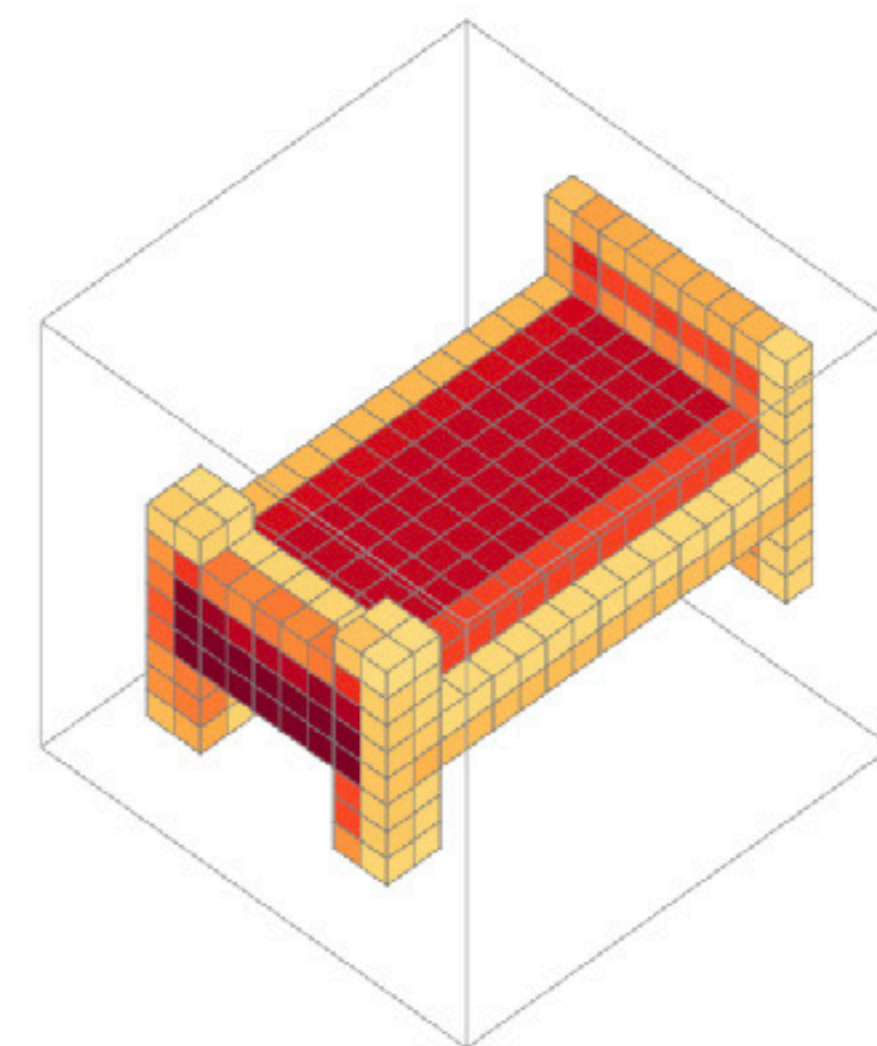
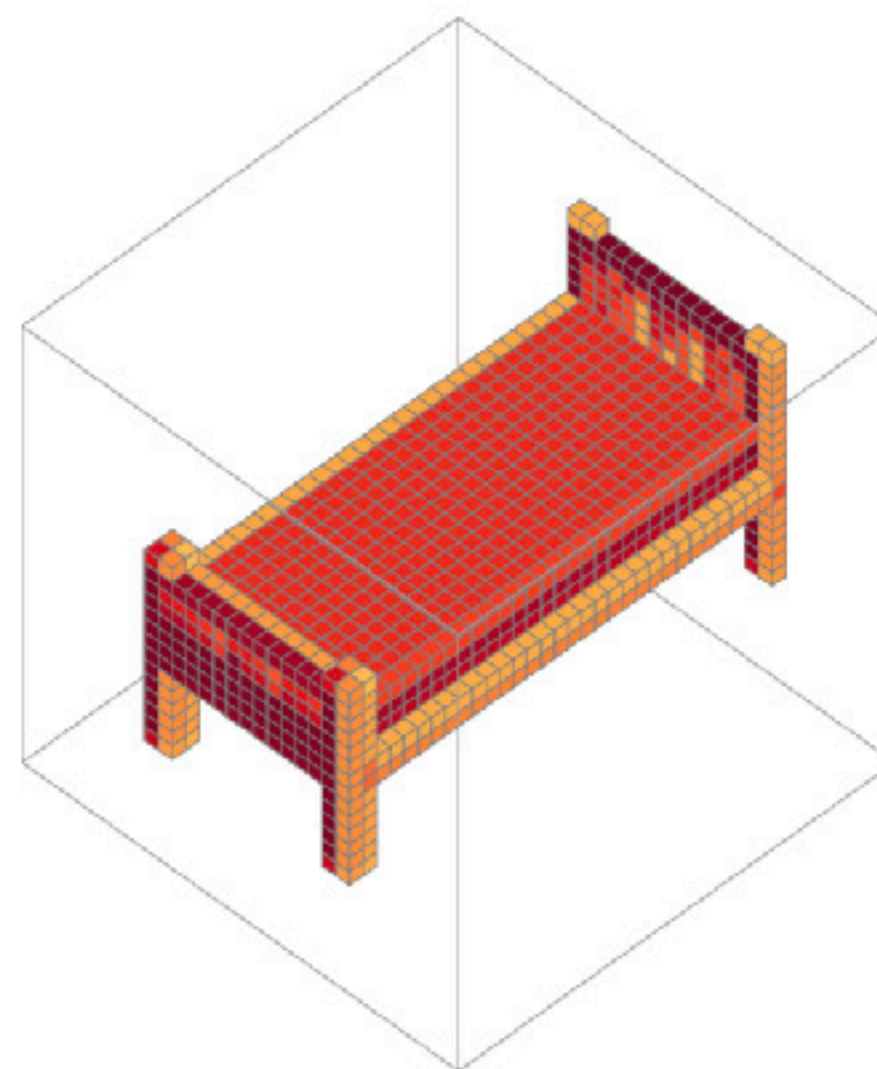
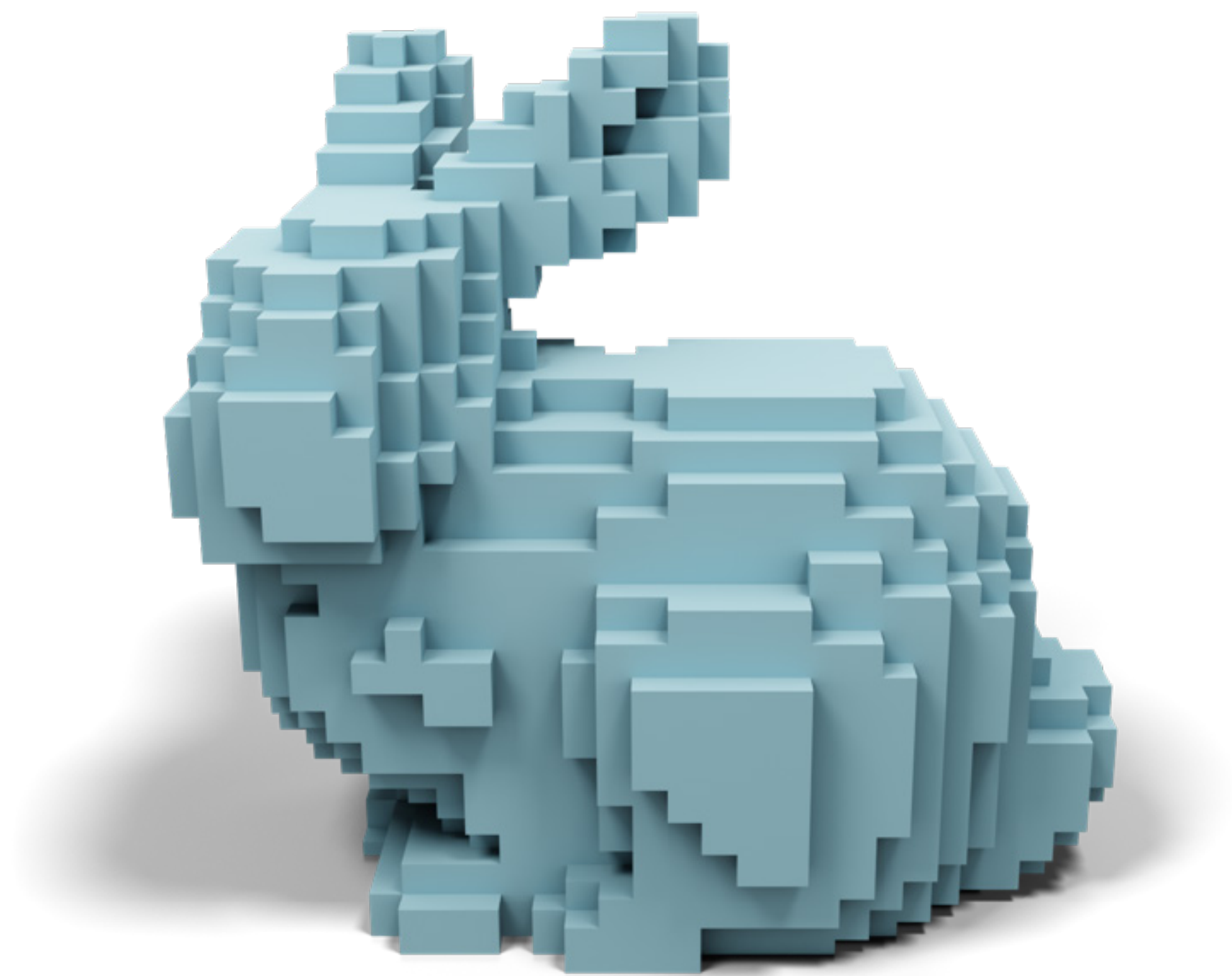


Voxel (3D Pixel) Representation



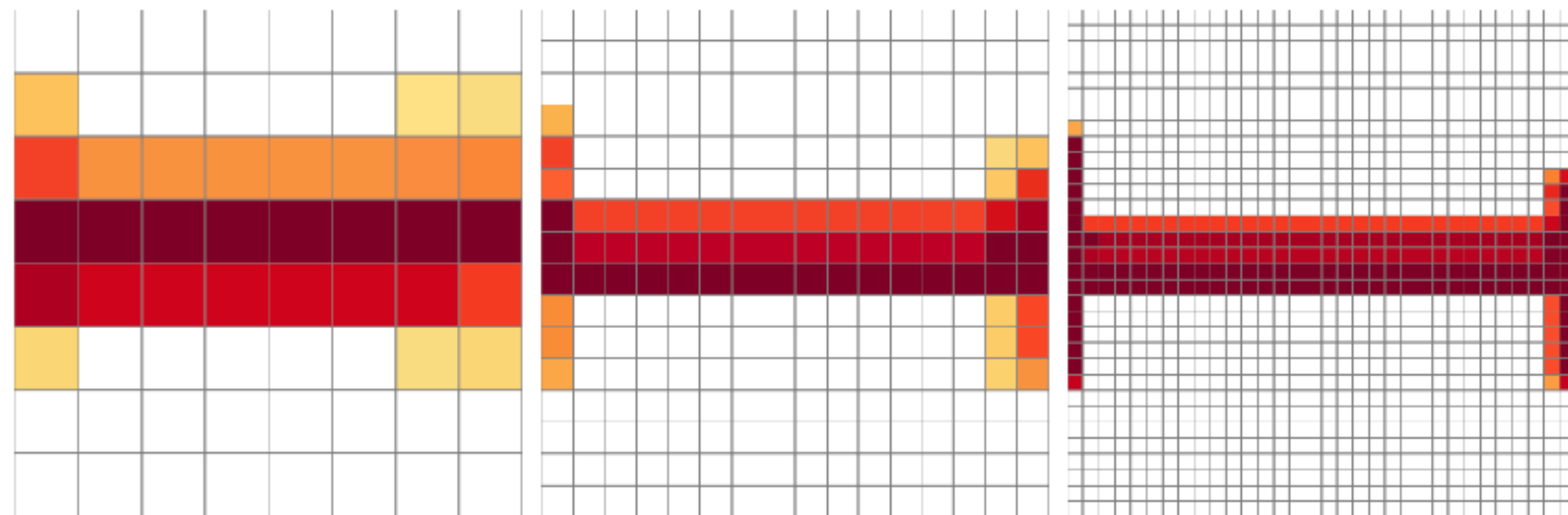
convolution

Voxel (3D Pixel) Representation

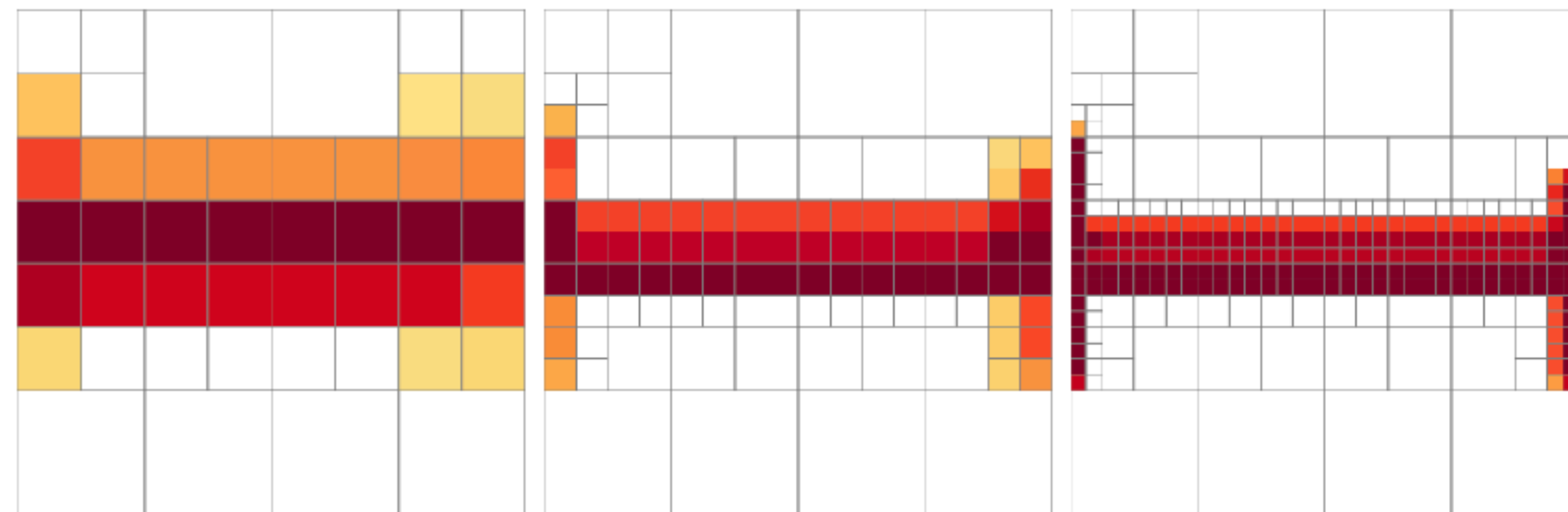


pooling

Large Memory Cost



↓
Octree



O-CNN: Octree-based Convolutional Neural Networks for 3D Shape Analysis

PENG-SHUAI WANG, Tsinghua University and Microsoft Research Asia

YANG LIU, Microsoft Research Asia

YU-XIAO GUO, University of Electronic Science and Technology of China and Microsoft Research Asia

CHUN-YU SUN, Tsinghua University and Microsoft Research Asia

XIN TONG, Microsoft Research Asia

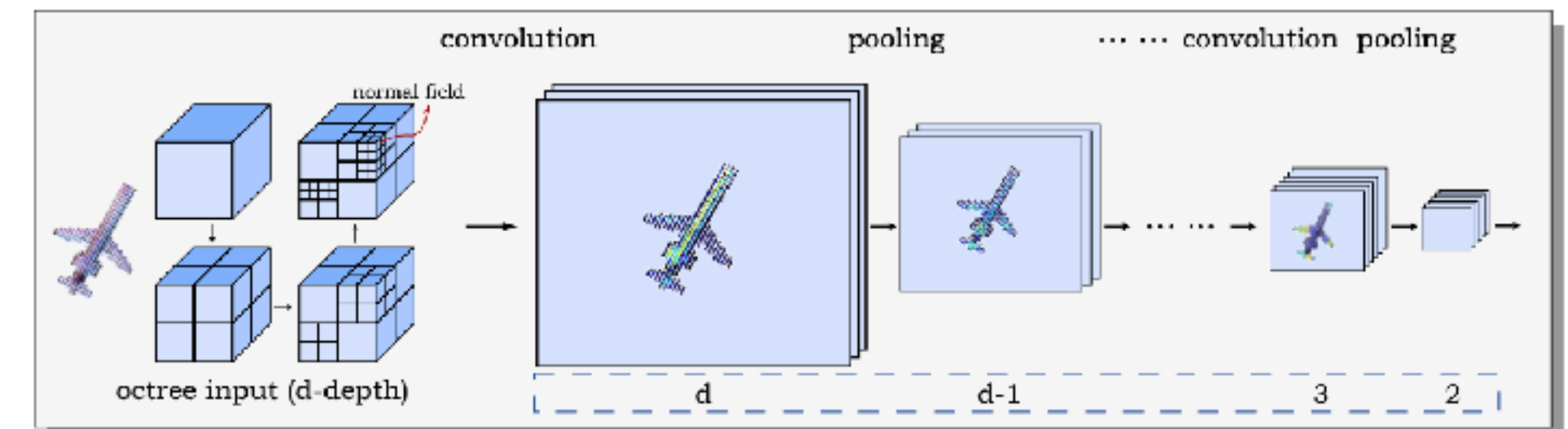


Fig. 1. An illustration of our octree-based convolutional neural network (O-CNN). Our method represents the input shape with an octree and feeds the averaged normal vectors stored in the finest leaf octants to the CNN as input. All the CNN operations are efficiently executed on the GPU and the resulting features are stored in the octree structure. Numbers inside the blue dashed square denote the depth of the octants involved in computation.

We present O-CNN, an Octree-based Convolutional Neural Network (CNN) for 3D shape analysis. Built upon the octree representation of 3D shapes, our method takes the average normal vectors of a 3D model sampled in the finest leaf octants as input and performs 3D CNN operations on the octants occupied by the 3D shape surface. We design a novel octree data structure to efficiently store the octant information and CNN features into the graphics memory and execute the entire O-CNN training and evaluation on the GPU. O-CNN supports various CNN structures and works for 3D shapes in different representations. By restraining the computations on the octants occupied by 3D surfaces, the memory and computational costs of the O-CNN grow quadratically as the depth of the octree increases, which makes the 3D CNN feasible for high-resolution 3D models. We compare the performance of the O-CNN with other existing 3D CNN solutions and demonstrate the efficiency and efficacy of O-CNN in three shape analysis tasks, including object classification, shape retrieval, and shape segmentation.

CCS Concepts: • Computing methodologies → Mesh models; Point-based models; Neural networks;

Additional Key Words and Phrases: octree, convolutional neural network, object classification, shape retrieval, shape segmentation

ACM Reference format:

Peng-Shuai Wang, Yang Liu, Yu-Xiao Guo, Chun-Yu Sun, and Xin Tong. 2017. O-CNN: Octree-based Convolutional Neural Networks for 3D Shape Analysis. *ACM Trans. Graph.* 36, 4, Article 72 (July 2017), 11 pages. <https://doi.org/10.1145/3072959.3073608>

1 INTRODUCTION

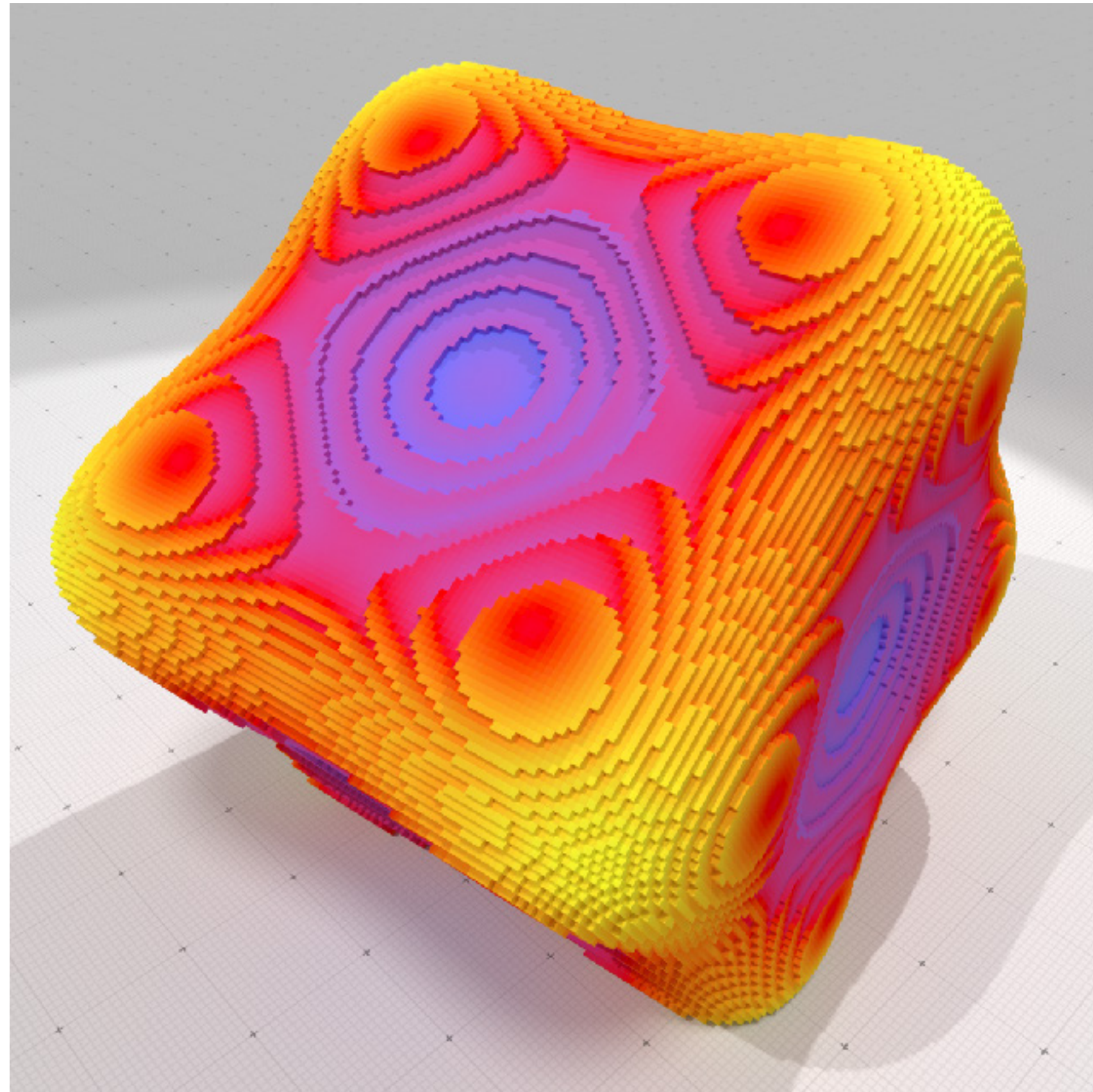
With recent advances in low-cost 3D acquisition devices and 3D modeling tools, the amount of 3D models created by end users has been increasing quickly. Analyzing and understanding these 3D shapes, as for classification, segmentation, and retrieval, have become more and more important for many graphics and vision applications. A key technique for these shape analysis tasks is to extract features of 3D models that can sufficiently characterize their shapes and parts.

In the computer vision field, convolutional neural networks (CNNs) are widely used for image feature extraction and have demonstrated their advantages over manually-crafted solutions in most image analysis and understanding tasks. However, it is a non-trivial task to adapt a CNN designed for regularly sampled 2D images to 3D shapes modeled by irregular triangle meshes or point clouds. A set of methods convert the 3D shapes to regularly sampled representations and apply a CNN to them. Voxel-based methods [Maturana and Scherer 2015; Wu et al. 2015] rasterize a 3D shape as an indicator function or distance function sampled over dense voxels and apply a 3D CNN over the entire 3D volume. Since the memory and computation cost grow cubically as the voxel resolution increases, these methods become prohibitively expensive for high-resolution voxels. Manifold-based methods [Boscaini et al. 2015, 2016; Masci

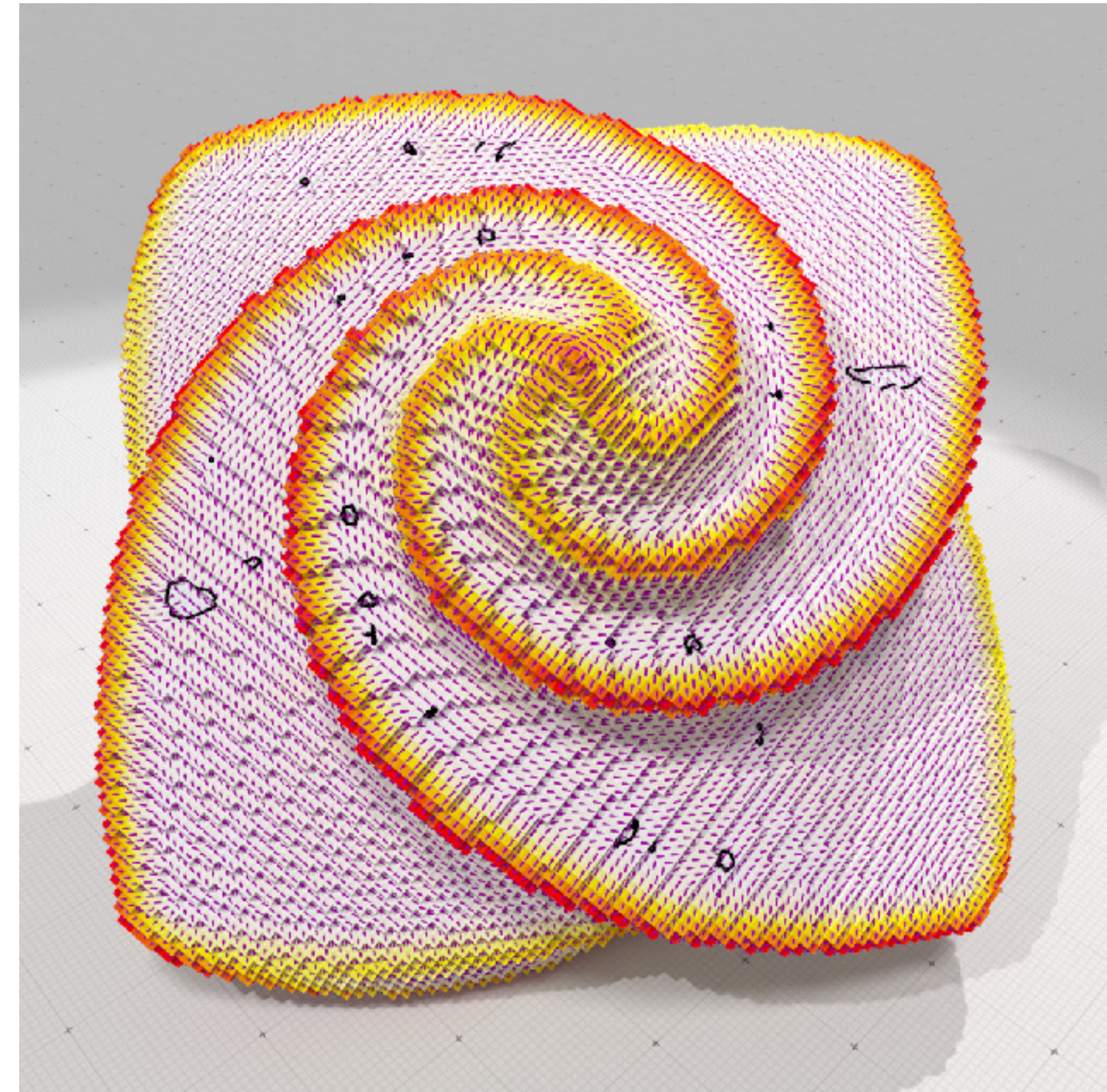
Not a smooth representation



Estimating surface quantities on voxels

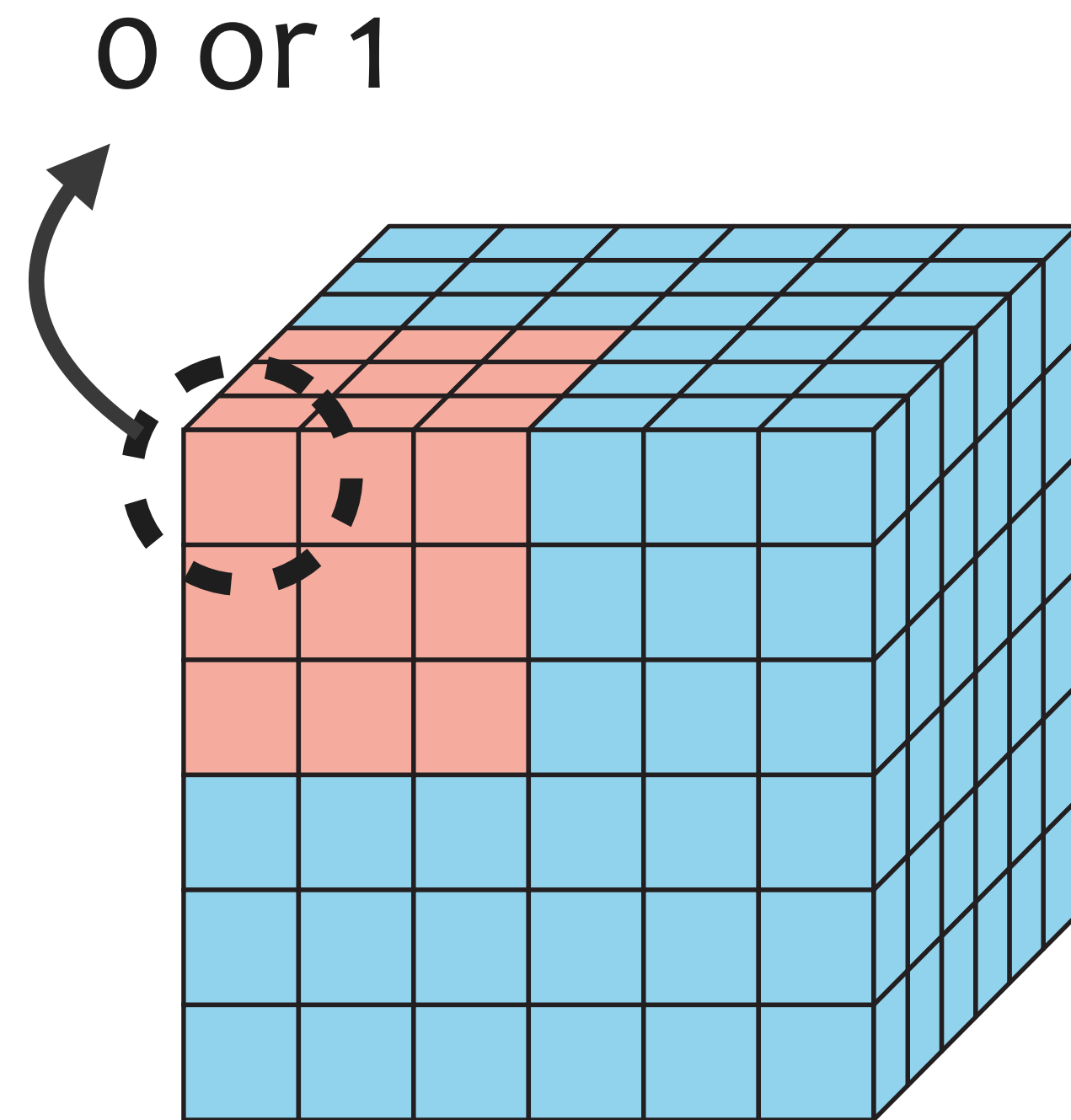


Caissard et al. 2019



Lachaud et al. 2020

Not store {0,1}

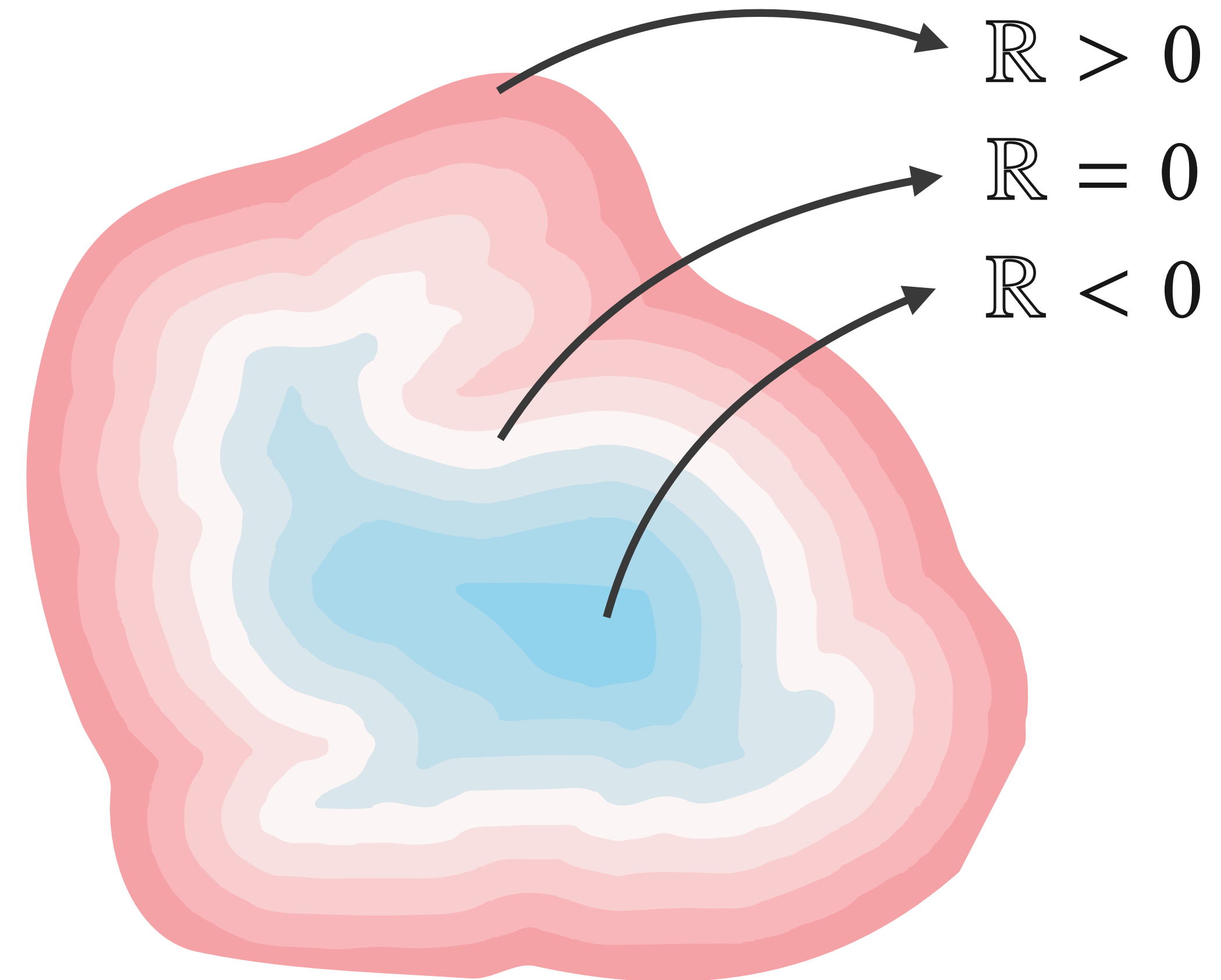
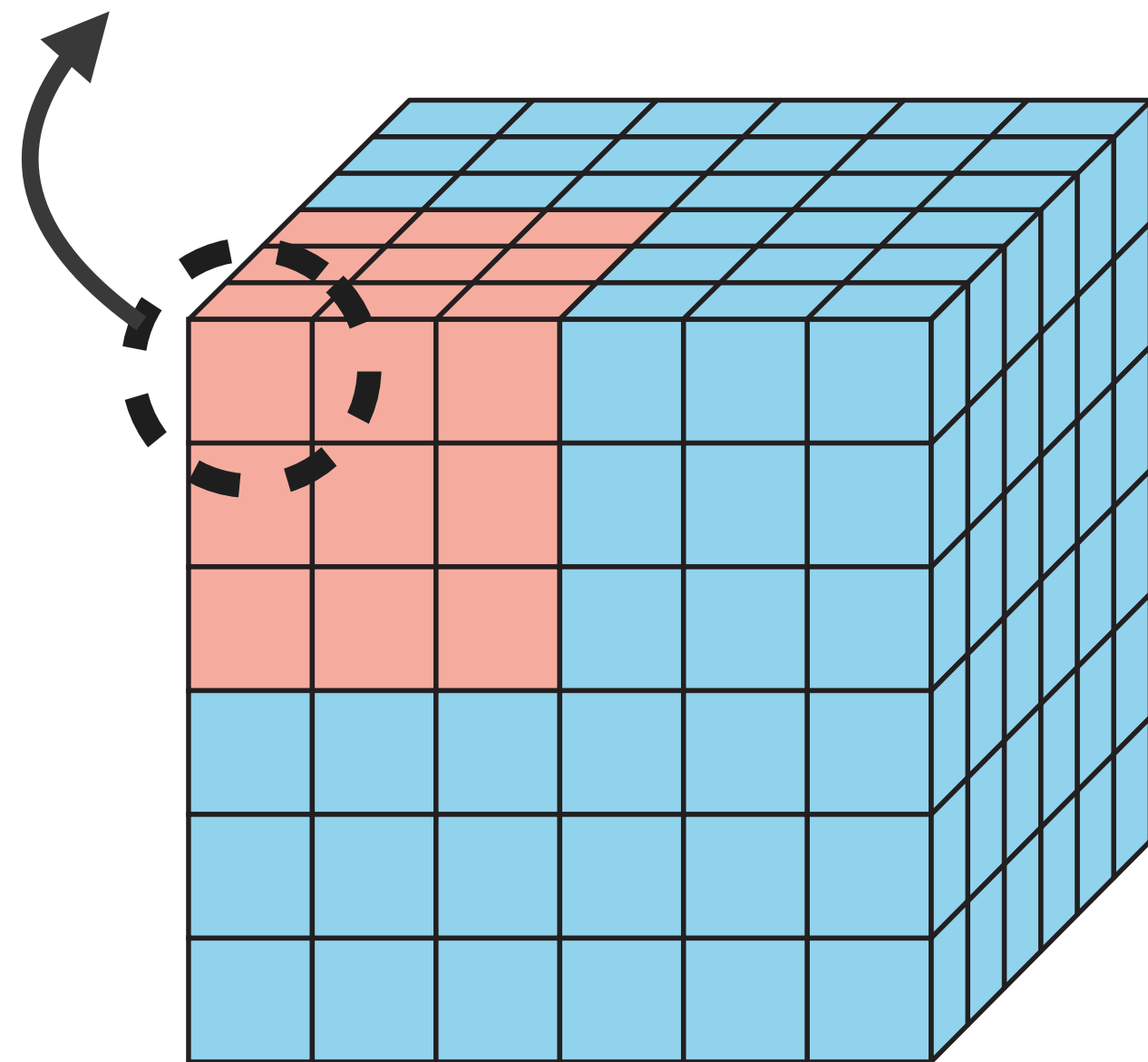


Not store {0,1}

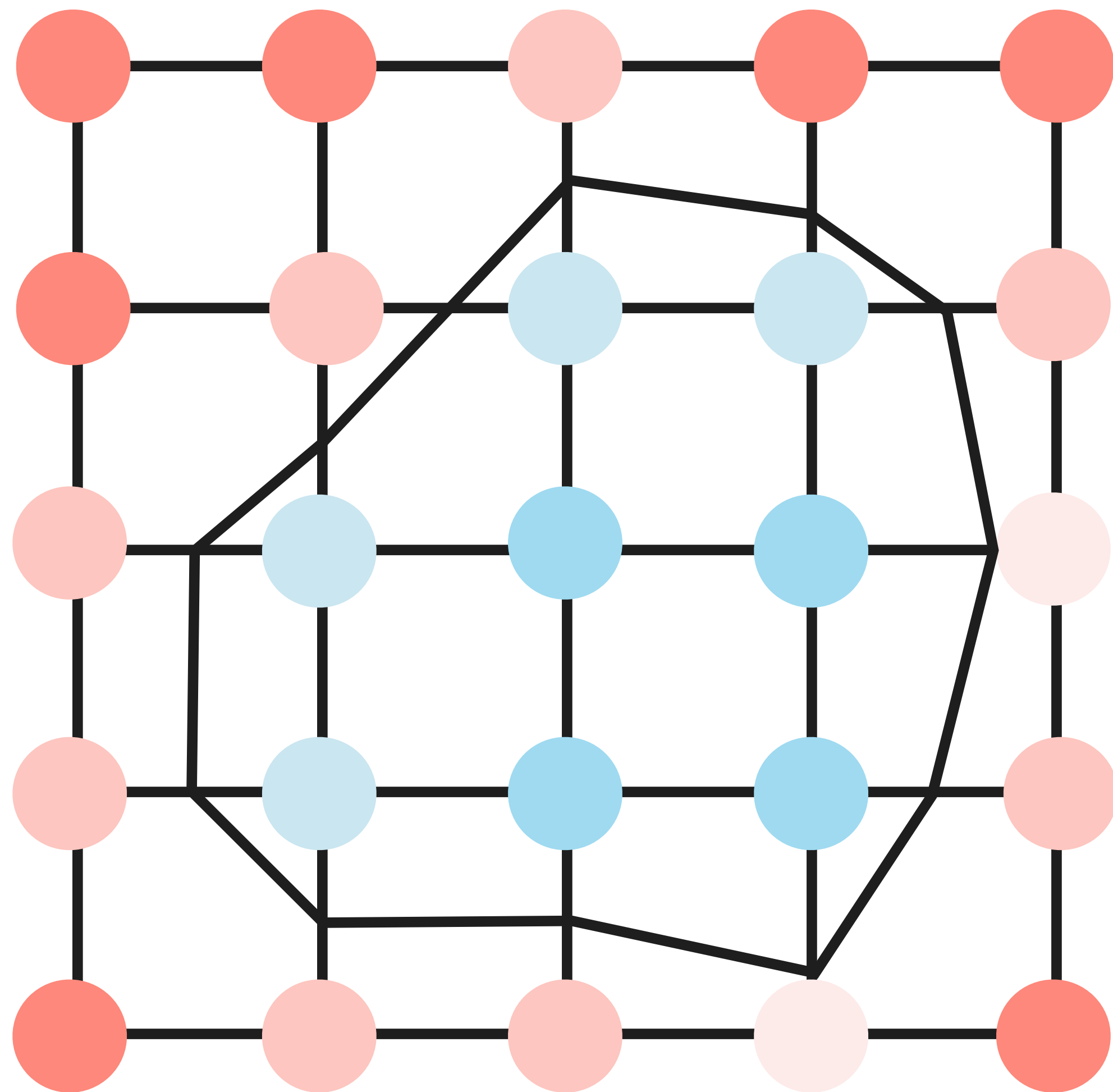
signed distance function (SDF)

[Dai et al. 2017, Zeng et al. 2017, Stutz et al. 2018]

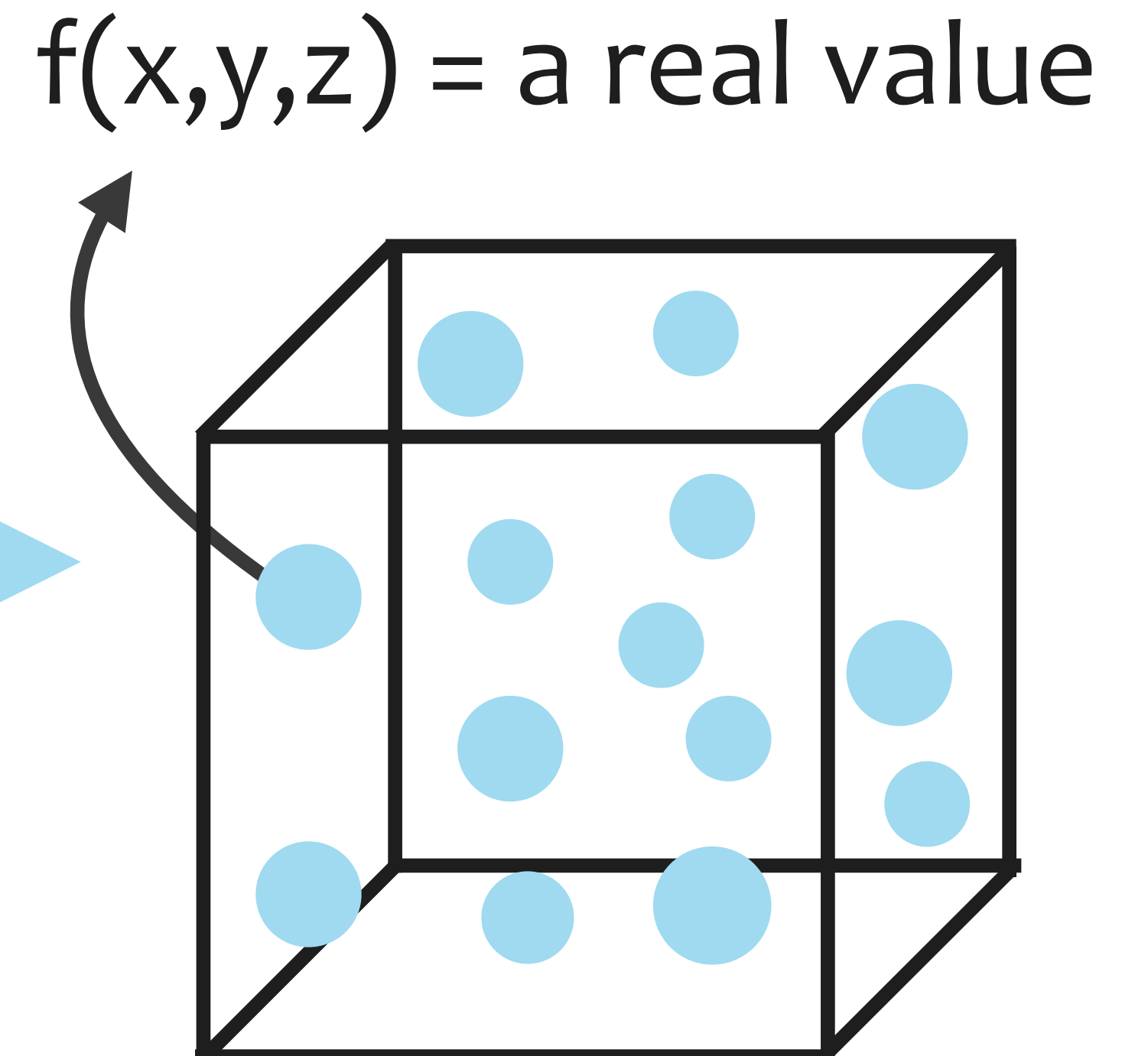
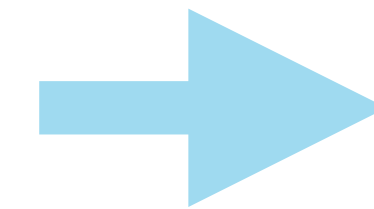
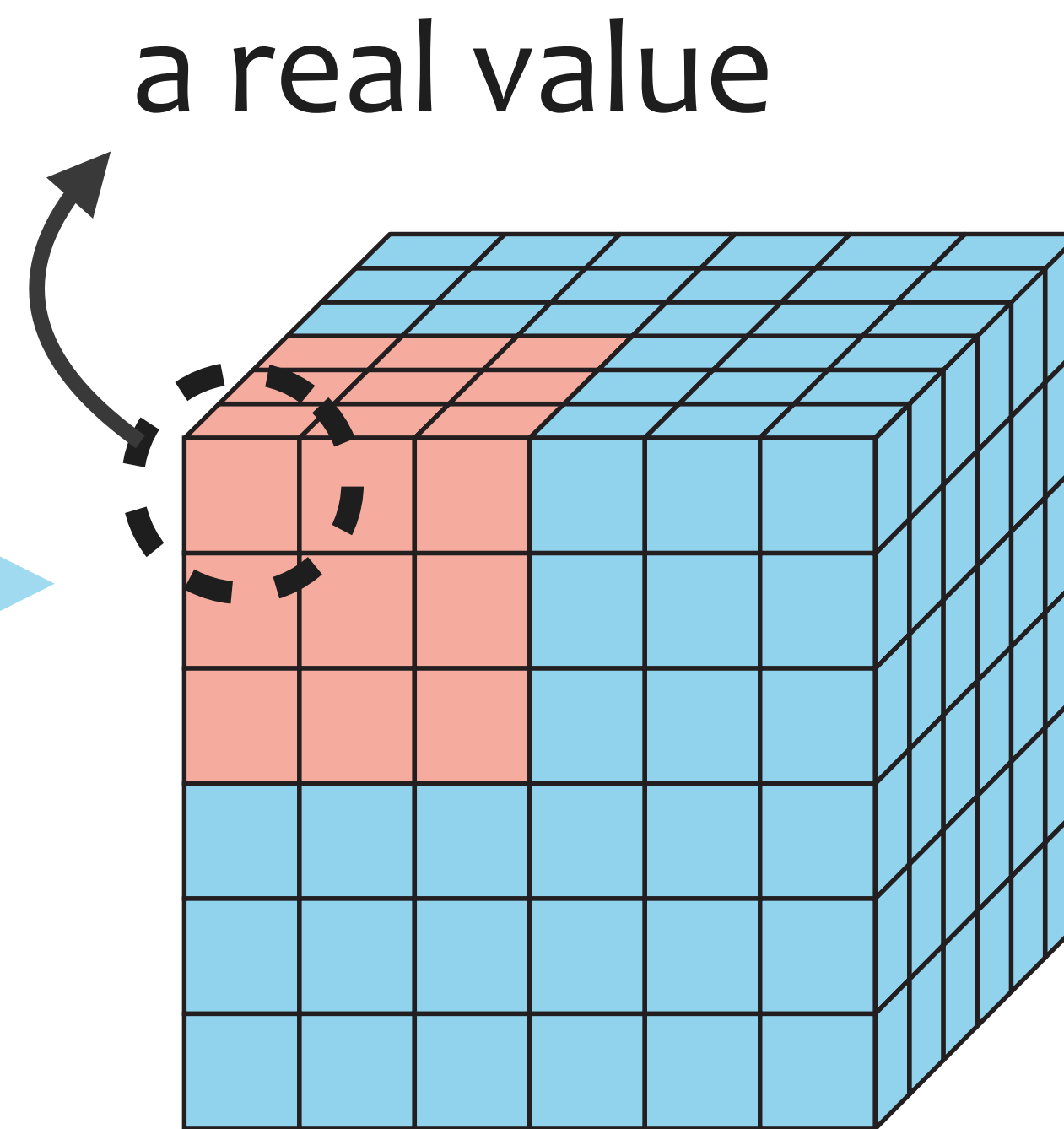
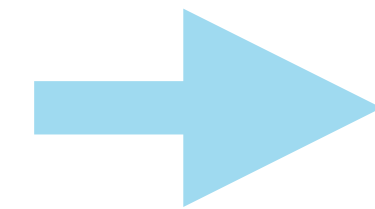
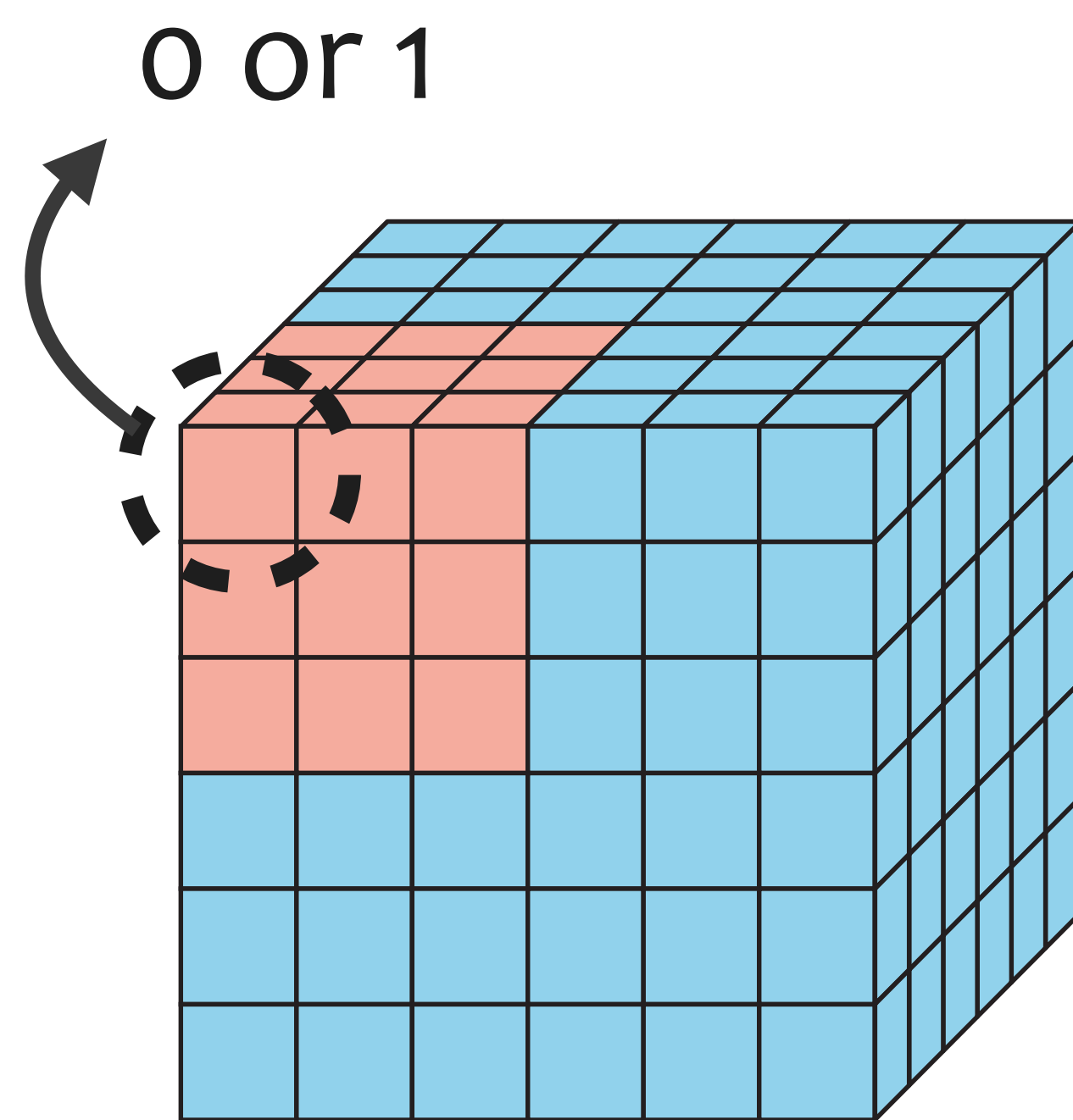
a real value



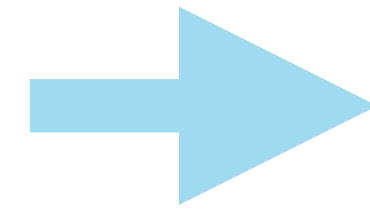
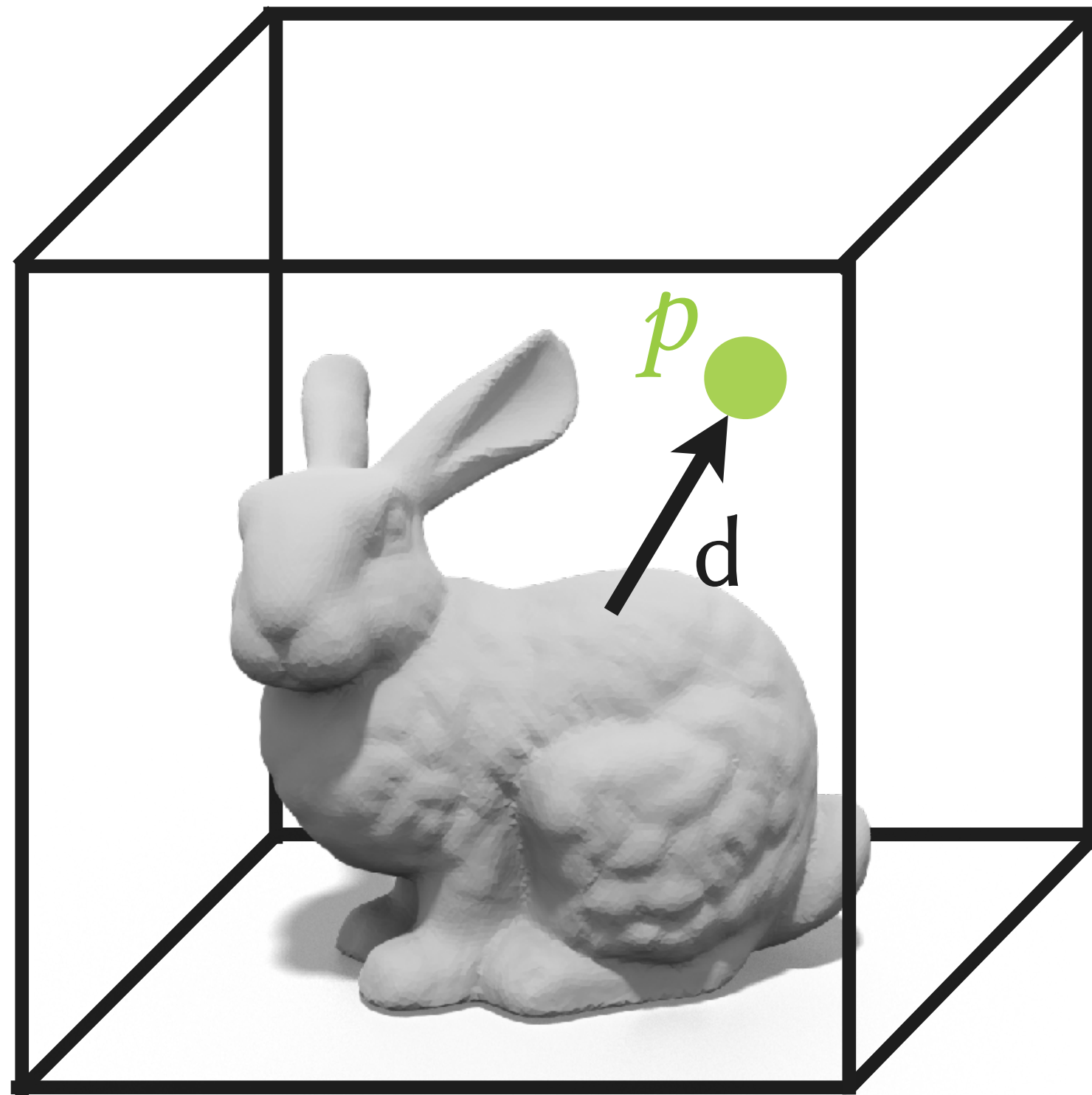
SDF to sub-pixel resolution



Get rid of the voxel grid

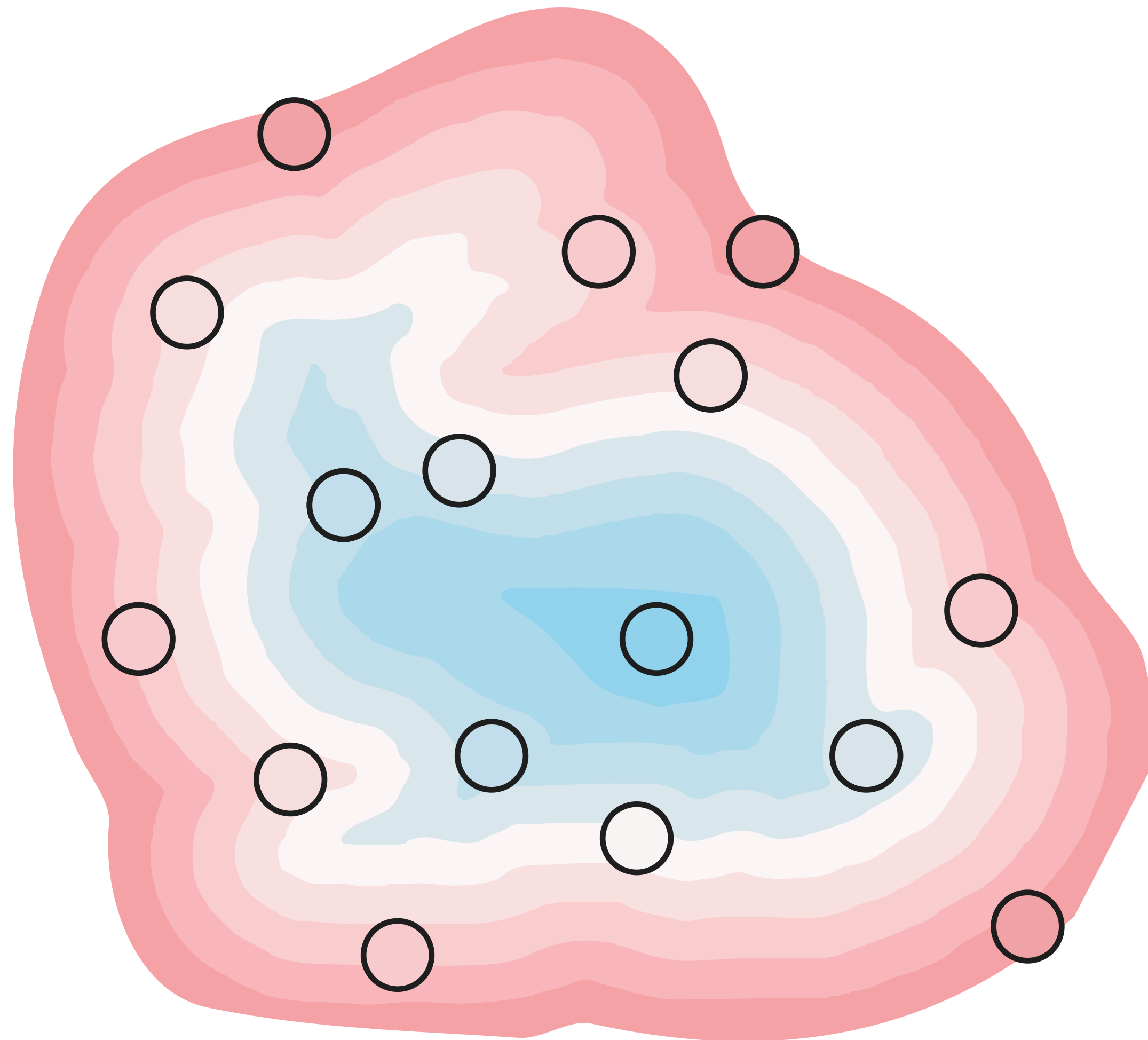


Neural Signed Distance Function



$$f_{\theta}(p_x, p_y, p_z) = \text{signed distance}$$

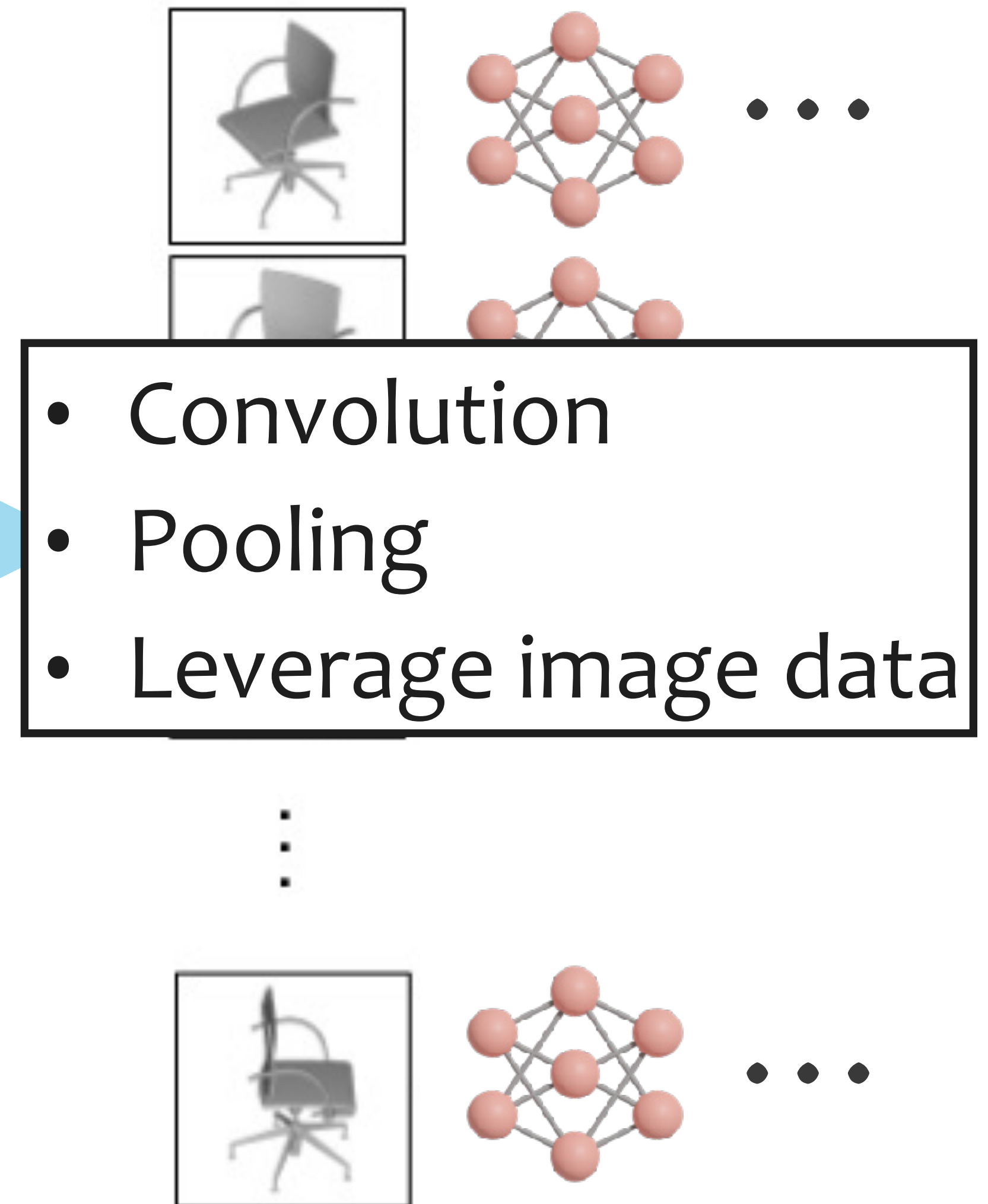
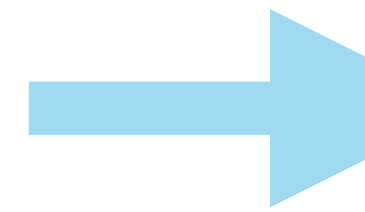
An Alternative Shape Representation



missing basic ingredients:

- differential operators
- differential quantities
- shape editing
- ...

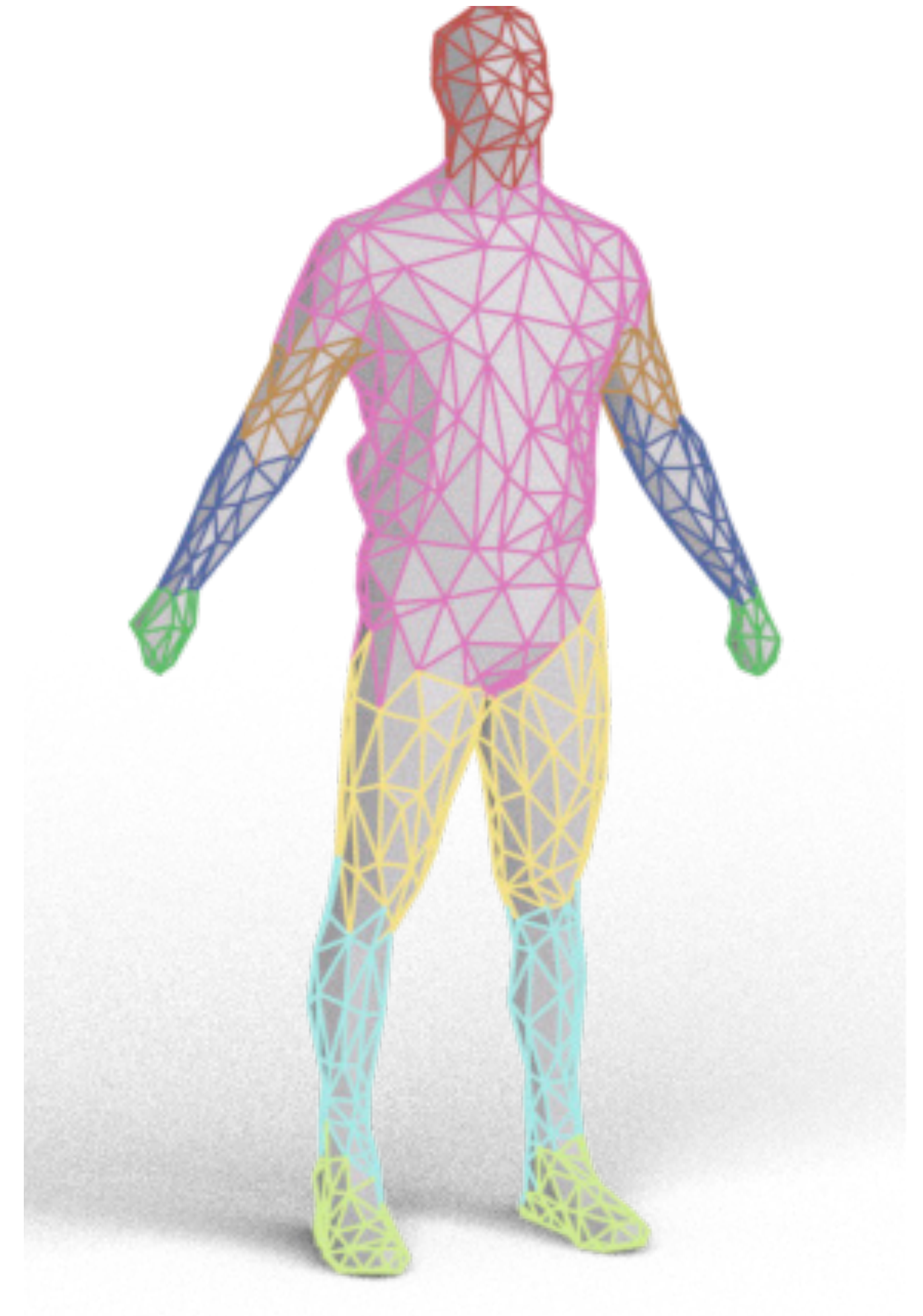
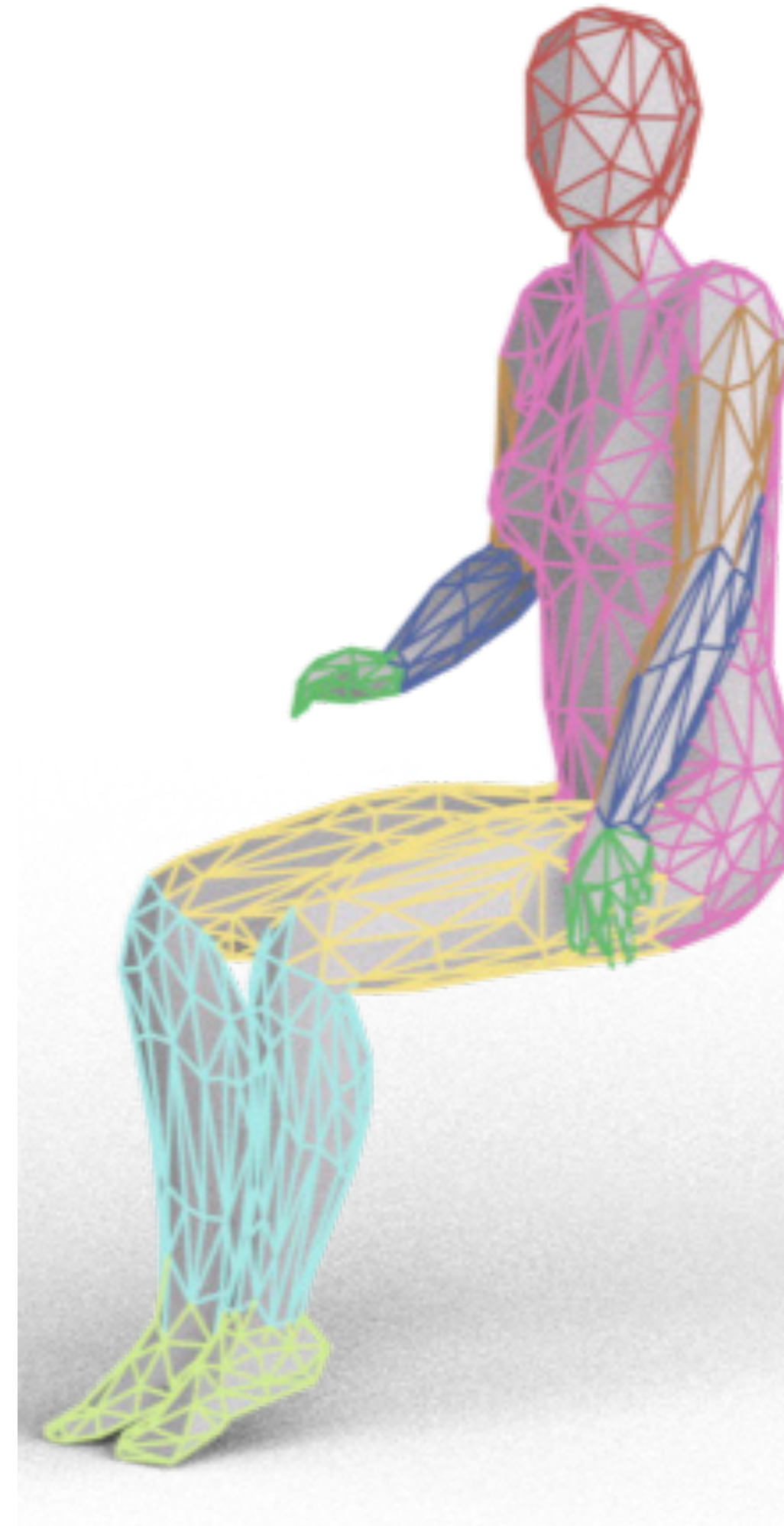
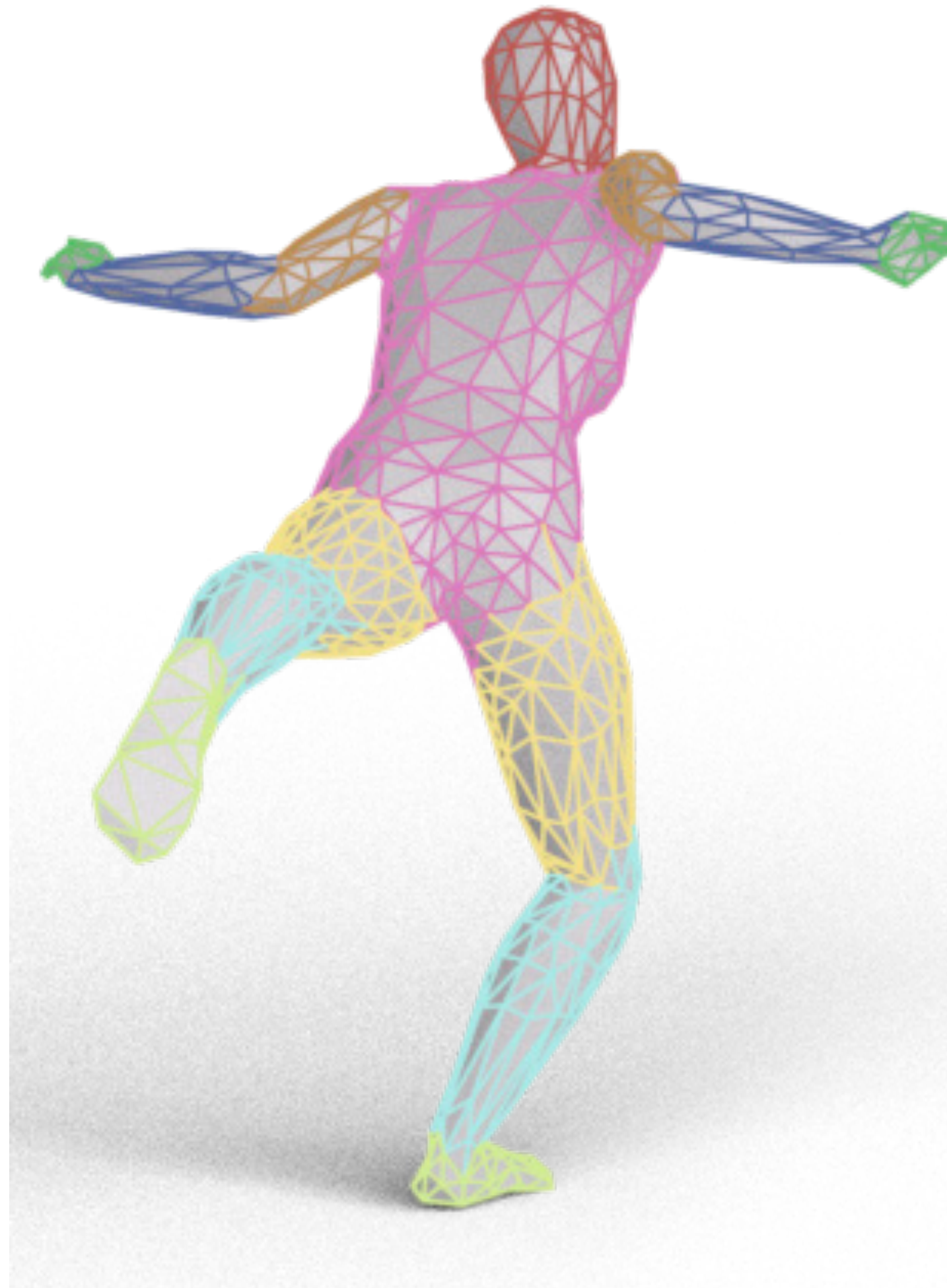
Use image convolution on surfaces



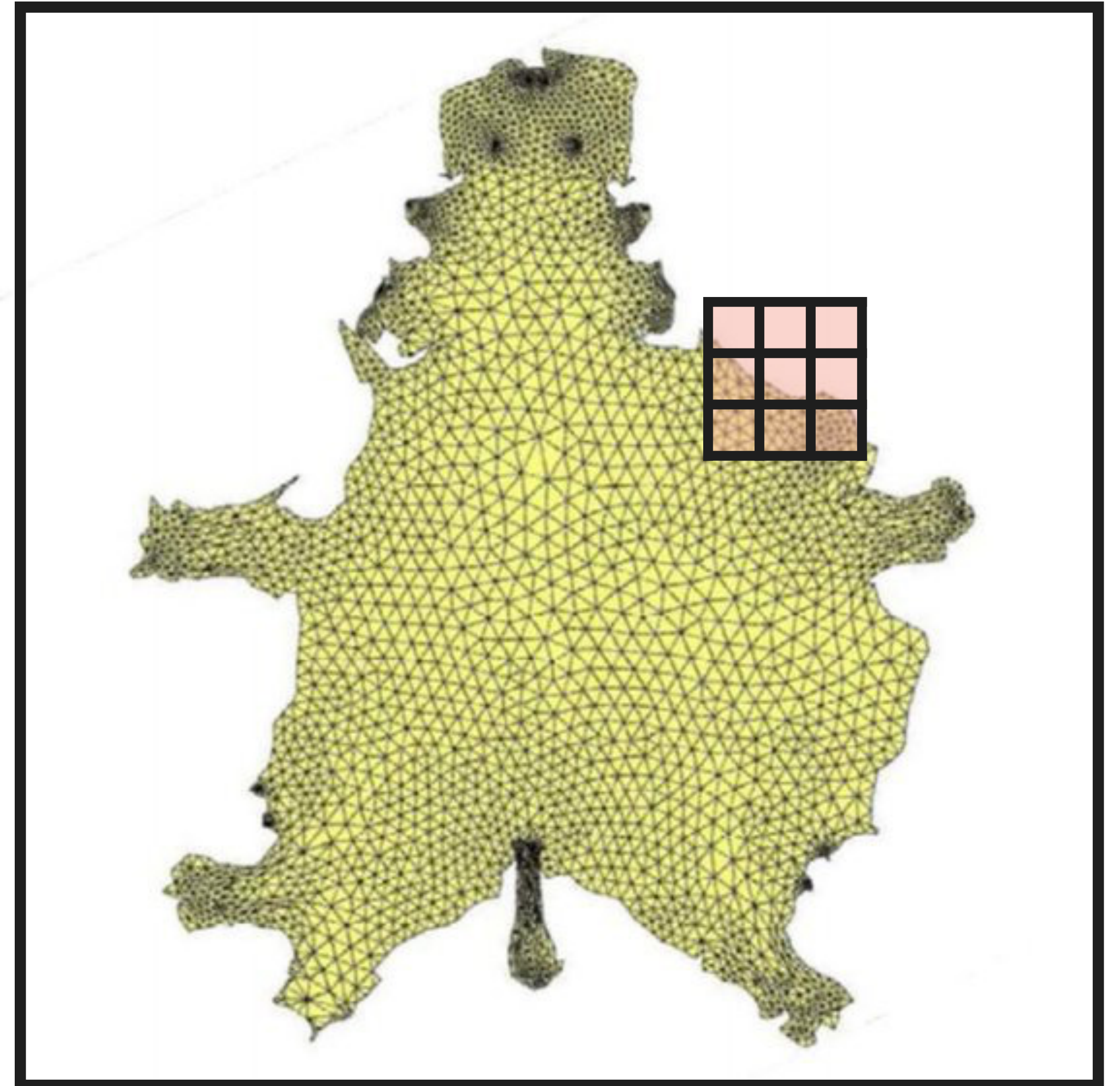
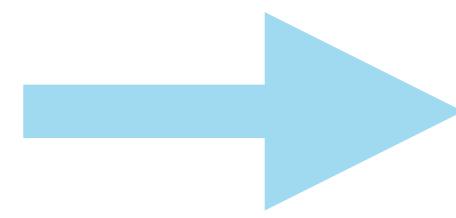
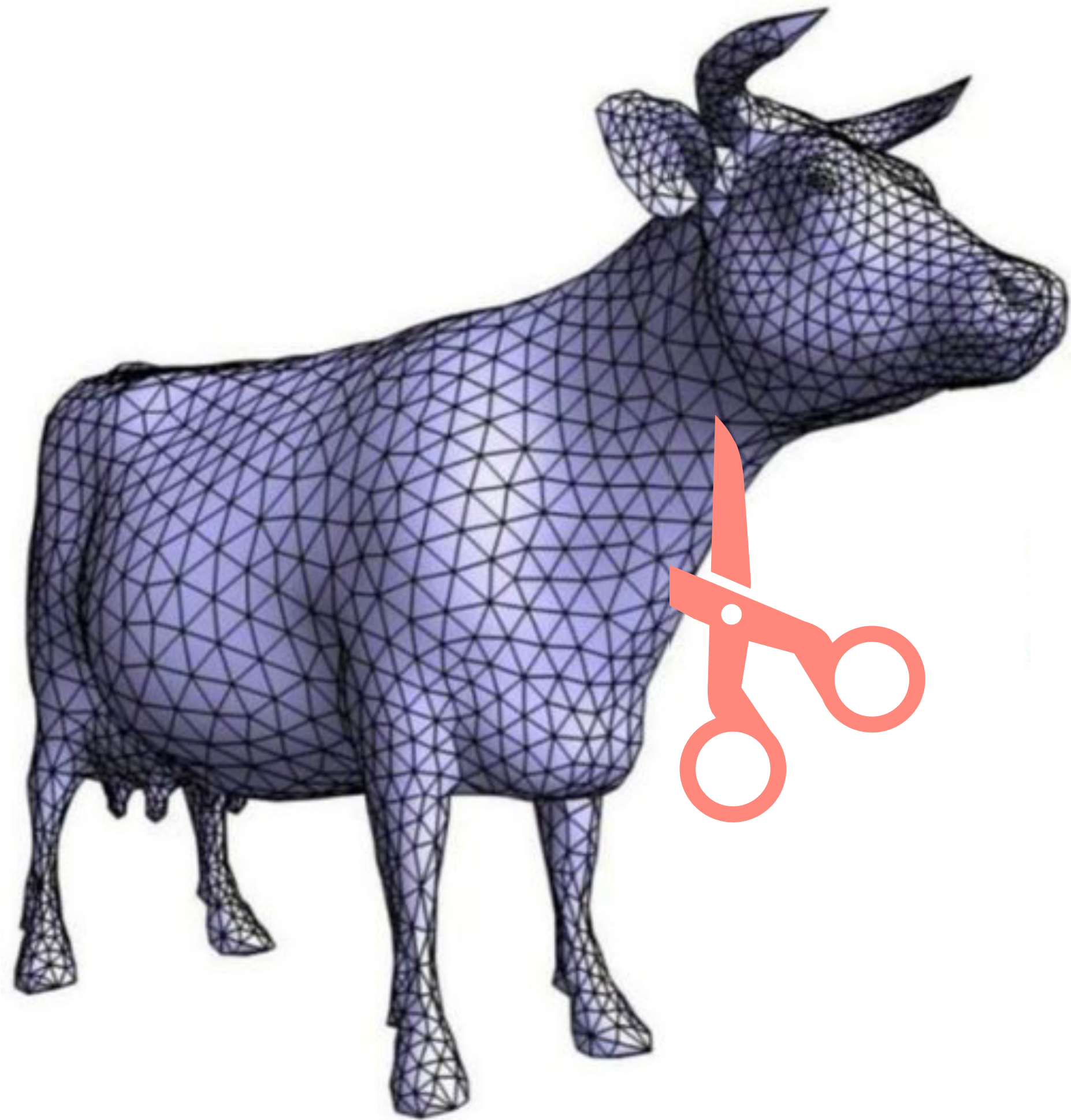
Leverage Image Data



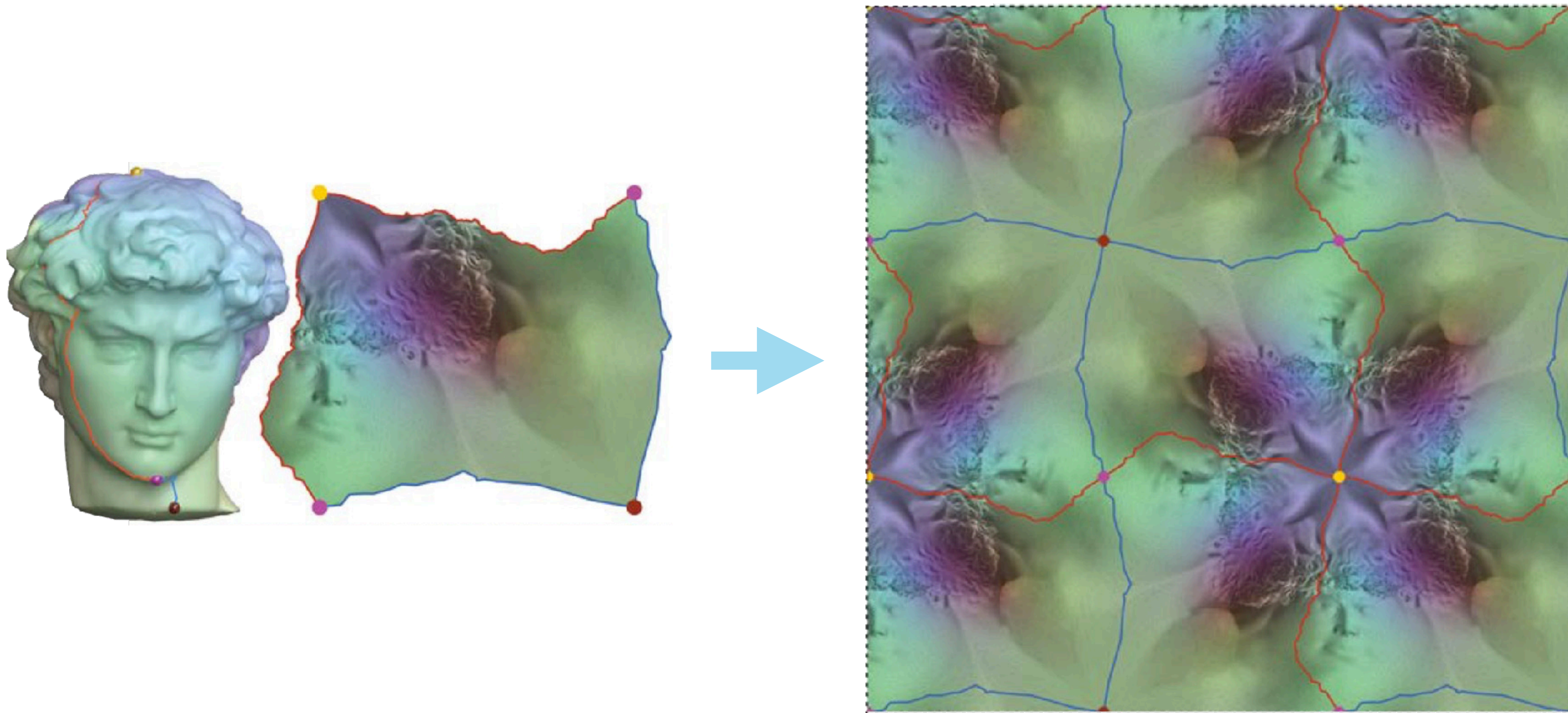
Extending to local tasks is hard



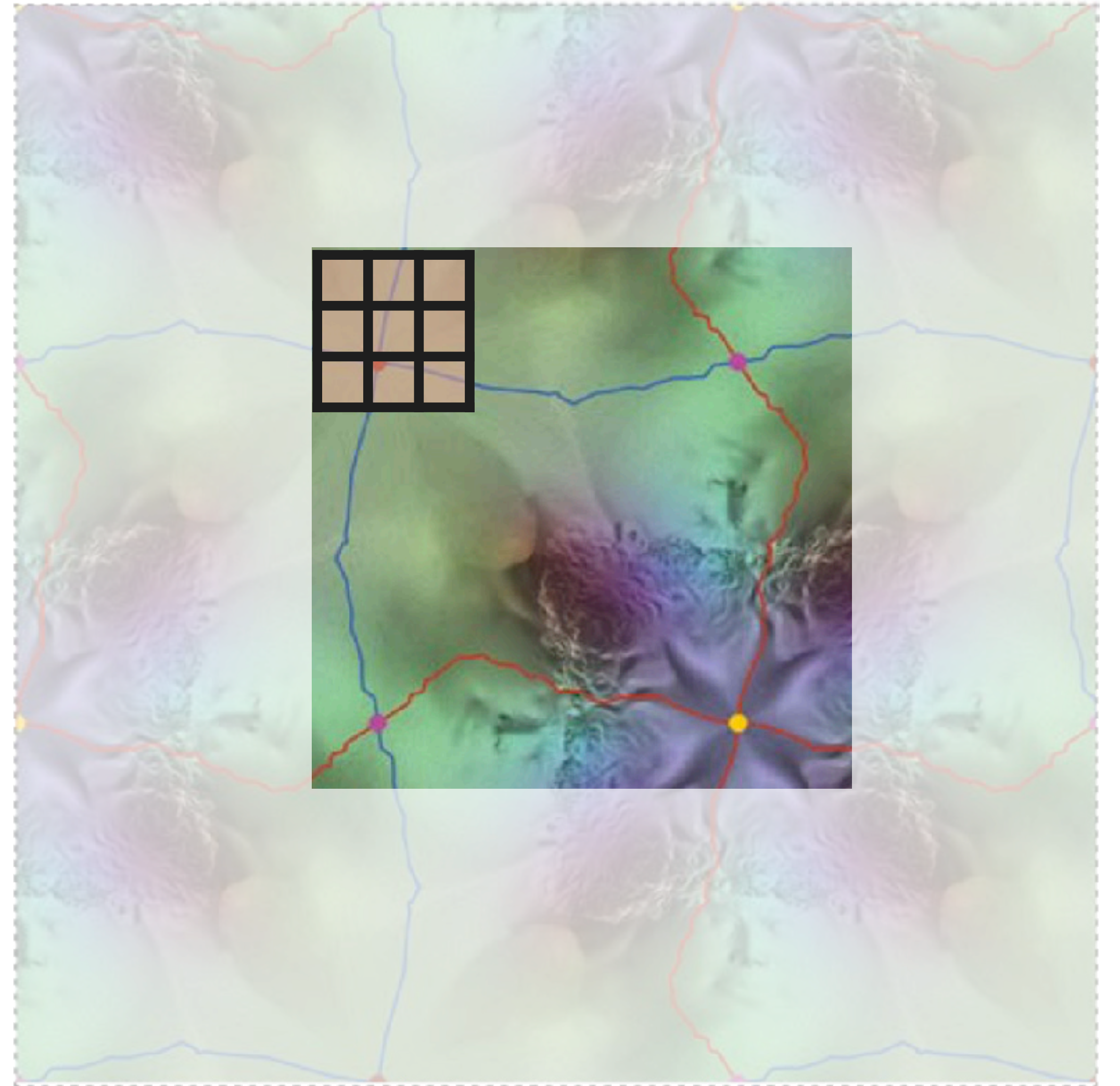
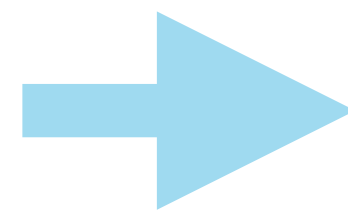
Global Parameterization



Seamless Parameterization

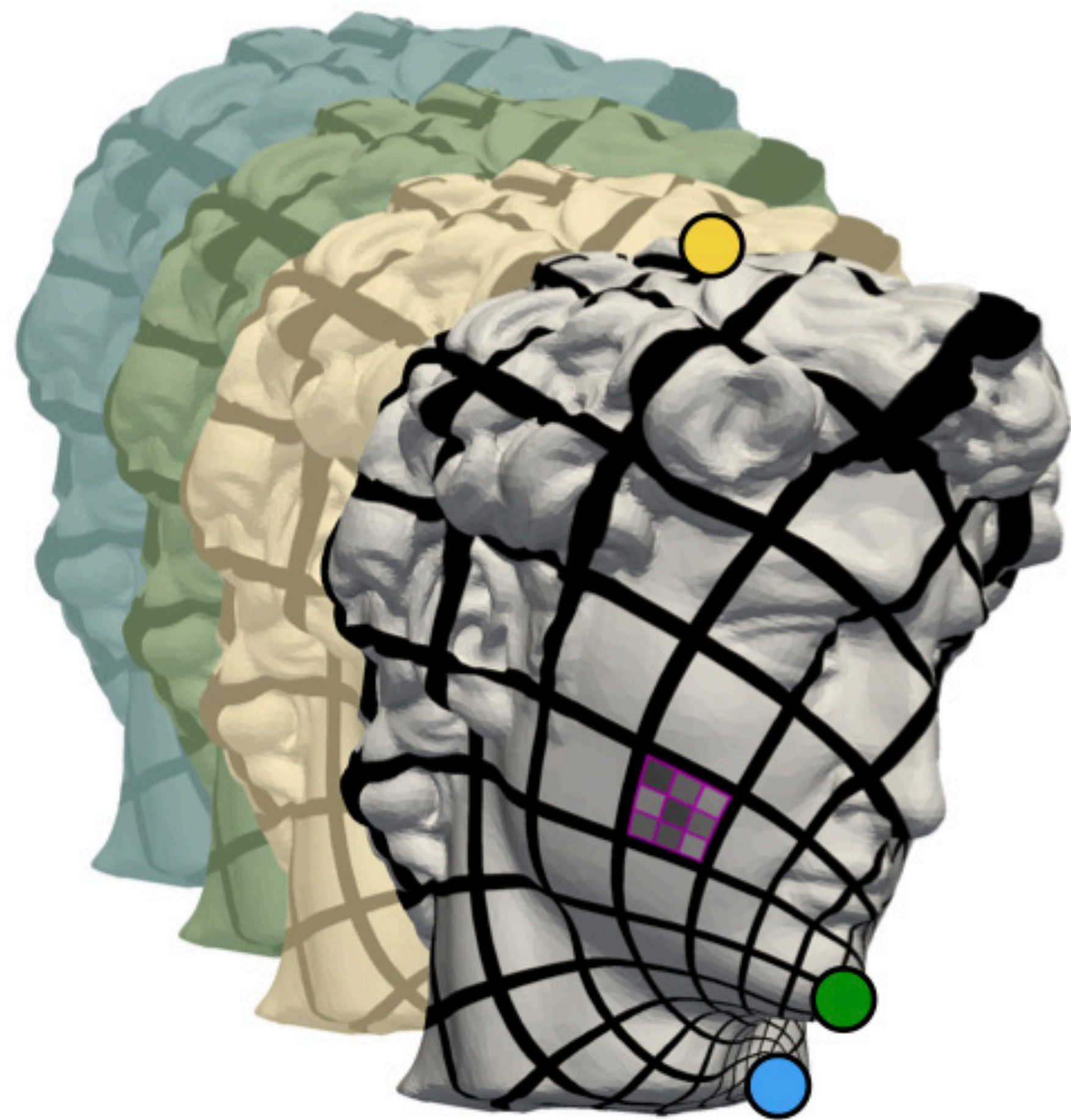


Seamless Parameterization

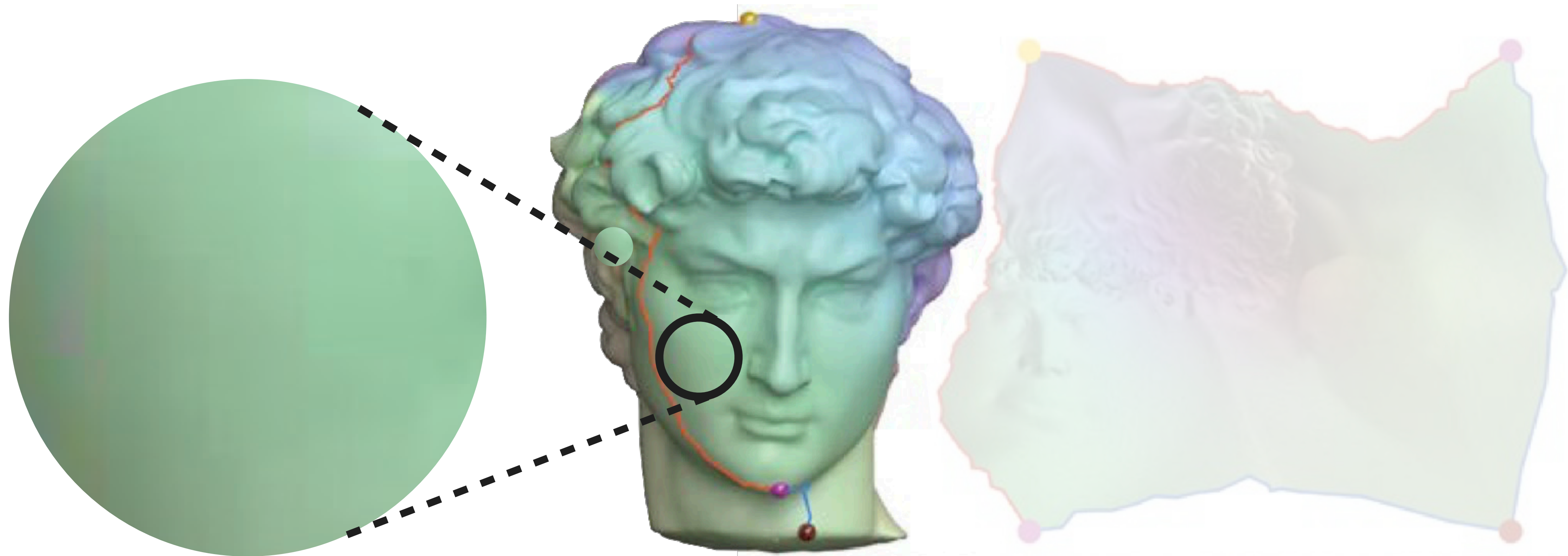


Challenges

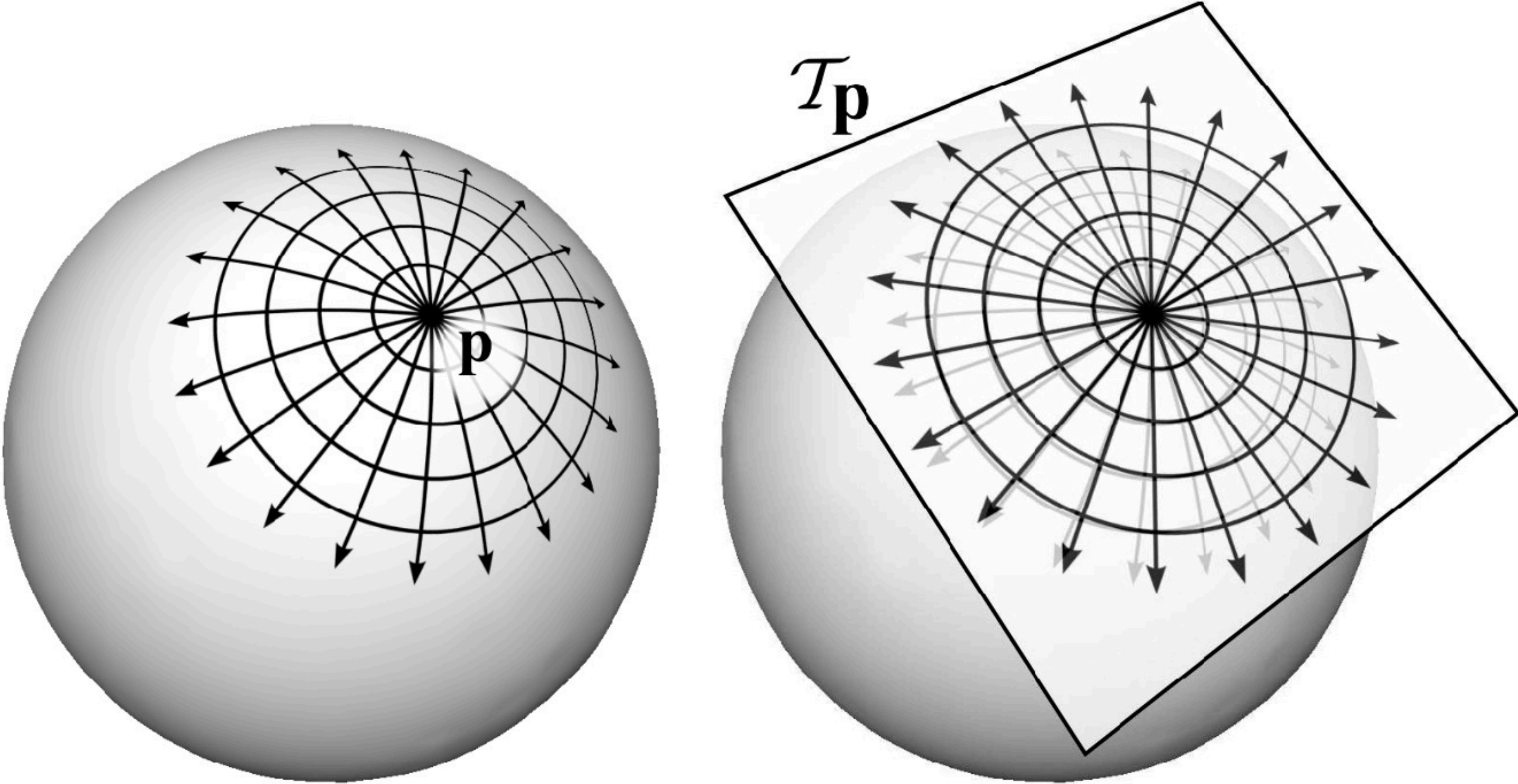
- Not unique
- Orientation
- Cannot avoid distortion



Local Parameterization

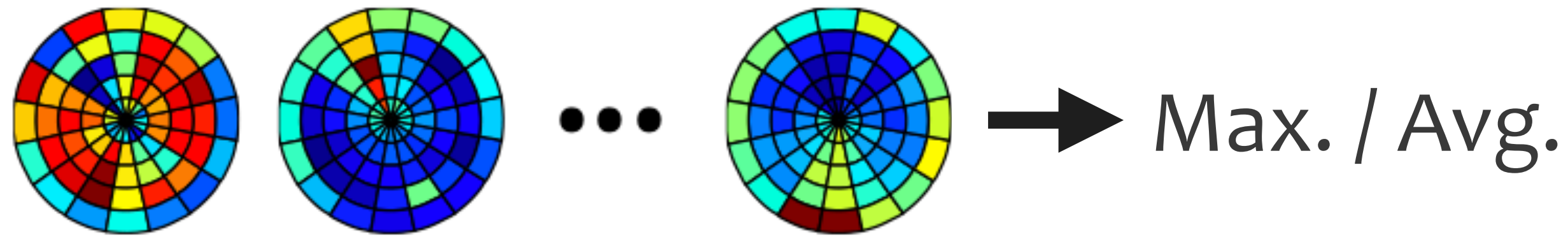


Exponential Maps

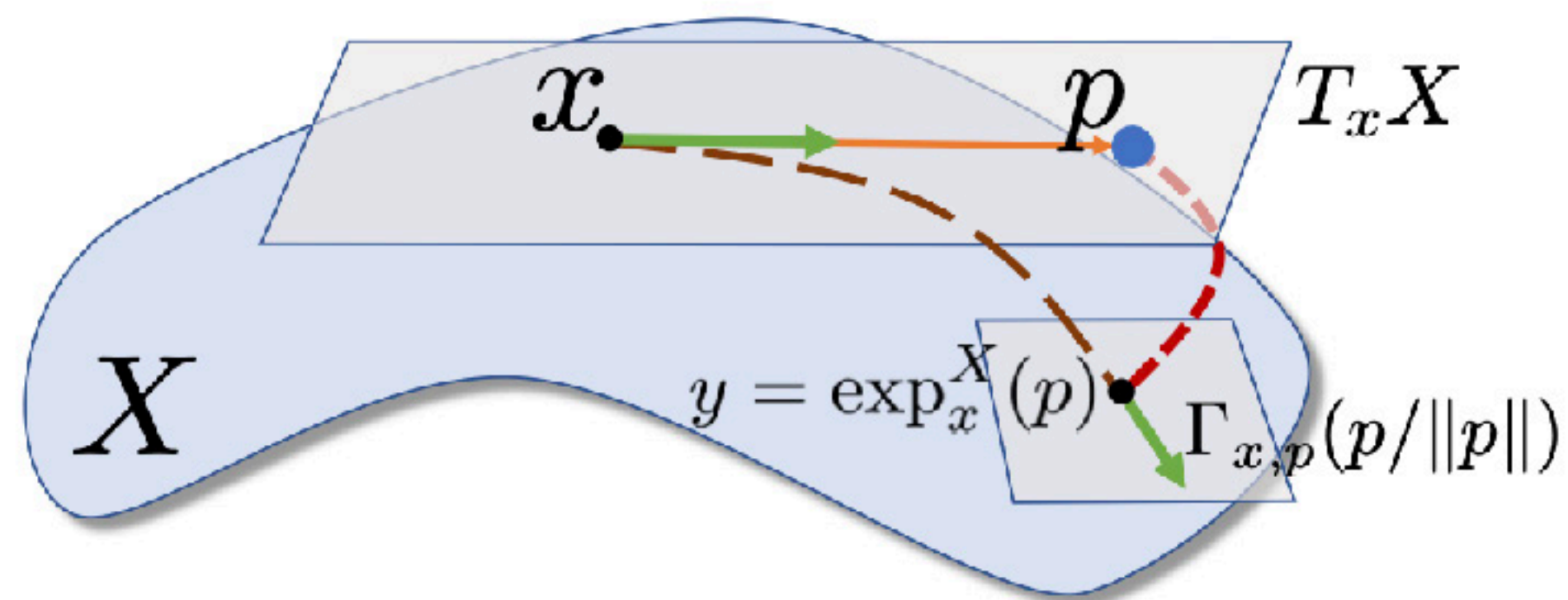


Which direction to use?

Consider all orientations
[Masci et al. 2015]



Pick one direction at a time
[Poulenard & Ovsjanikov 2018]

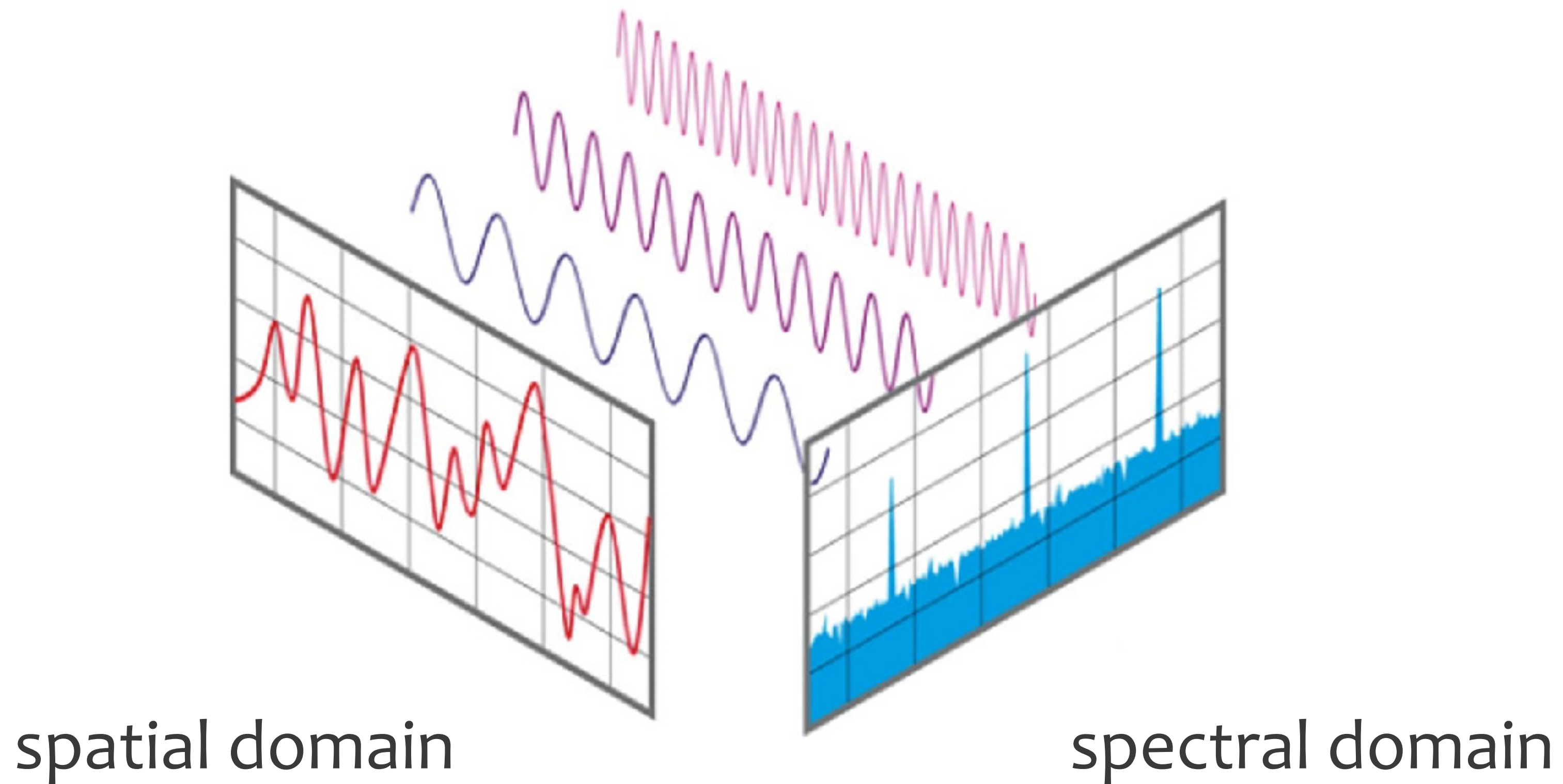


Rotation-Equivariant
[Wiersma et al. 2020]



Spectral Convolution

Convolution in the spatial domain is the **point-wise product** in the spectral domain.

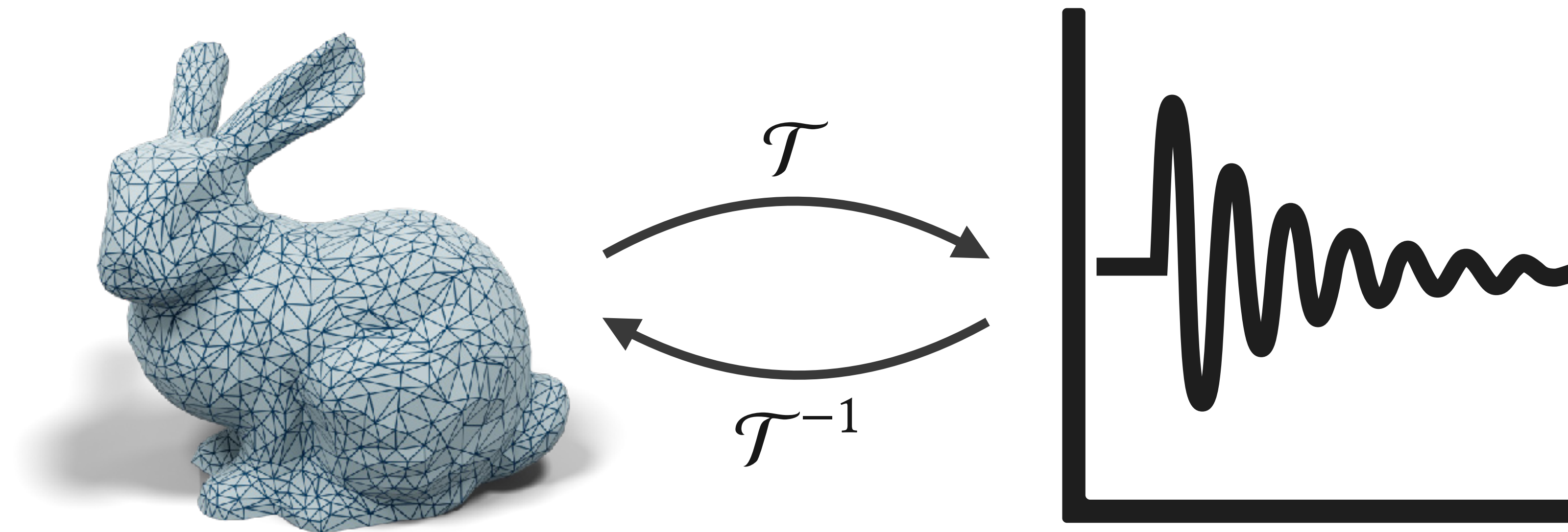


Spectral Convolution (e.g., [Defferrard et al. 2016])

$$y = \mathcal{T}^{-1} \left(w \odot \mathcal{T}(x) \right)$$

filter weights spatial signal

inverse FT FT



Issues on Efficiency, Localization, Memory

Convolutional Neural Networks on Graphs with Fast Localized Spectral Filtering

Michaël Defferrard

Xavier Bresson

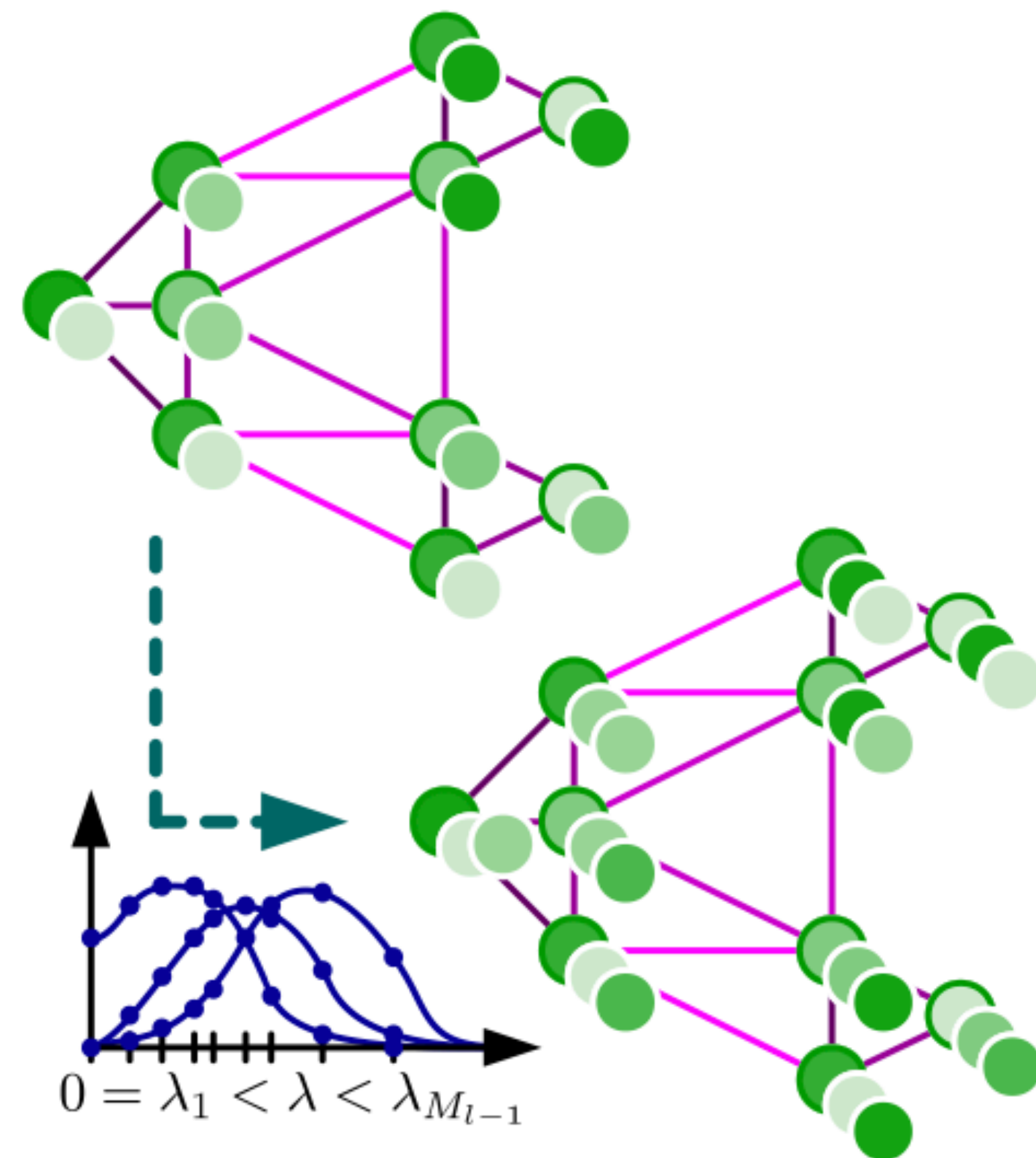
Pierre Vandergheynst

EPFL, Lausanne, Switzerland

{michael.defferrard,xavier.bresson,pierre.vandergheynst}@epfl.ch

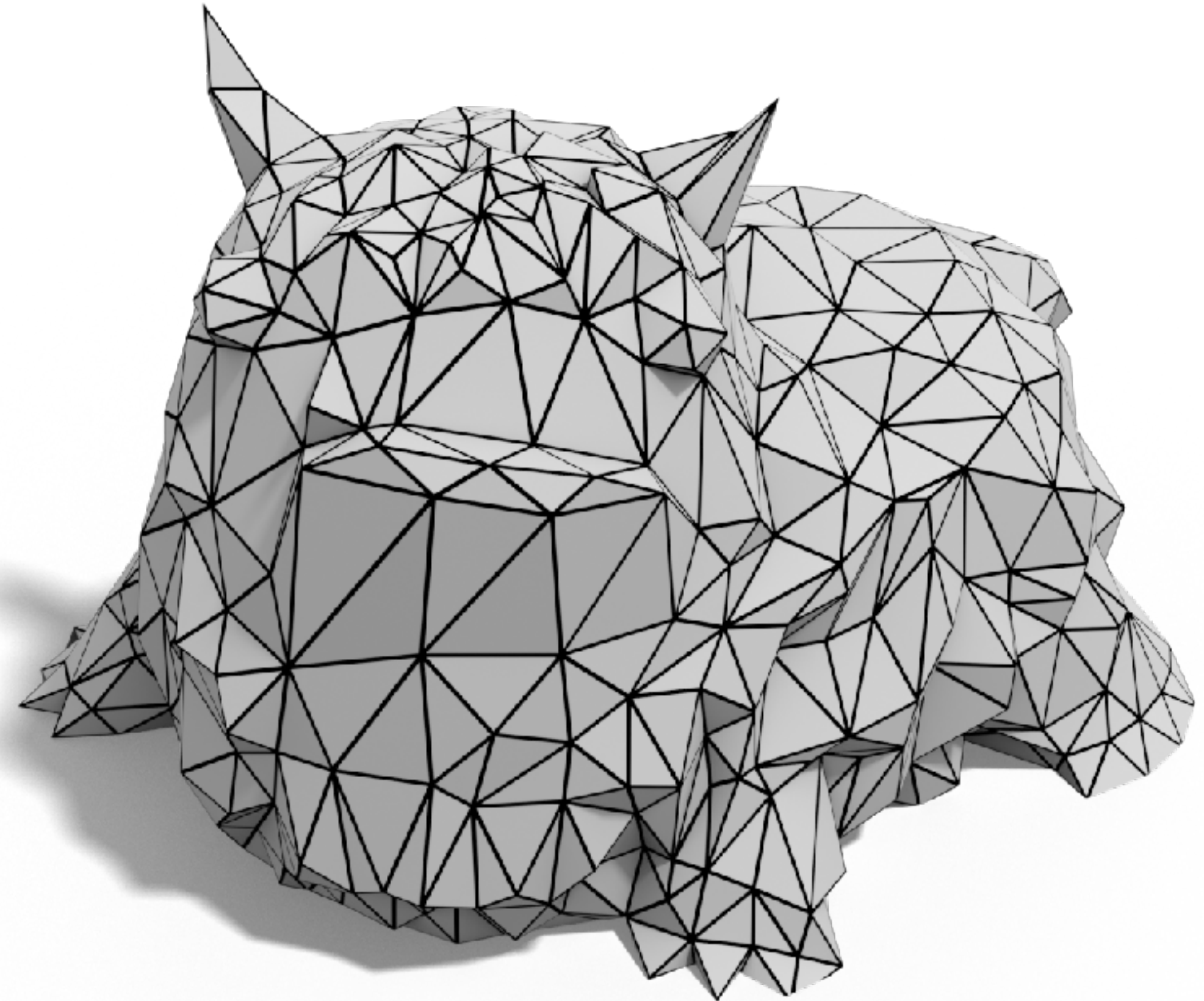
Abstract

In this work, we are interested in generalizing convolutional neural networks (CNNs) from low-dimensional regular grids, where image, video and speech are represented, to high-dimensional irregular domains, such as social networks, brain connectomes or words' embedding, represented by graphs. We present a formulation of CNNs in the context of spectral graph theory, which provides the necessary mathematical background and efficient numerical schemes to design fast localized convolutional filters on graphs. Importantly, the proposed technique offers the same linear computational complexity and constant learning complexity as classical CNNs, while being universal to any graph structure. Experiments on MNIST and 20NEWS demonstrate the ability of this novel deep learning system to learn local, stationary, and compositional features on graphs.



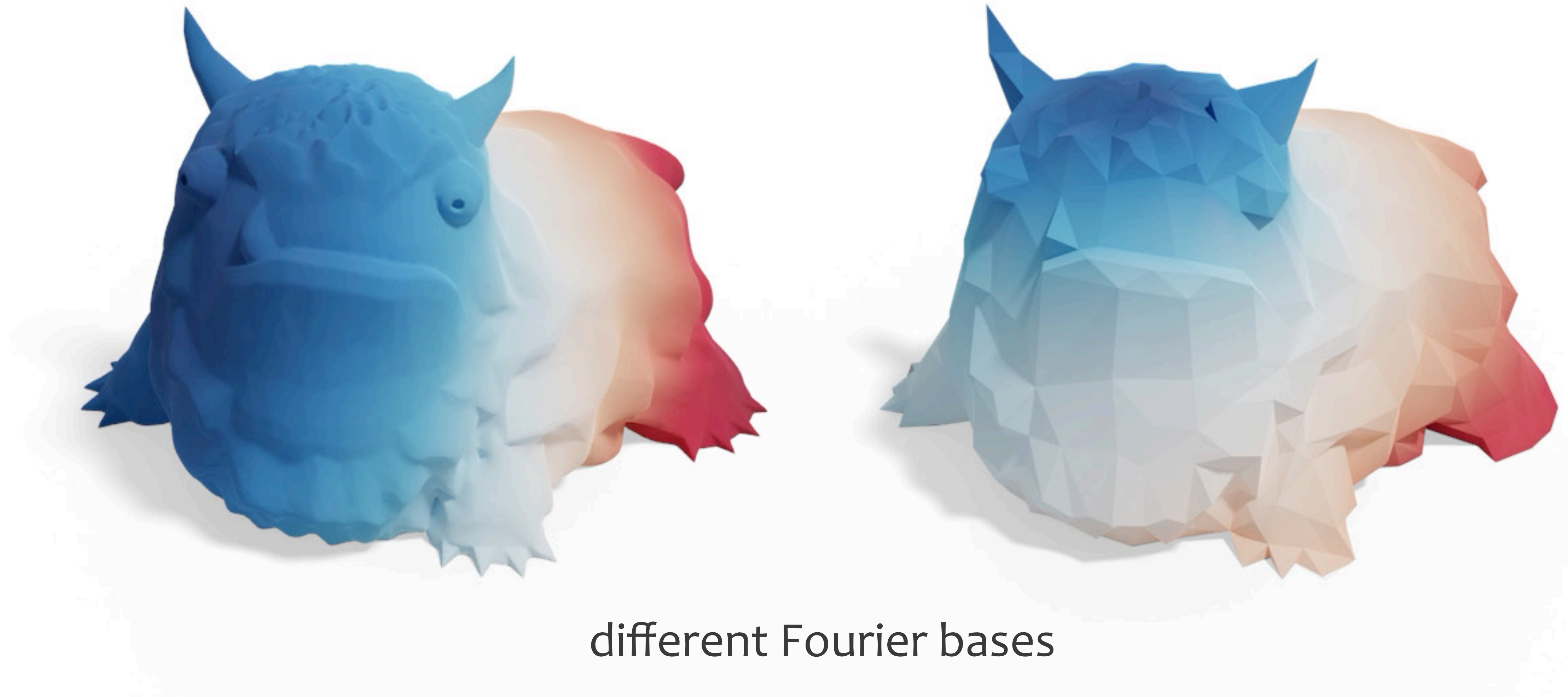
Do not generalize to other shapes

(even the same shape with a different connectivity)



Do not generalize to other shapes

(even the same shape with a different connectivity)



different Fourier bases

Synchronizing Spectral Spaces

SyncSpecCNN: Synchronized Spectral CNN for 3D Shape Segmentation

Li Yi¹ Hao Su¹ Xingwen Guo² Leonidas Guibas¹
¹Stanford University ²The University of Hong Kong

Abstract

In this paper, we study the problem of semantic annotation on 3D models that are represented as shape graphs. A functional view is taken to represent localized information on graphs, so that annotations such as part segment or keypoint are nothing but 0-1 indicator vertex functions. Compared with images that are 2D grids, shape graphs are irregular and nonisomorphic data structures. To enable the prediction of vertex functions on them by convolutional neural networks, we resort to spectral CNN method that enables weight sharing by parameterizing kernels in the spectral domain spanned by graph laplacian eigenbases. Under this setting, our network, named SyncSpecCNN, strive to overcome two key challenges: how to share coefficients and conduct multi-scale analysis in different parts of the graph for a single shape, and how to share information across related but different shapes that may be represented by very different graphs. Towards these goals, we introduce a spectral parameterization of dilated convolutional kernels and a spectral transformer network. Experimentally we tested our SyncSpecCNN on various tasks, including 3D shape part segmentation and 3D keypoint prediction. State-of-the-art performance has been achieved on all benchmark datasets.

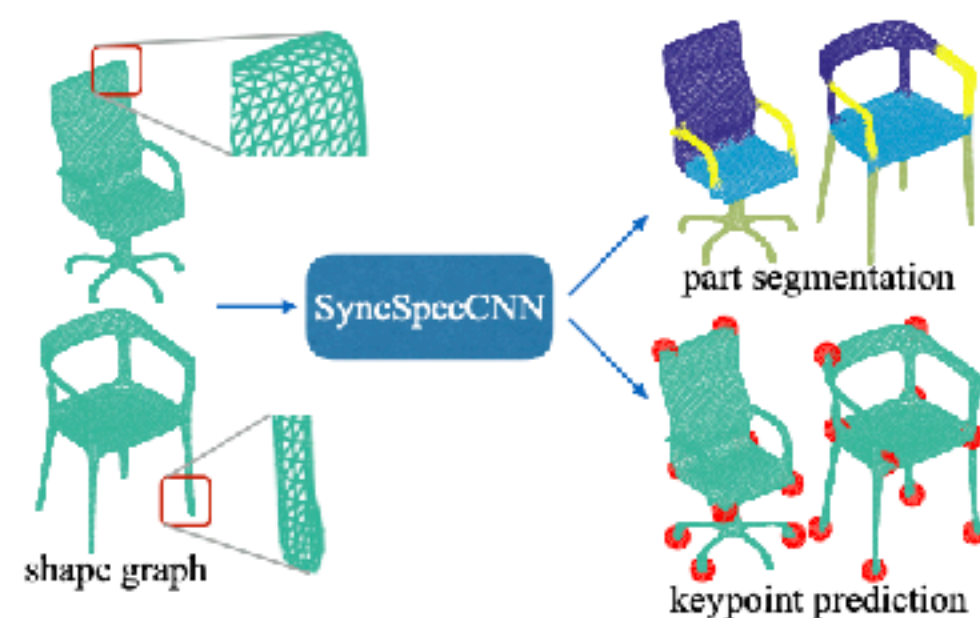
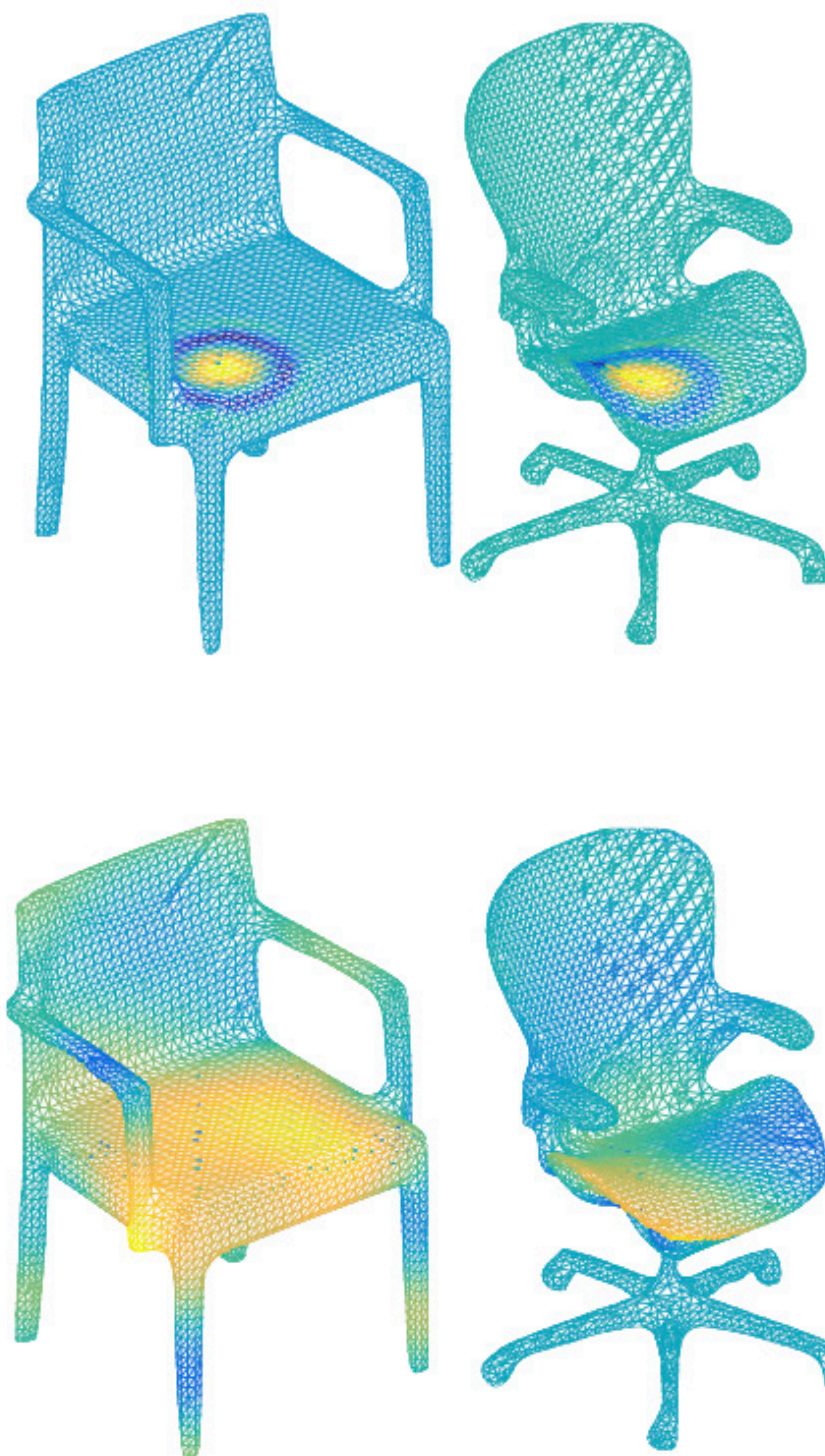


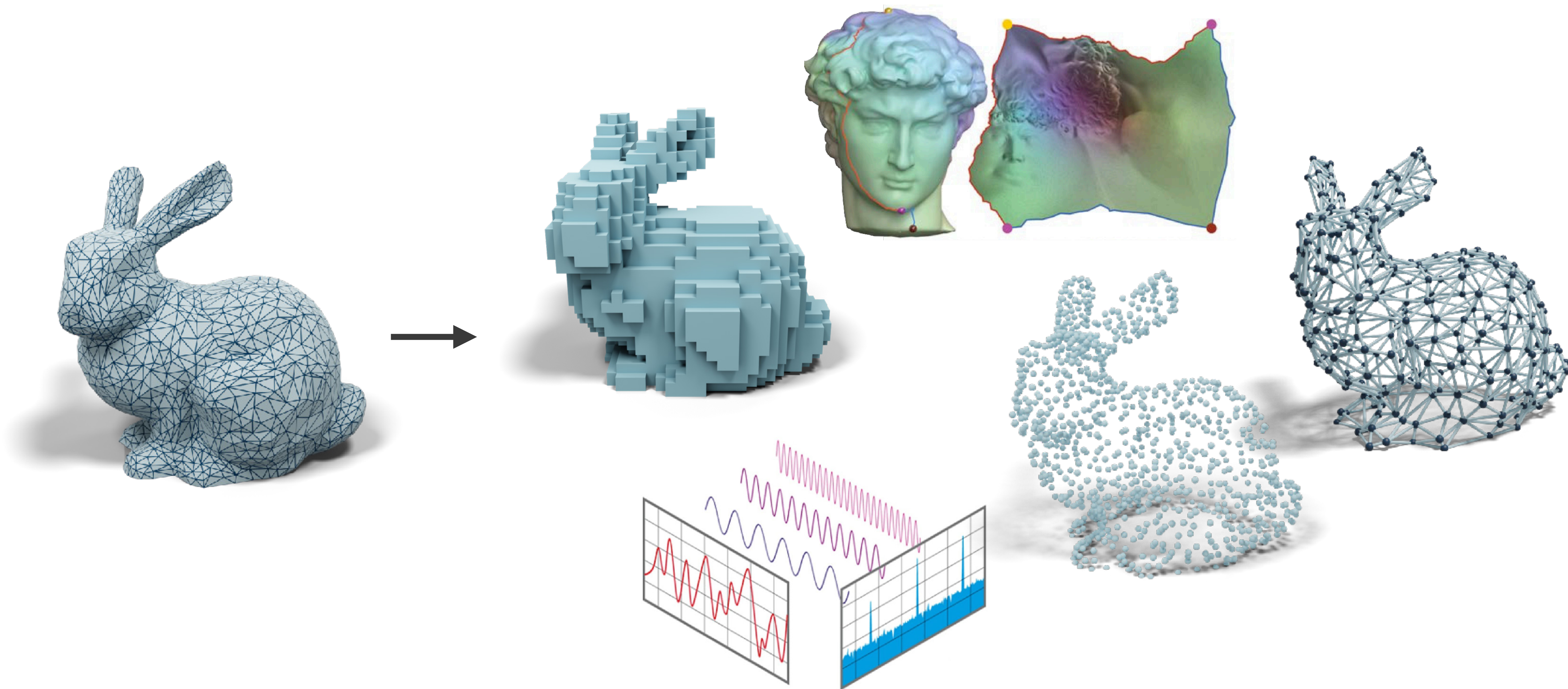
Figure 1. Our SyncSpecCNN takes a shape graph equipped with vertex functions (i.e. spatial coordinate function) as input and predicts a per-vertex label. The framework is general and not limited to a specific type of output. We show 3D part segmentation and 3D keypoint prediction as example outputs here.

It is not straightforward to apply traditional deep learning approaches to 3D models because a mesh representation can be combinatorially irregular and does not permit the optimizations exploited by convolutional approaches, such as weight sharing, which depend on regular grid structures. In this paper we take a functional approach to represent information about shapes, starting with the observation that a shape part is itself nothing but a 0-1 indicator function defined on the shape.

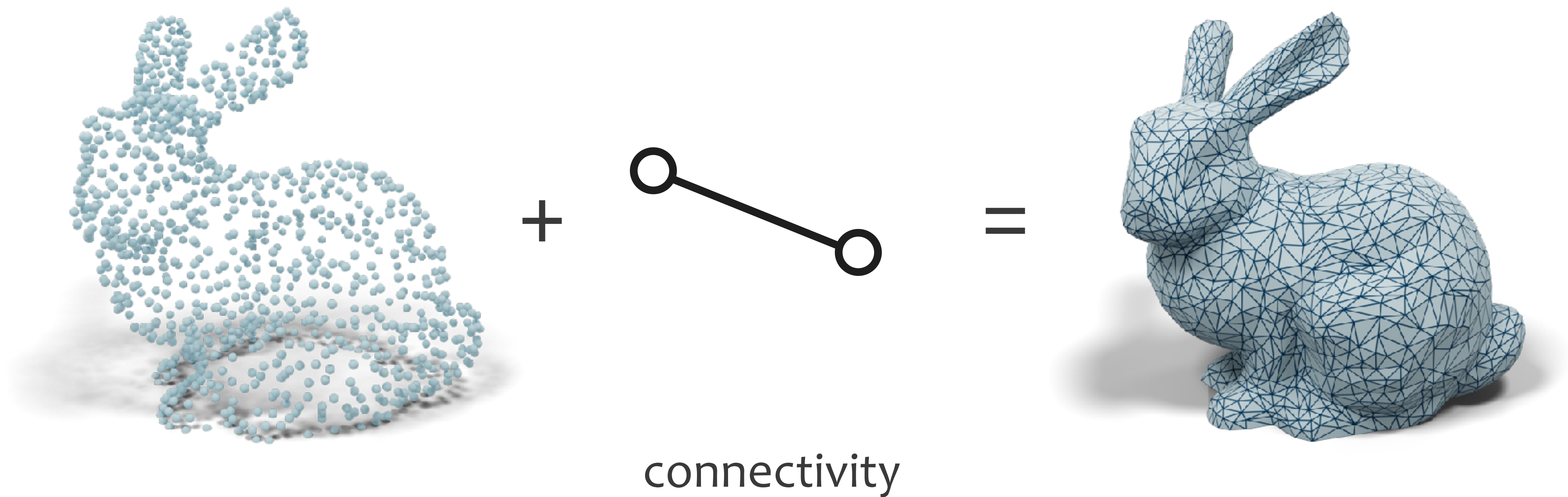
Our basic problem is to learn functions on shapes. We start with example functions provided on a given shape



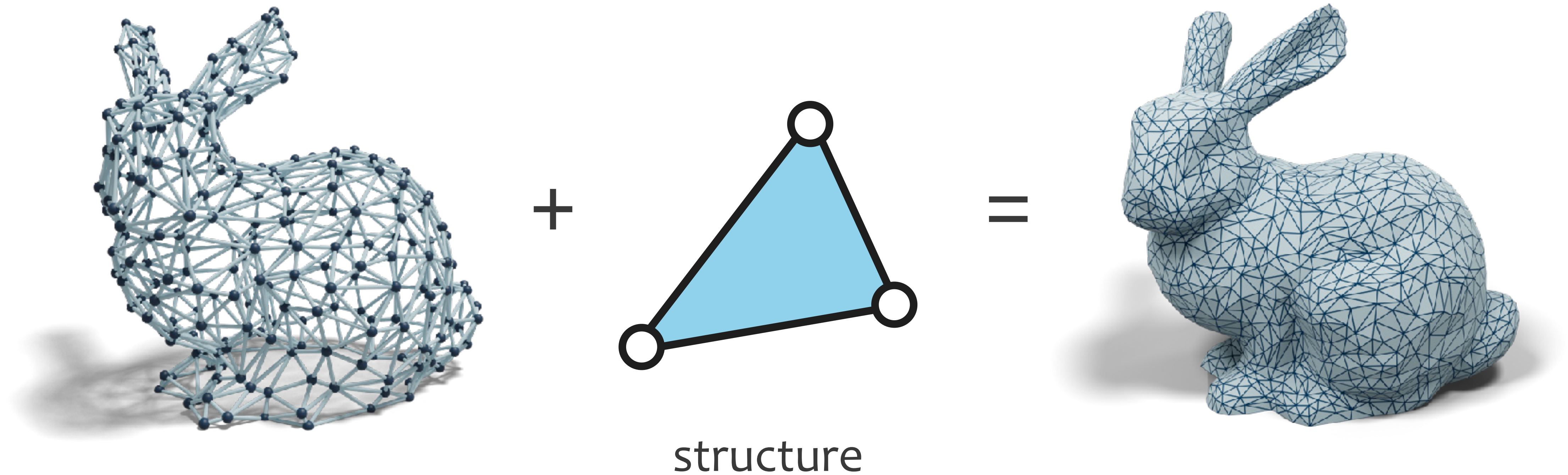
Different representations



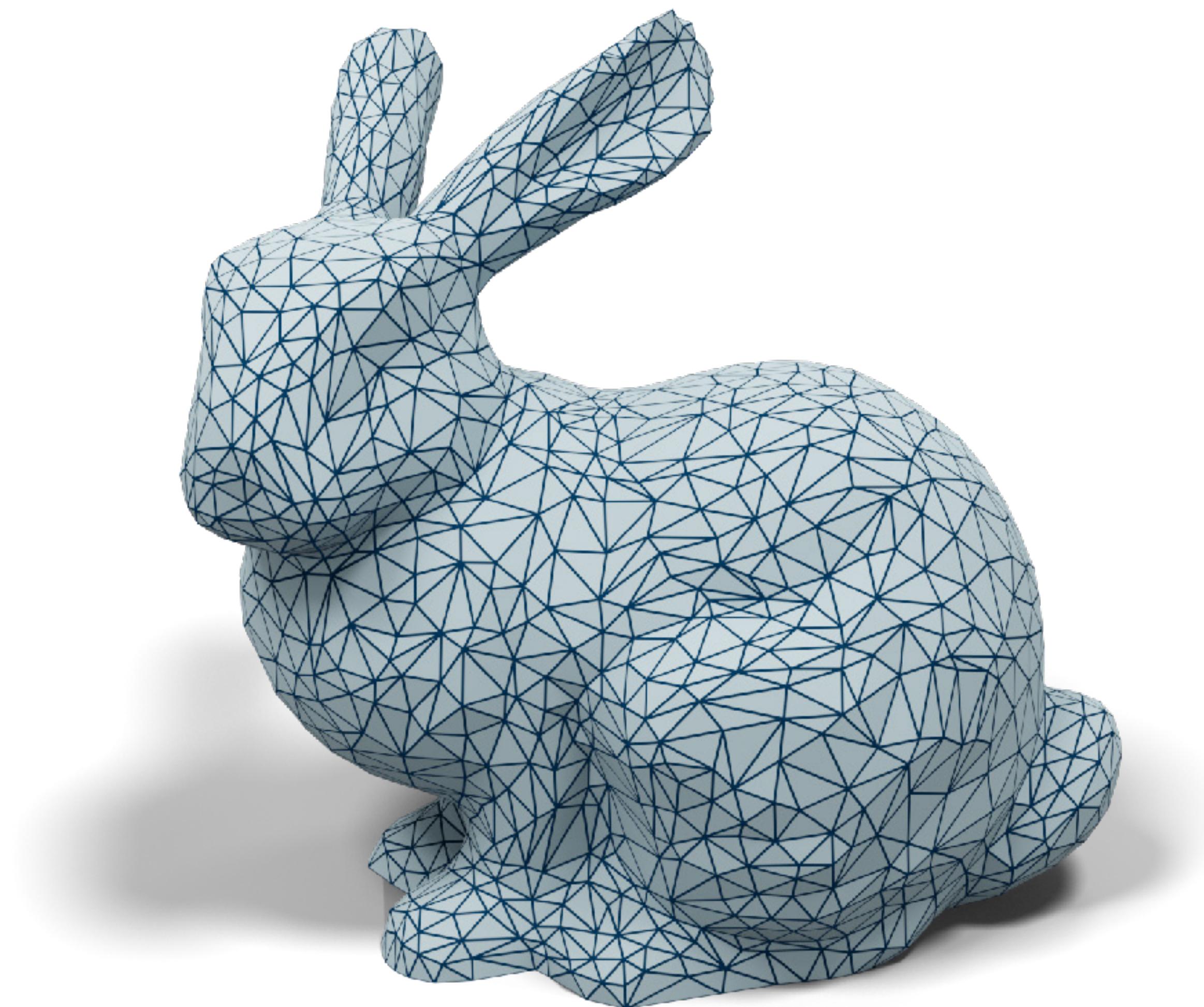
Why not point cloud convolution?



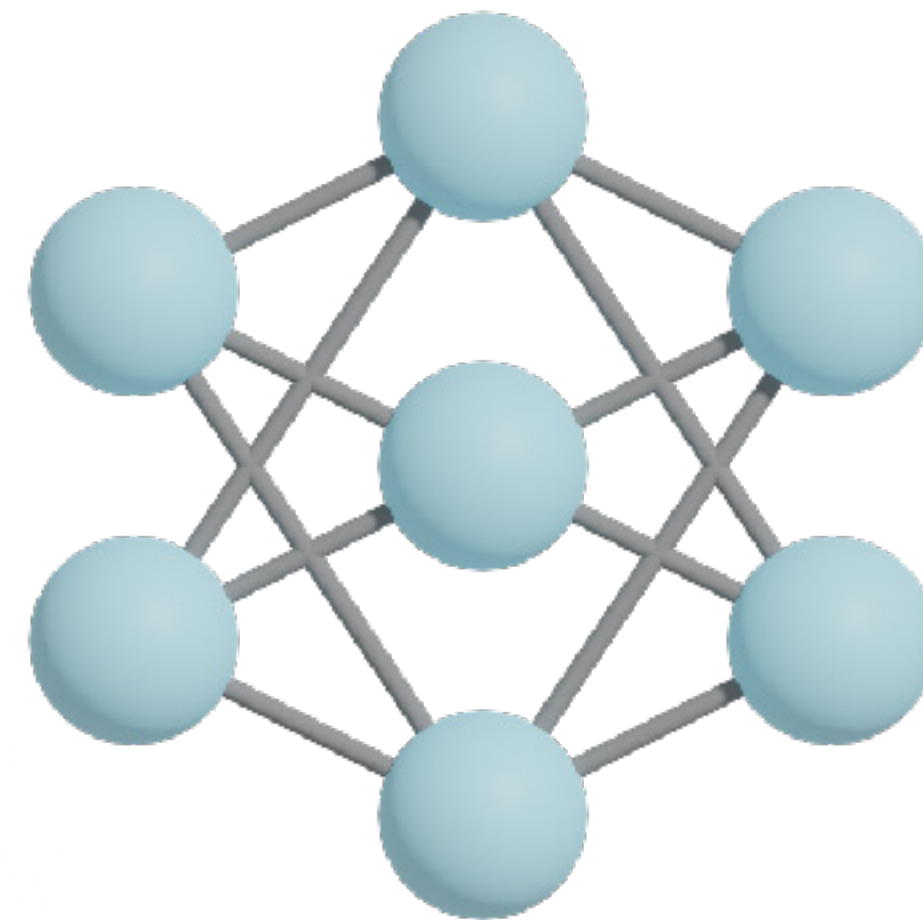
Why not graph convolution?



Surface Meshes



Neural Networks on Meshes



Example Outputs

Global shape descriptor

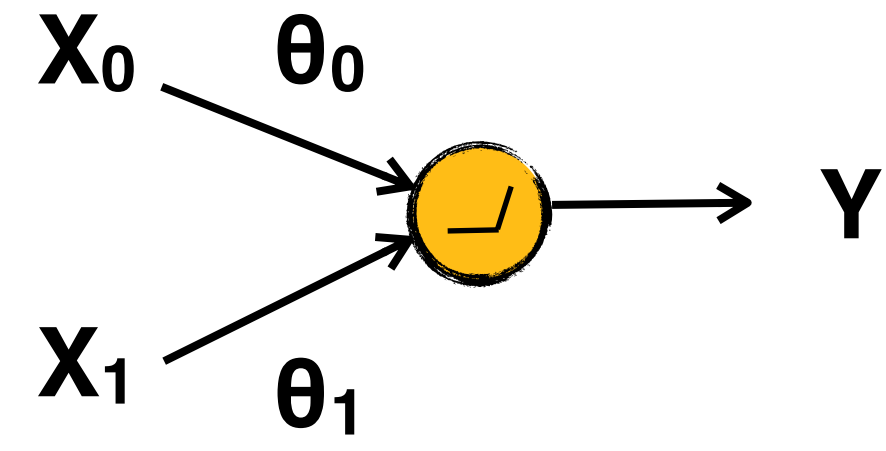
Probability to collapse an edge

Displacement per vertex

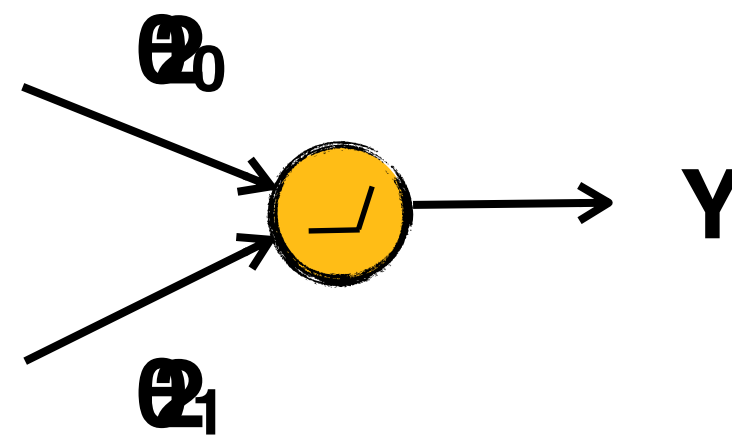
Segmentation label per-face

⋮

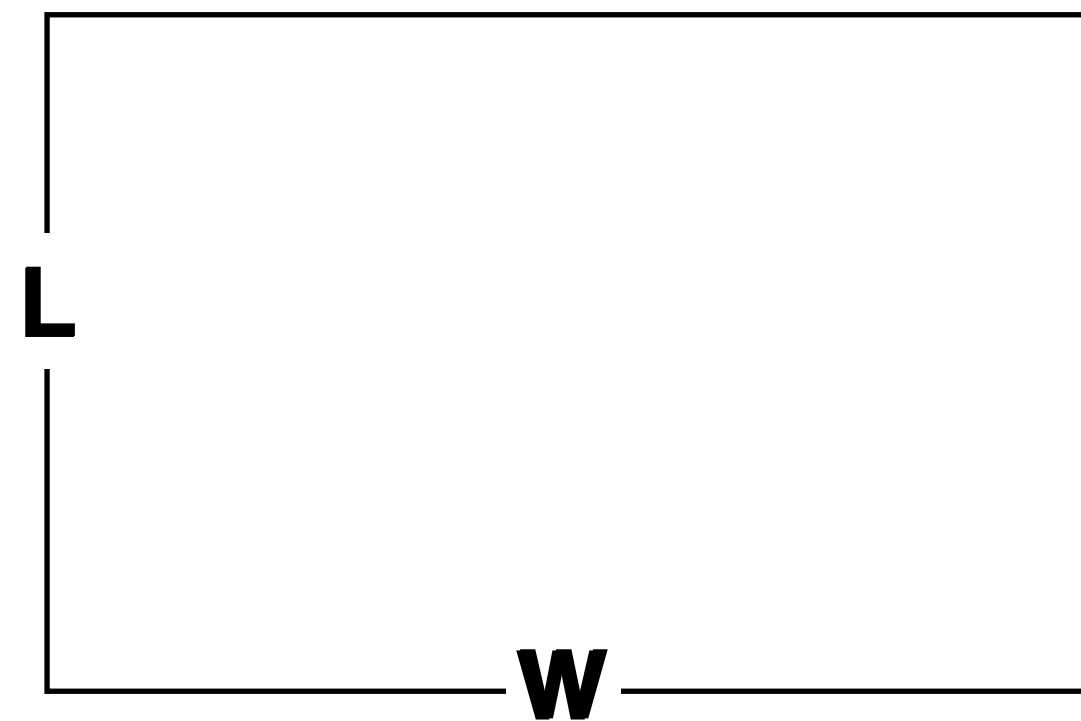
Neuron



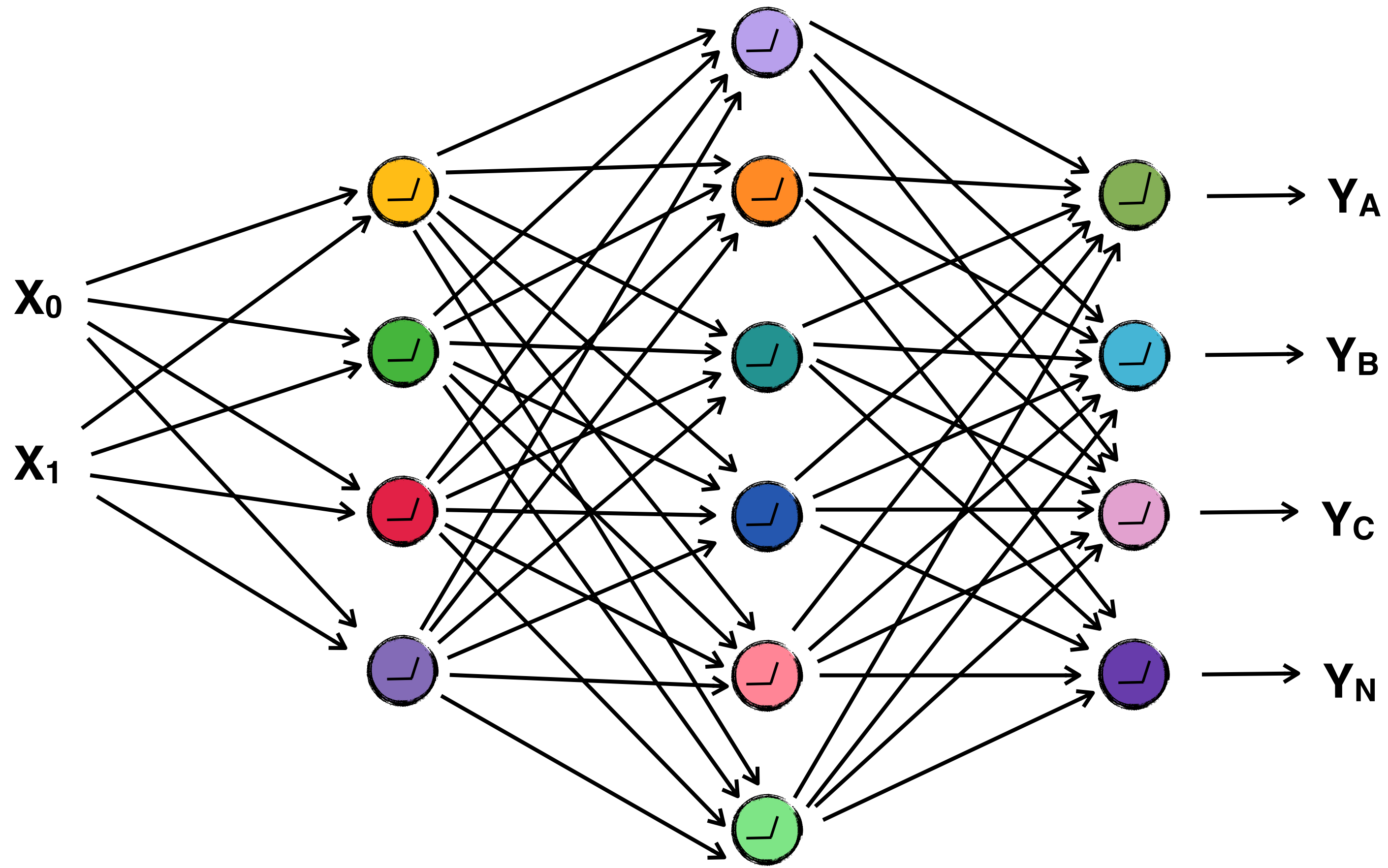
Neuron



$$Y = \text{ReLU}(2 \times L + 2 \times W)$$

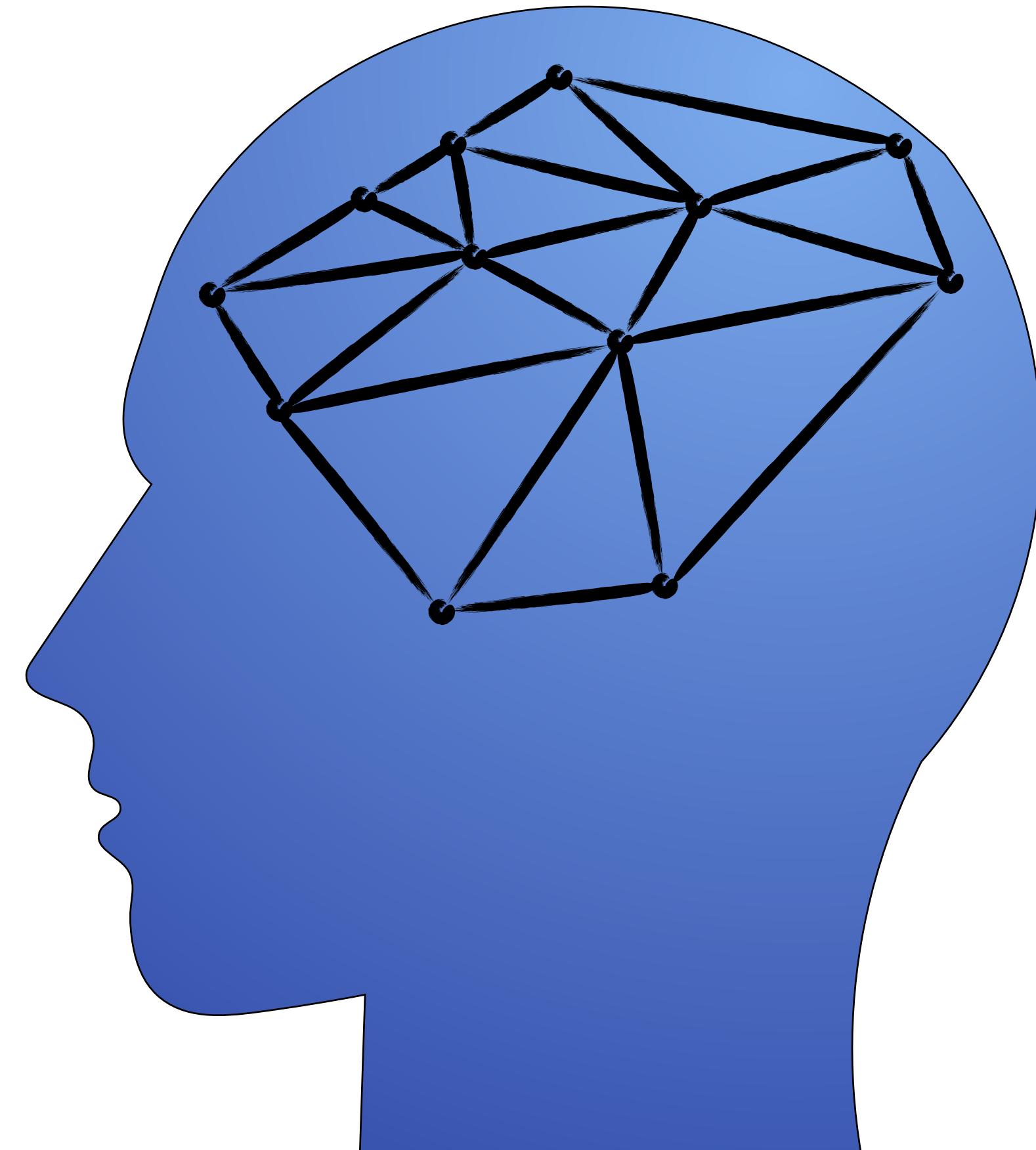


Fully-connected



Inductive Bias

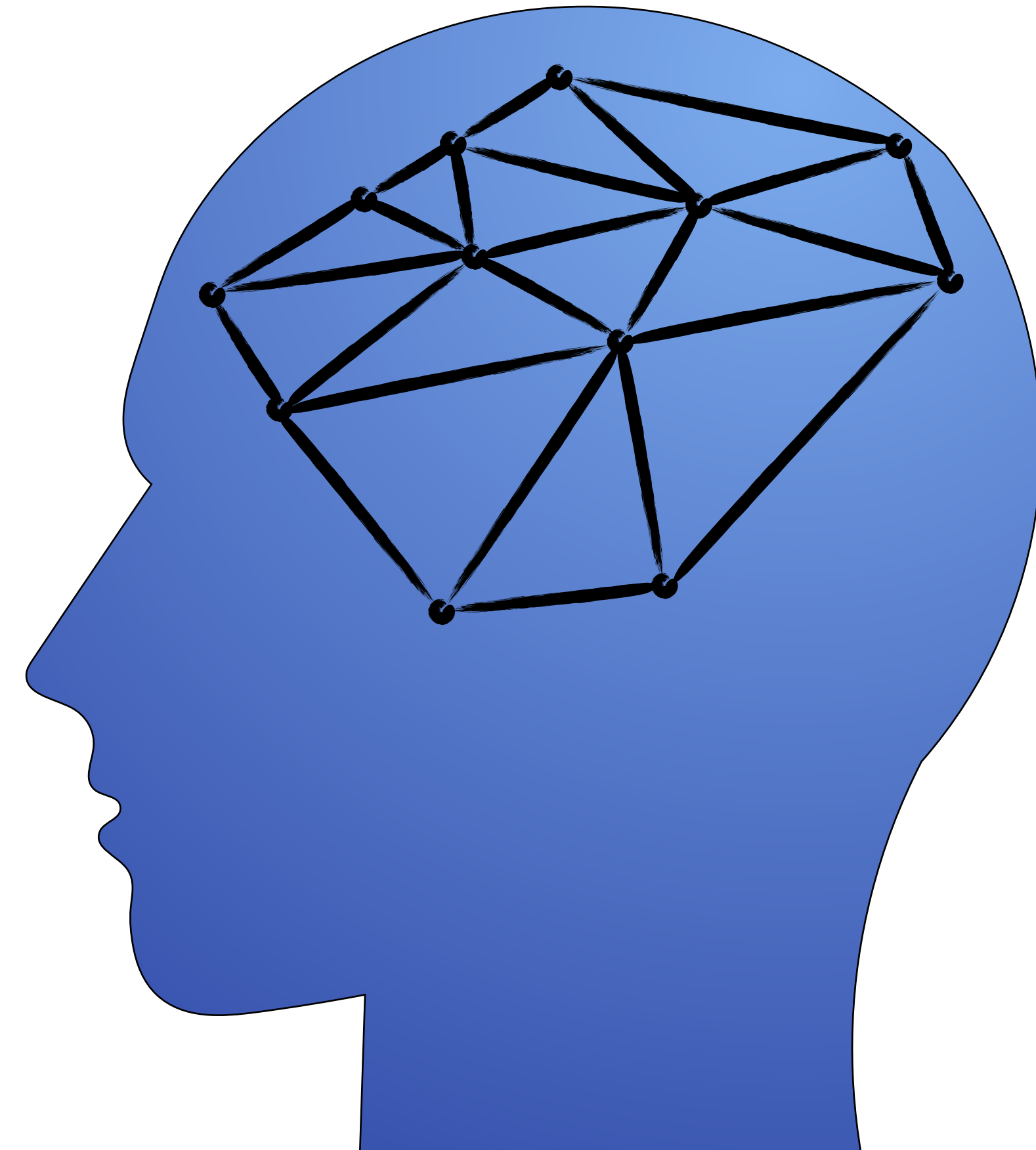
The set of assumptions that we encode into our network, which make it better suited for the task



Good **Inductive Bias**

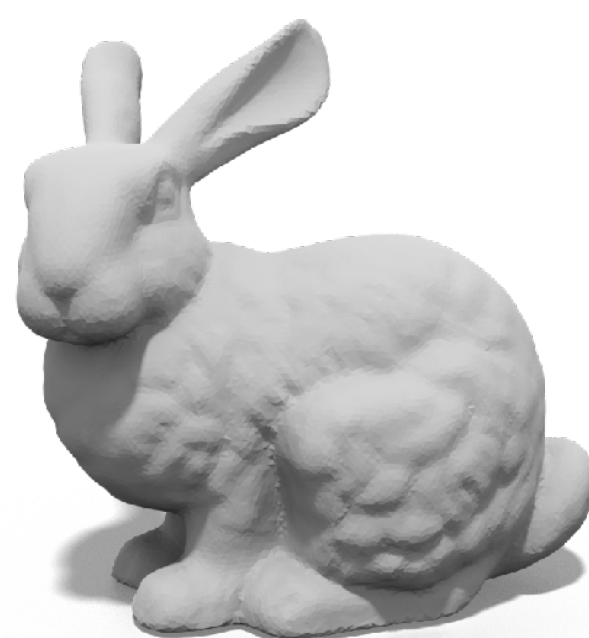


*Robust to irrelevant
variations of the input*

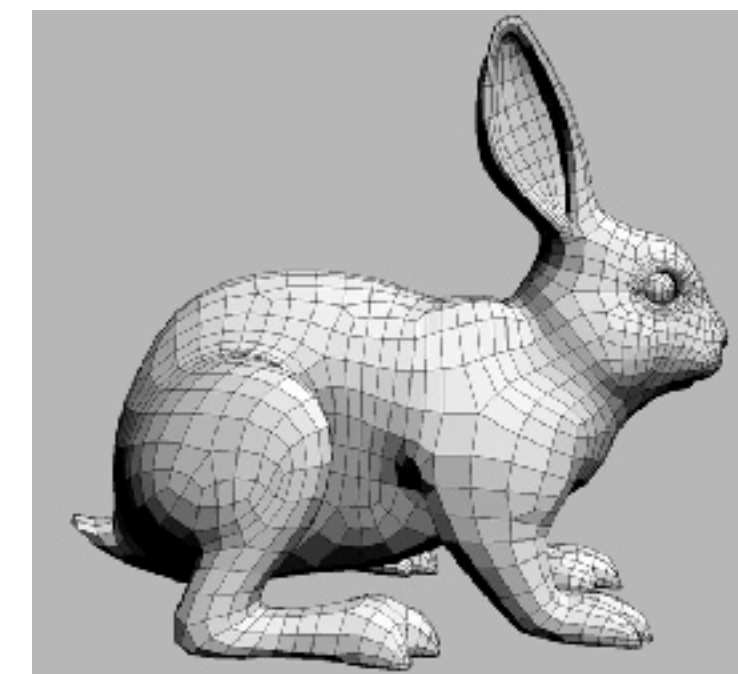




Local tasks



\approx



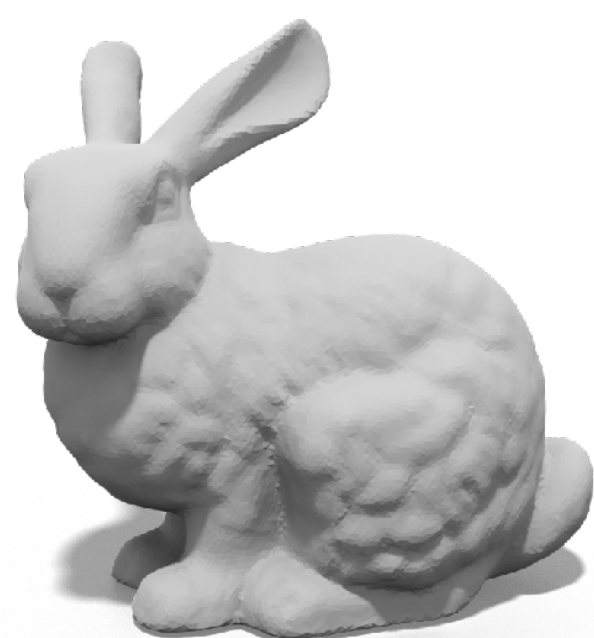
\neq



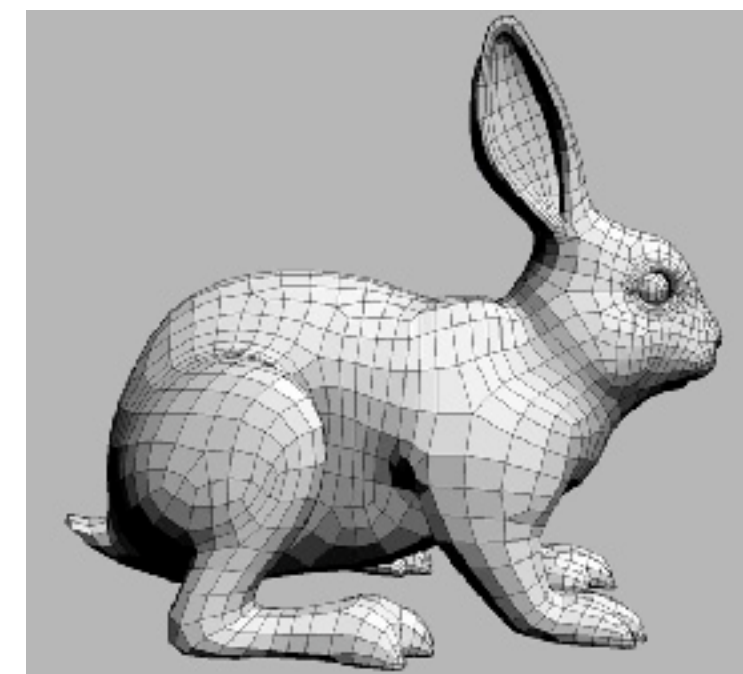
Global tasks



Local tasks



\approx



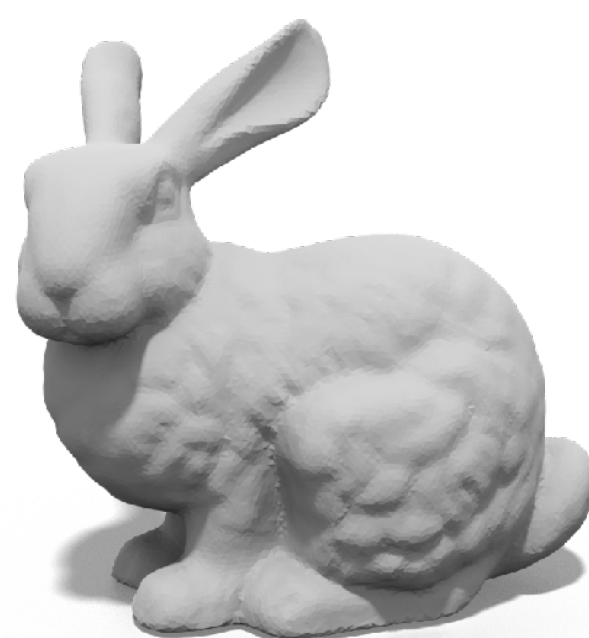
\neq



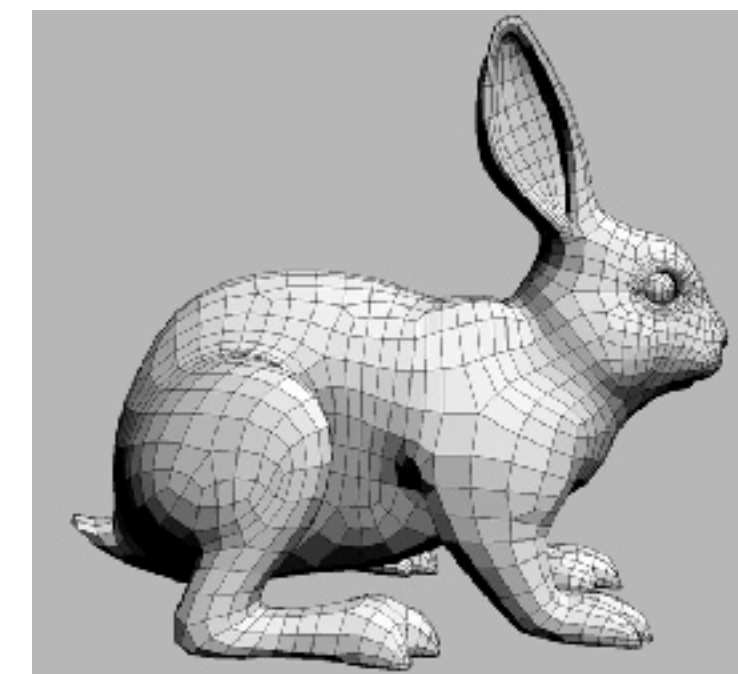
Global tasks



Local tasks



\approx



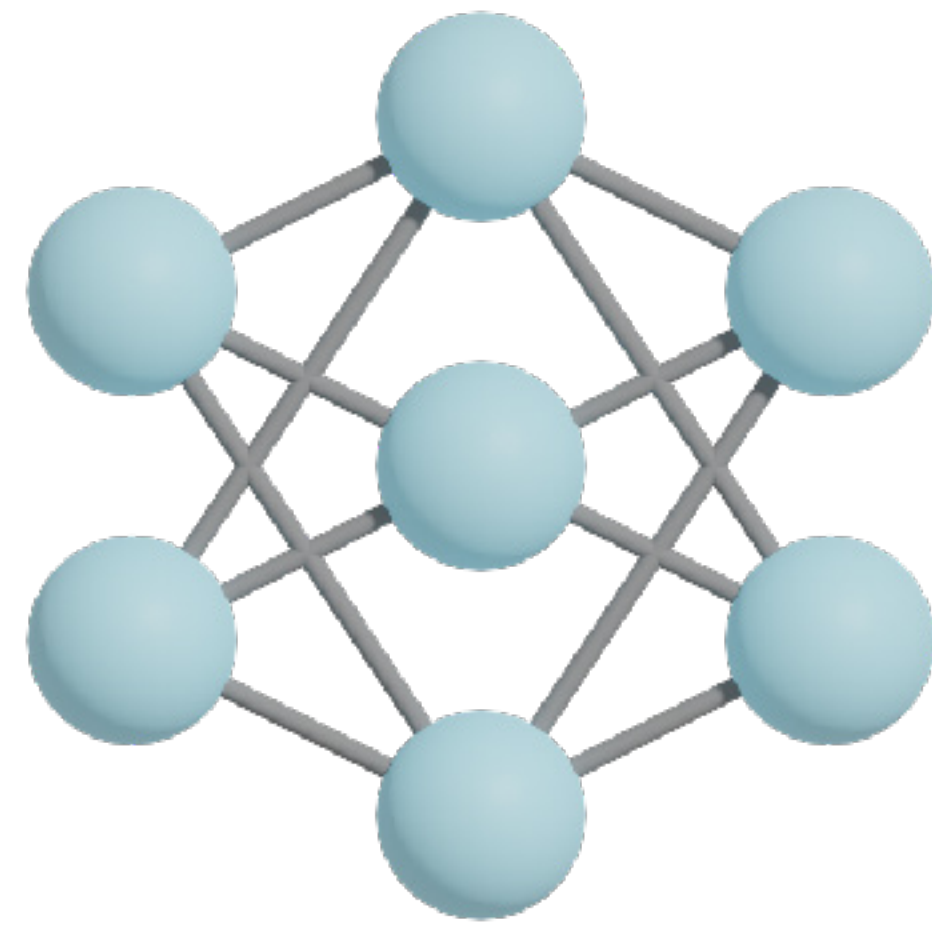
\neq



Global tasks

Local task

predict values per mesh element

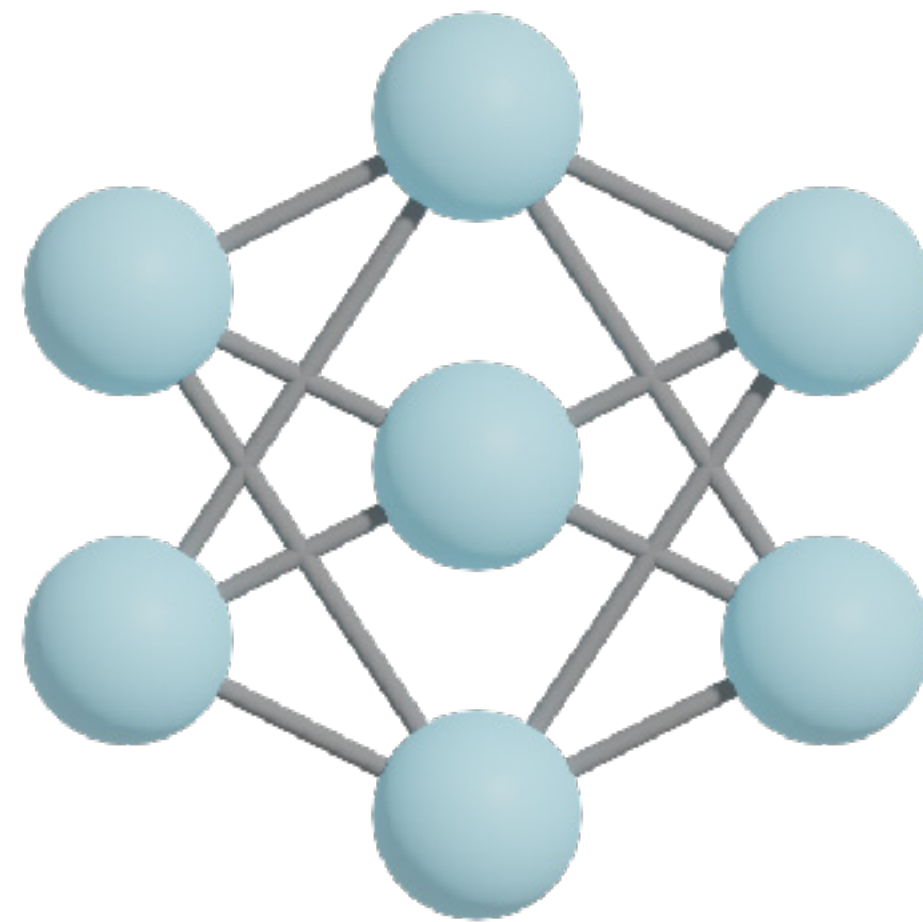


Local task

predict values per mesh element

Faces

f_0
 f_1
 f_2
 f_3
 f_4
 \vdots
 f_N



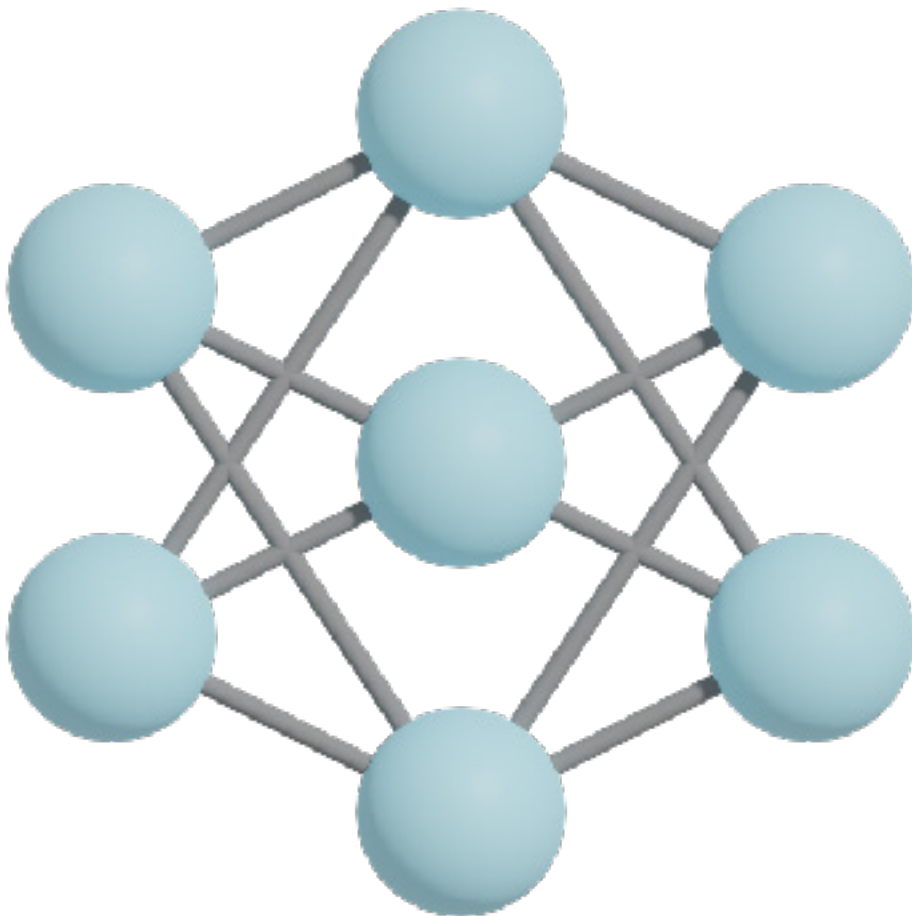
seat
legs
back
seat
legs
 \vdots
seat

Local task

predict values per mesh element

Faces

- f_0
- f_1
- f_2
- f_3
- f_4
- \vdots
- f_N

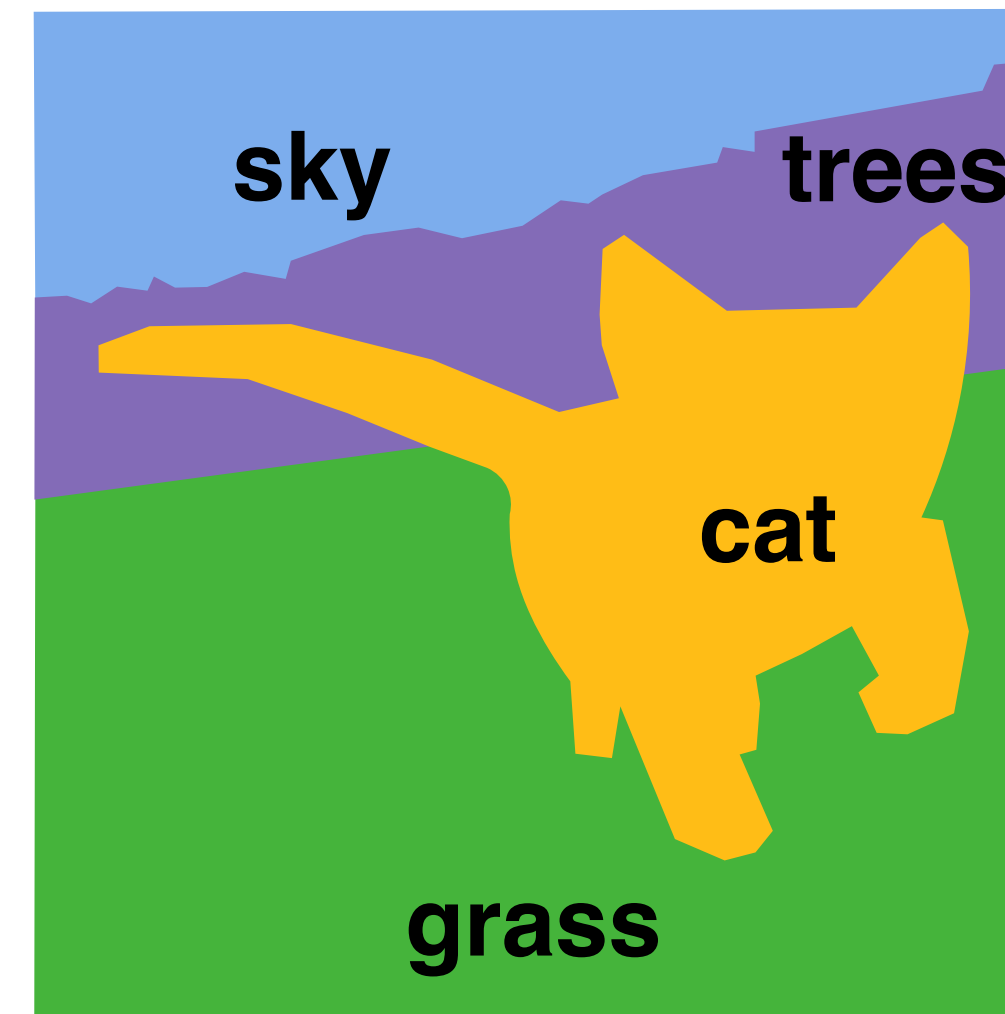
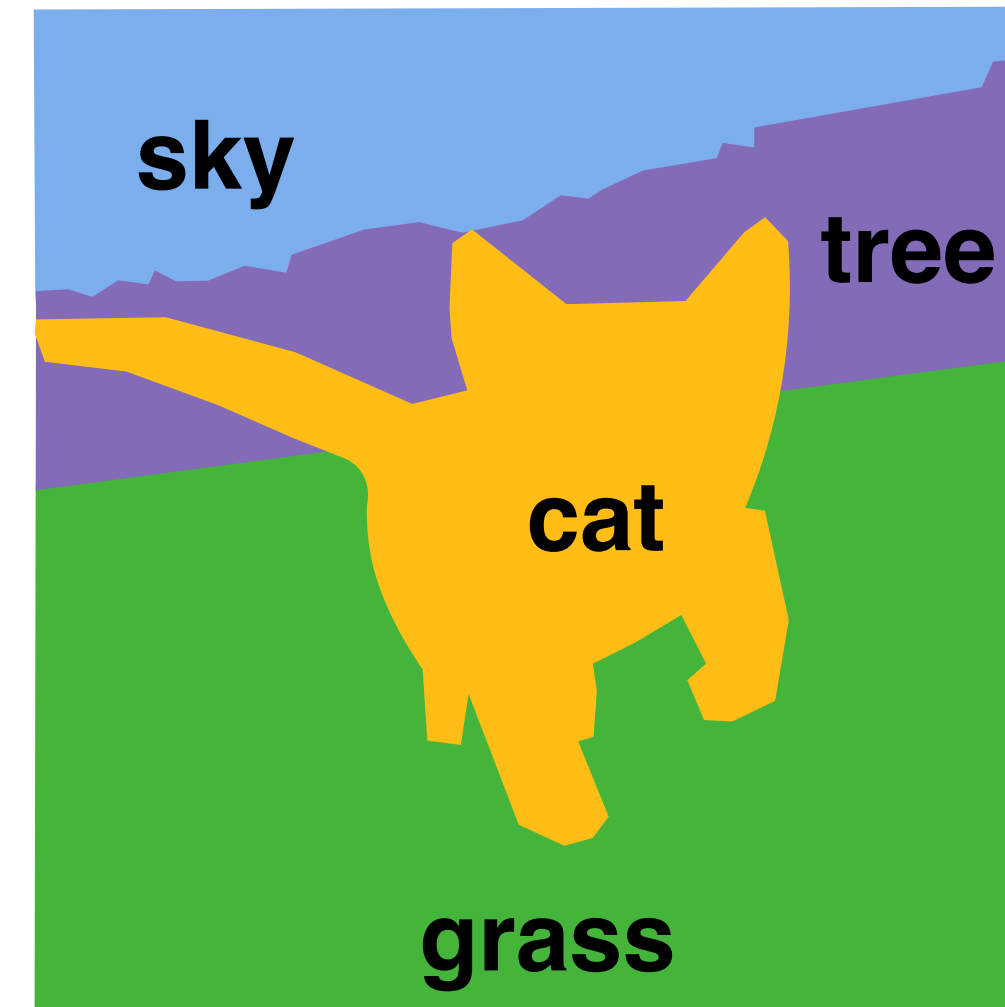


- seat
- legs
- back
- seat
- legs
- \vdots
- seat

Fully connected network not suitable for this task

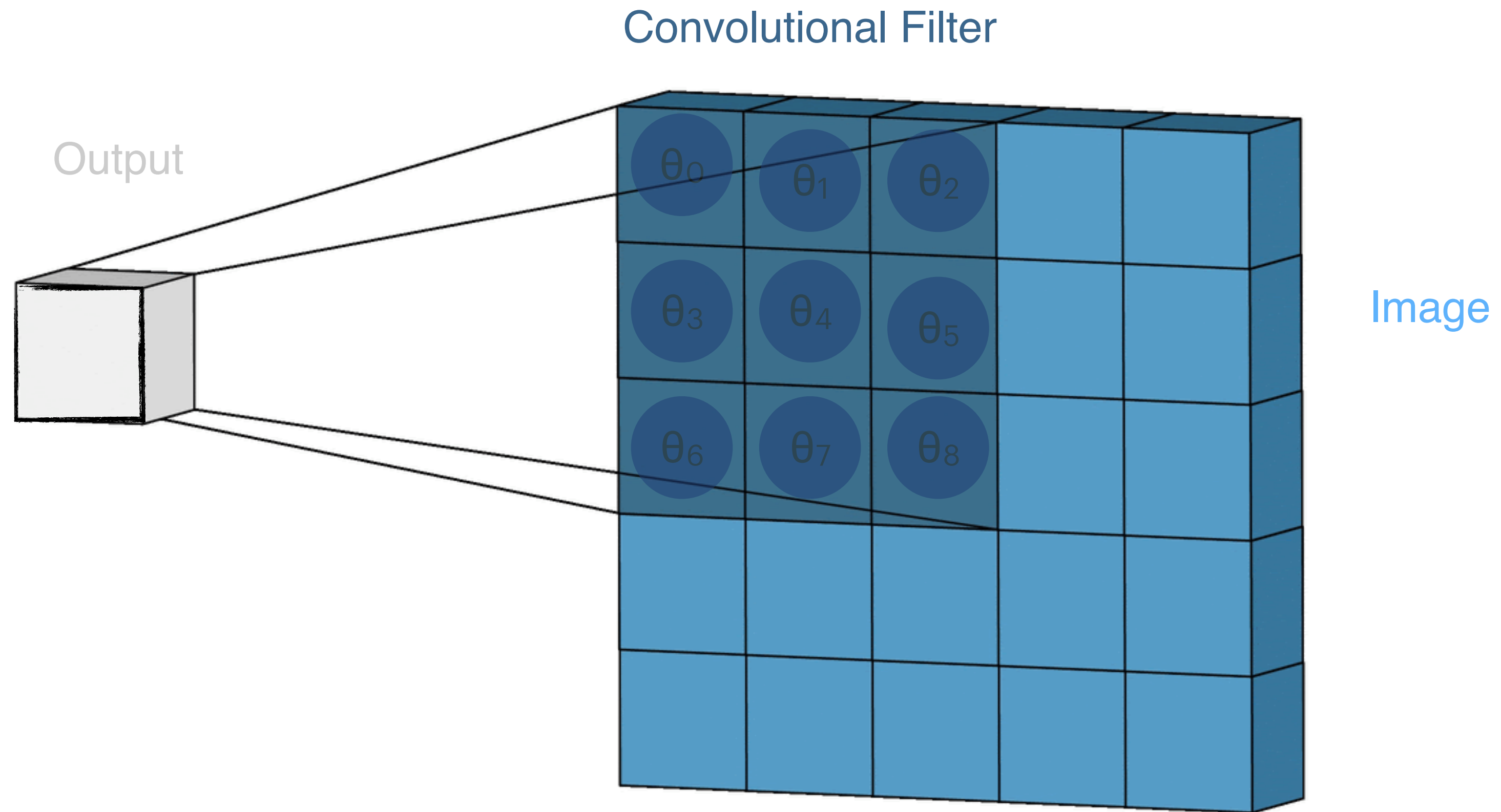
Inspiration: image segmentation

Shared weights are a good inductive bias

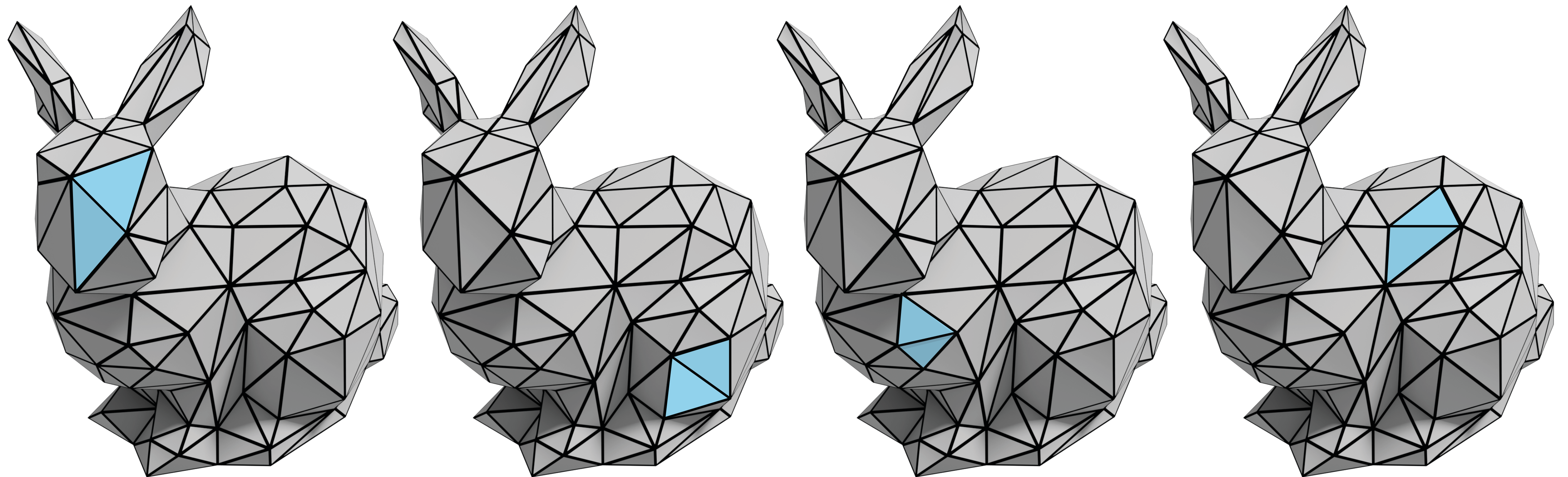


Convolution

Shared-weights

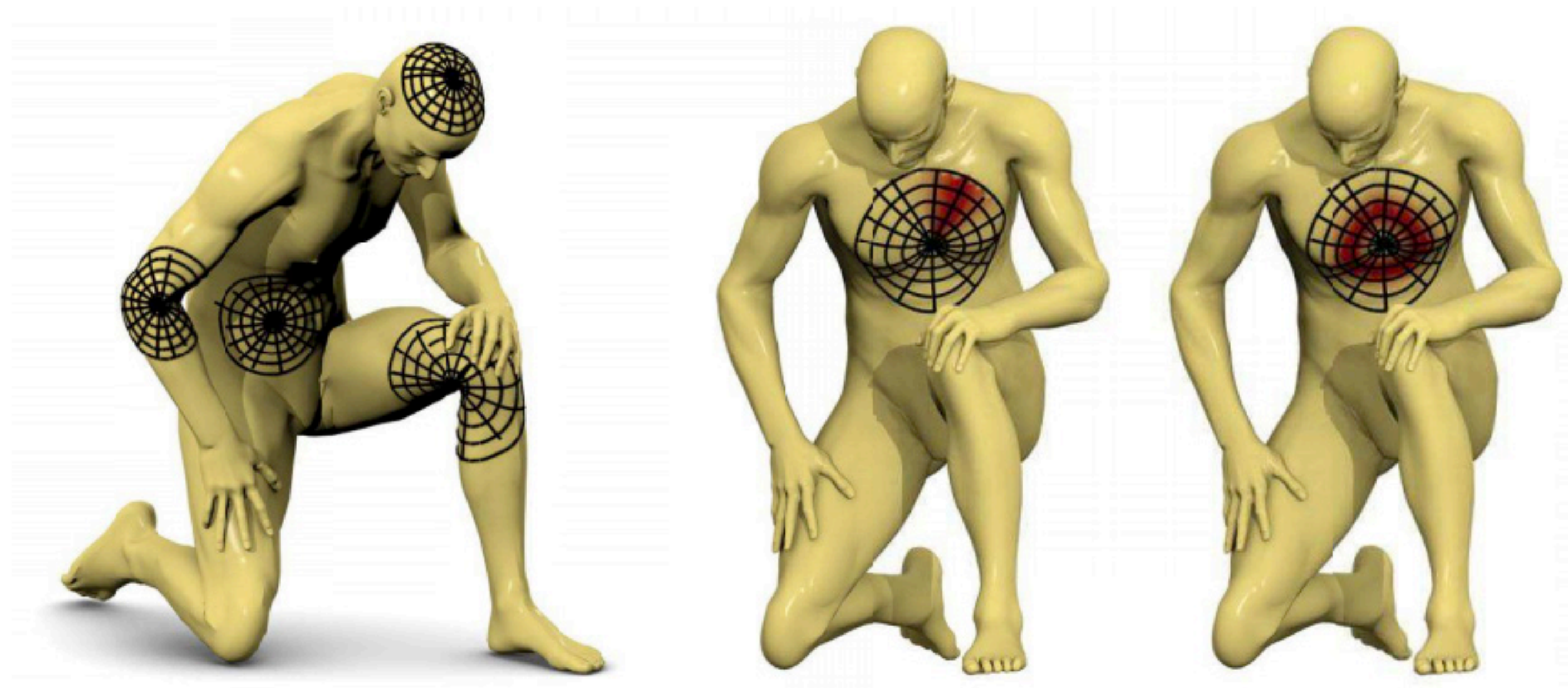


Convolutions on meshes

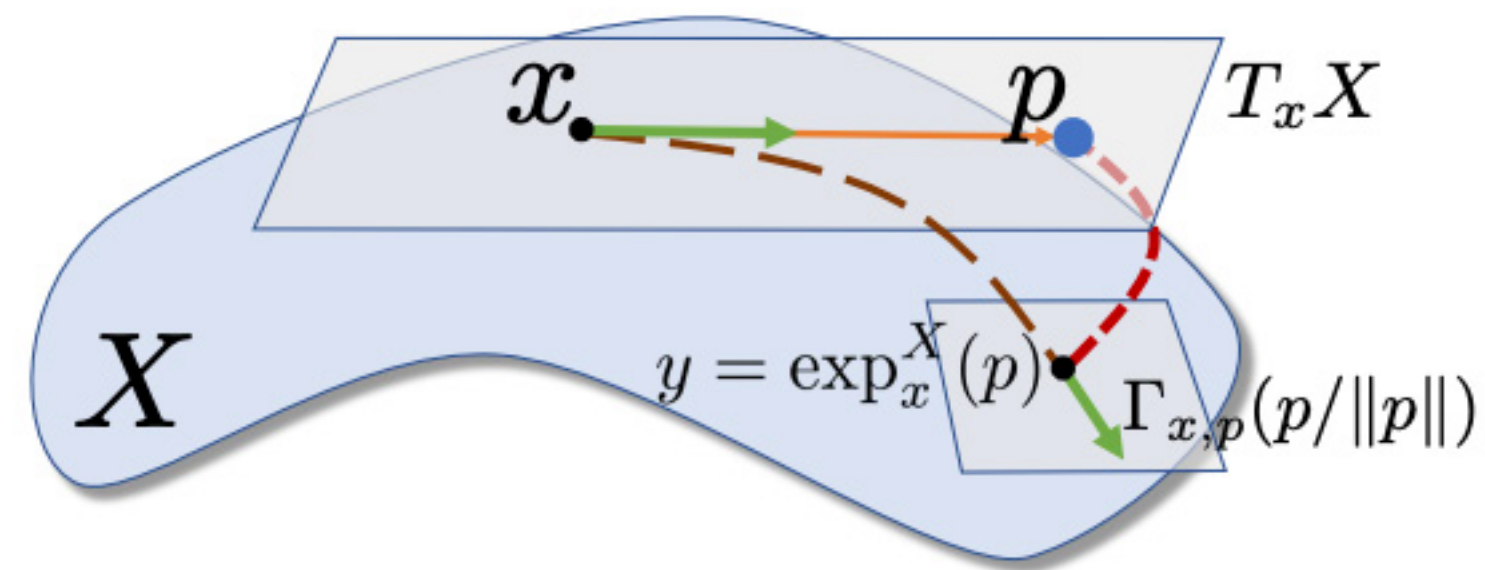


Learn over intrinsic patches

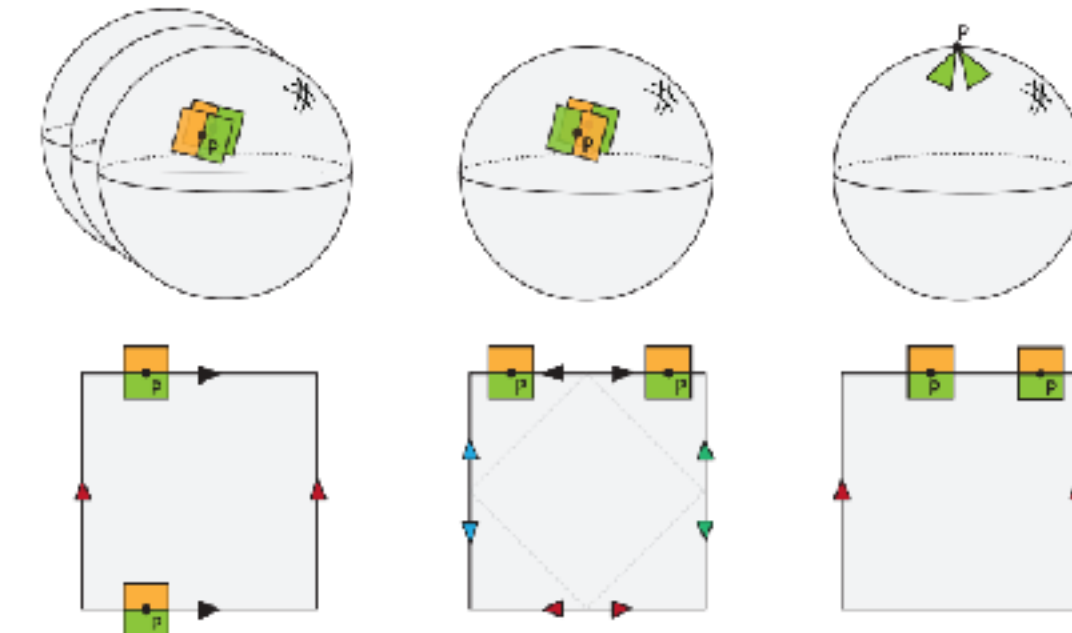
local parameterizations



Intrinsic Techniques



MDGCNN. Poulenard & Ovsjanikov [SIGGRAPH Asia 2018]

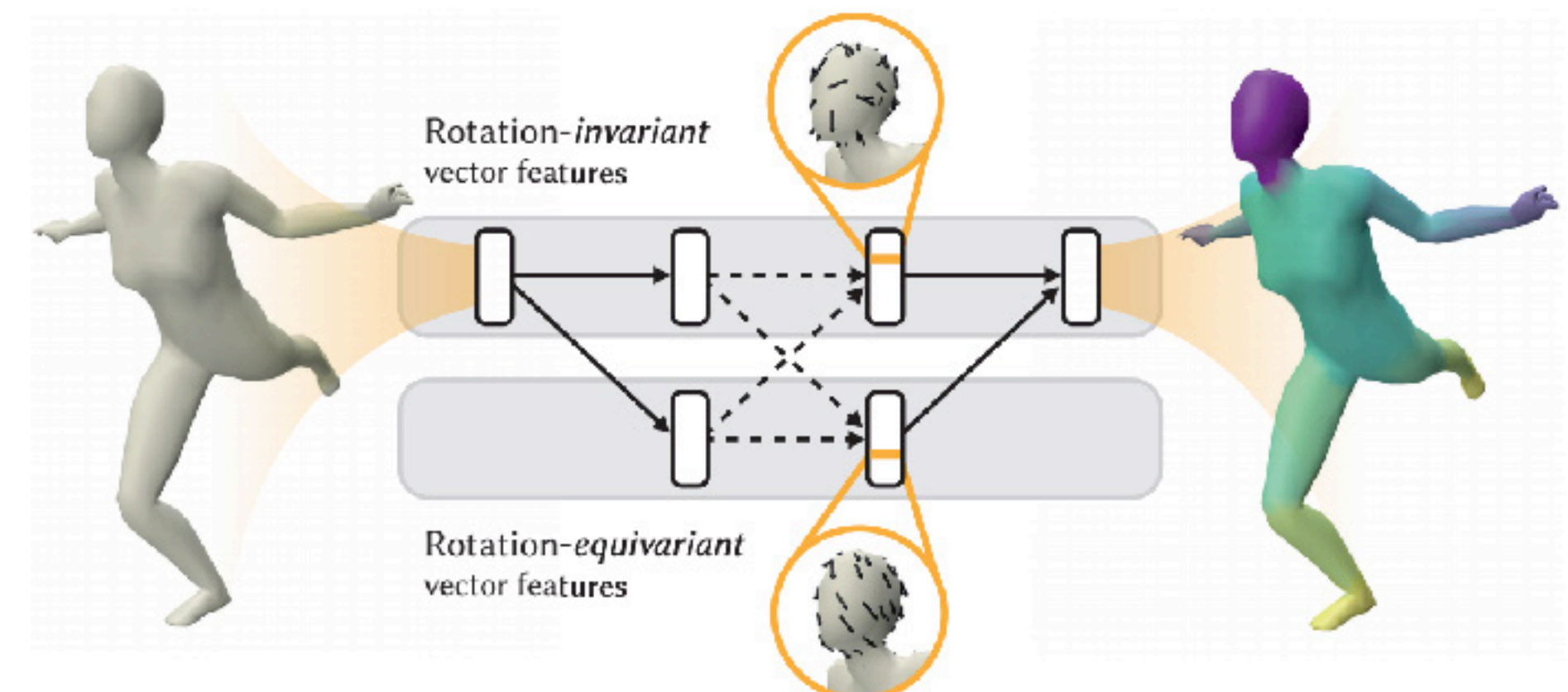


Surface Networks via General Covers. Haim et. al [ICCV 2019]

Toric Covers. Maron et. al [SIGGRAPH 2017]

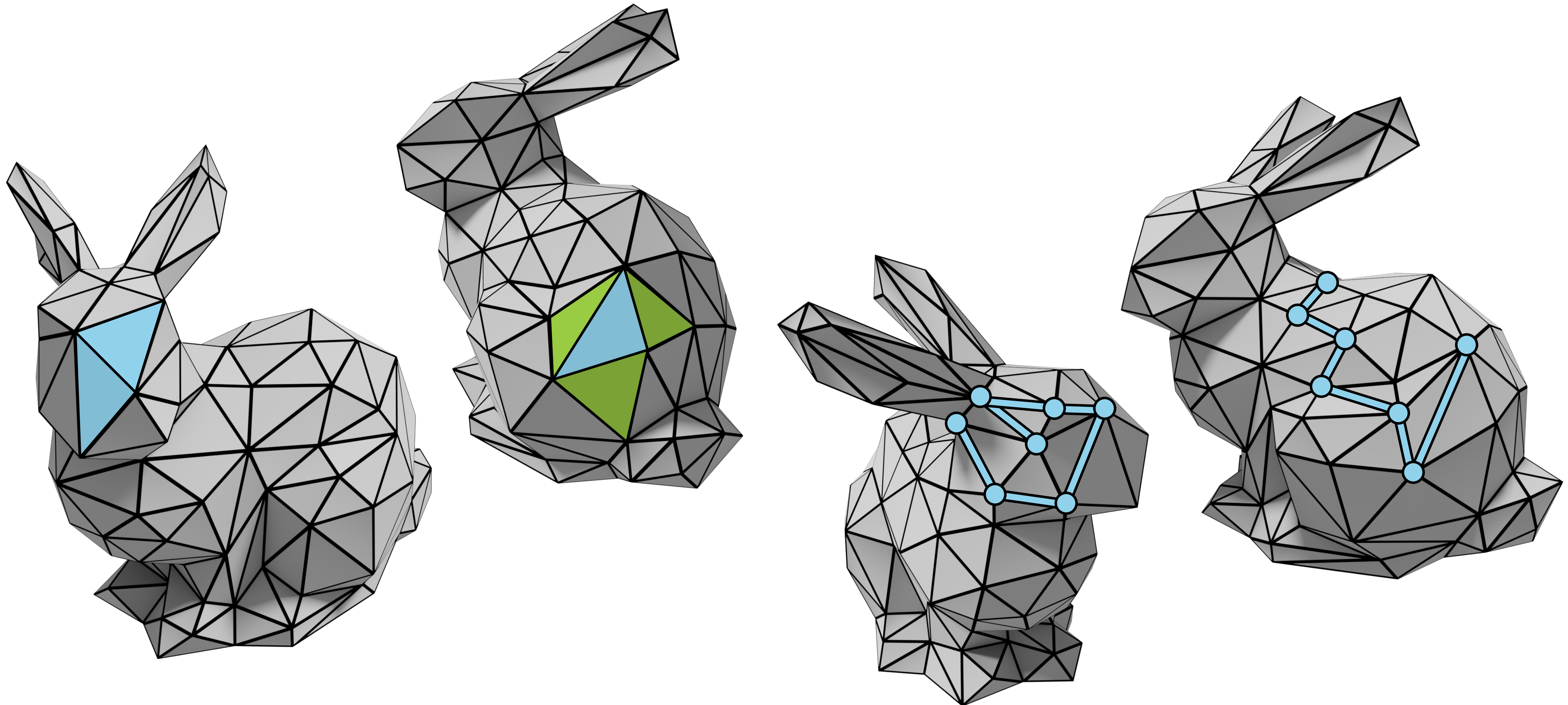


HodgeNet. Smirnov & Solomon [SIGGRAPH 2021]



CNNs on Surfaces. Wiersma & Eisemann [SIGGRAPH 2020]

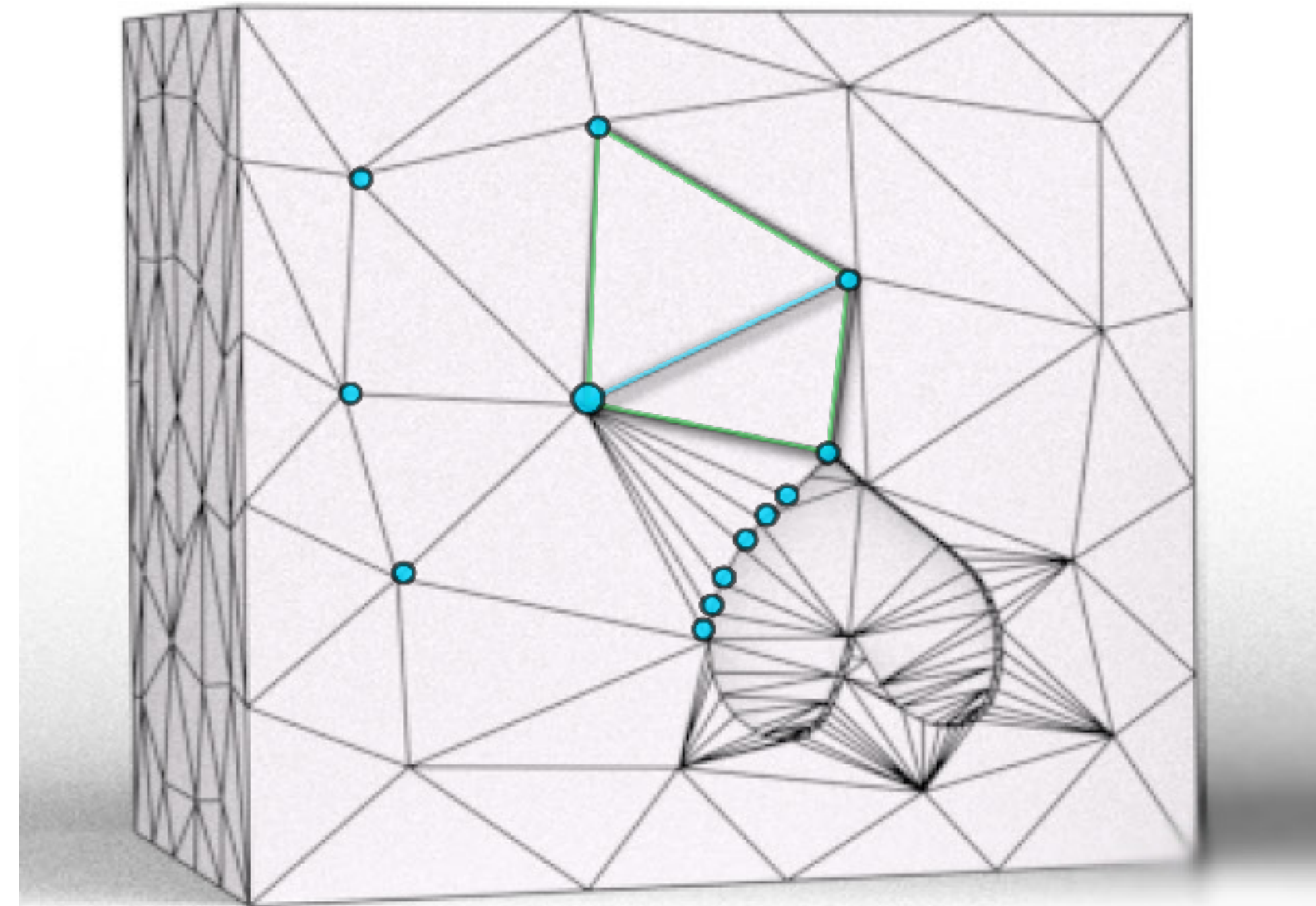
Convolutions on meshes



Fixed size neighborhood



**Mesh edges have
4 edge-neighbors**

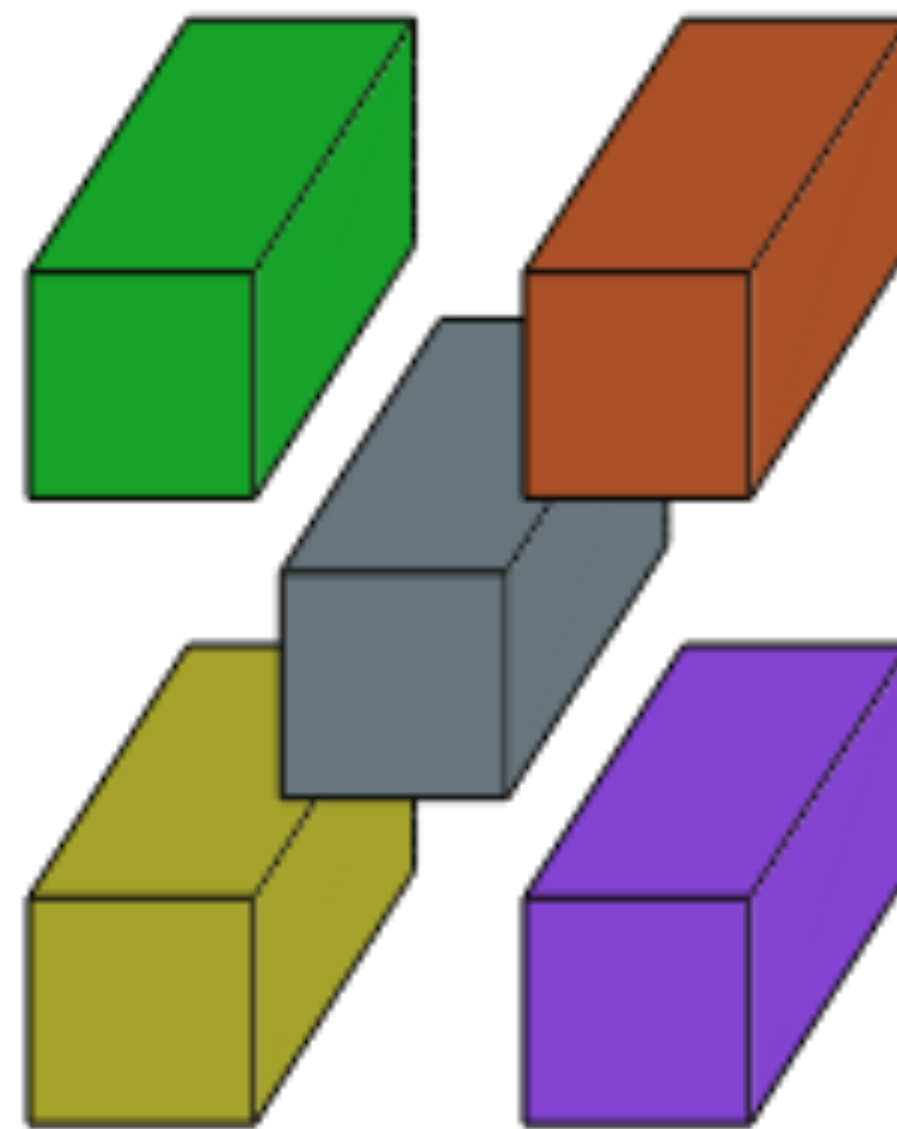
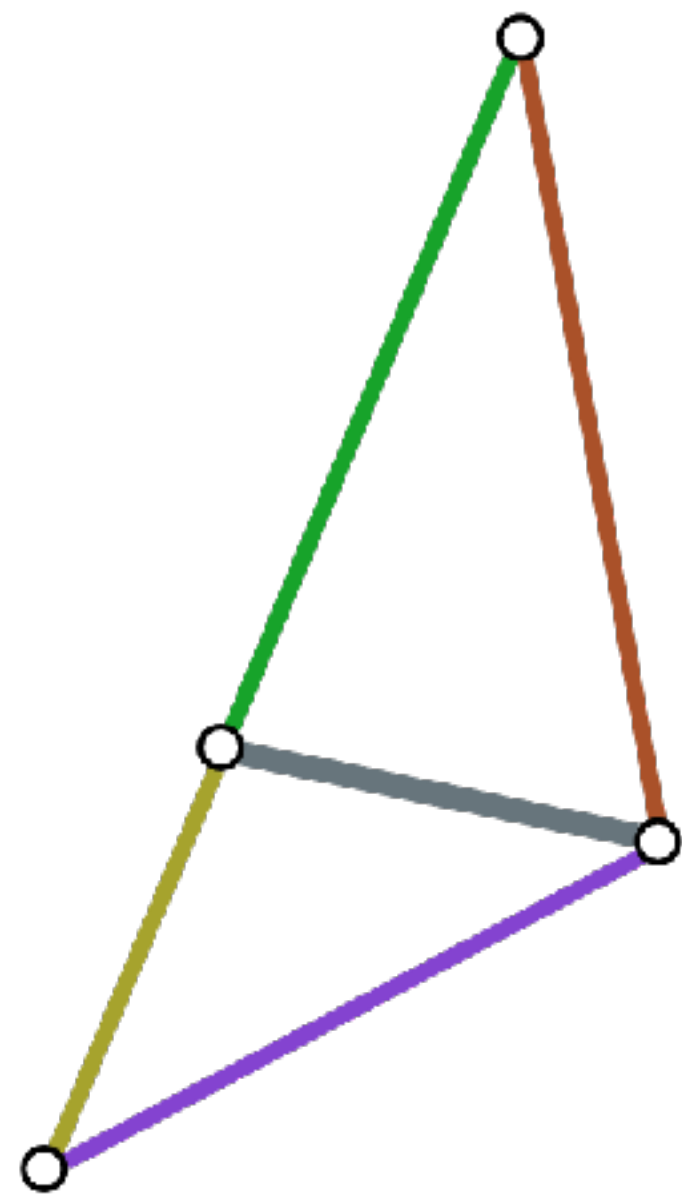


Vertices
 $\langle x, y, z \rangle$

Edges
 $\langle v_i, v_j \rangle$

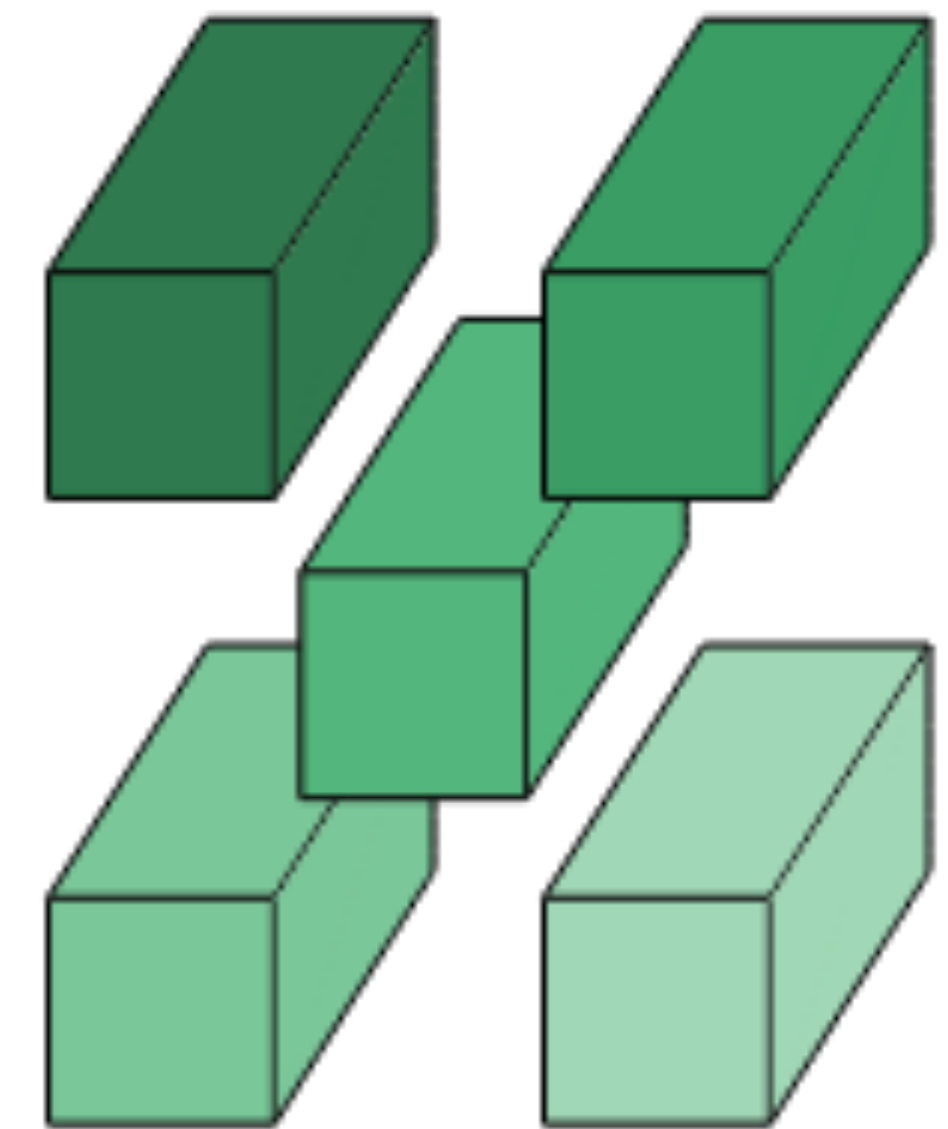
Faces
 $\langle v_i, v_j, v_k \rangle$

Learn Filters on Edge Features



Edge Features

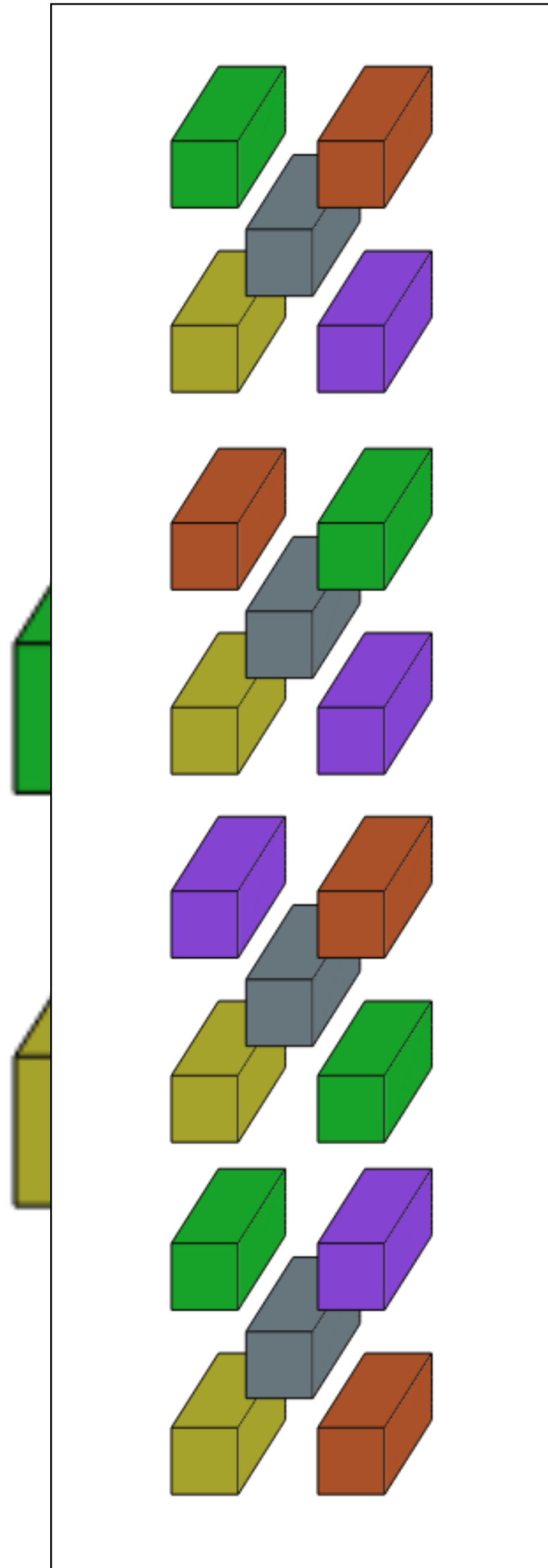
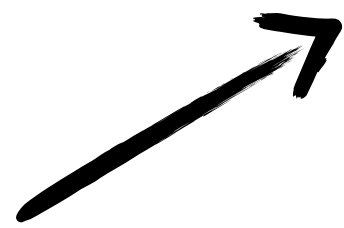
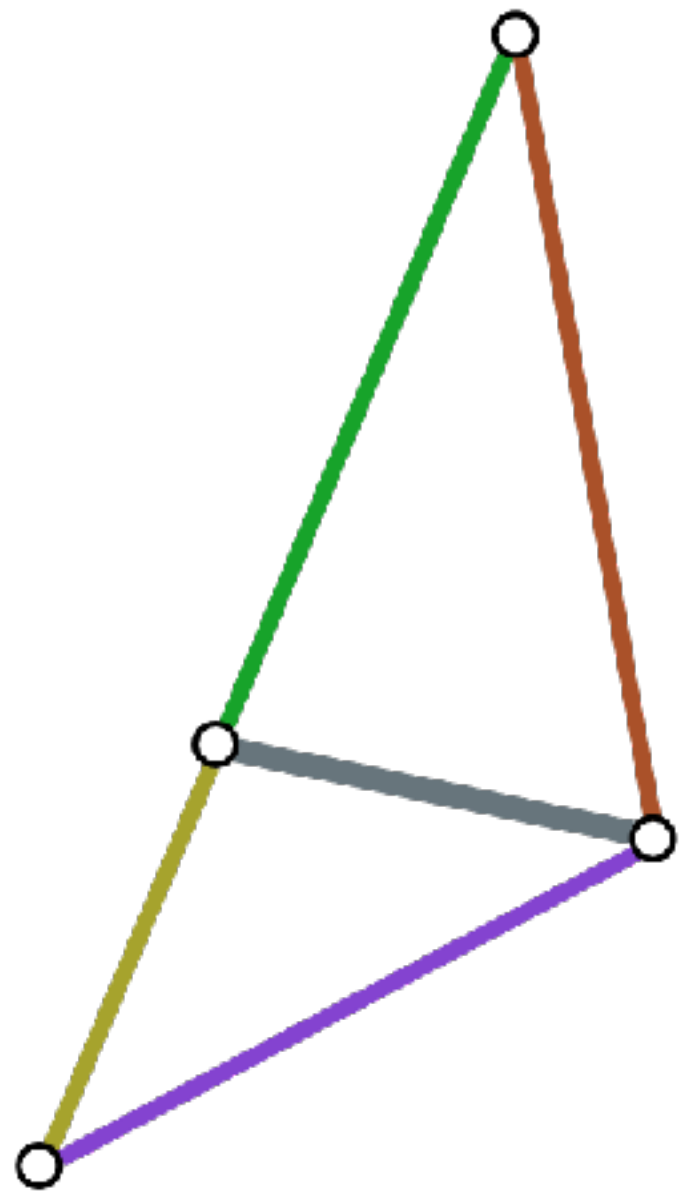
*



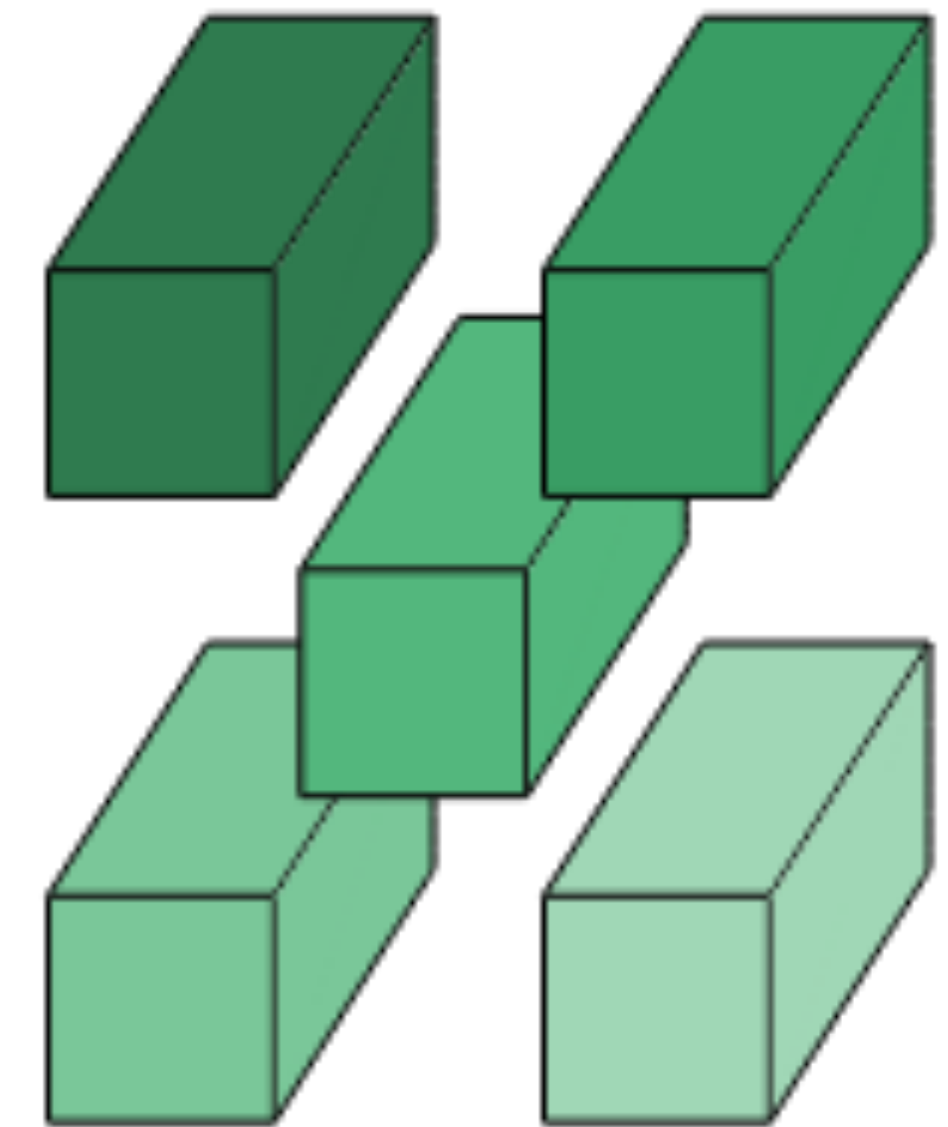
Conv Kernel

Learn Filters on Edge Features

Different ordering of edge indices

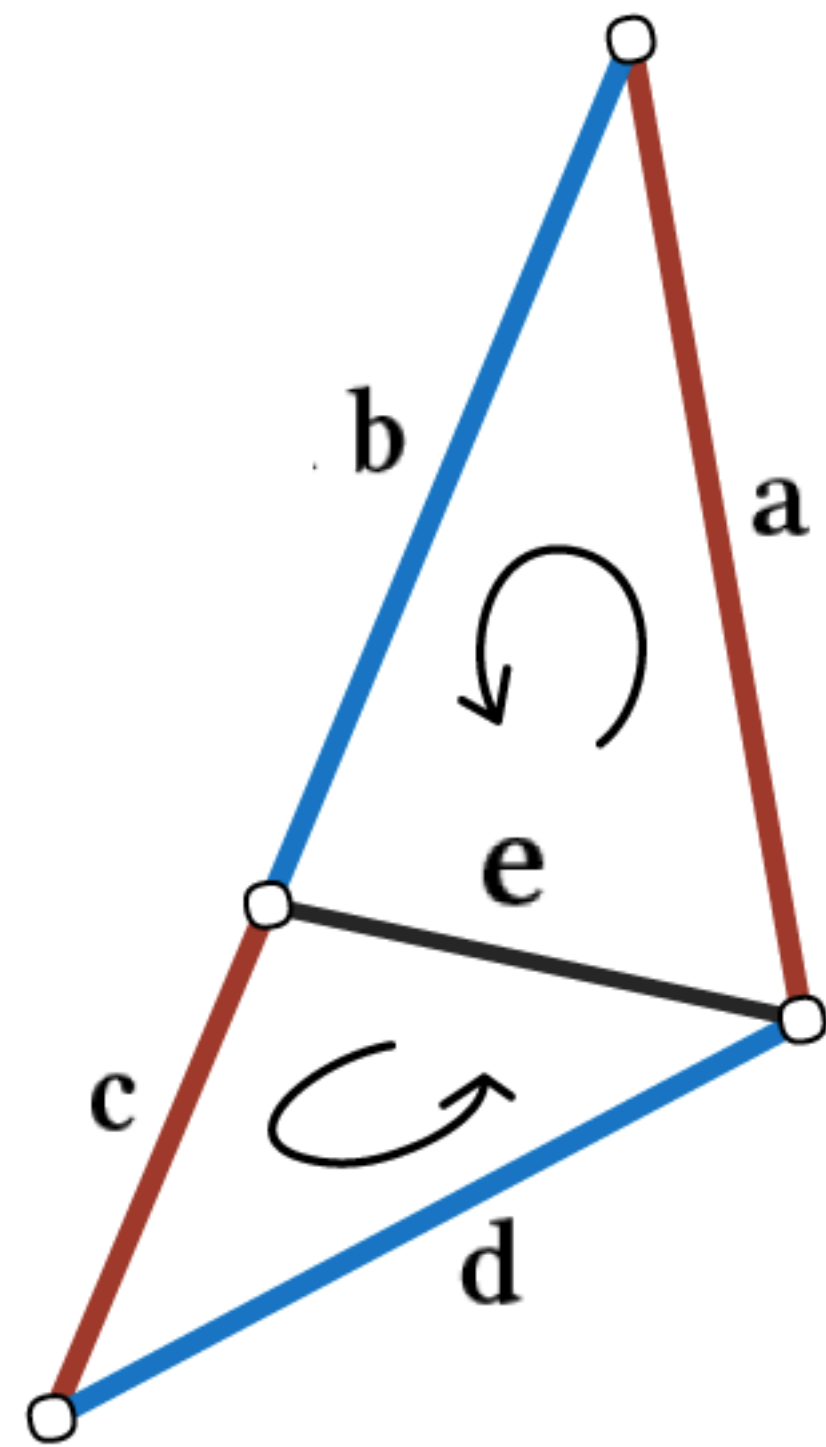


*



Conv Kernel

Mesh Convolution Order



Face normal

- Consistent ordering in each face
- Two *valid* orderings

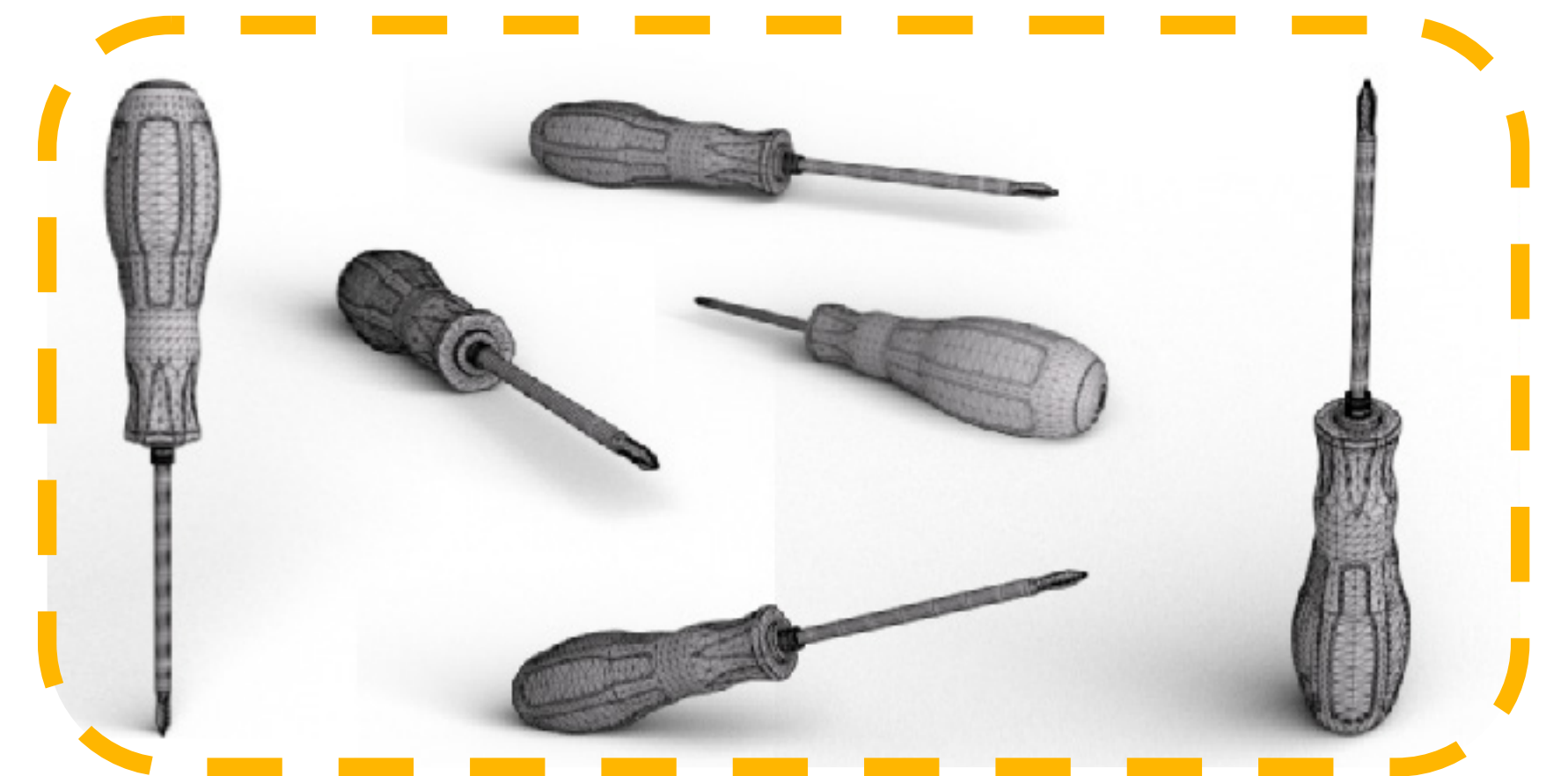
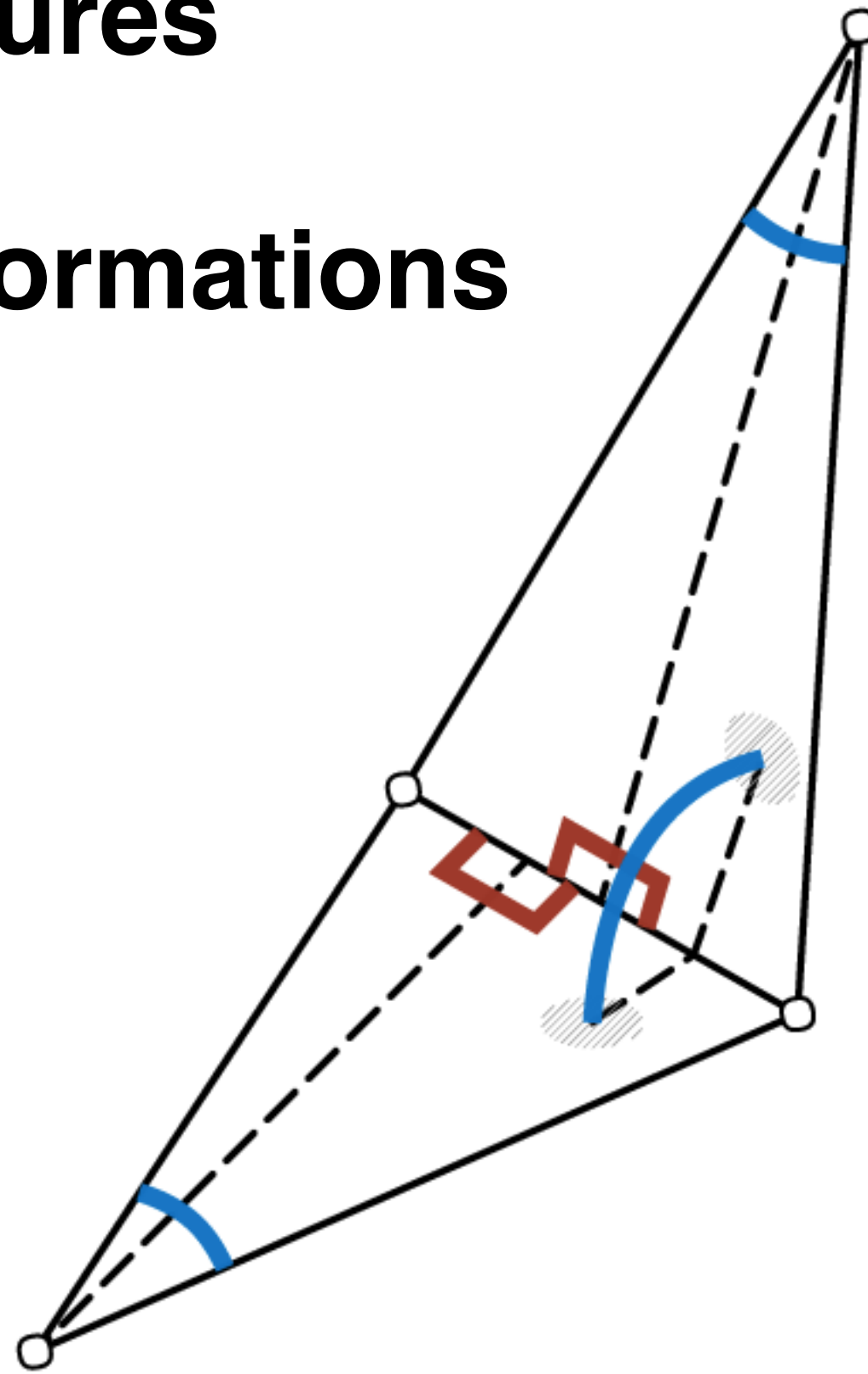
Build symmetric features

$$e \rightarrow (a+c, |a-c|, b+d, |b-d|)$$

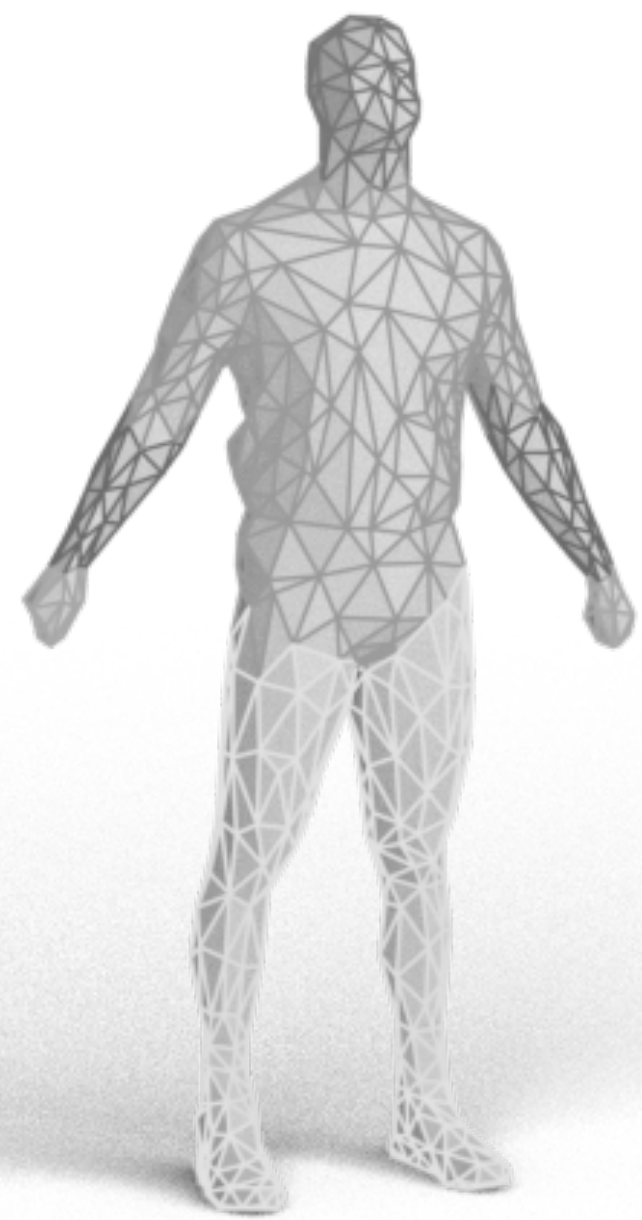
Input edge features

Relative geometric features

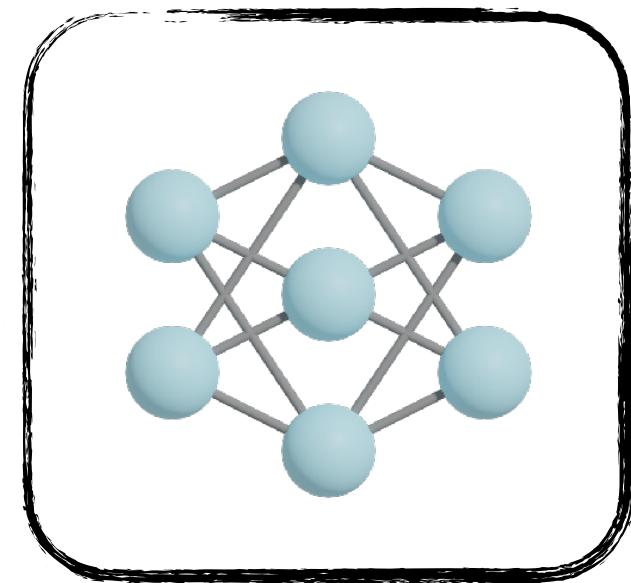
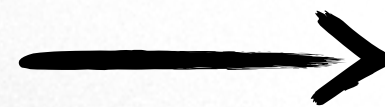
Invariant to rigid transformations



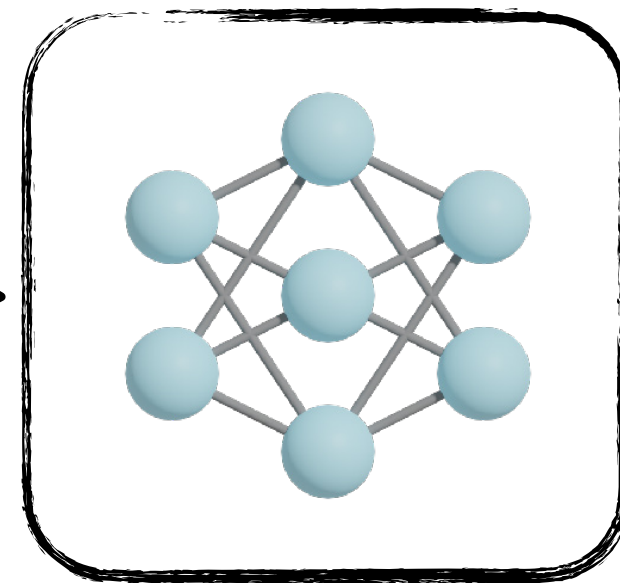
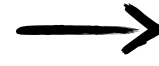
Recap: learning local descriptors



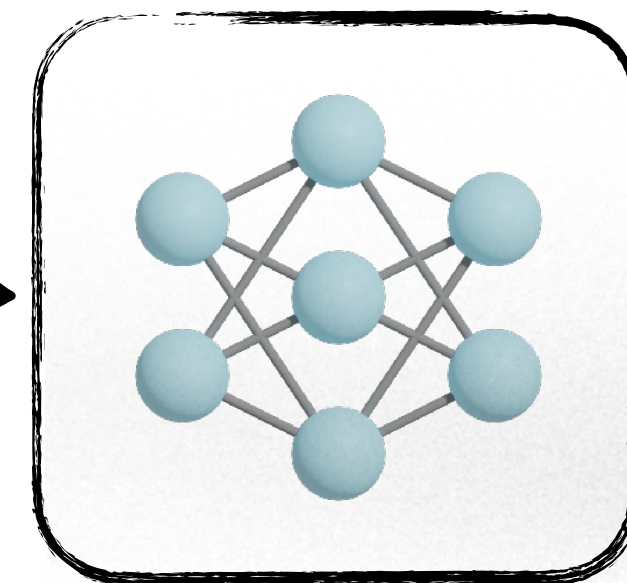
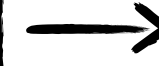
Input mesh



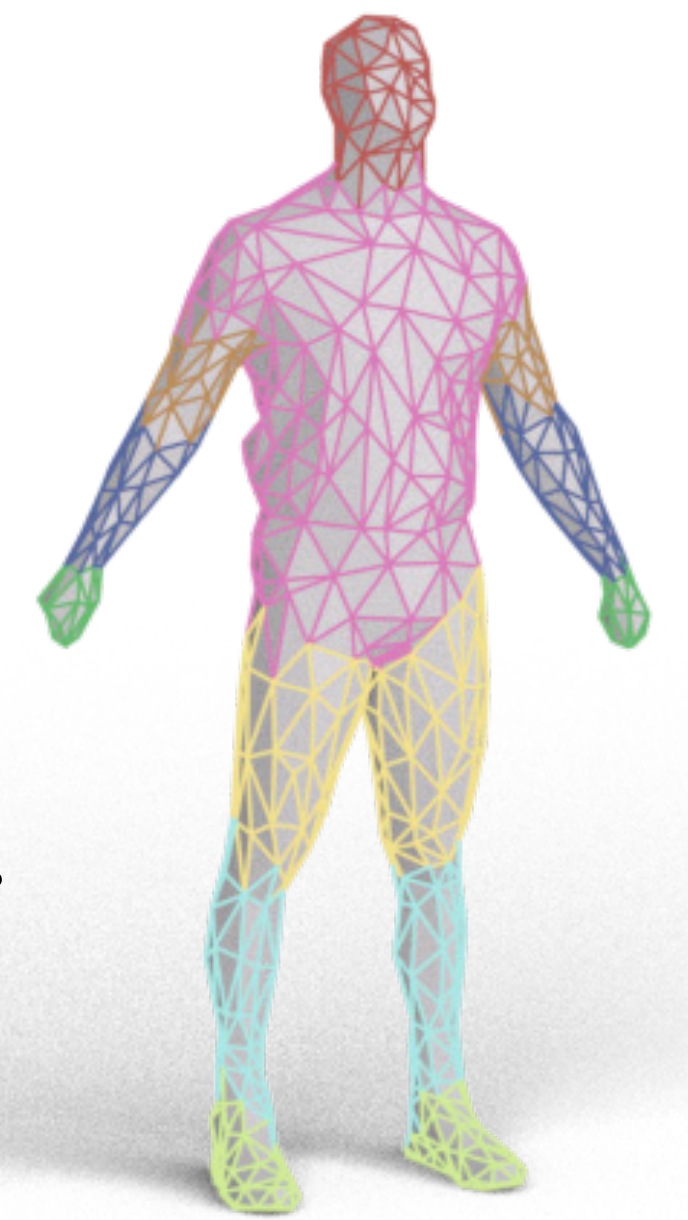
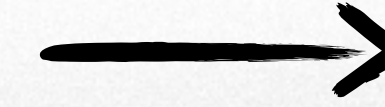
Convolution



Convolution

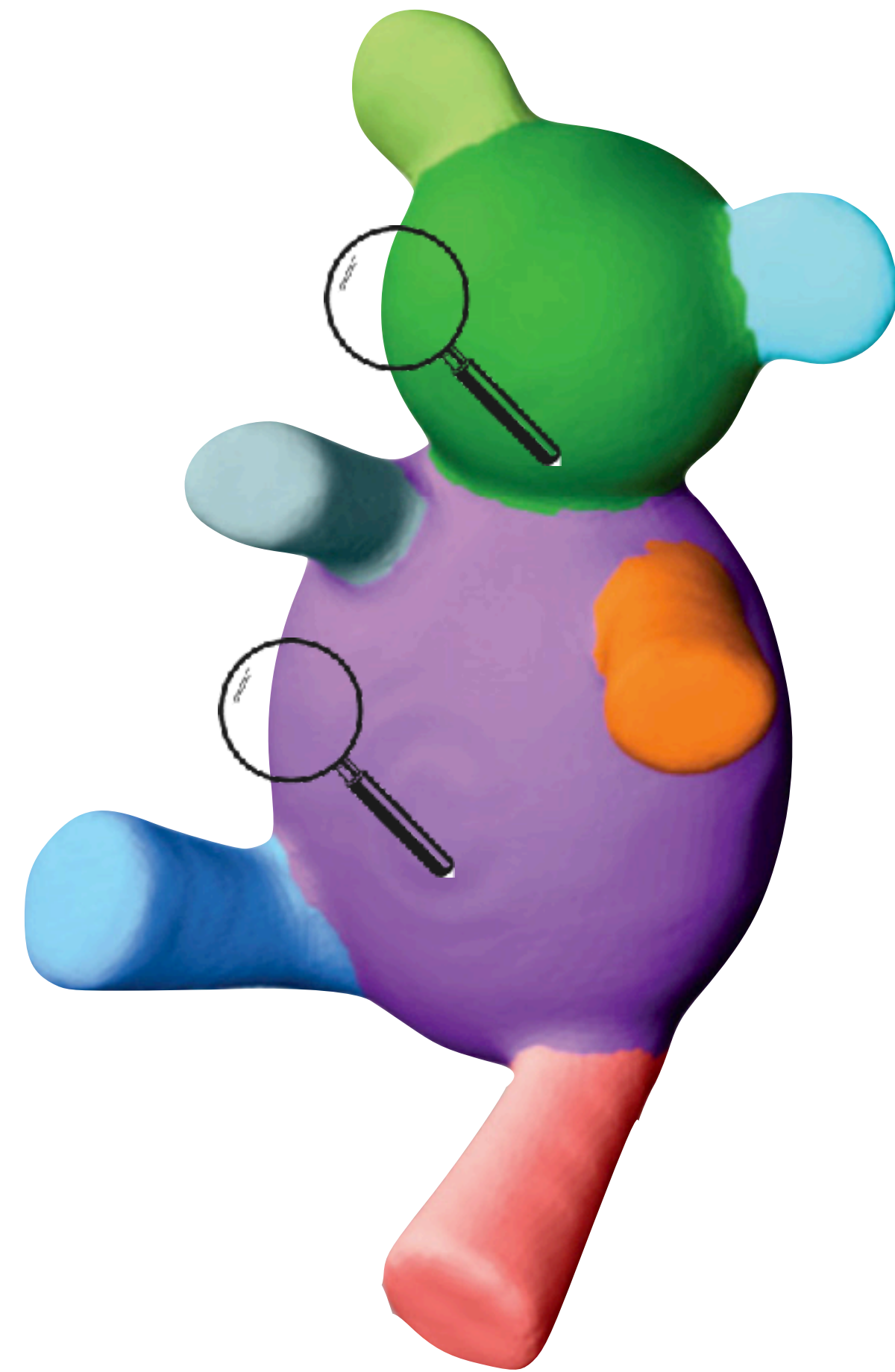


Convolution



Per edge attribute

Incorporating more context



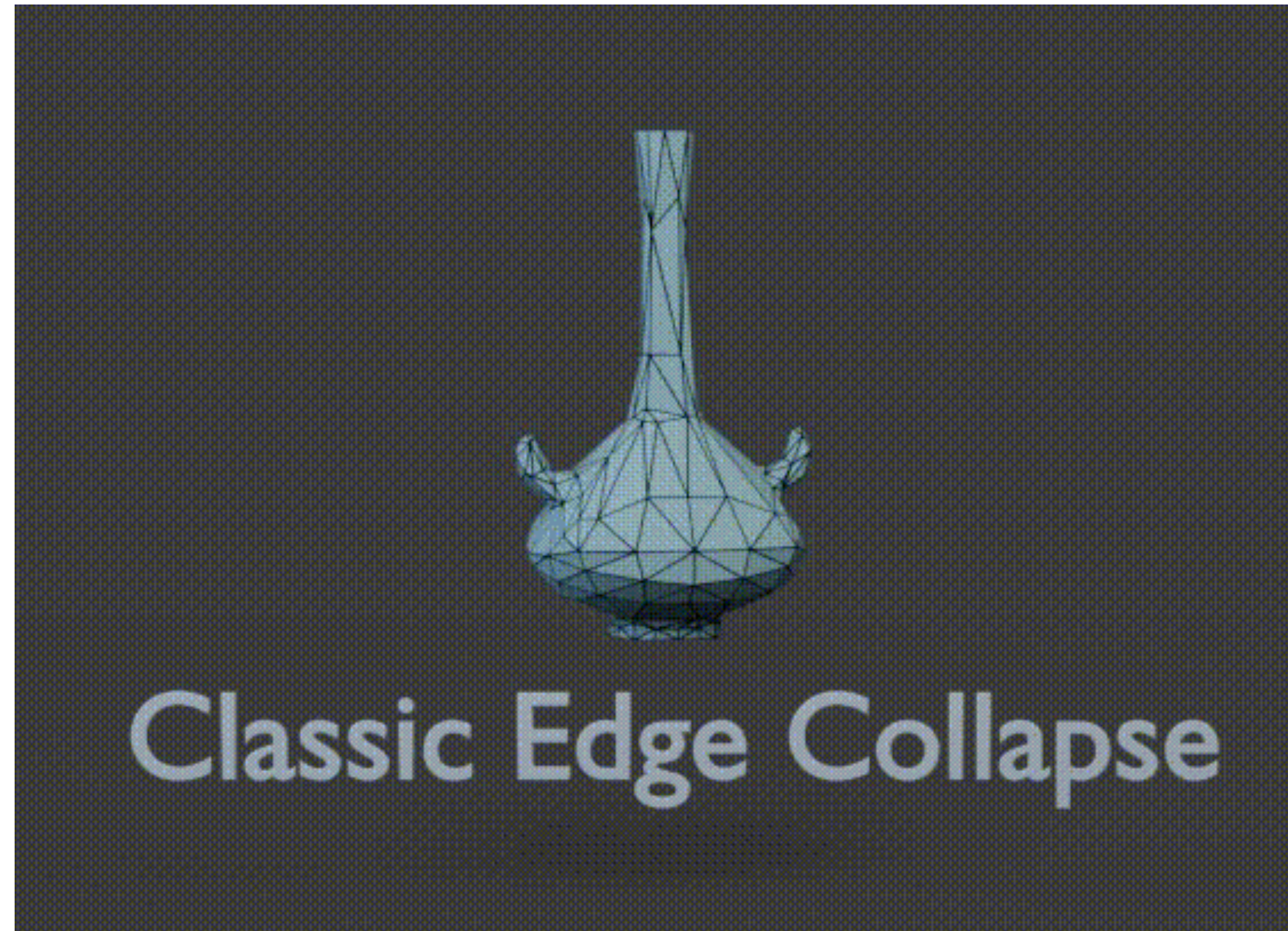
Inspiration: image pooling

4	6	1	1
1	3	1	3
4	0	0	8
8	5	4	0

Input (4x4)

Output (2x2)

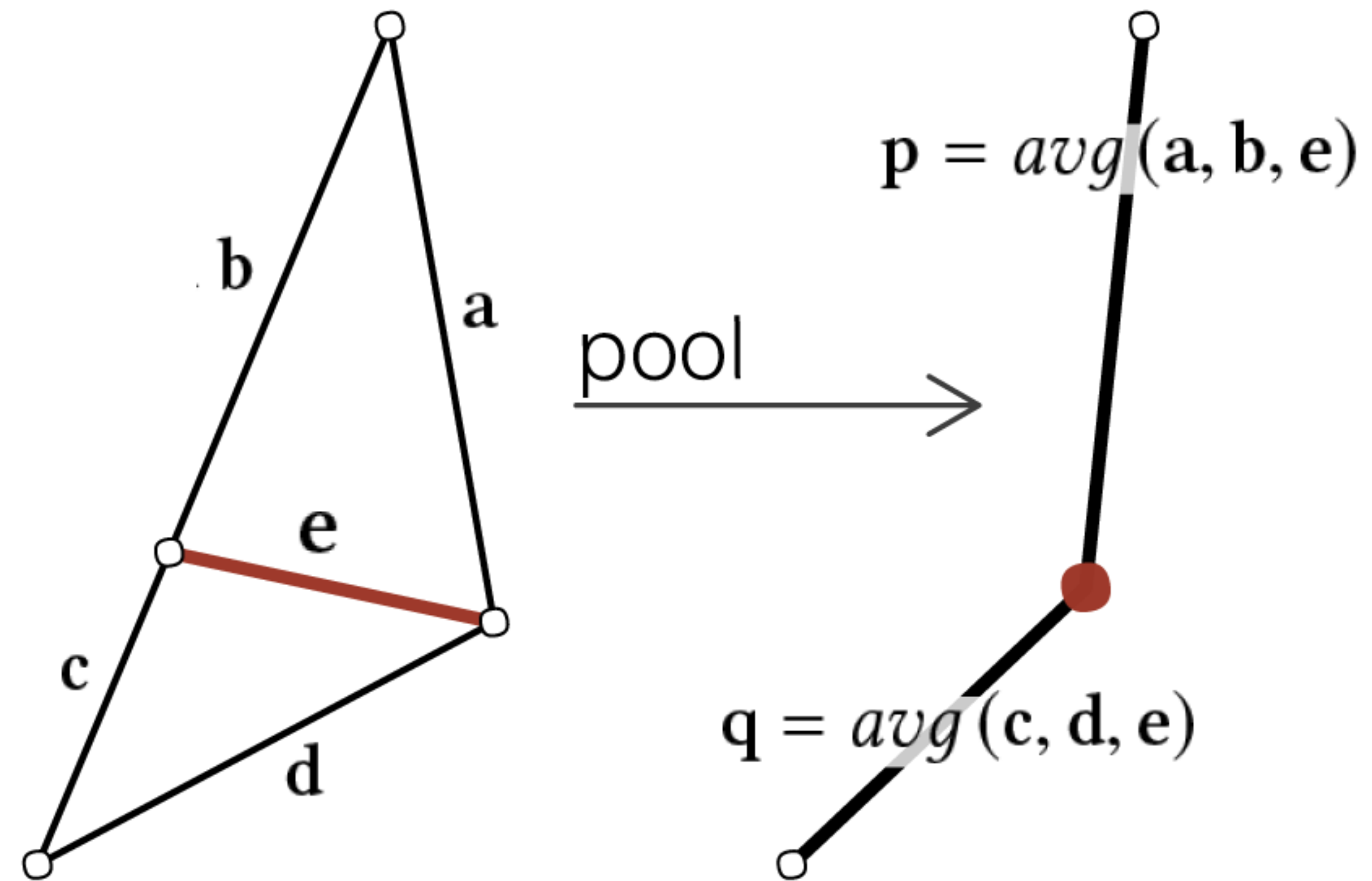
Mesh pooling via edge collapse



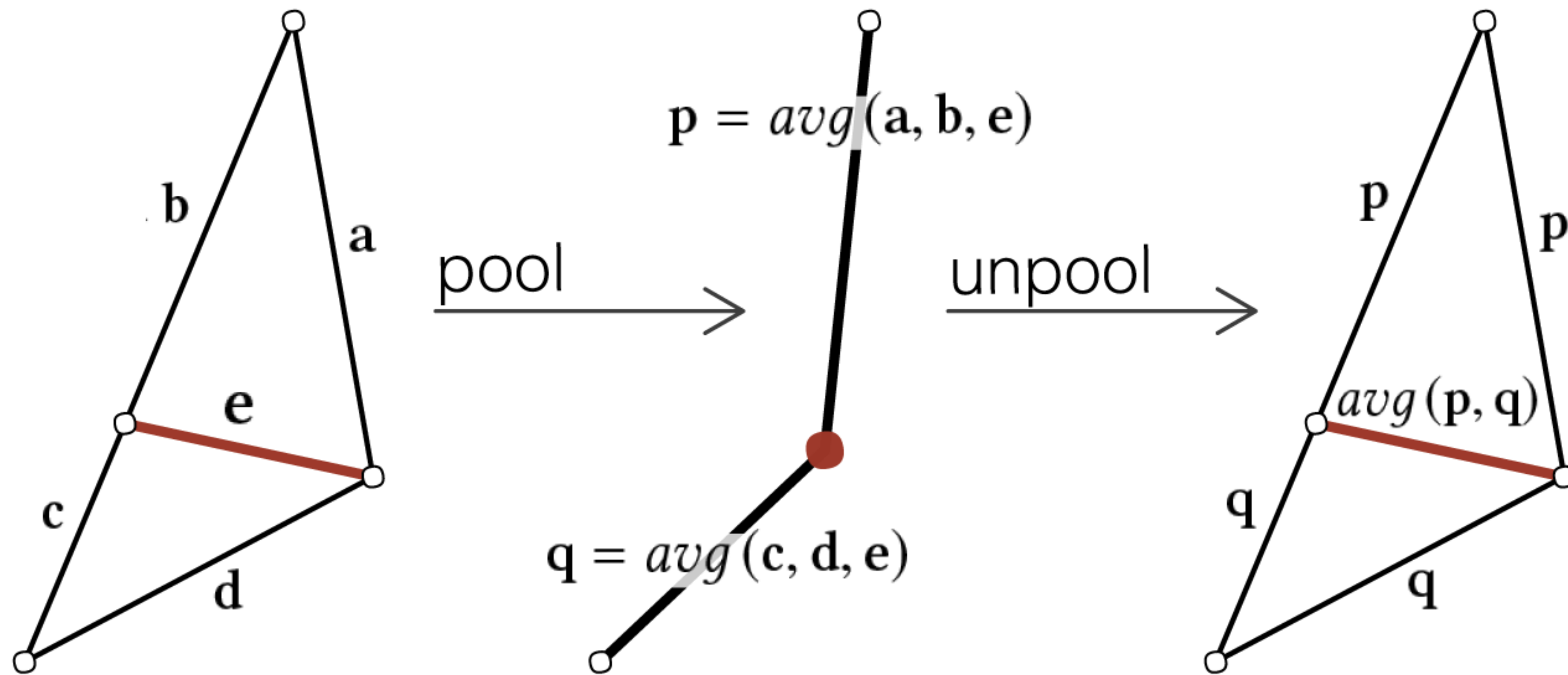
Mesh pooling via edge collapse



Mesh pooling via edge collapse

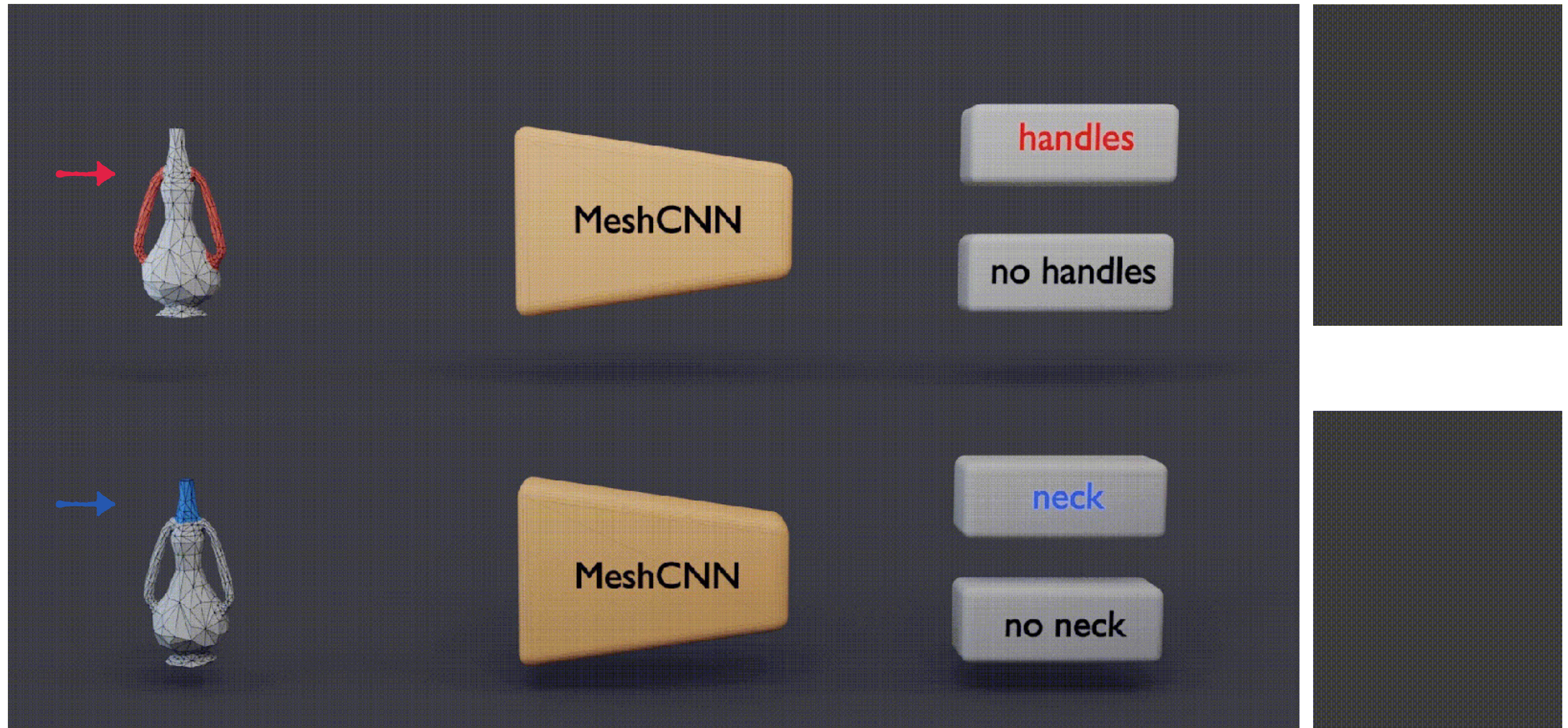


Mesh unpooling

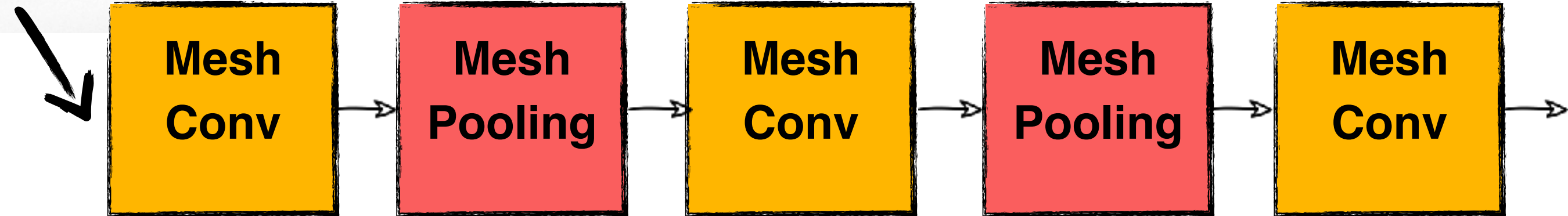


Different tasks

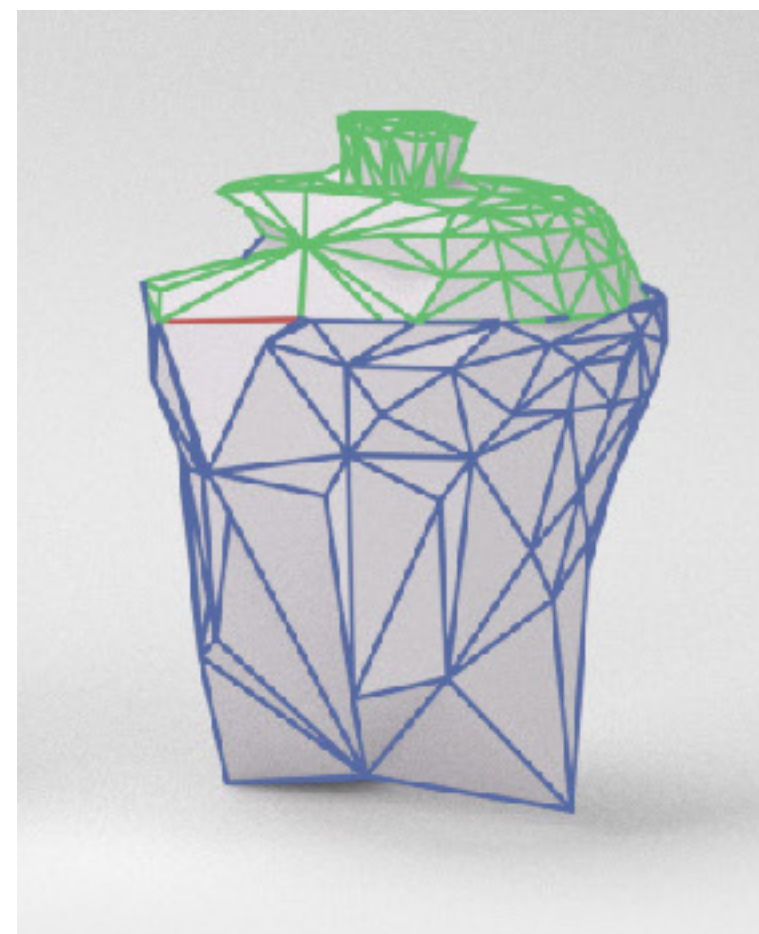
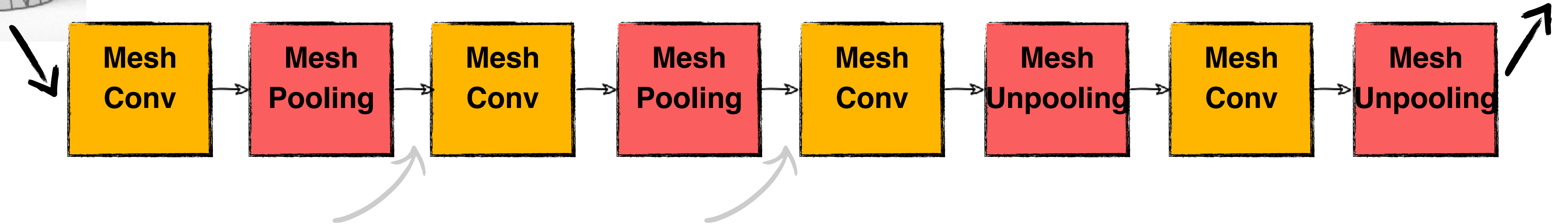
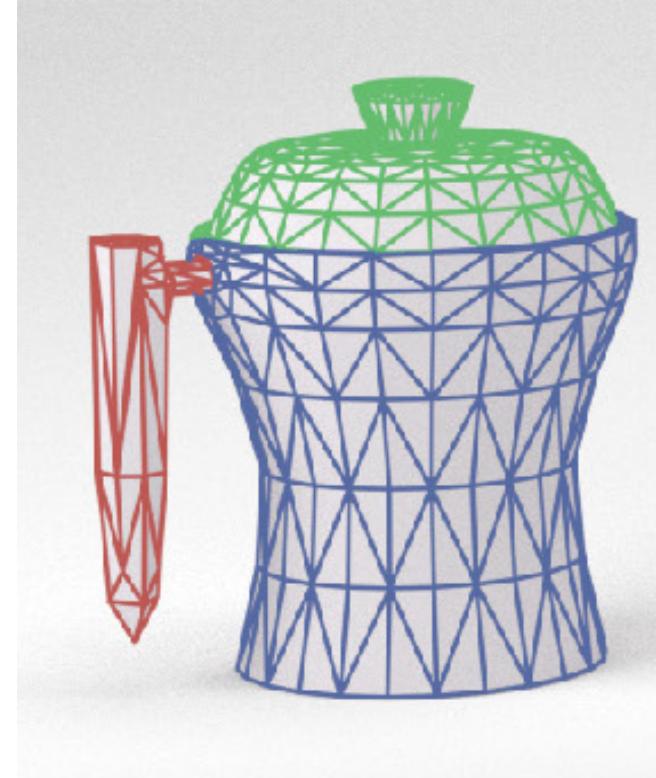
Different simplifications



MeshCNN



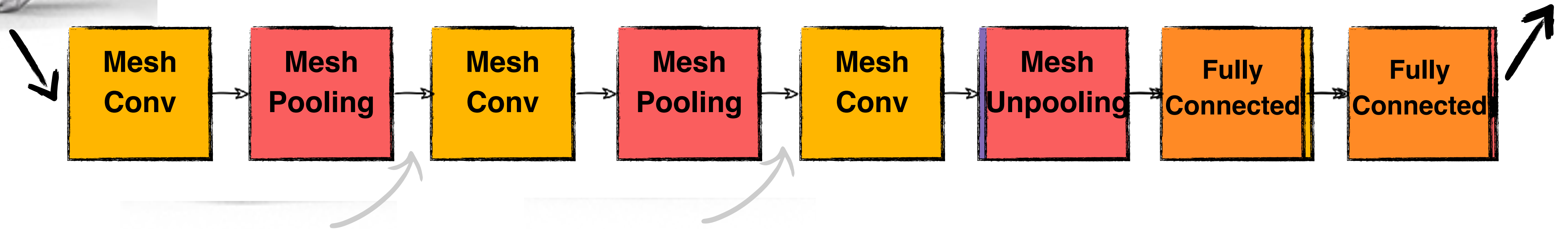
MeshCNN Segmentation Overview



MeshCNN Classification Overview



Human

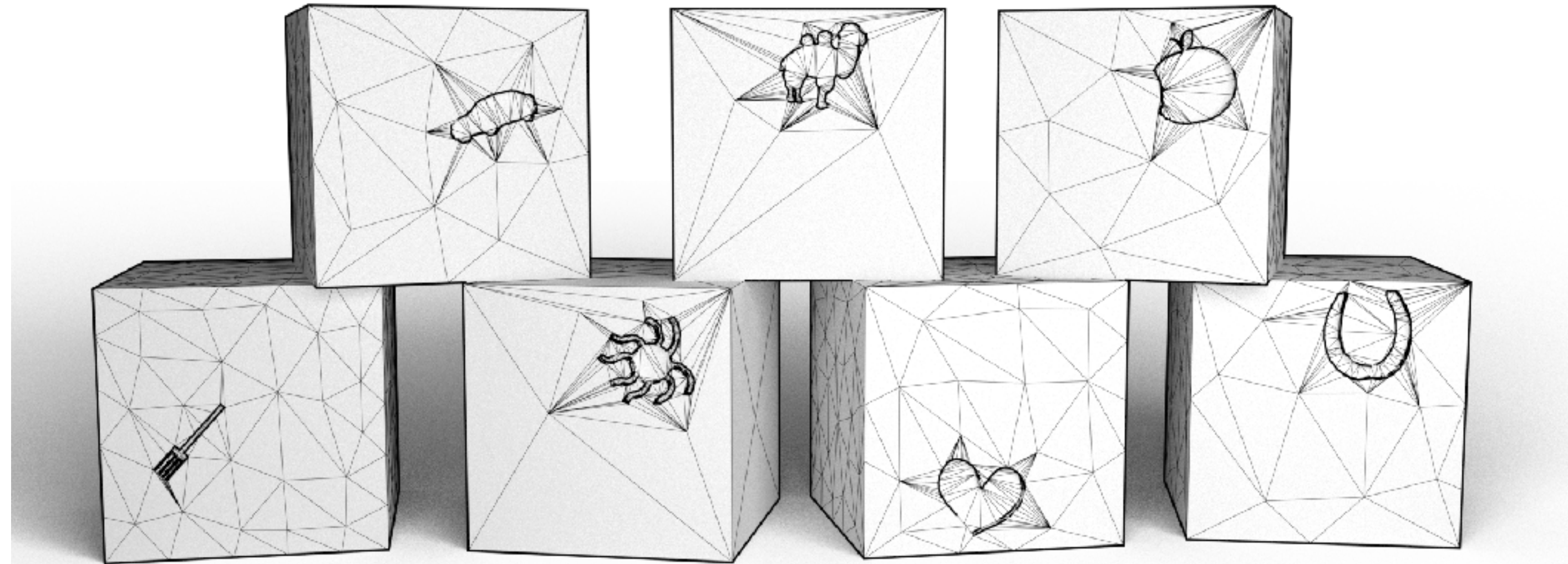


Shape Classification

Method	Split 16	Split 10
MeshCNN	98.6	91.0%
GWCNN	96.6%	90.3%
GI	96.6%	88.6%
SN	48.4%	52.7%
SG	70.8%	62.6%



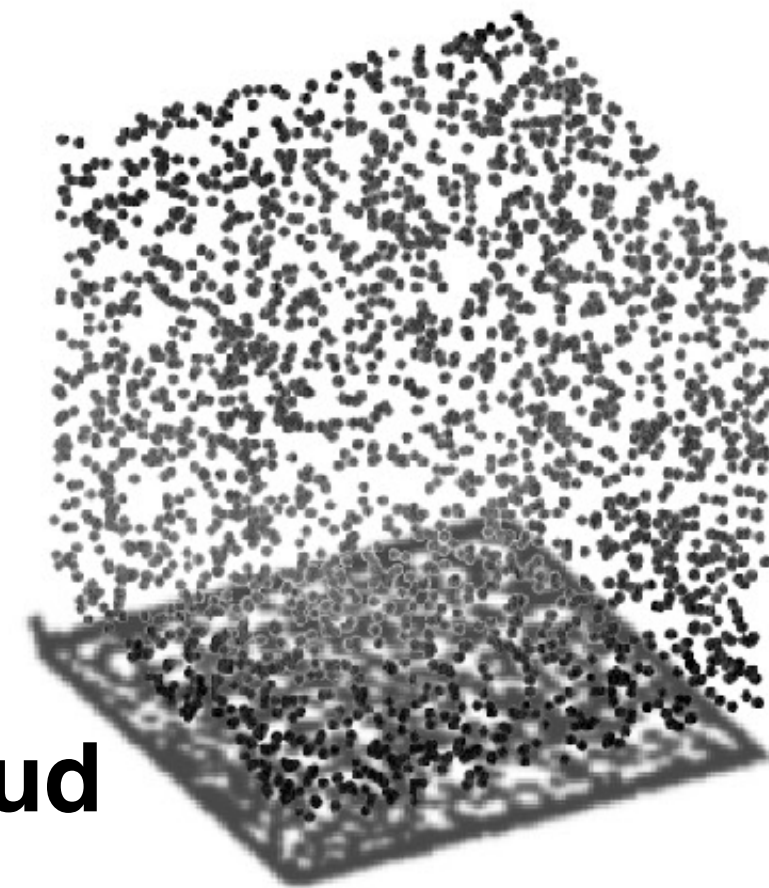
Cube Engraving Classification



Which engraving does this have?

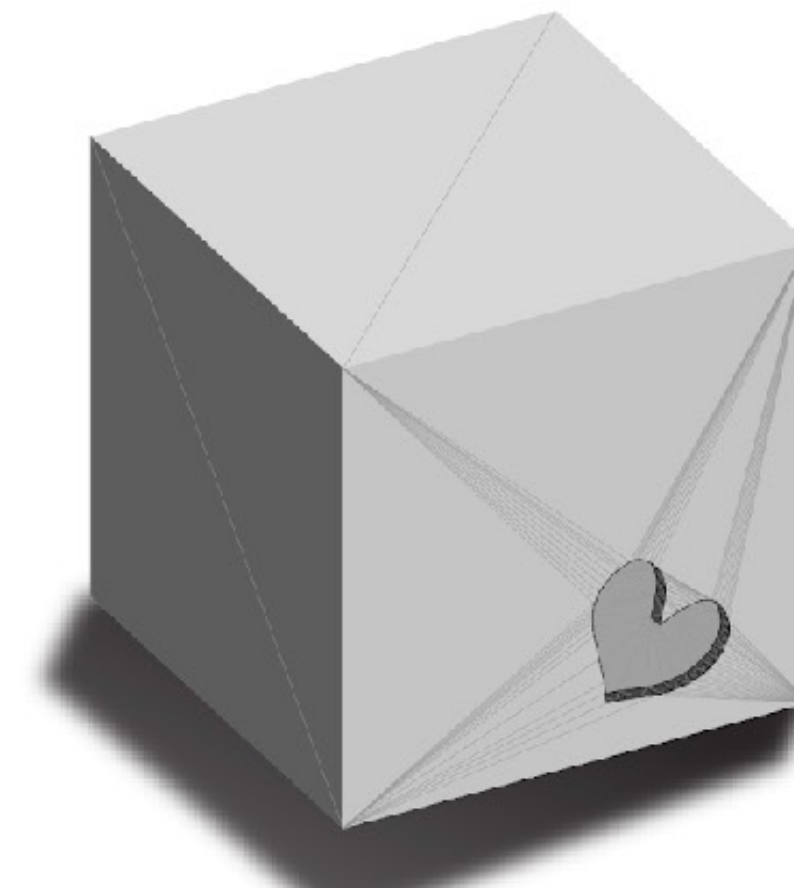
64.26%

Point cloud

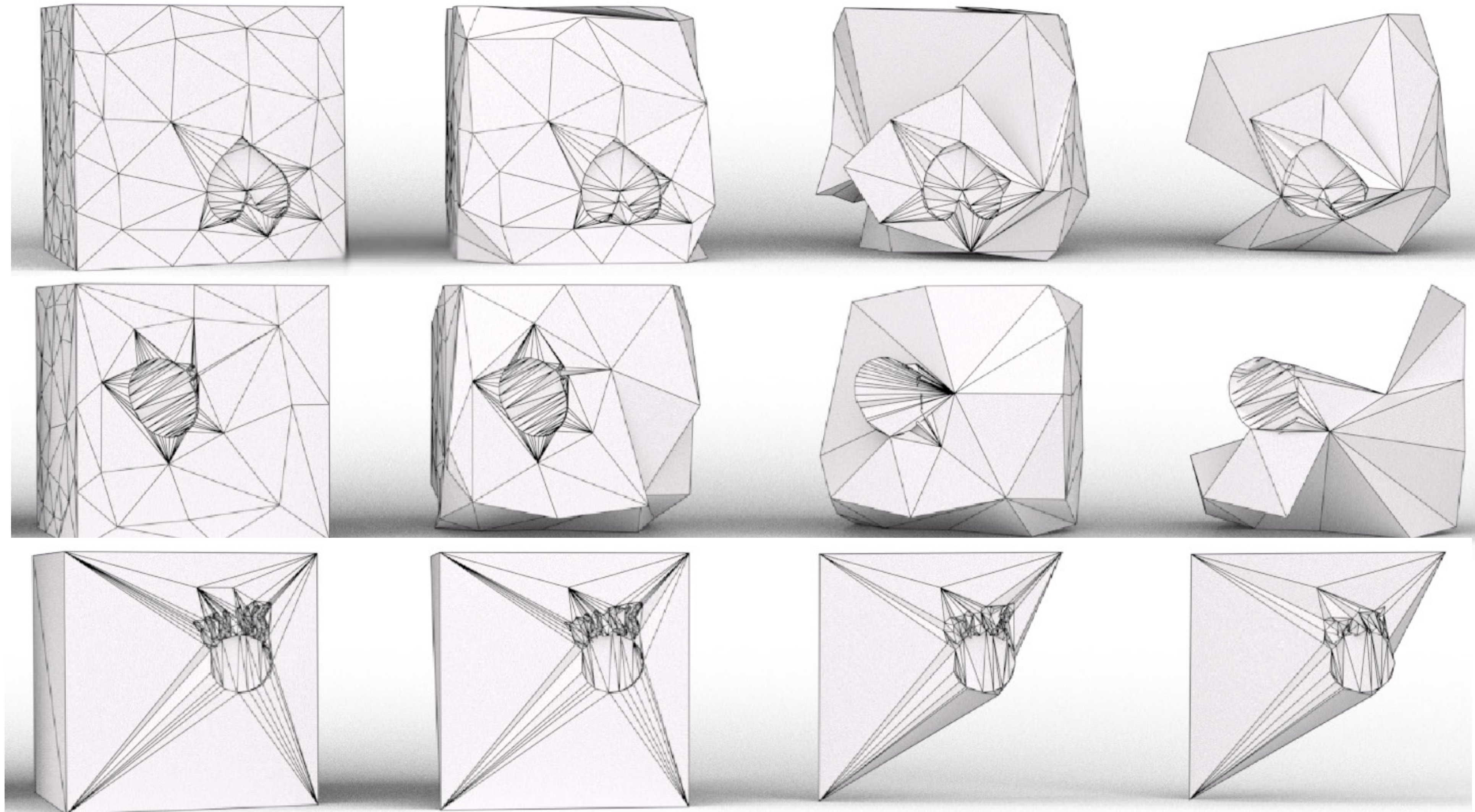


Mesh

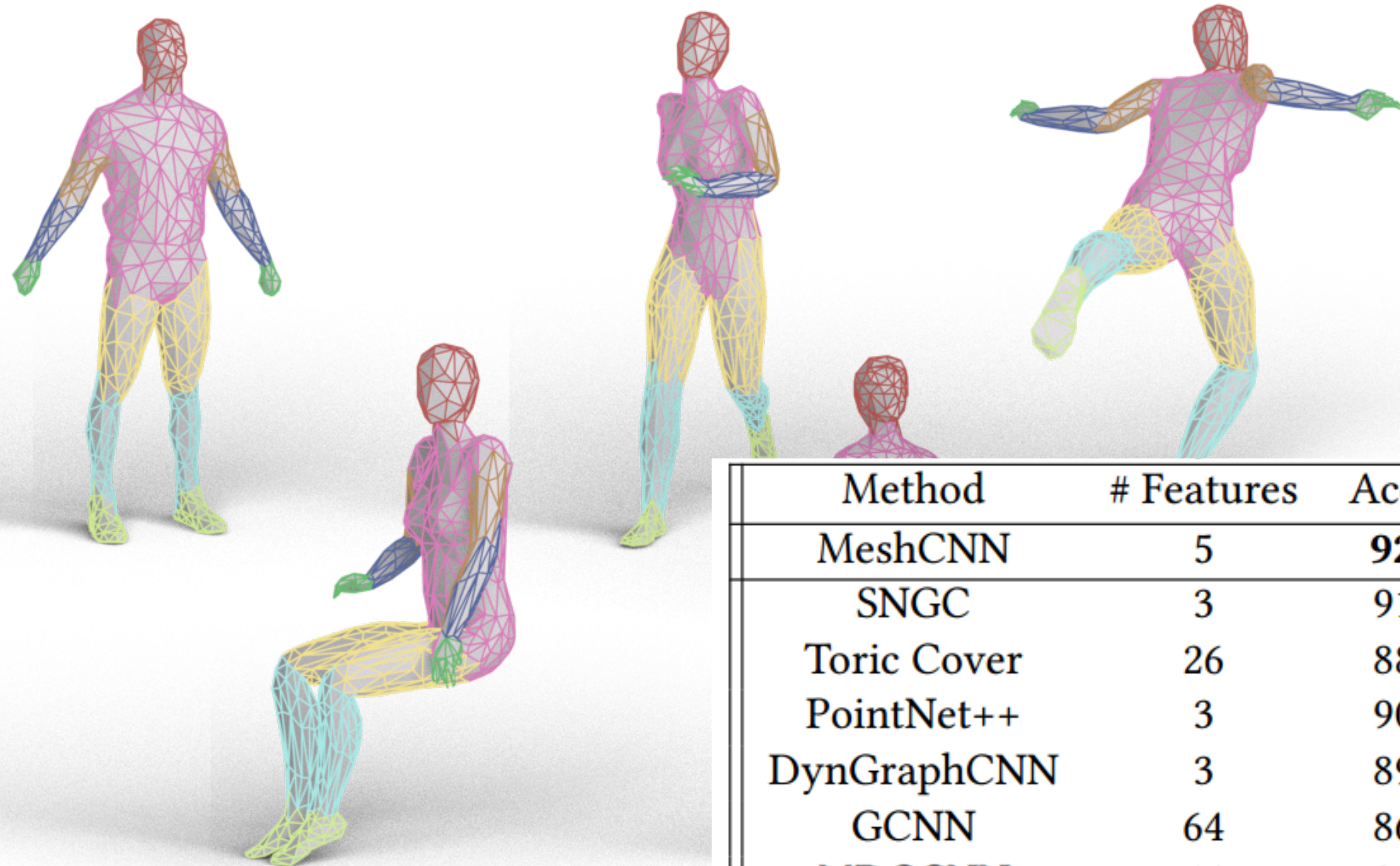
92.16%



Intermediate Mesh Pooling

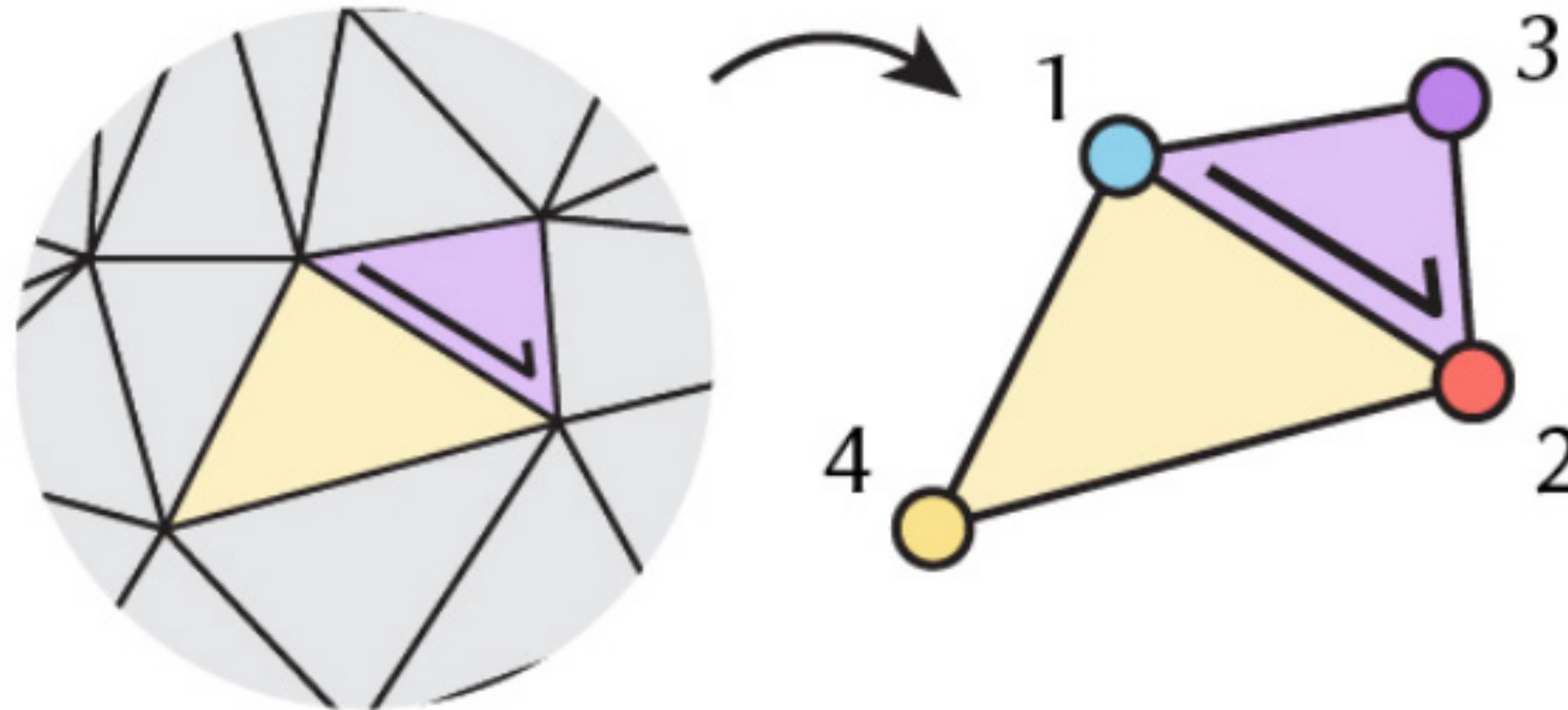


Human Segmentation

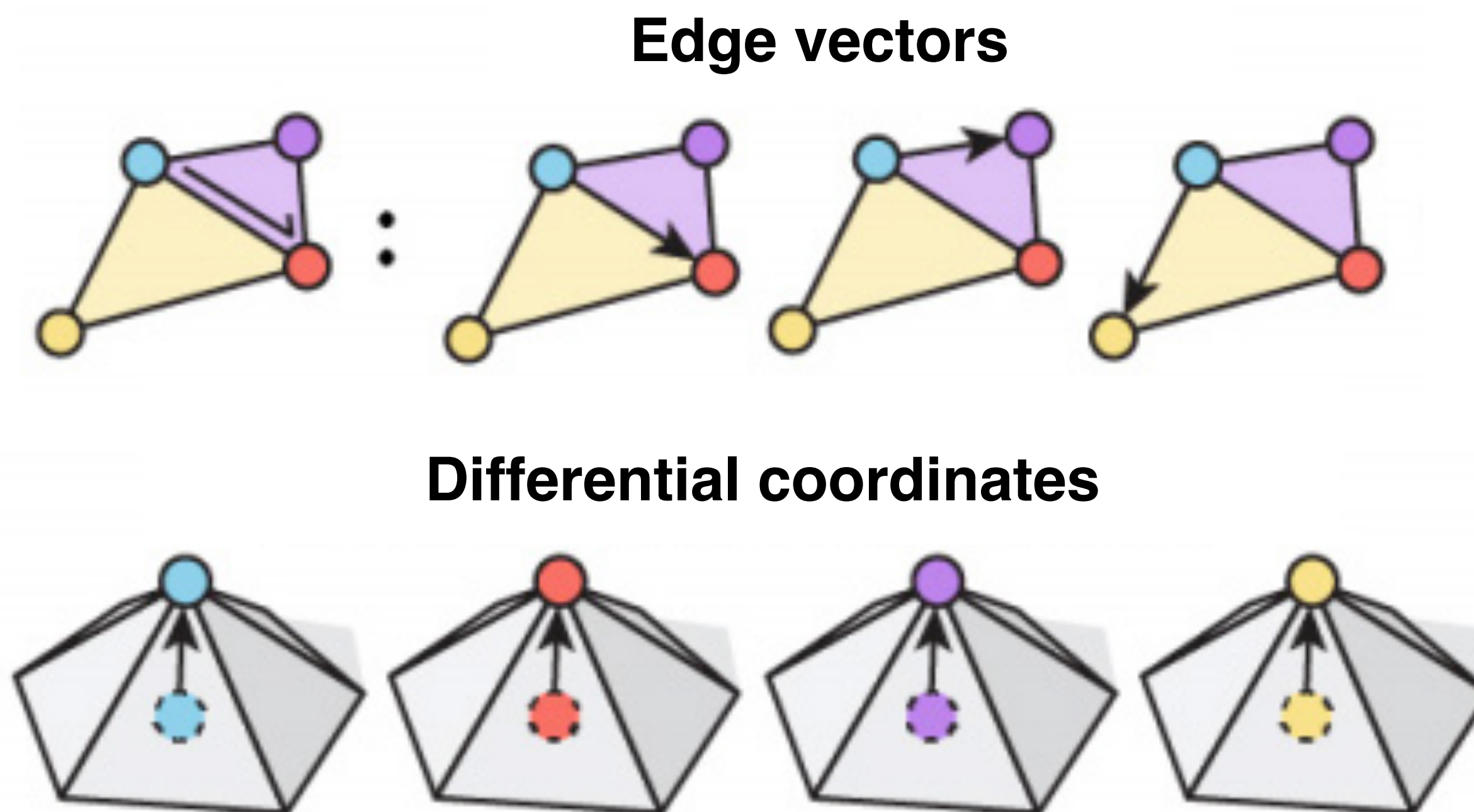


Method	# Features	Accuracy
MeshCNN	5	92.30%
SNGC	3	91.02%
Toric Cover	26	88.00%
PointNet++	3	90.77%
DynGraphCNN	3	89.72%
GCNN	64	86.40%
MDGCNN	64	89.47%

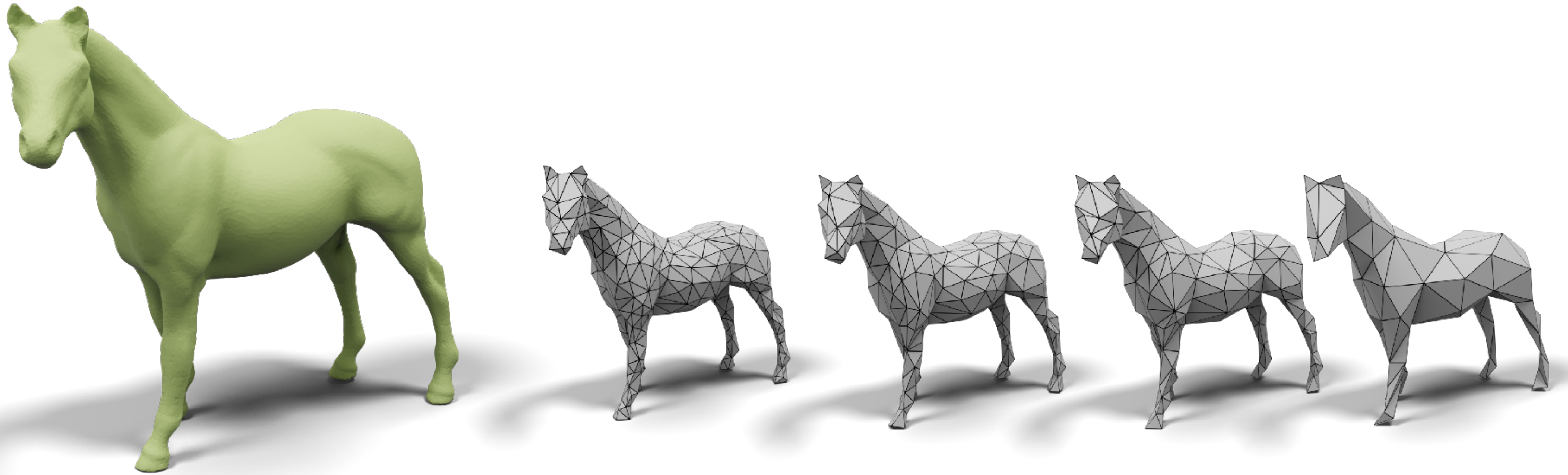
Convolutions on half-edges



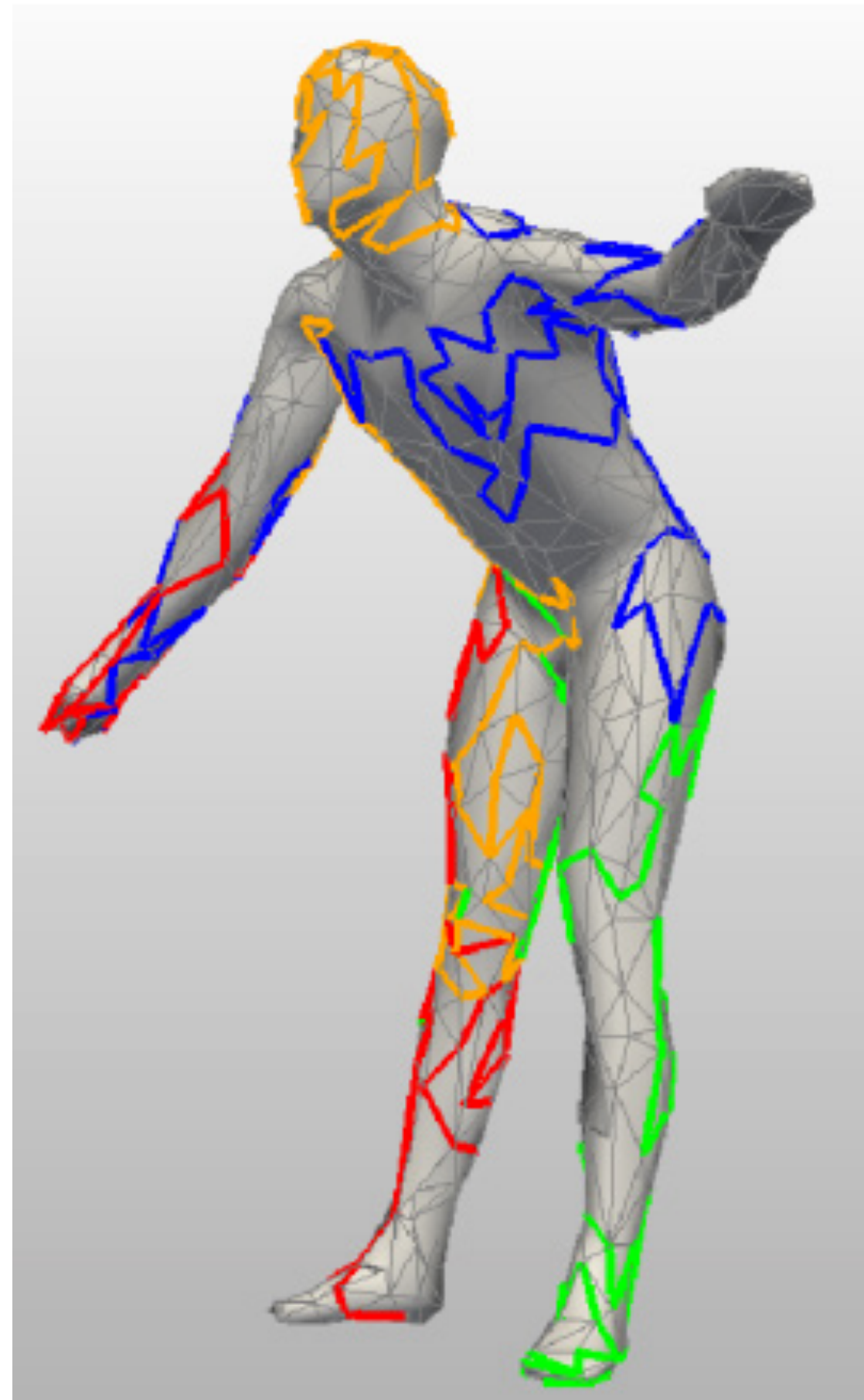
Half-edge input features



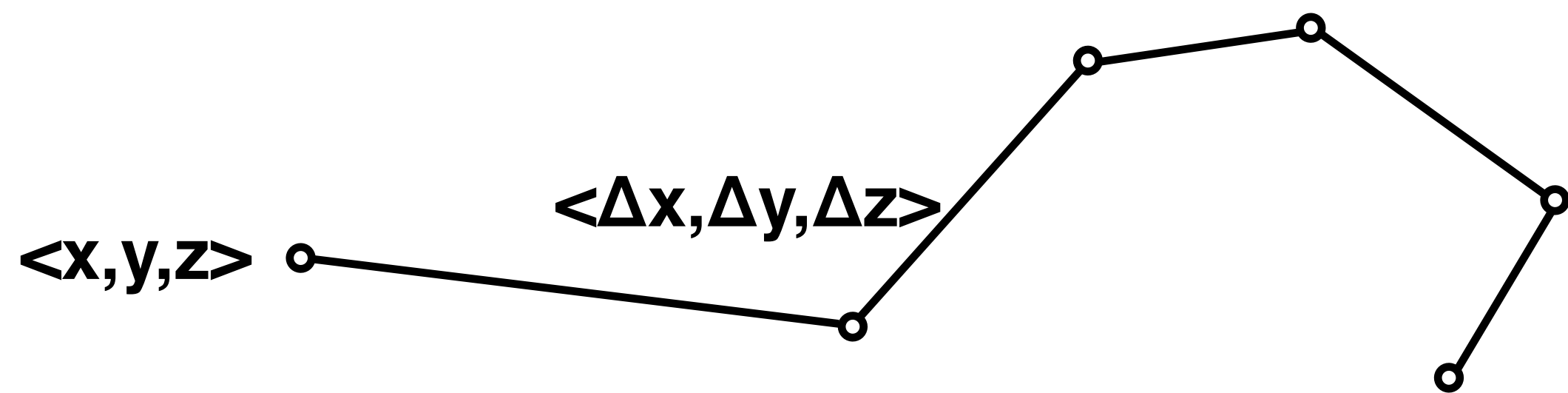
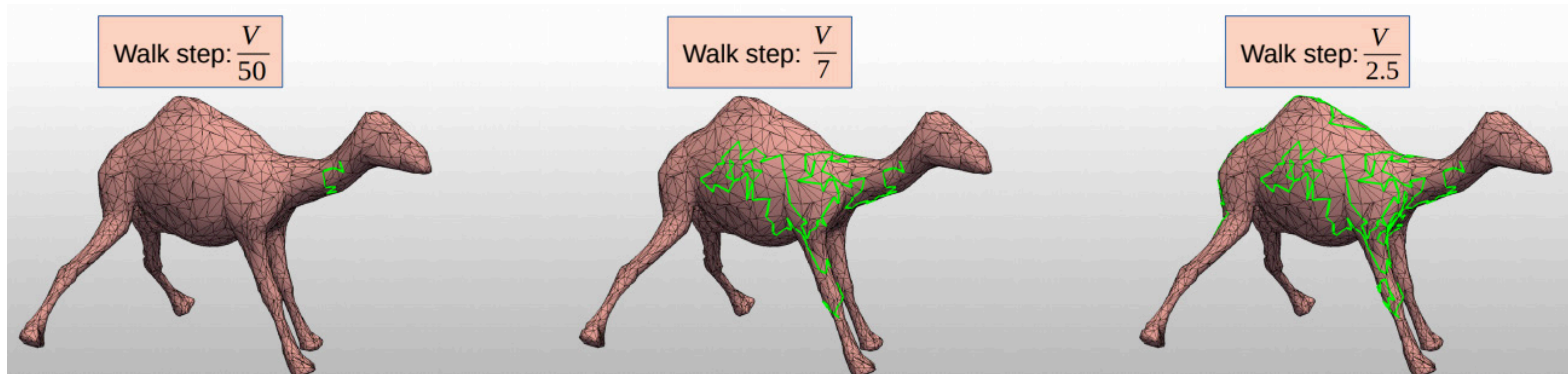
Input mesh coarsening



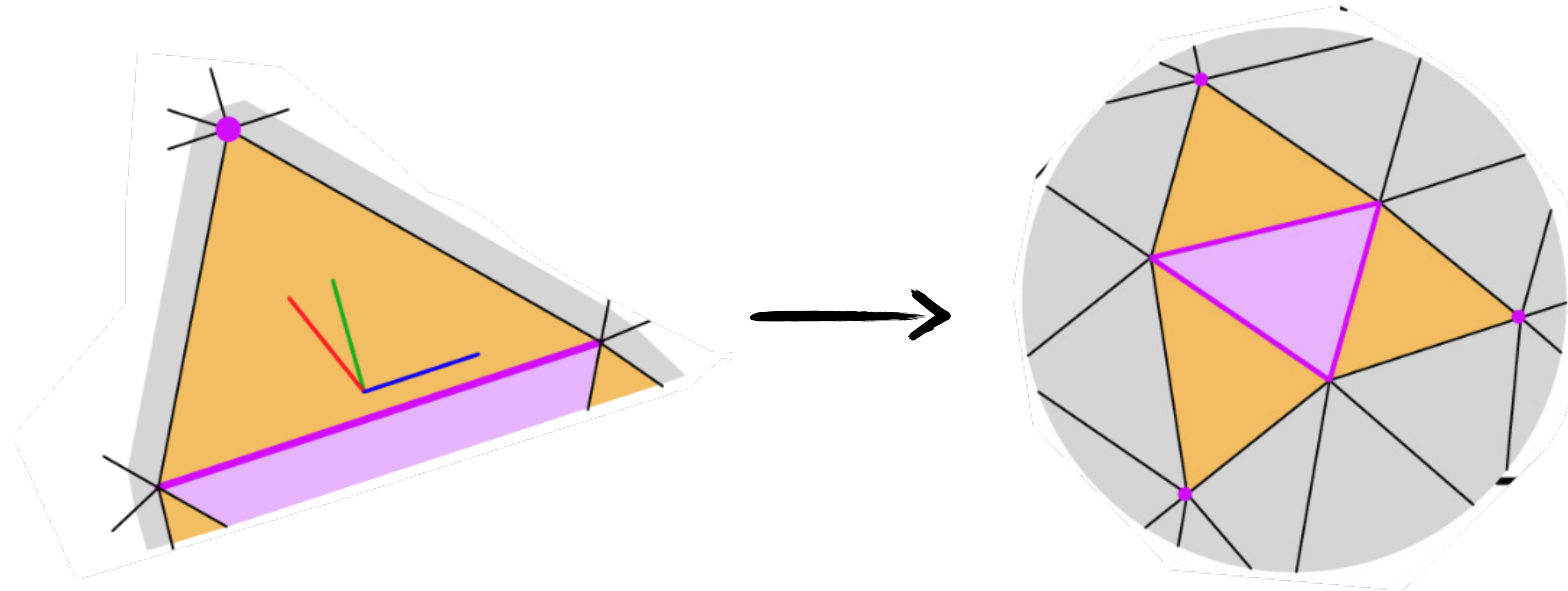
Learning on random walks



Learning on random walks



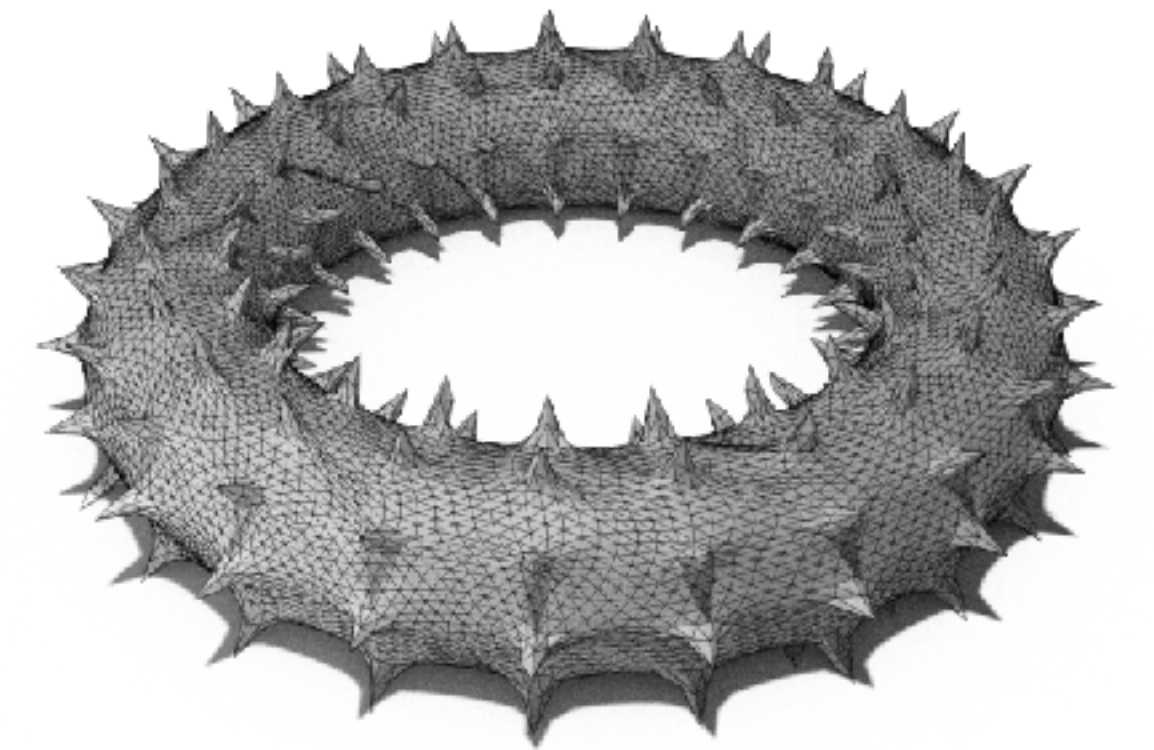
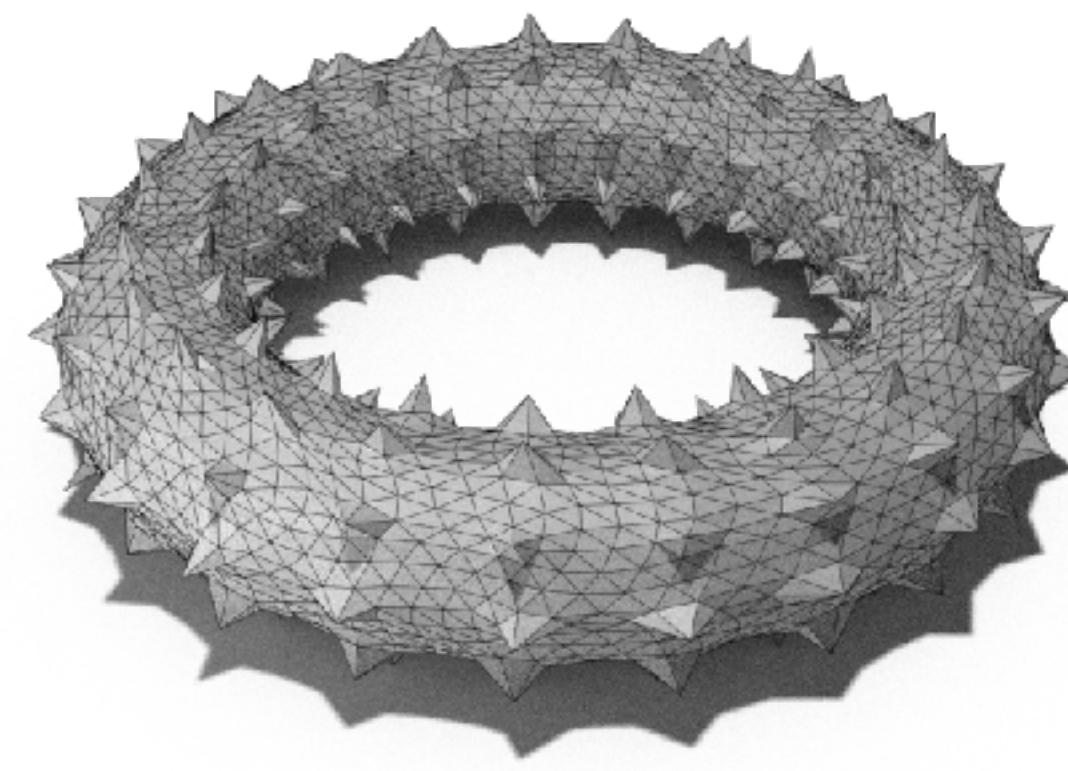
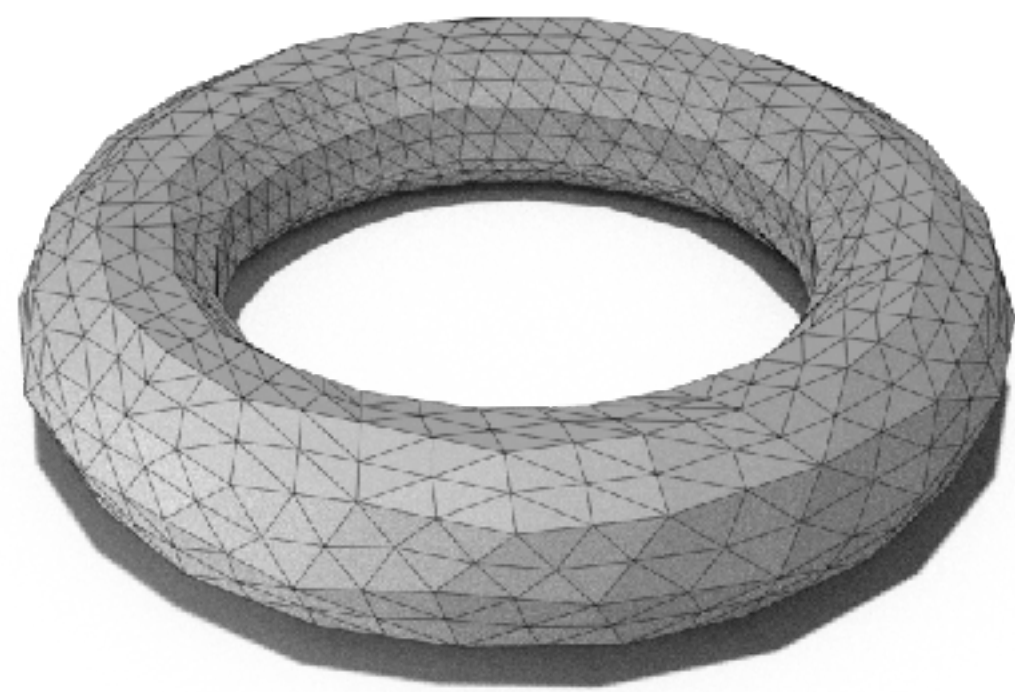
Convolutions on mesh faces



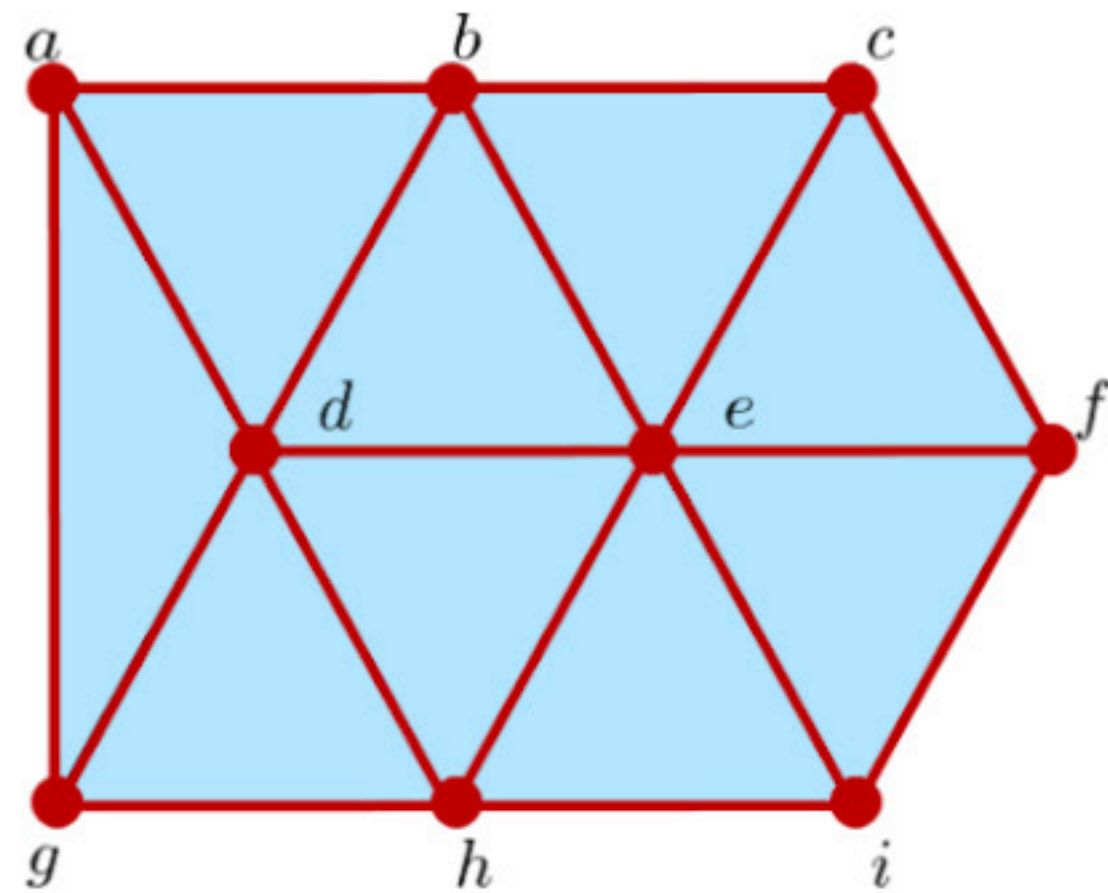
Input features

Face-based convolution

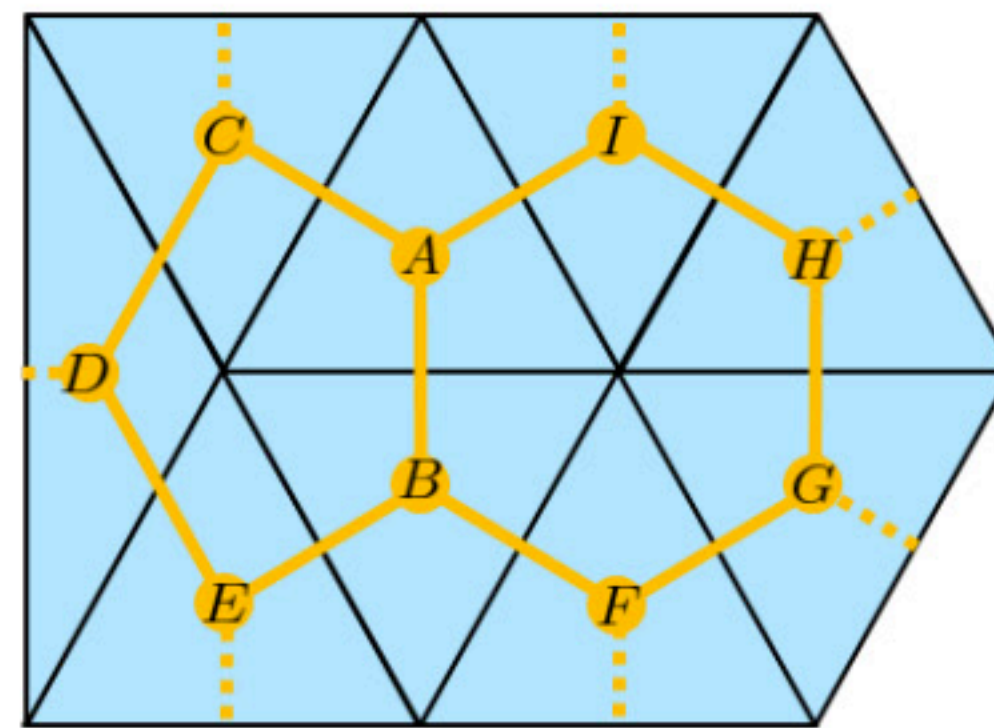
Input mesh untexturing



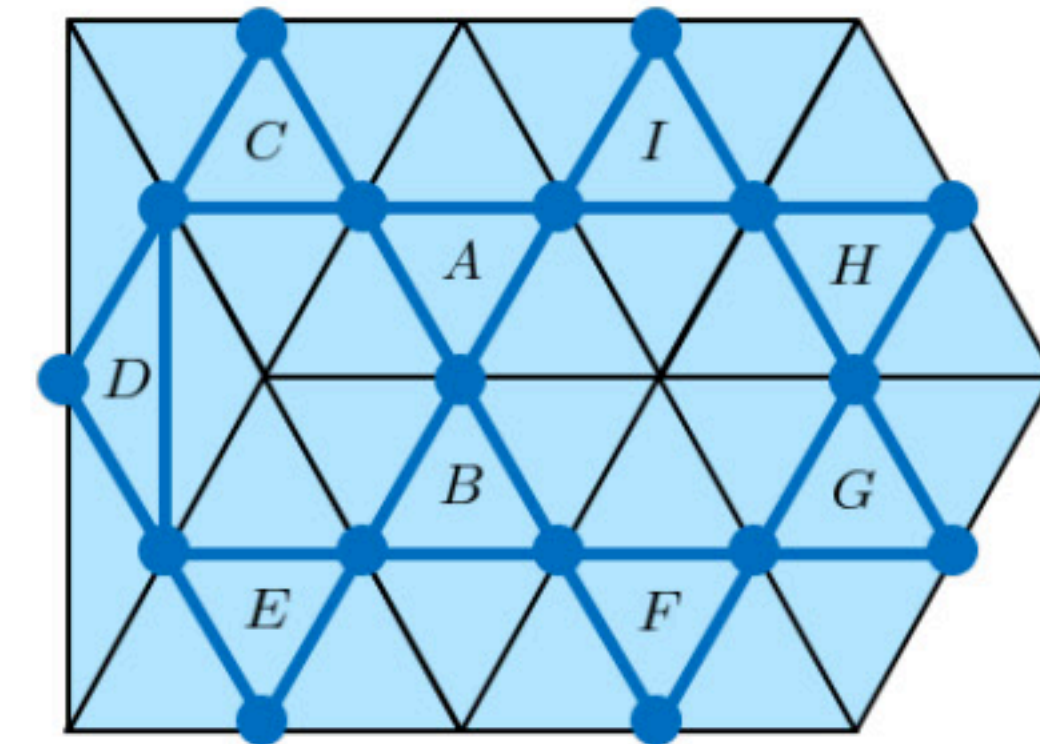
Convolutions on primal/dual mesh graphs



Mesh

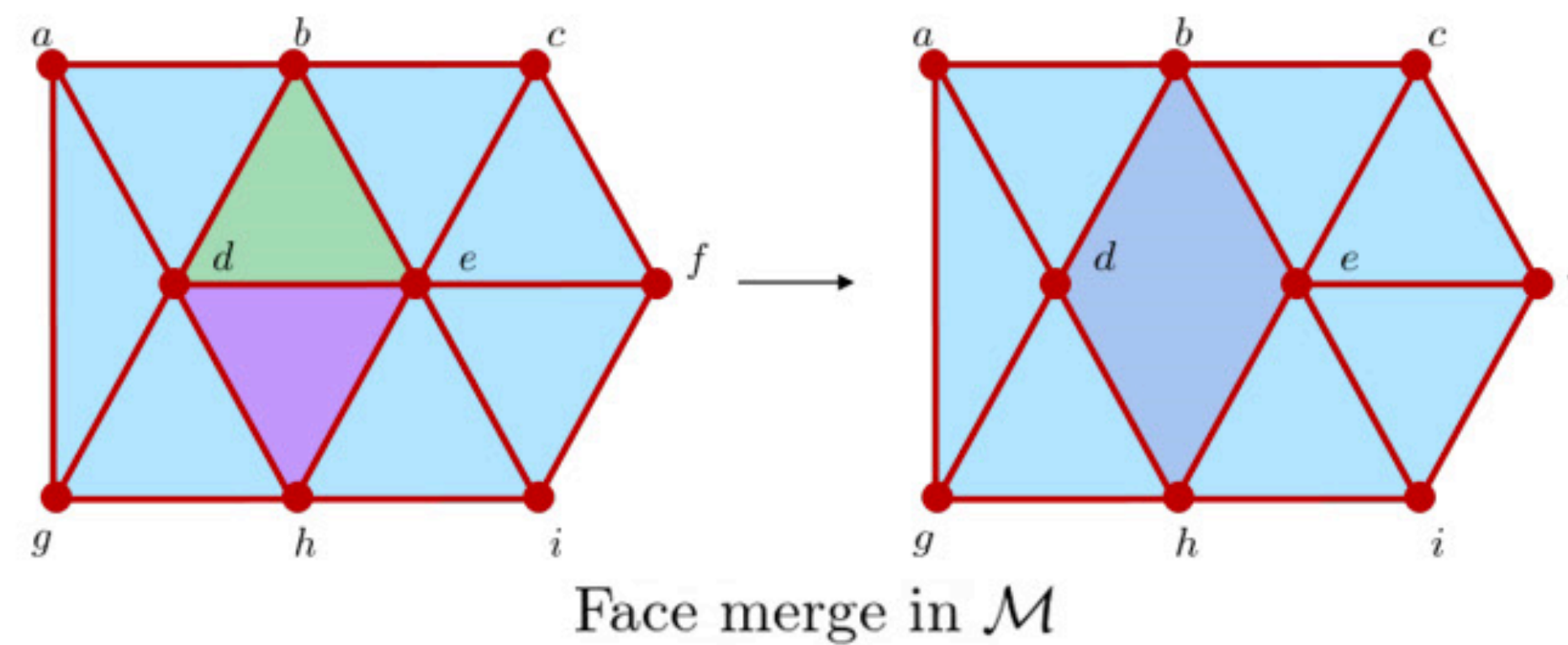
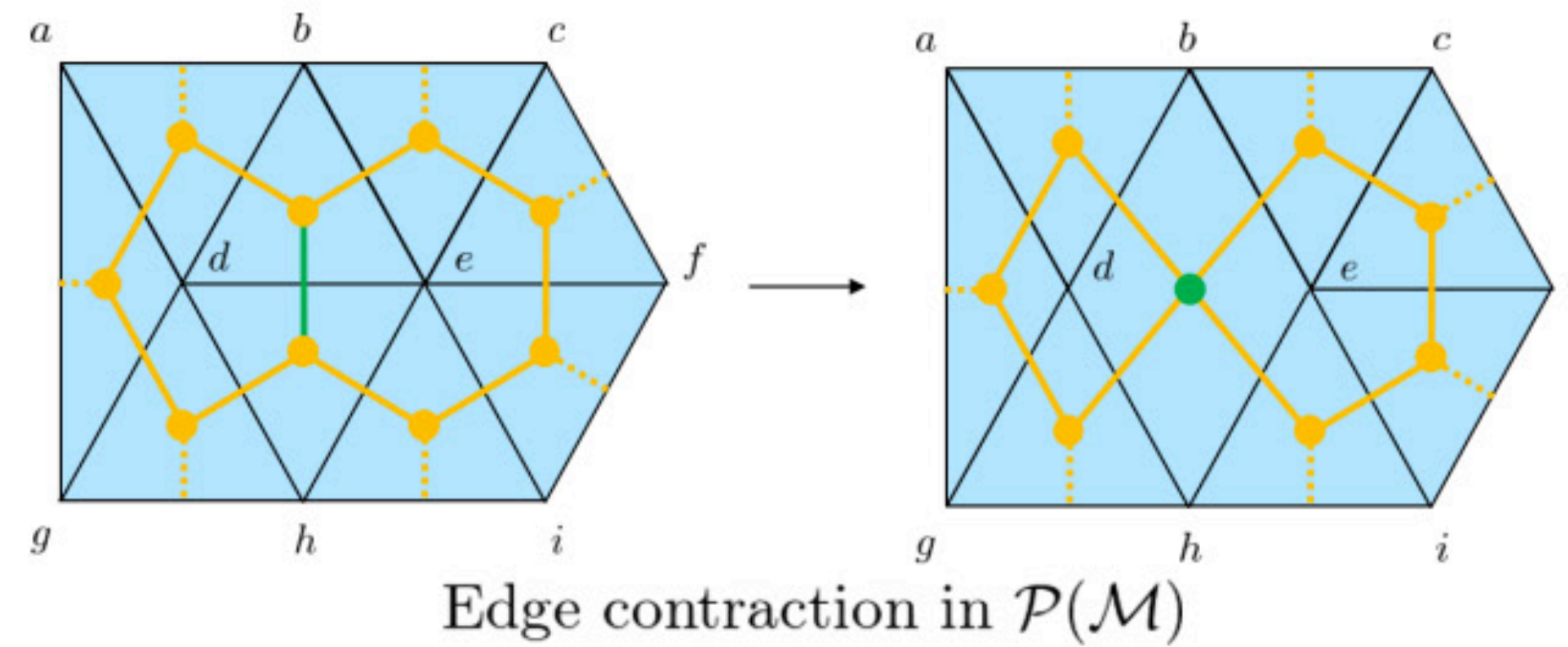


Primal Graph

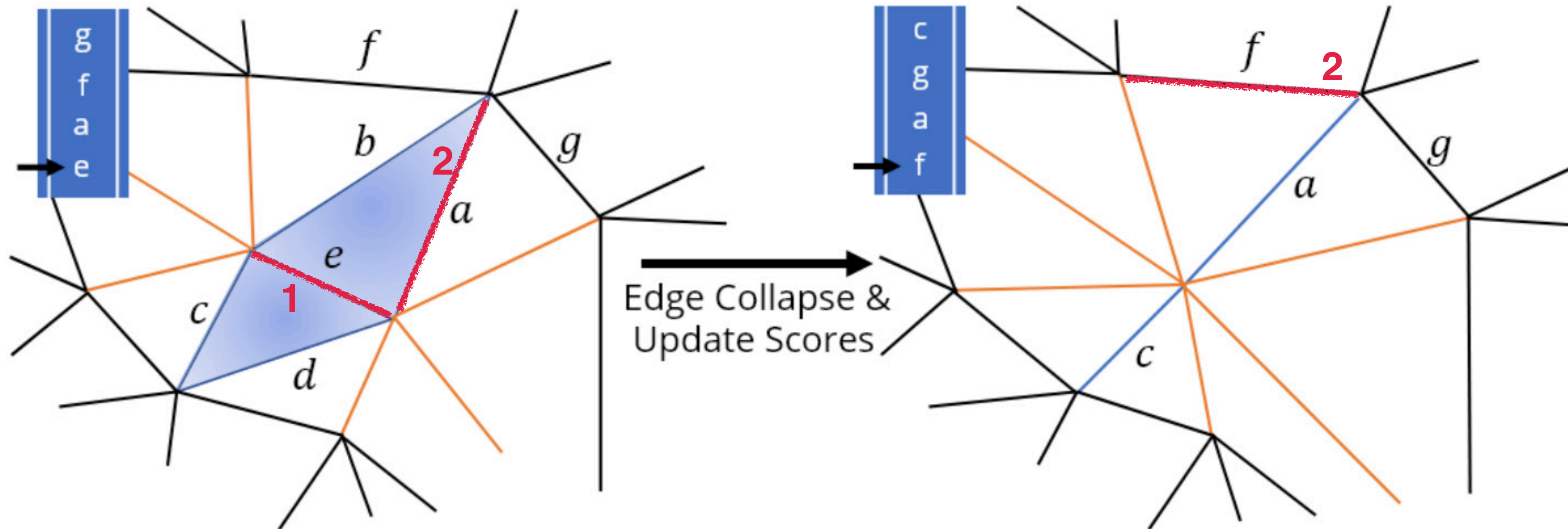


Dual Graph

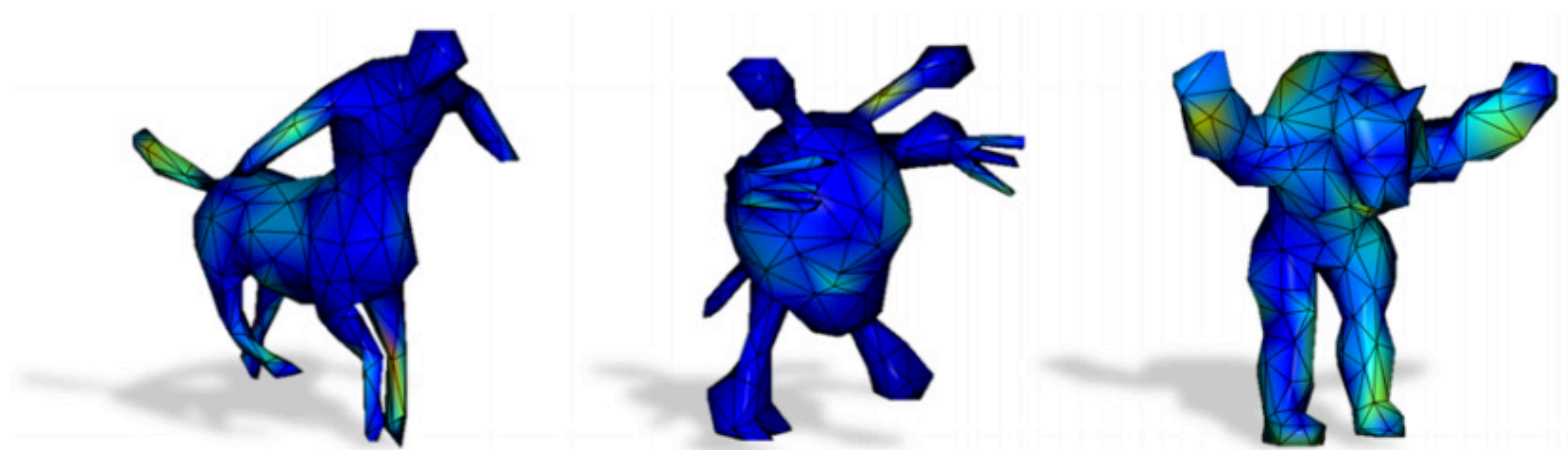
Mesh Pooling via Edge Contraction



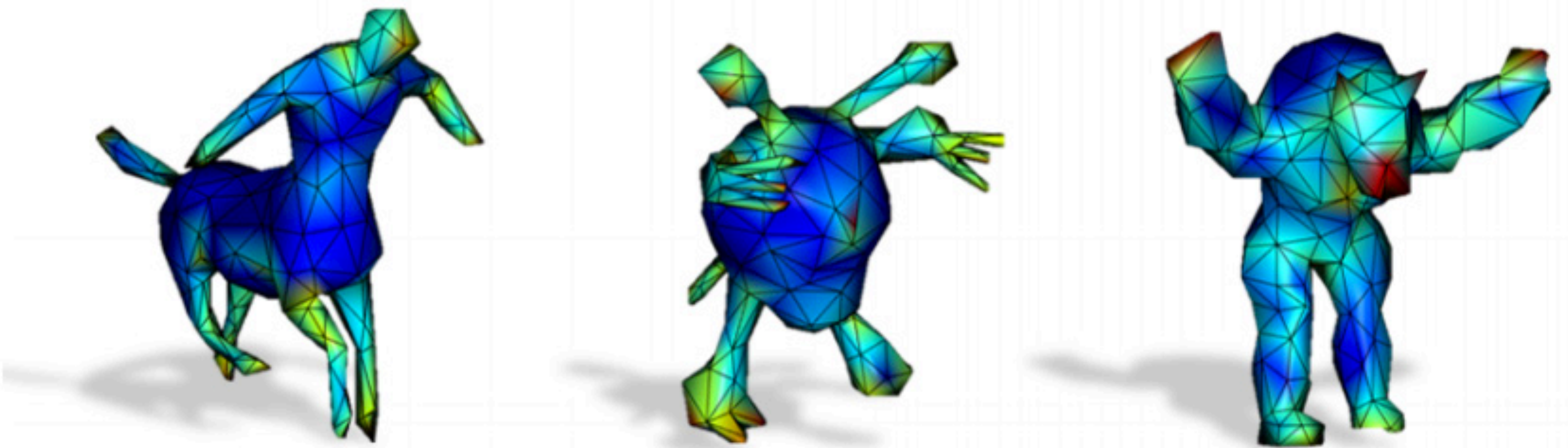
Enhanced mesh pooling



Enhanced mesh pooling

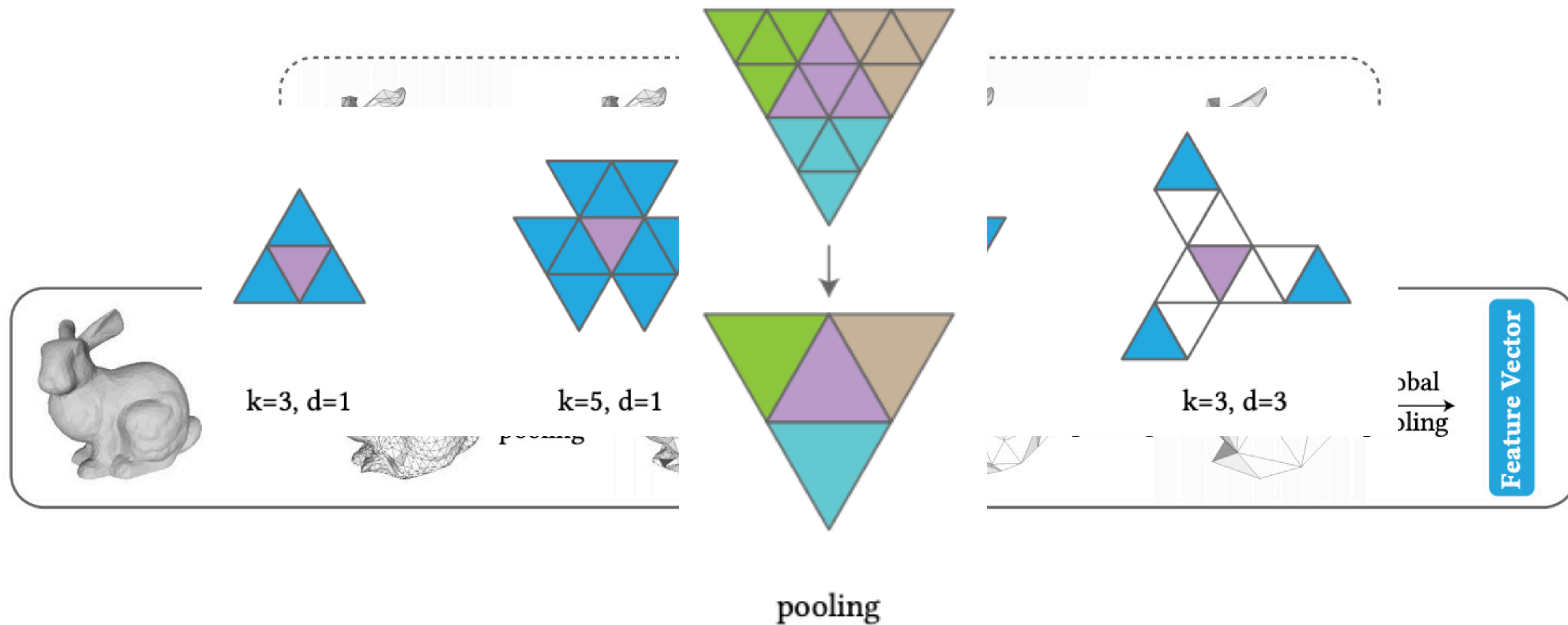


Original mesh pooling

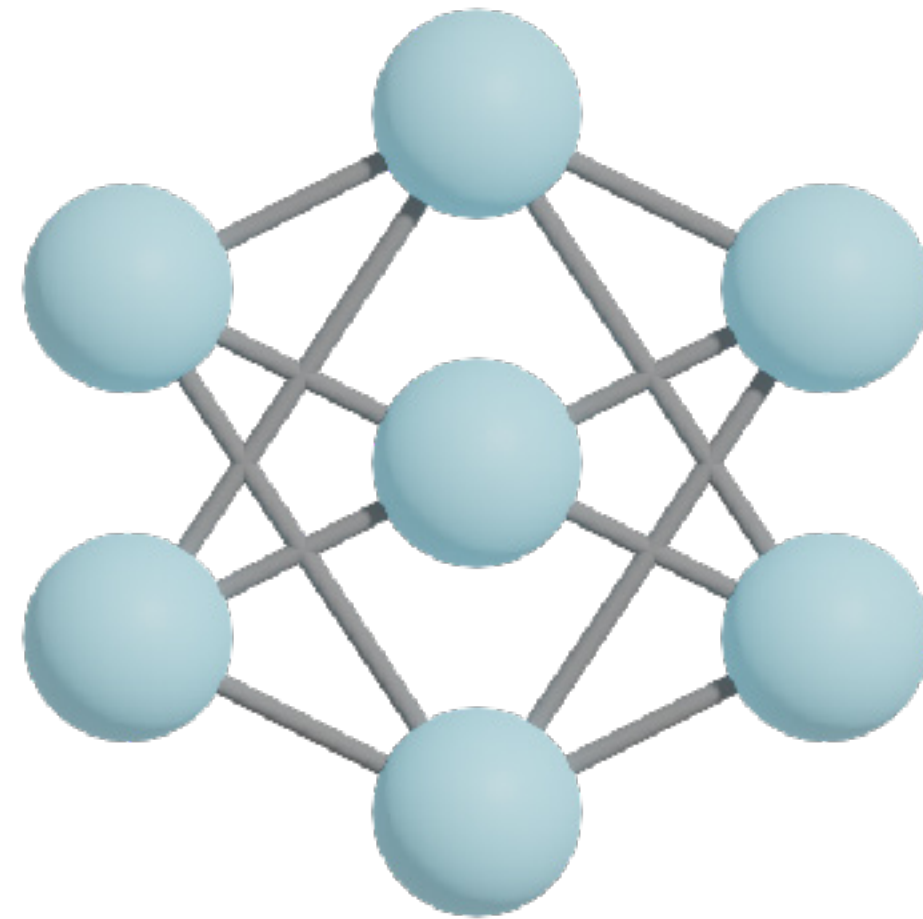


Enhanced mesh pooling

Convolution and pooling from subdivision



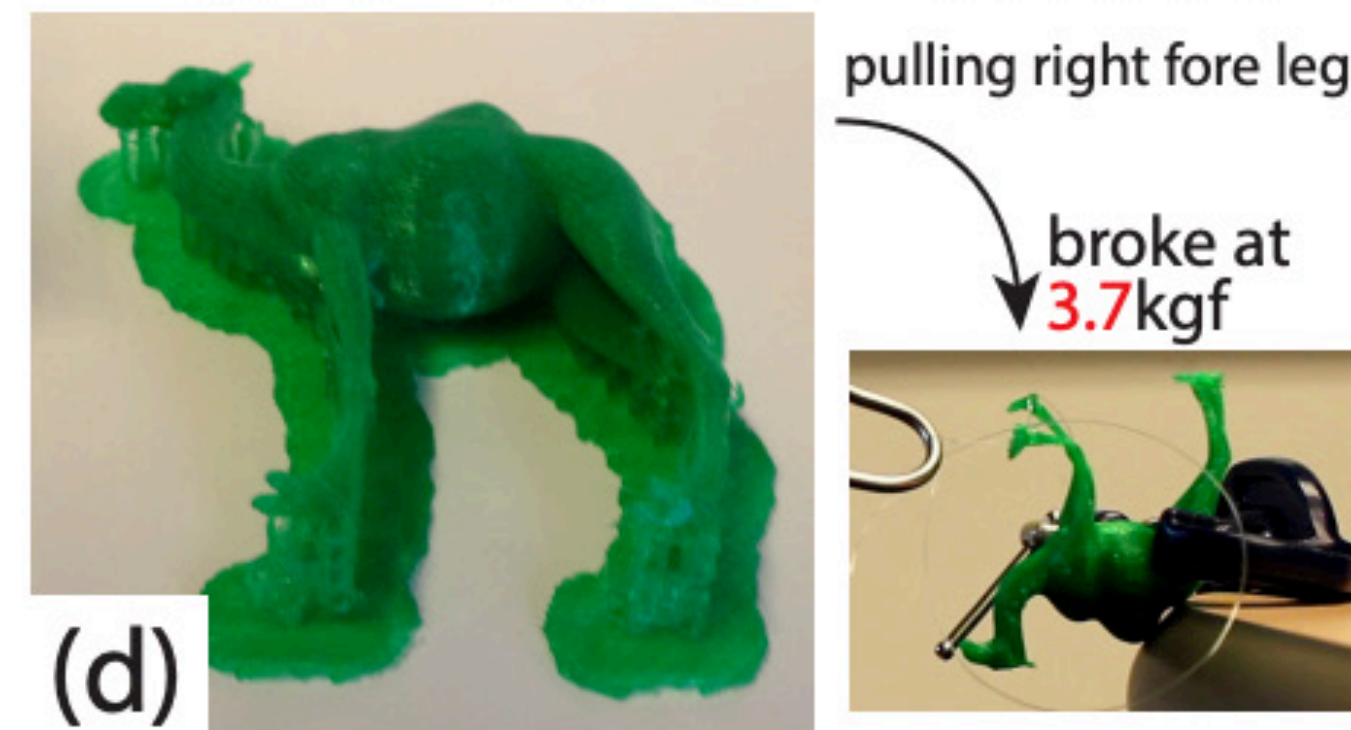
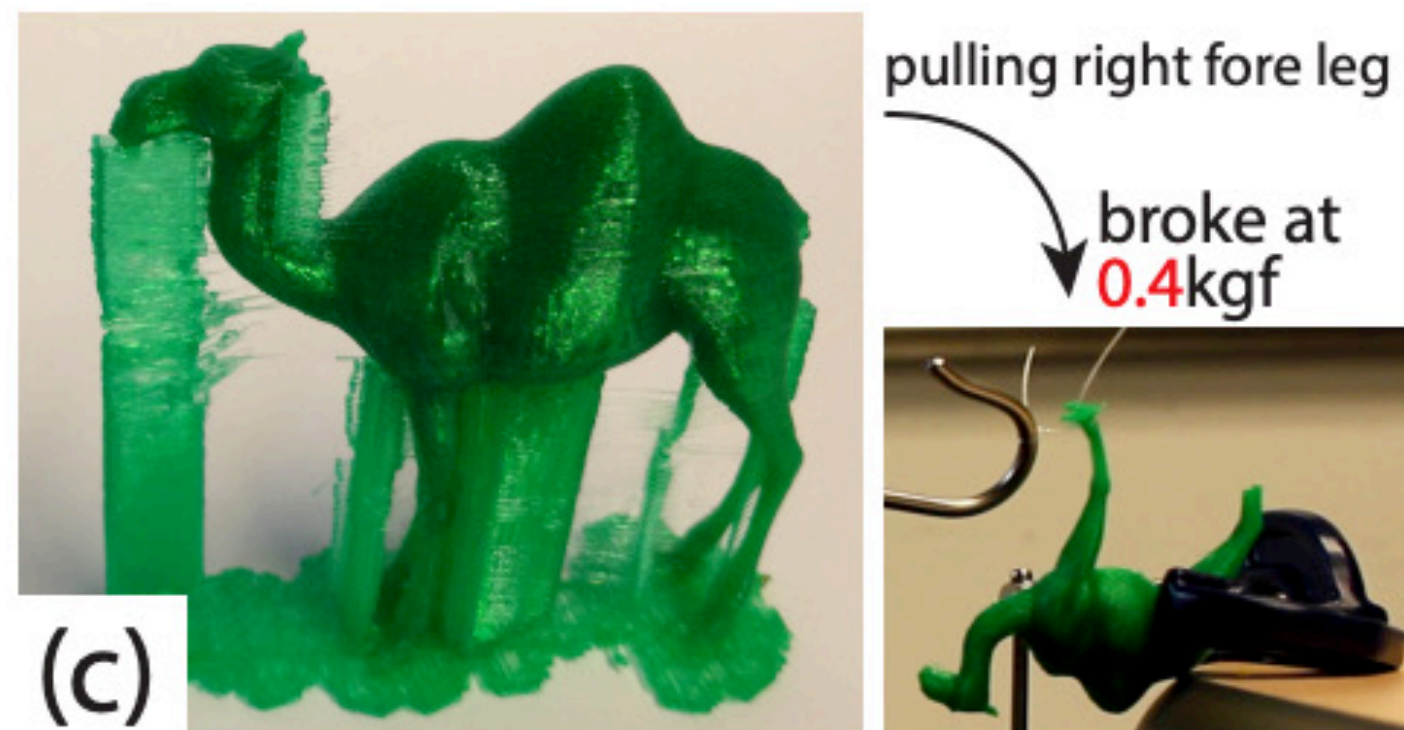
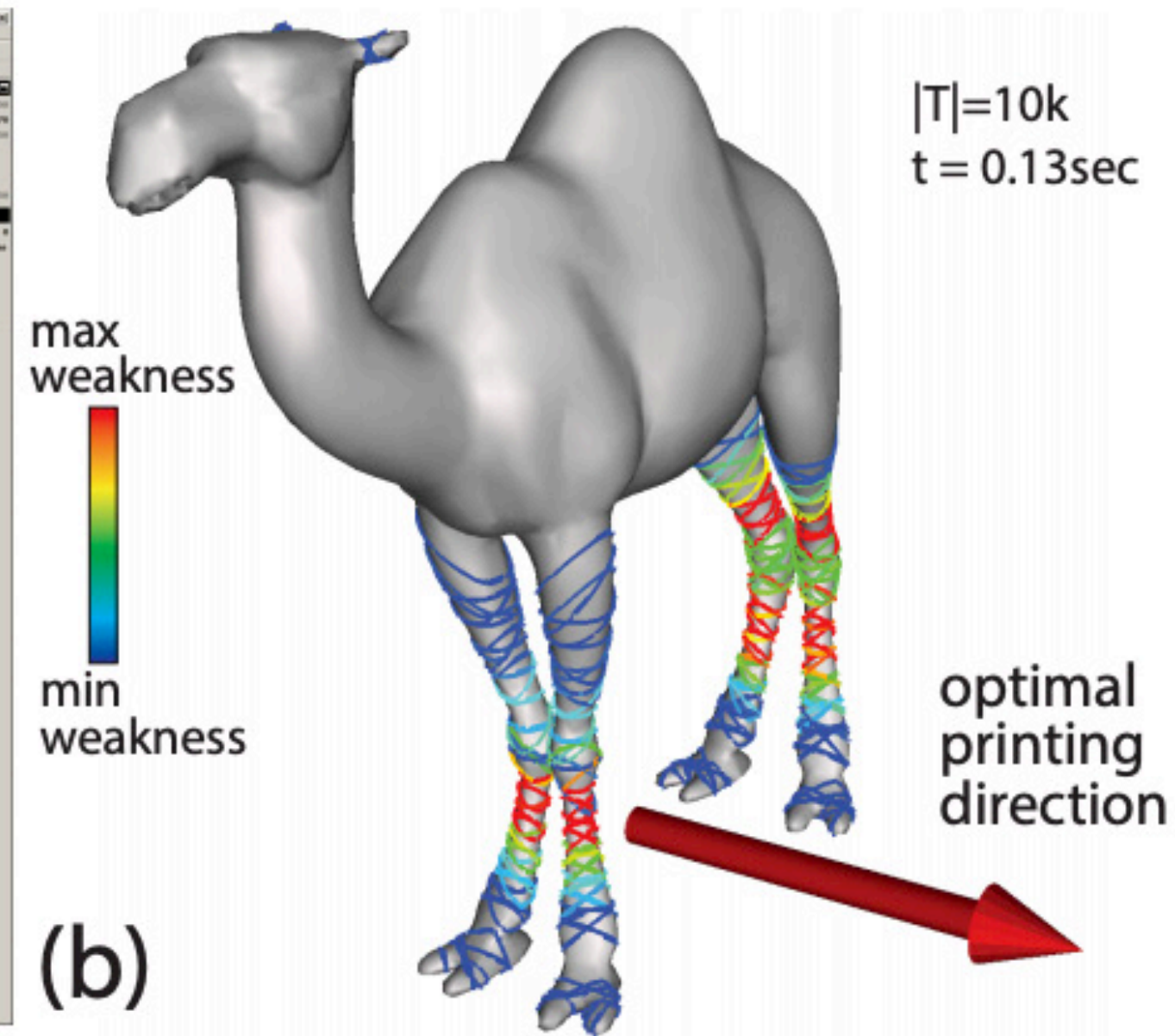
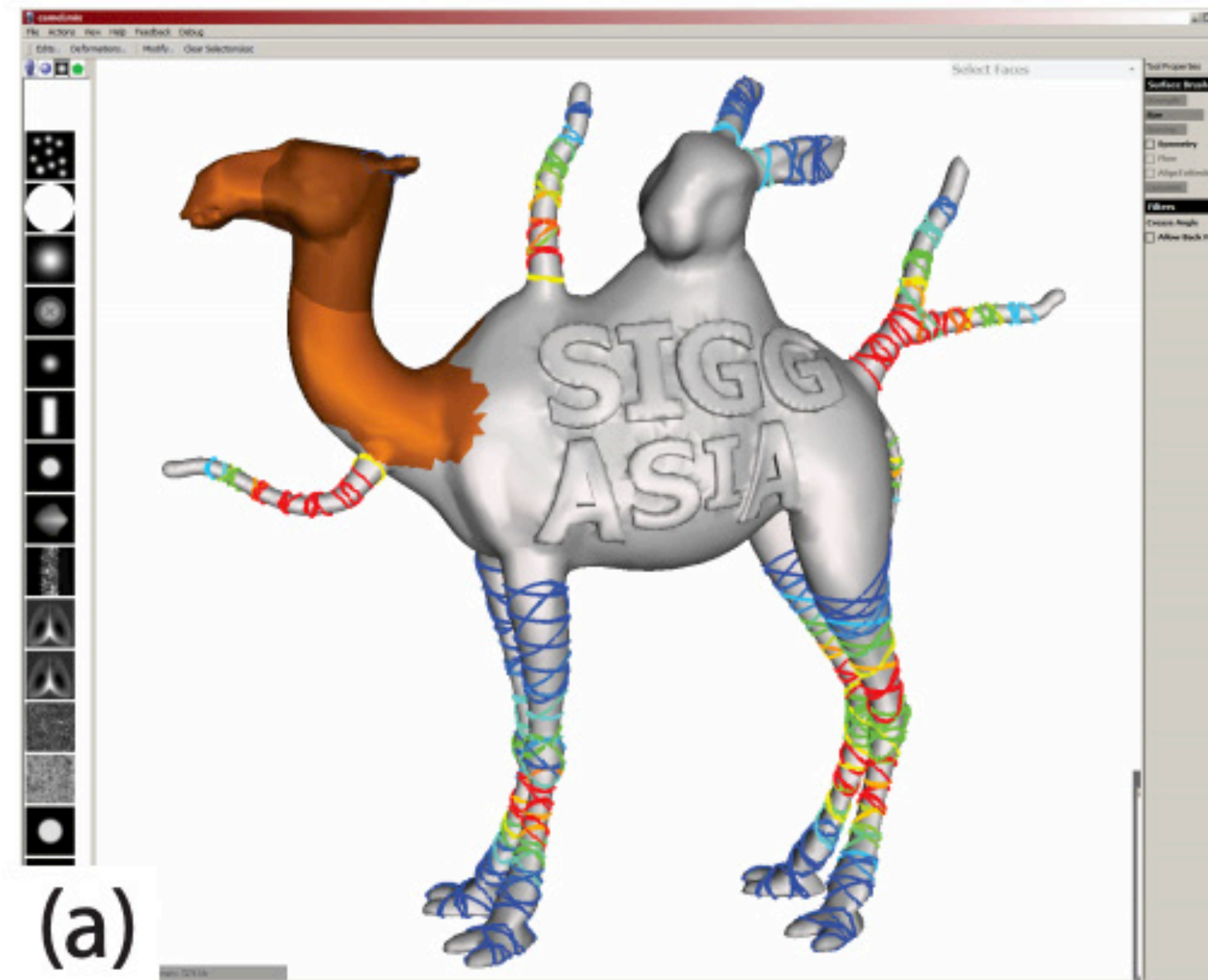
Invariance to rigid transformations



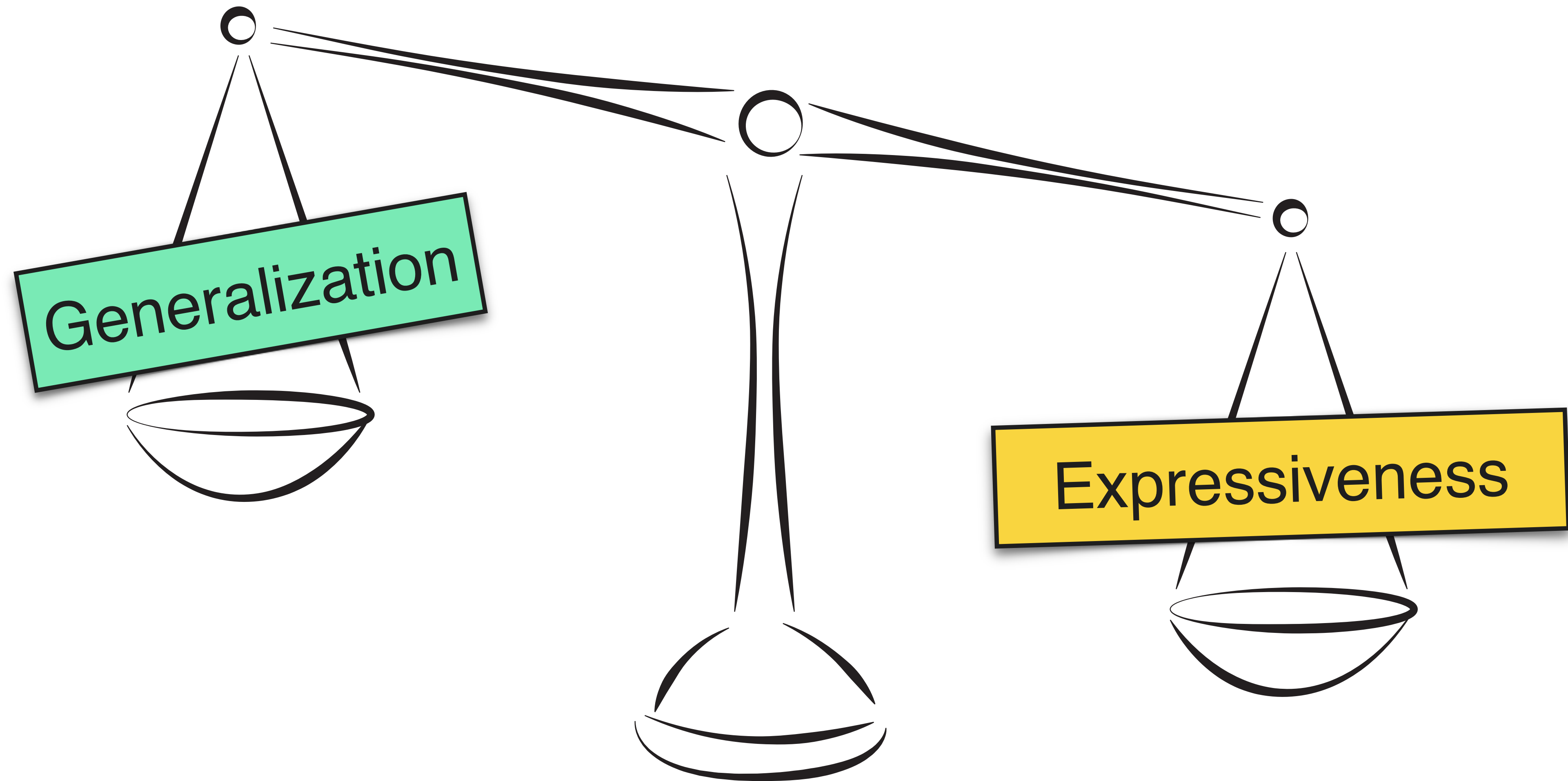
still
∨
It's a bunny

Invariance to rigid transformations

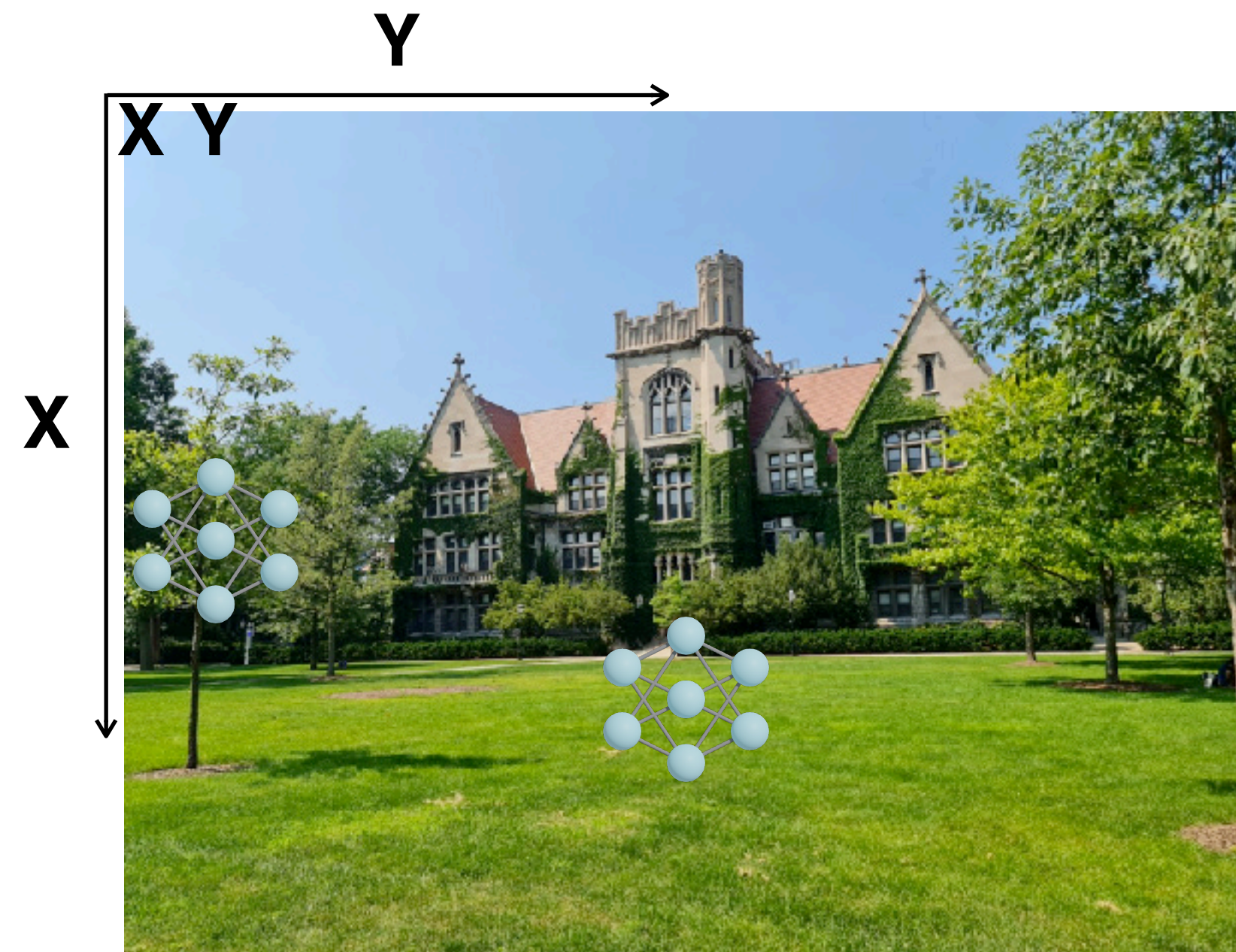
... sometimes this can be too restrictive



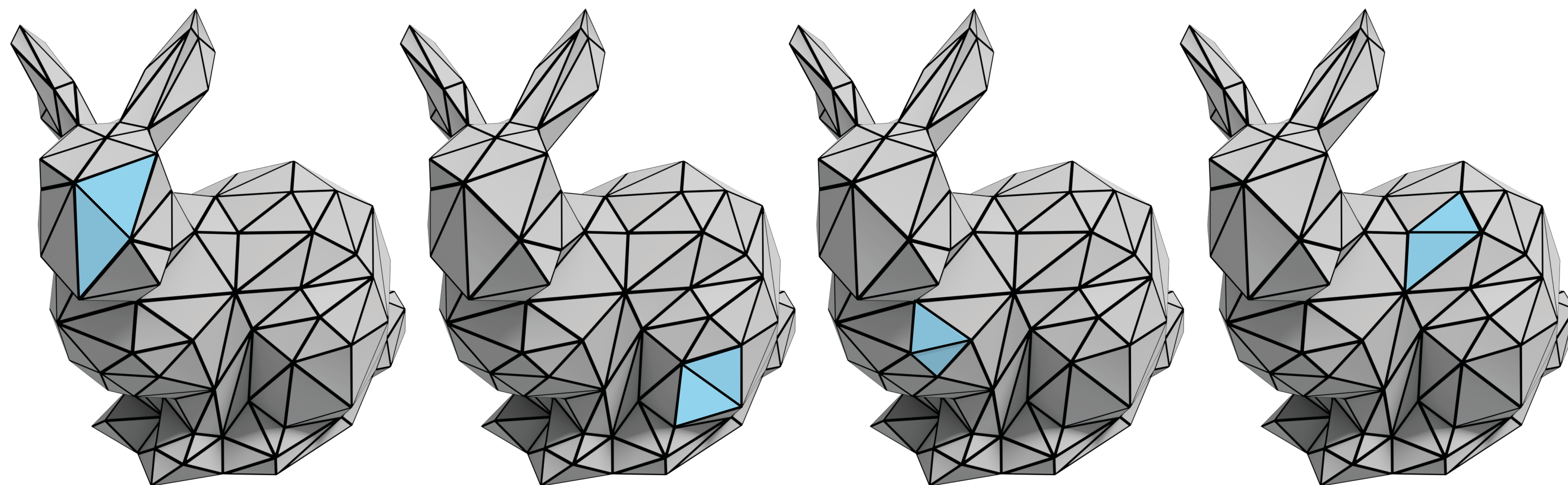
Expressiveness vs. Generalization



Break shift-invariance

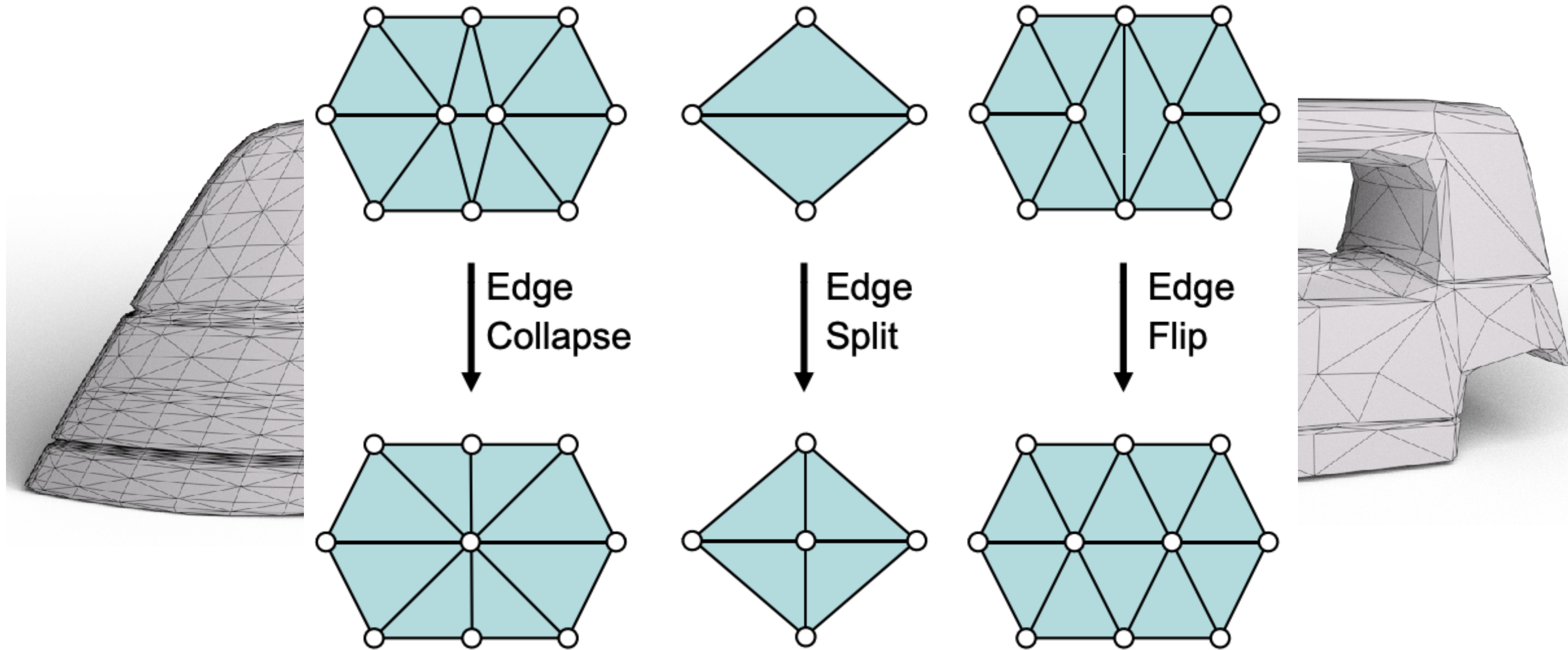


Gain expressive power
Helps better fit the data

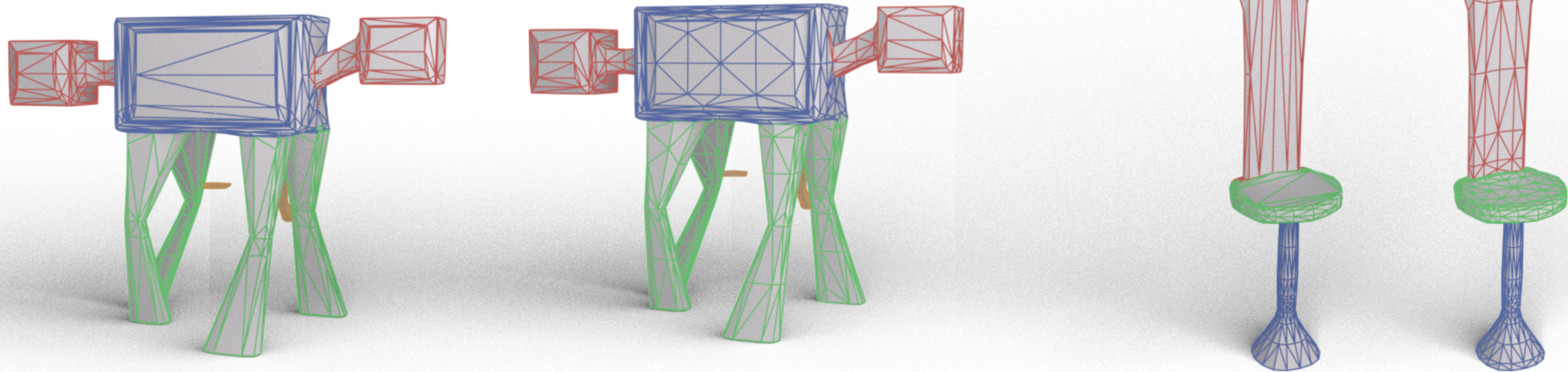


Triangulation robustness

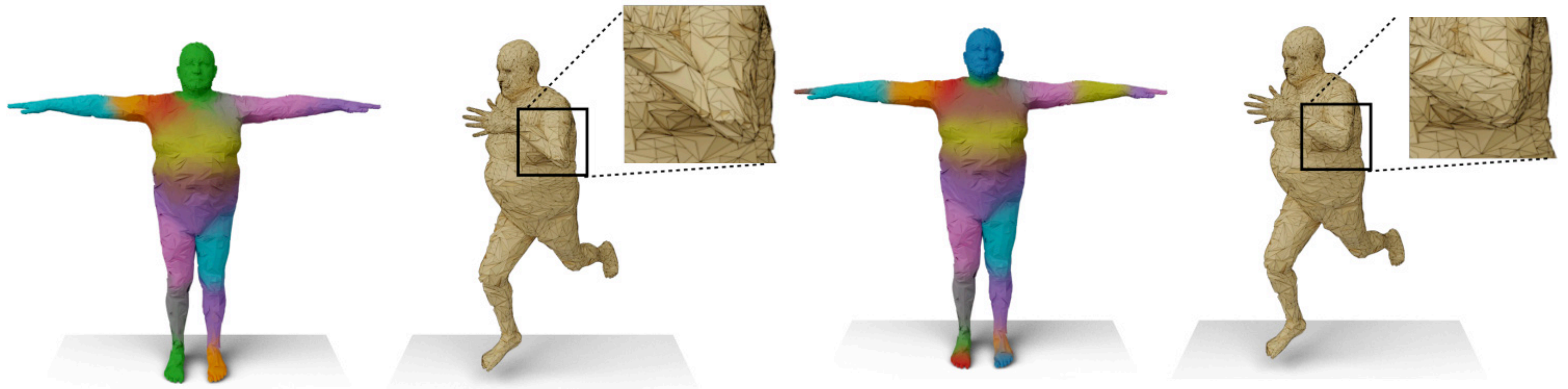
Perform simple augmentations



Triangulation robustness in segmentation



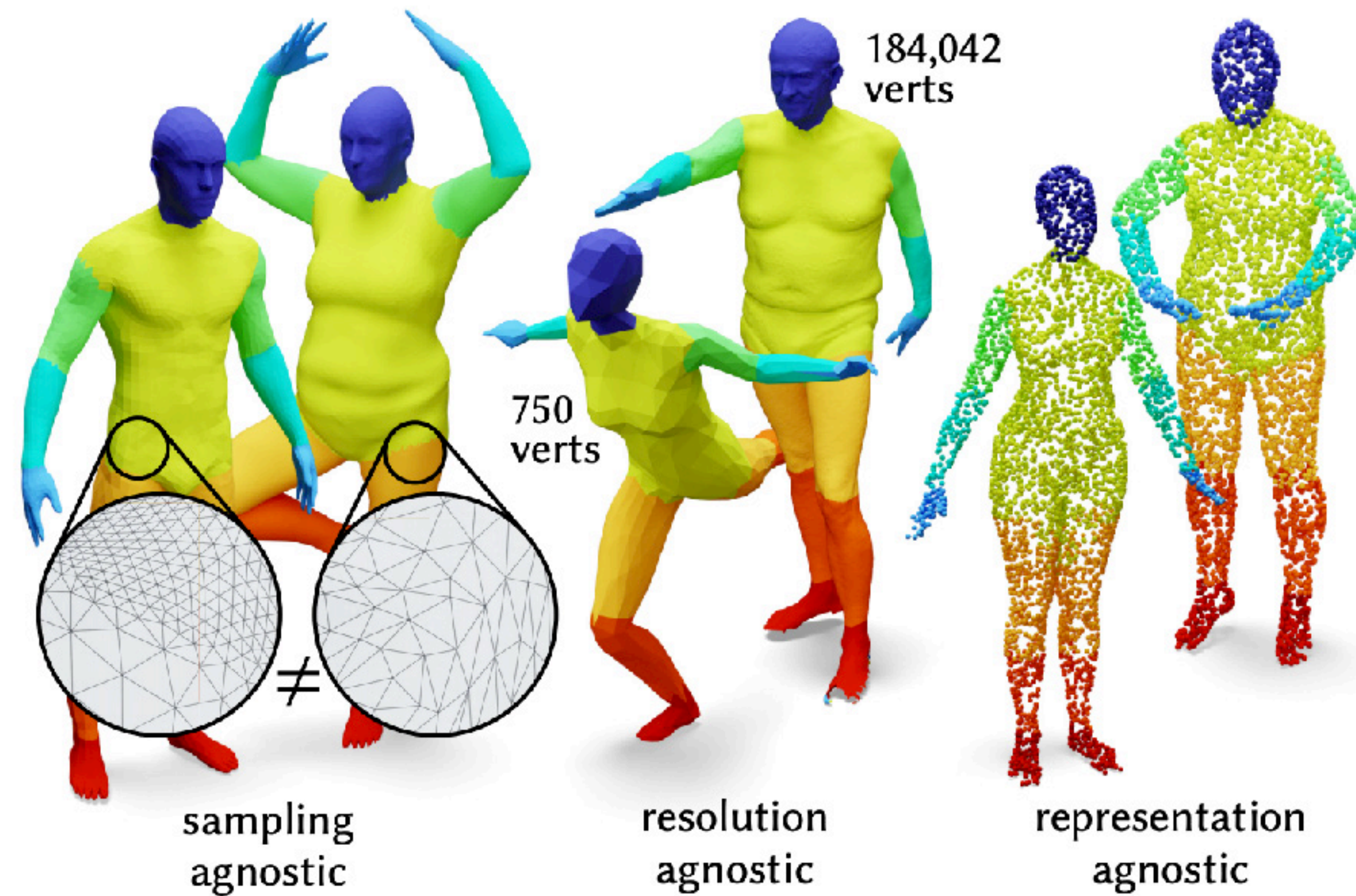
Triangulation robustness in deformation



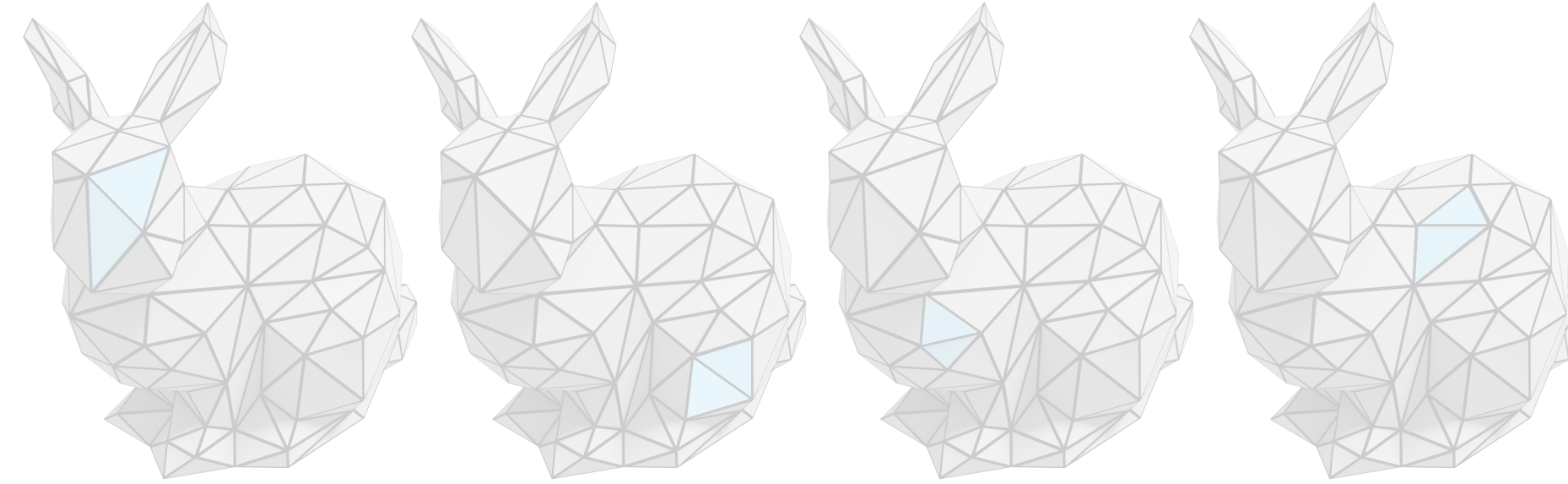
Without augmentation

With augmentation

Triangulation robustness via diffusion



Mesh Convolutional Neural Networks



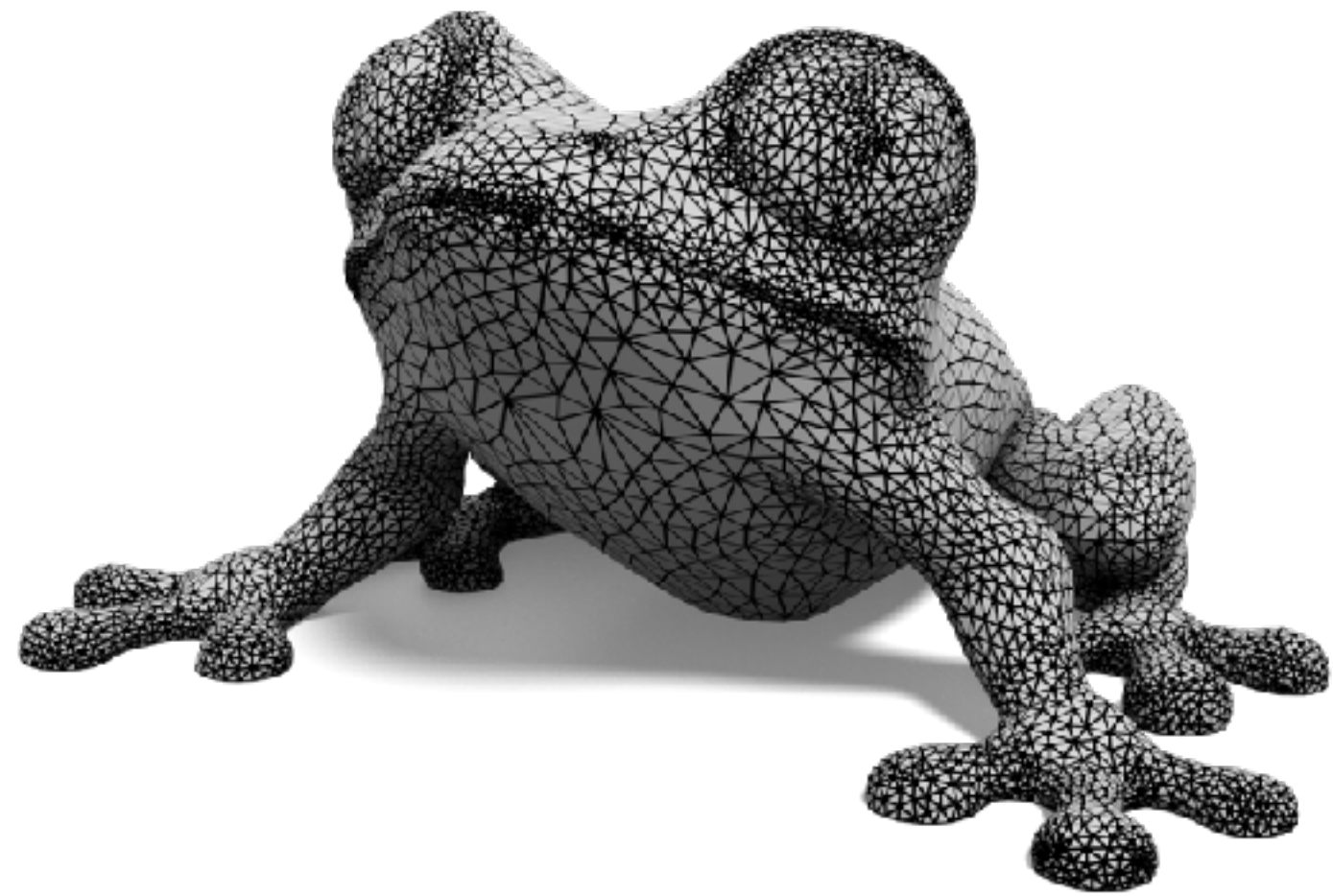
Machine Learning & Geometry Processing



Learning from a Single Mesh



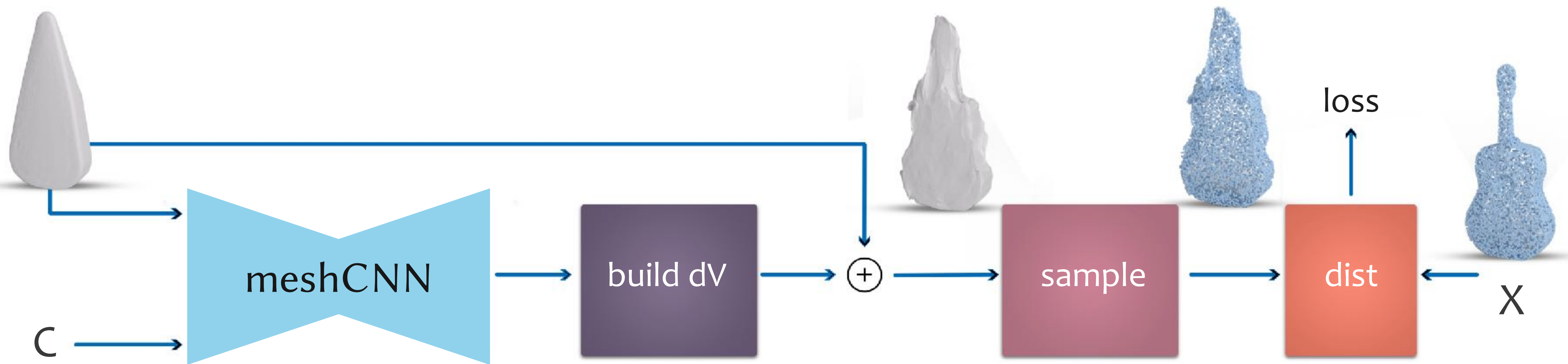
A Fundamental Tool: MeshCNN



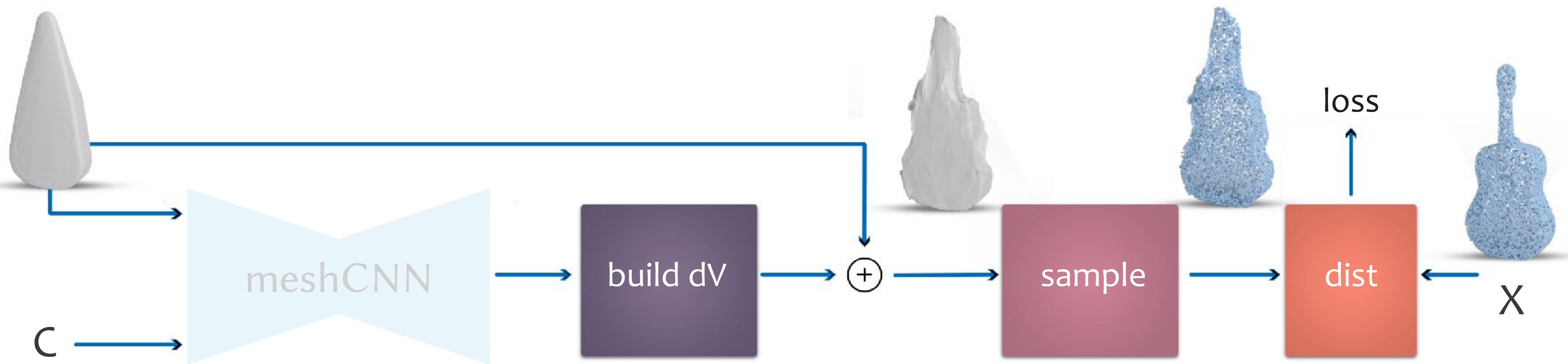
meshCNN

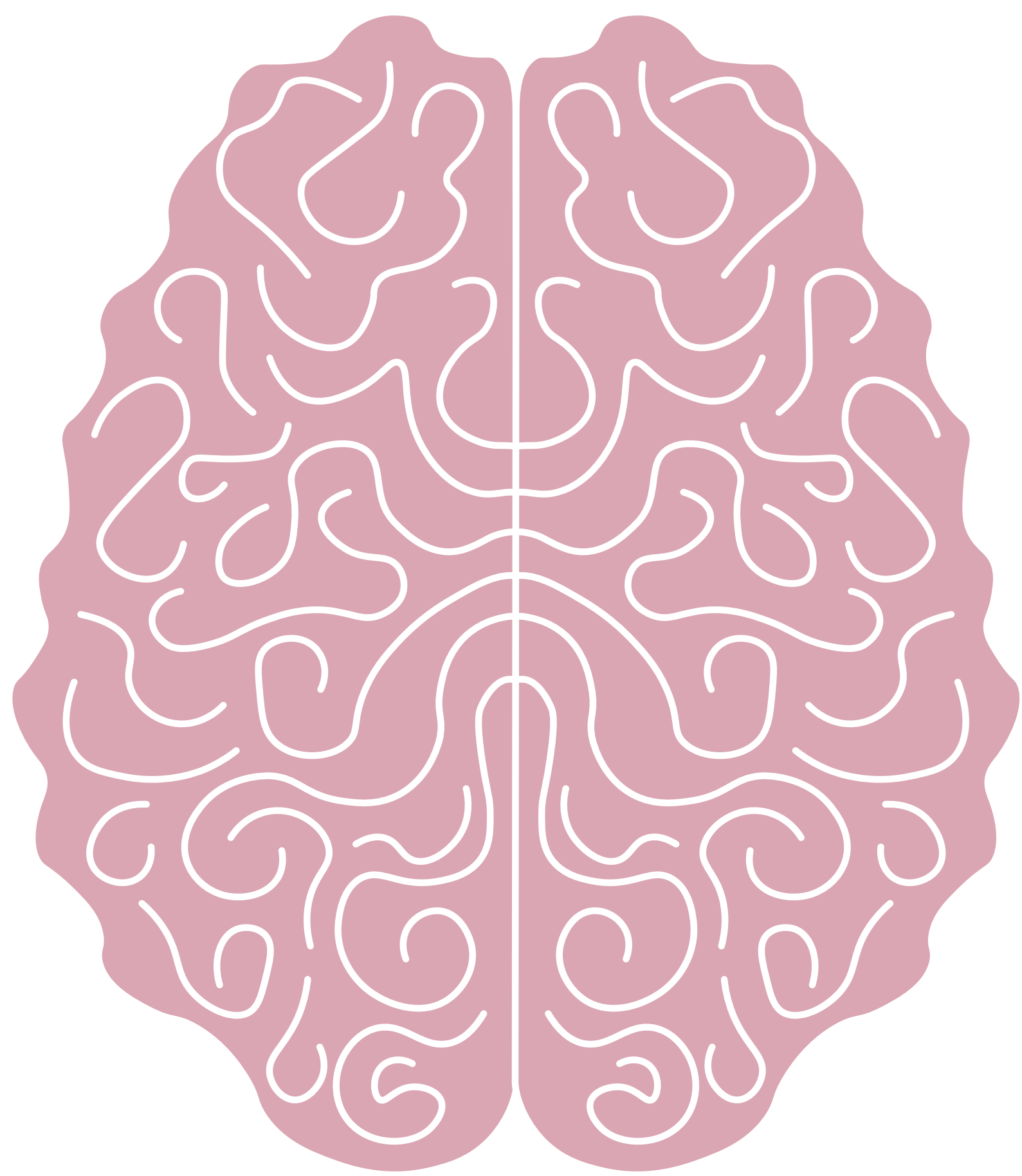


A Small Component



A Small Component





VS

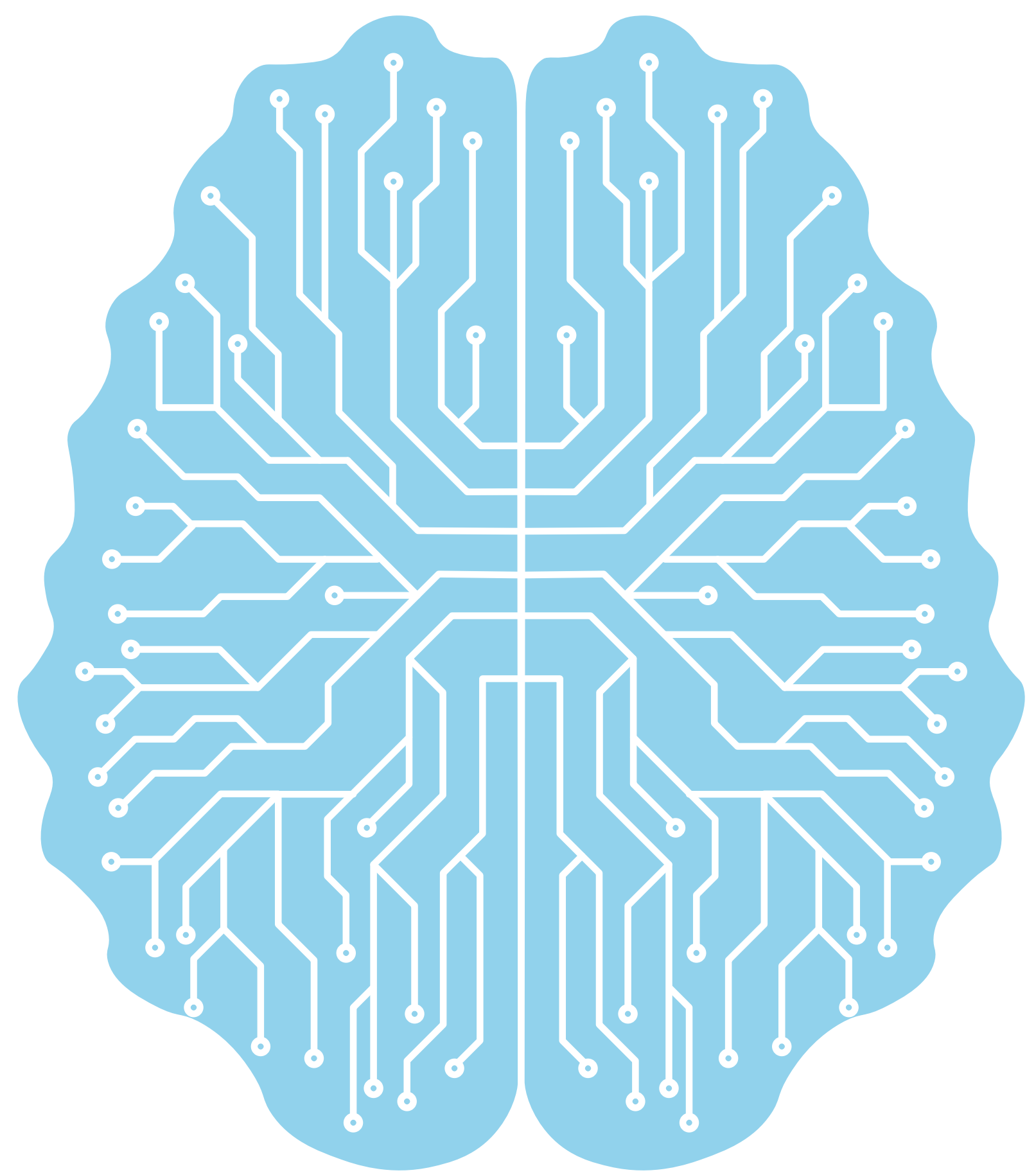


Image Processing



SIFT
[Lowe 1999]

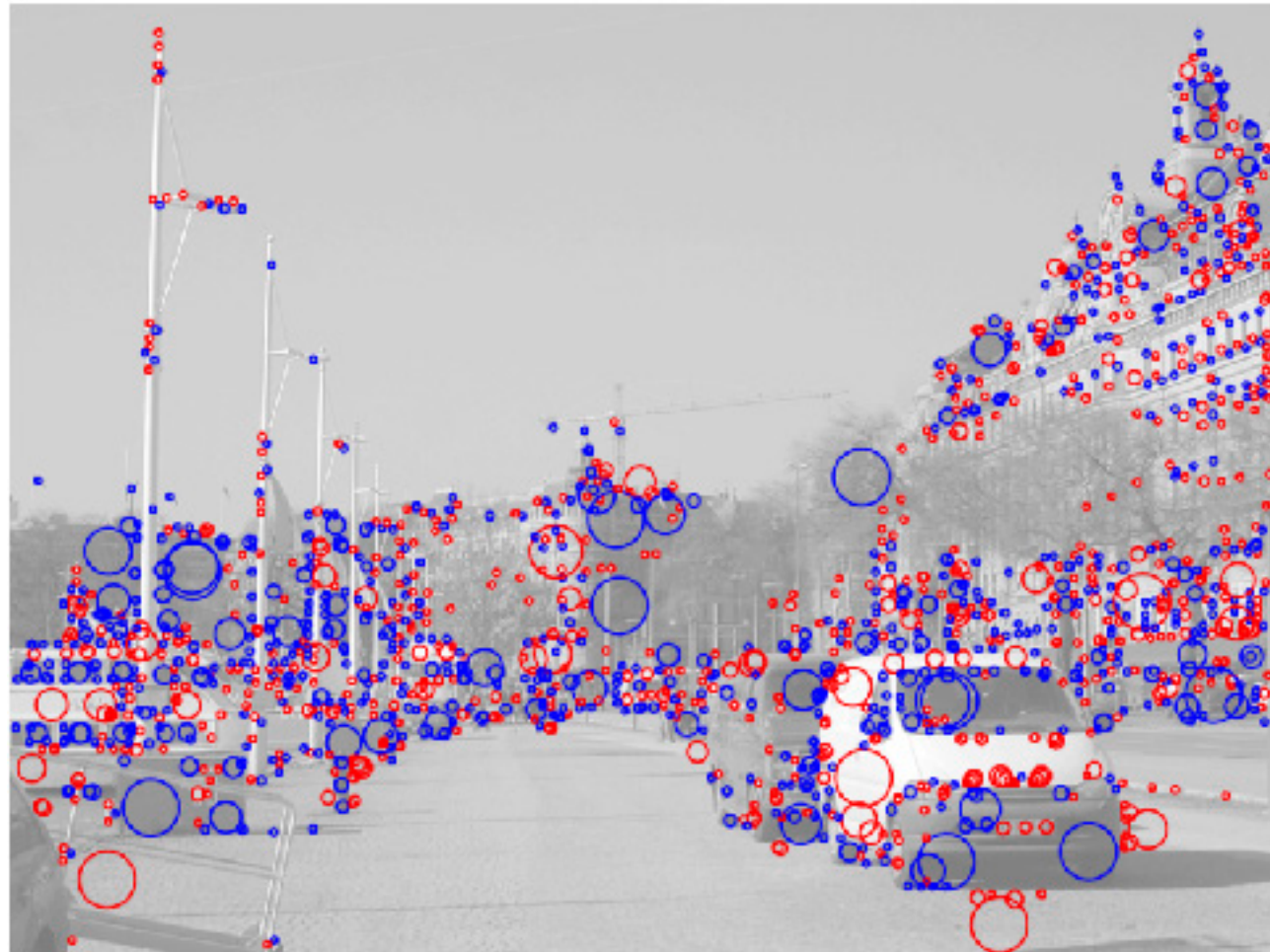
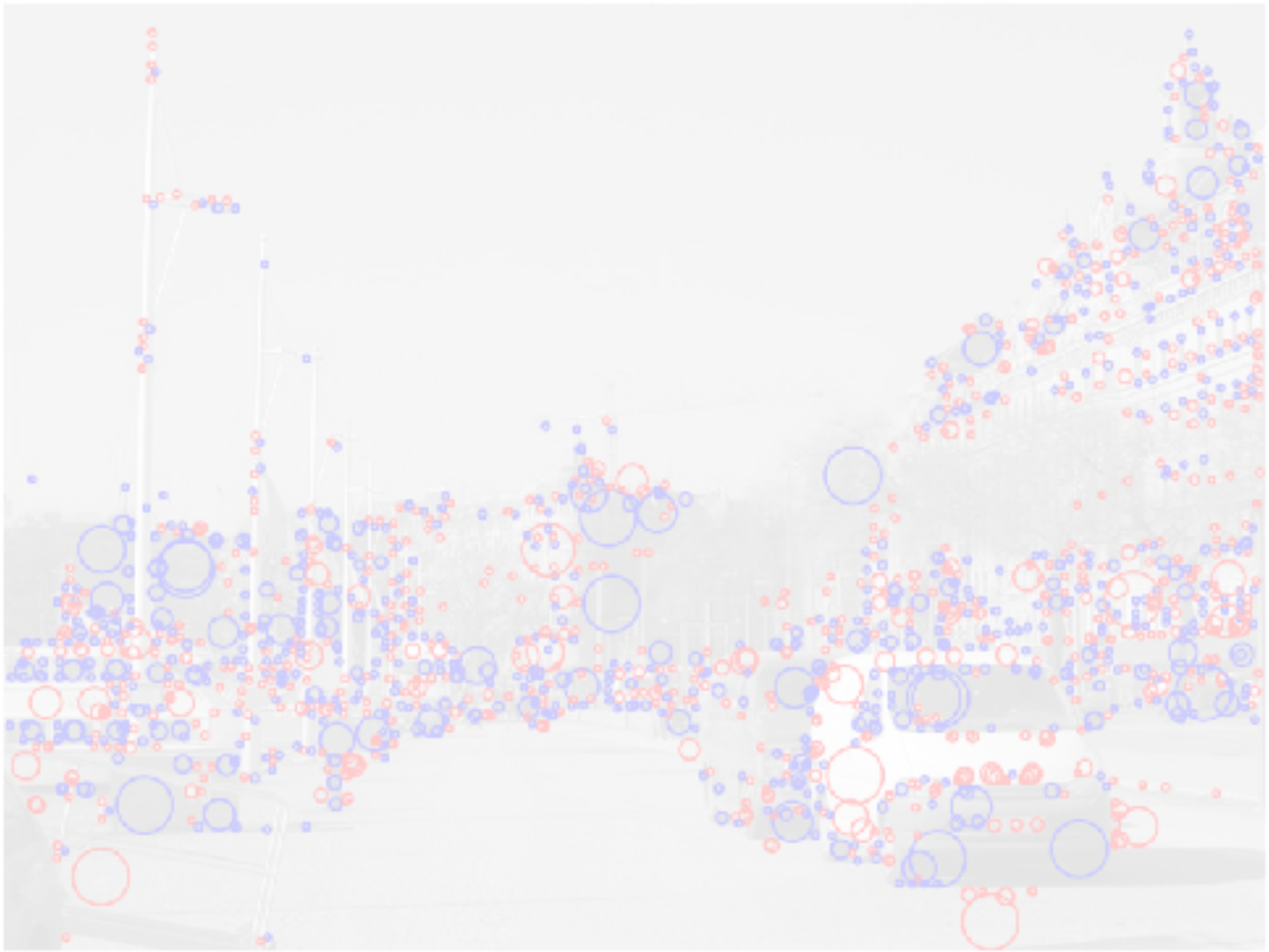
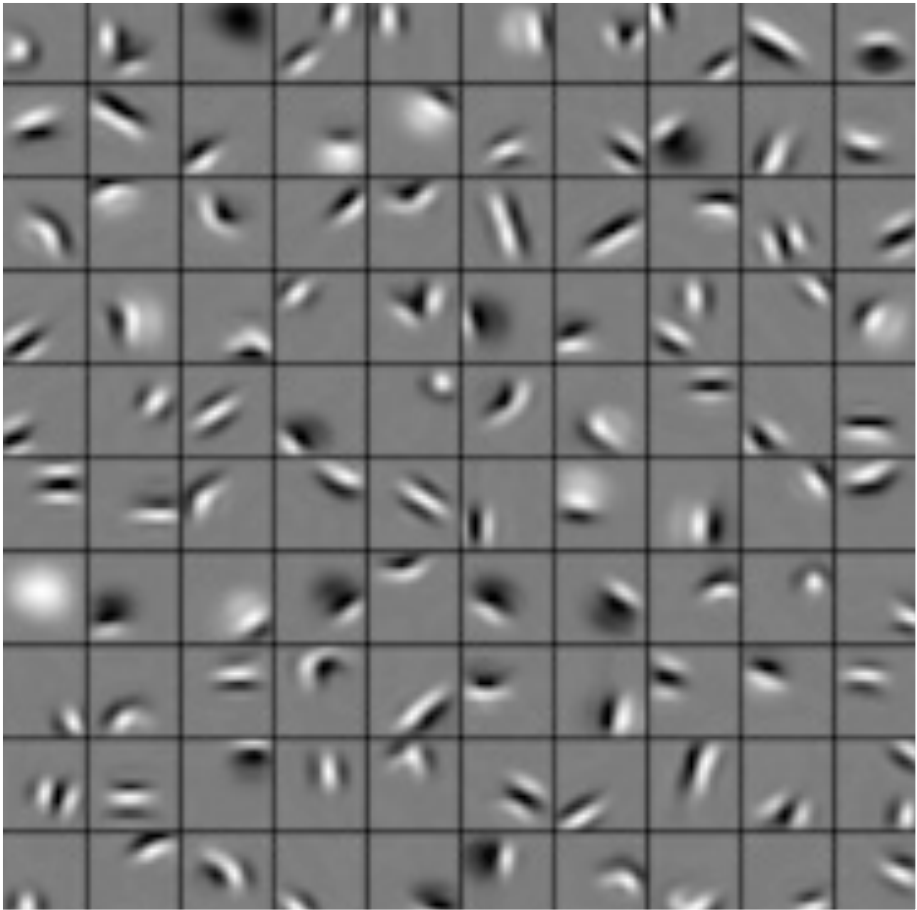
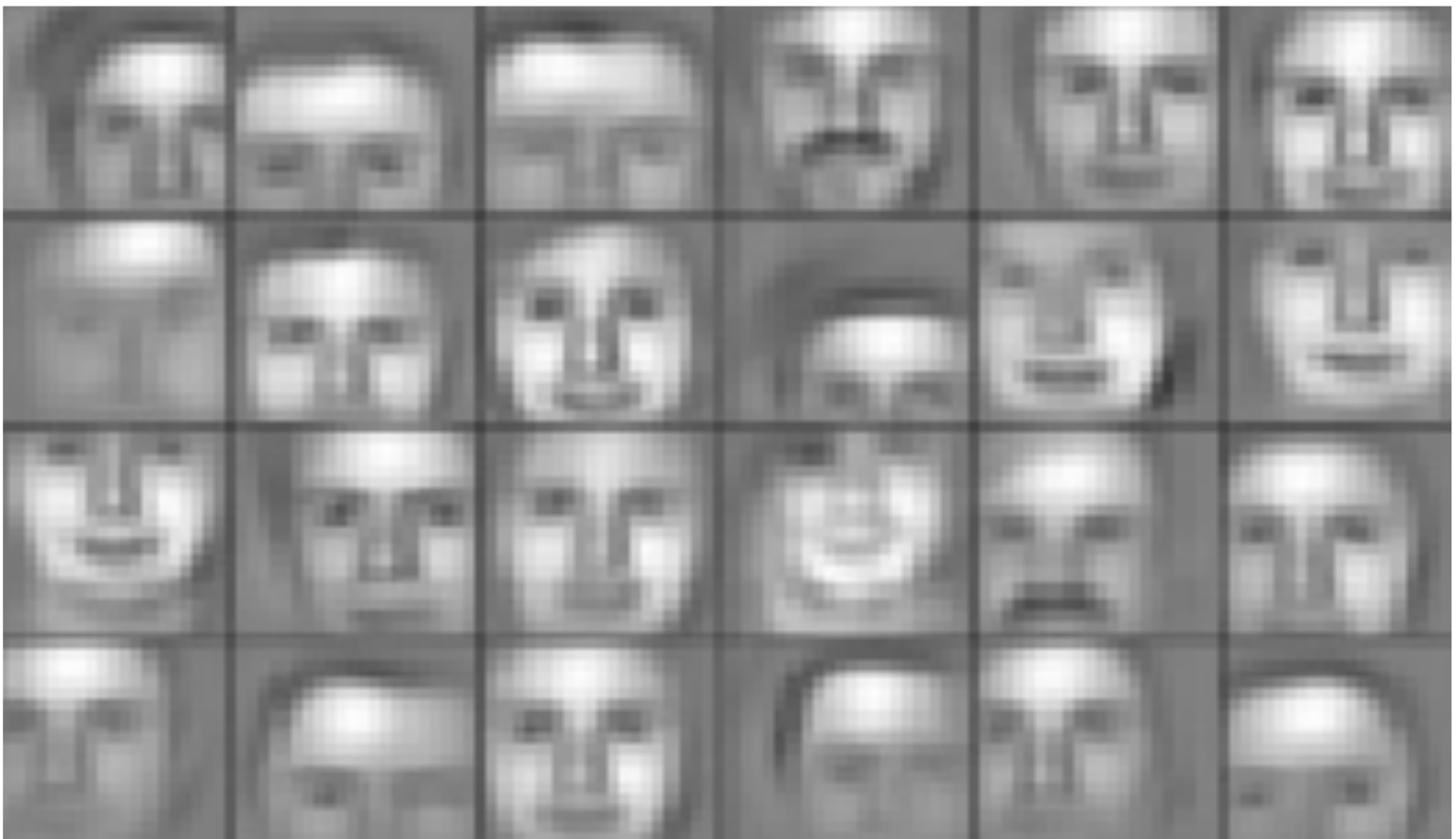


Image Processing

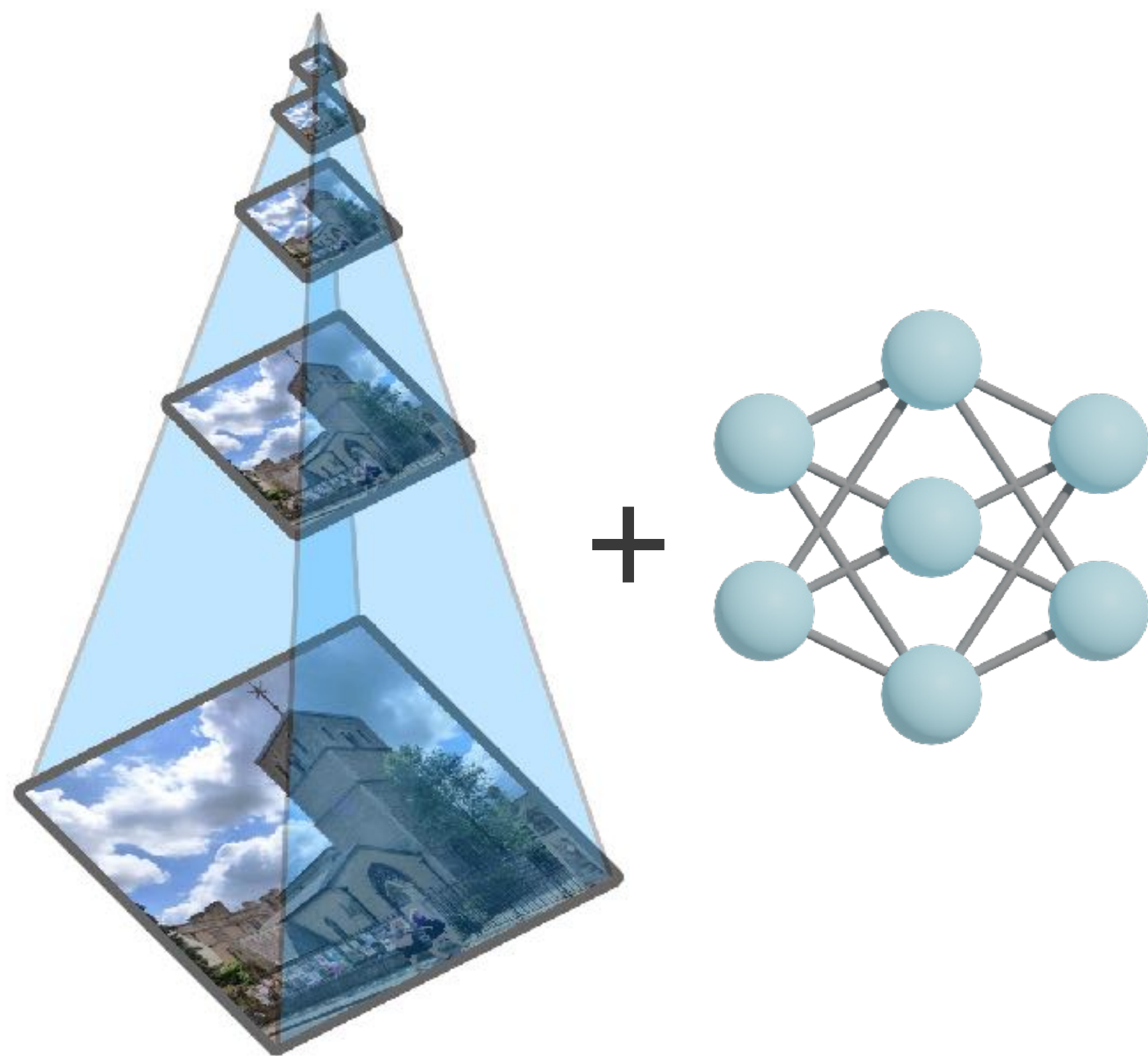


SIFT
[Lowe 1999]

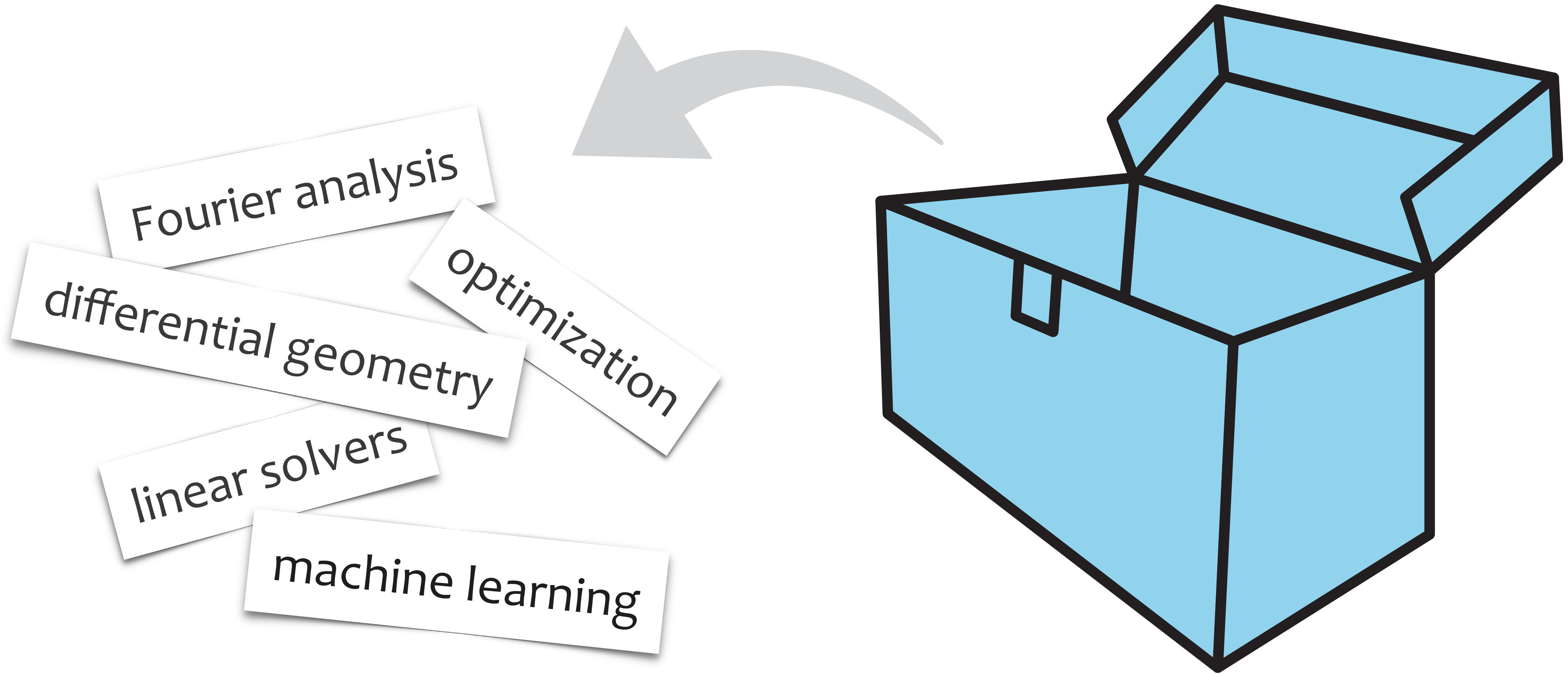
learned
features



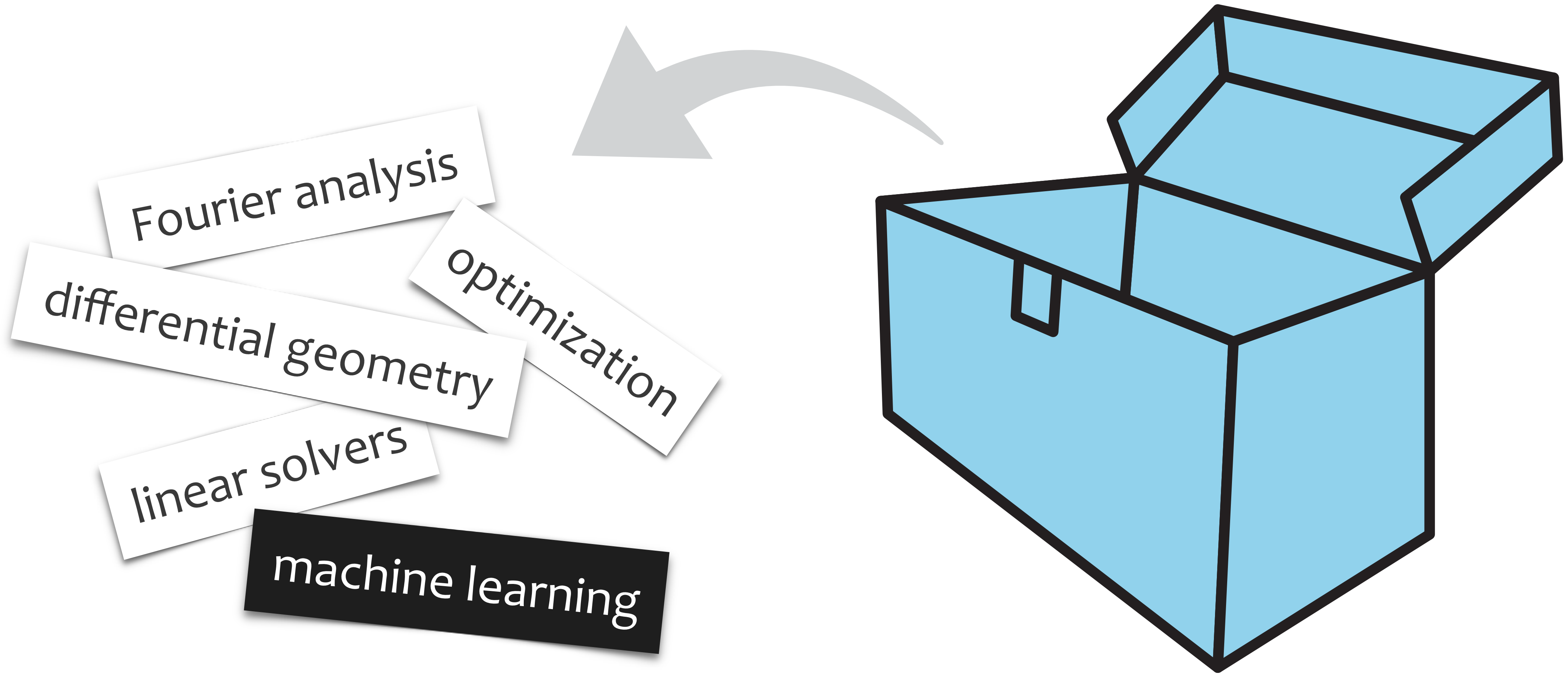
E.g., Optimal Flow via Pyramid



A tool in our toolbox



A tool in our toolbox

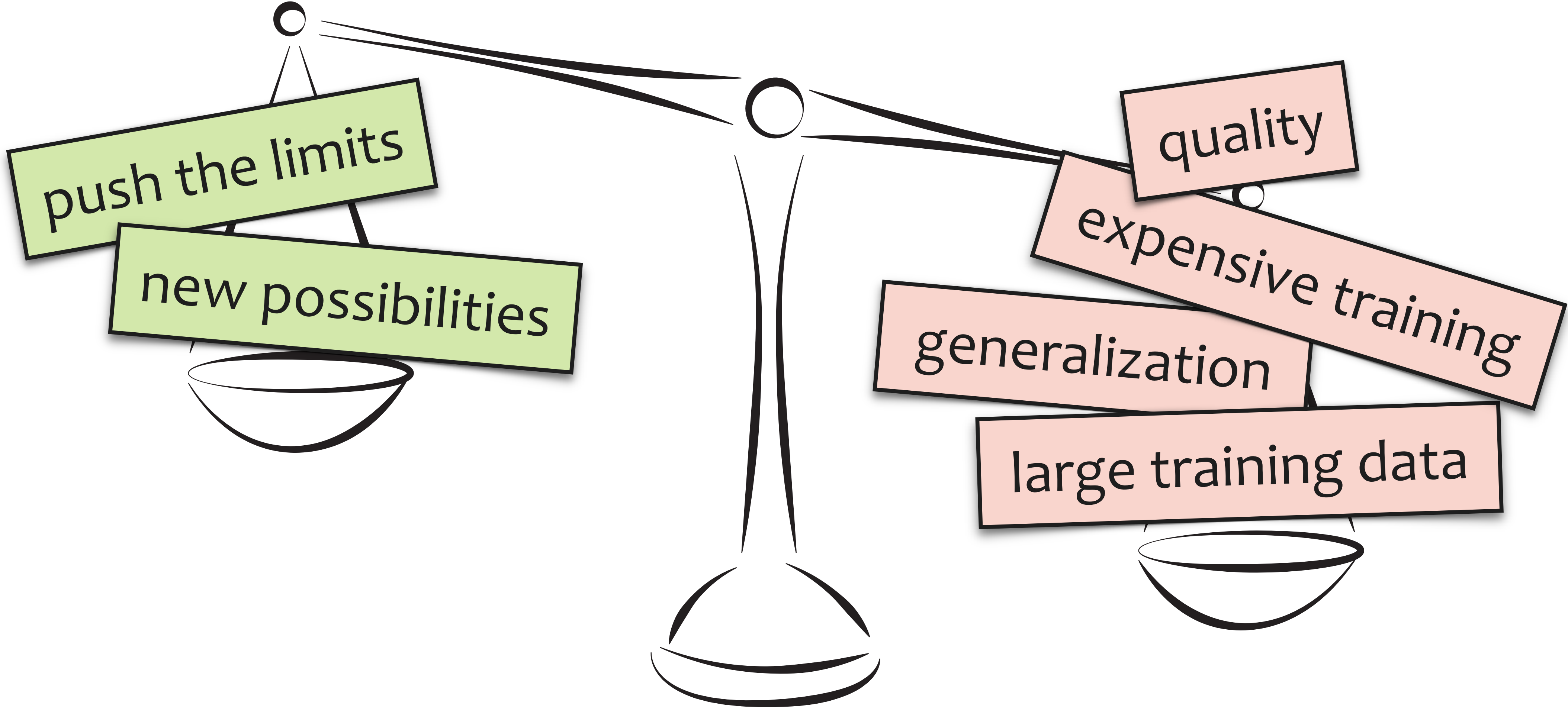


No-free-lunch

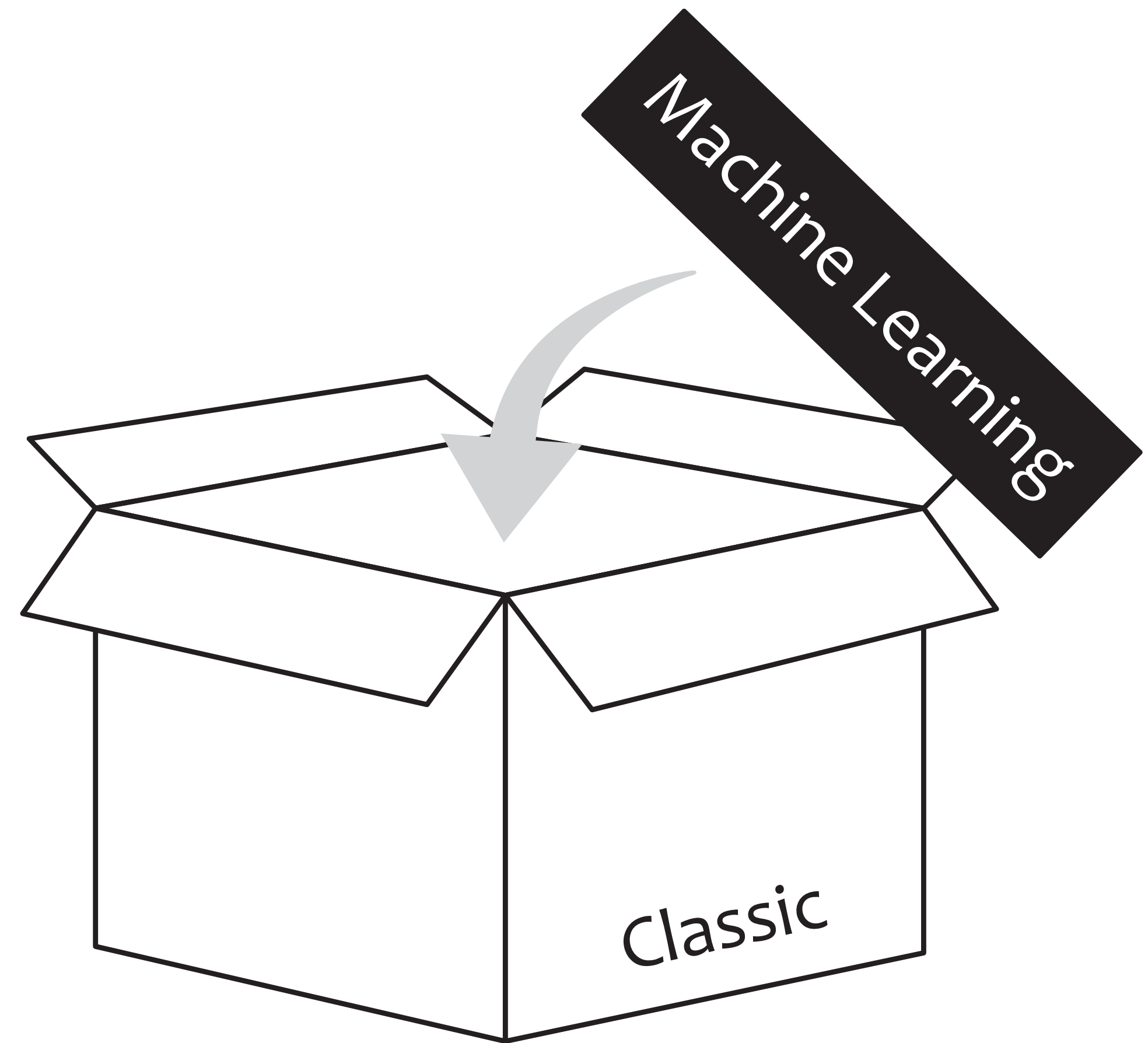
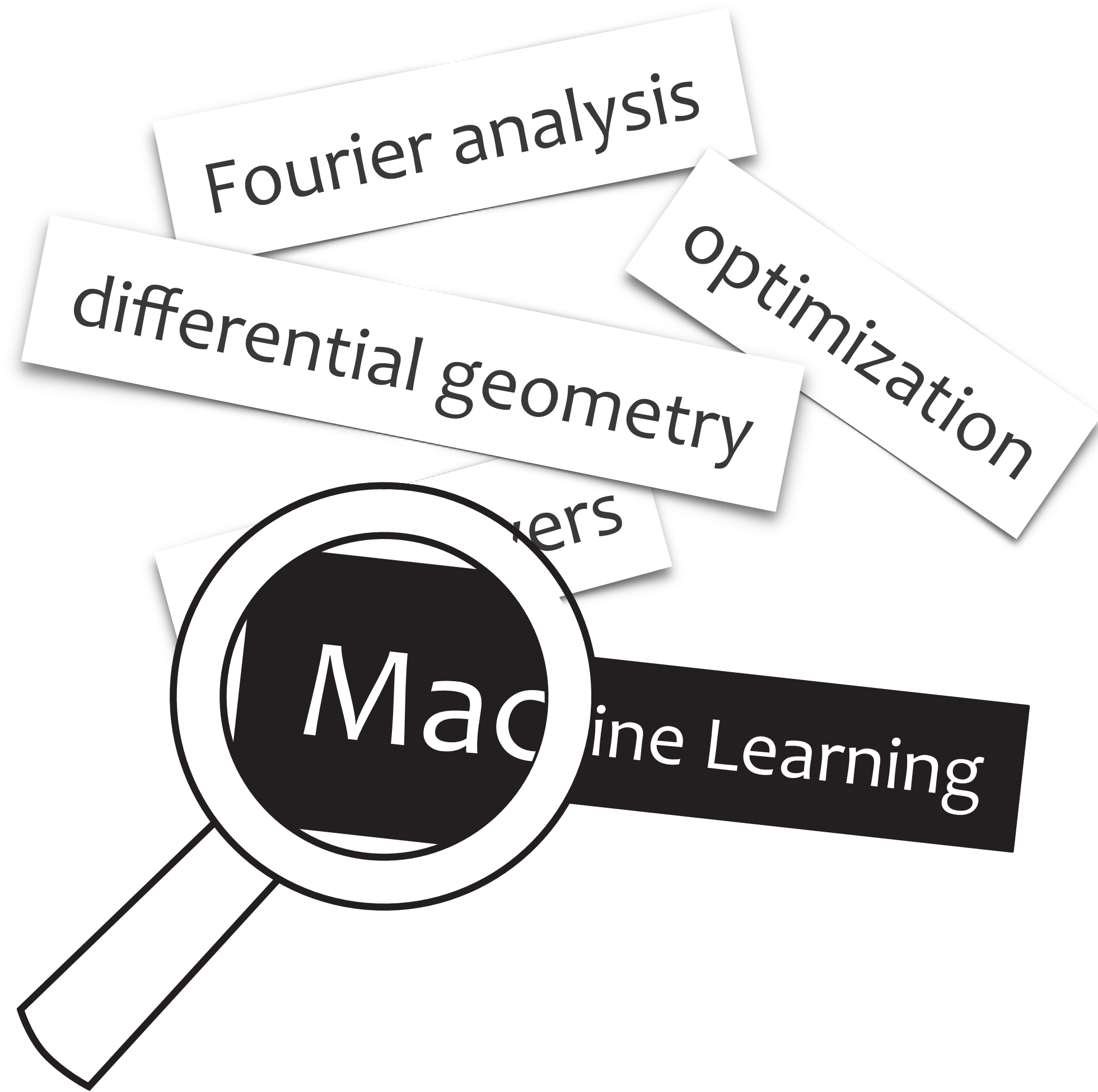
push the limits

new possibilities

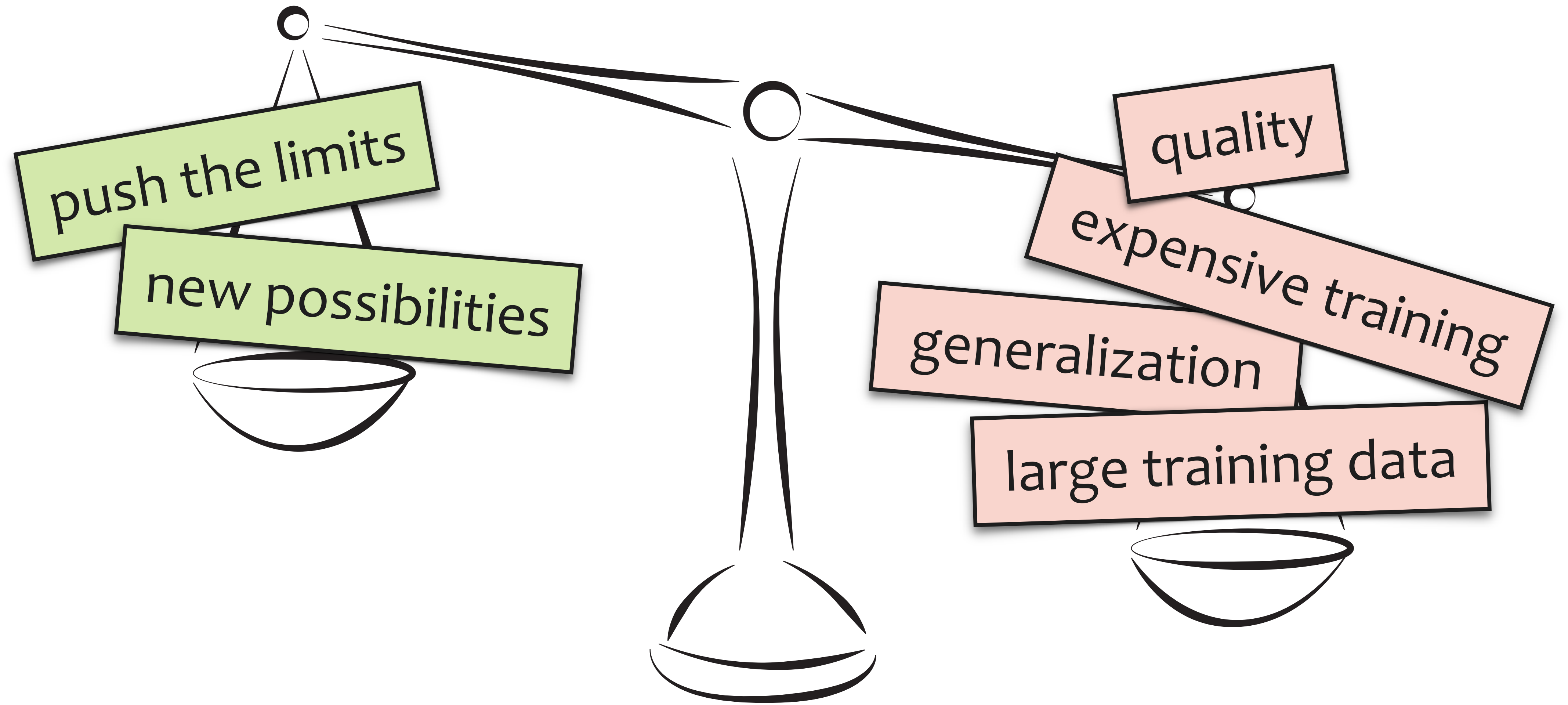
No-free-lunch

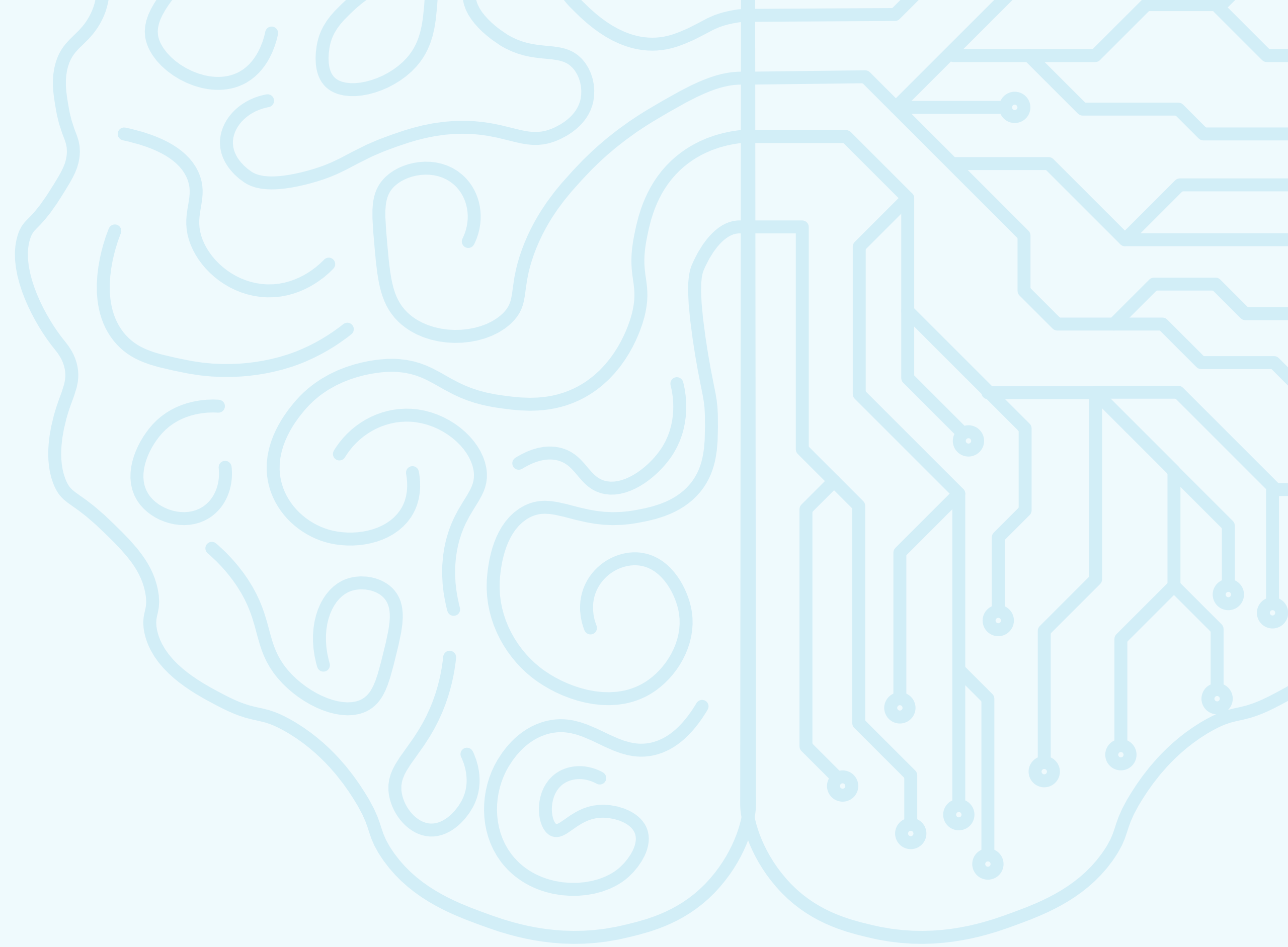


Overview



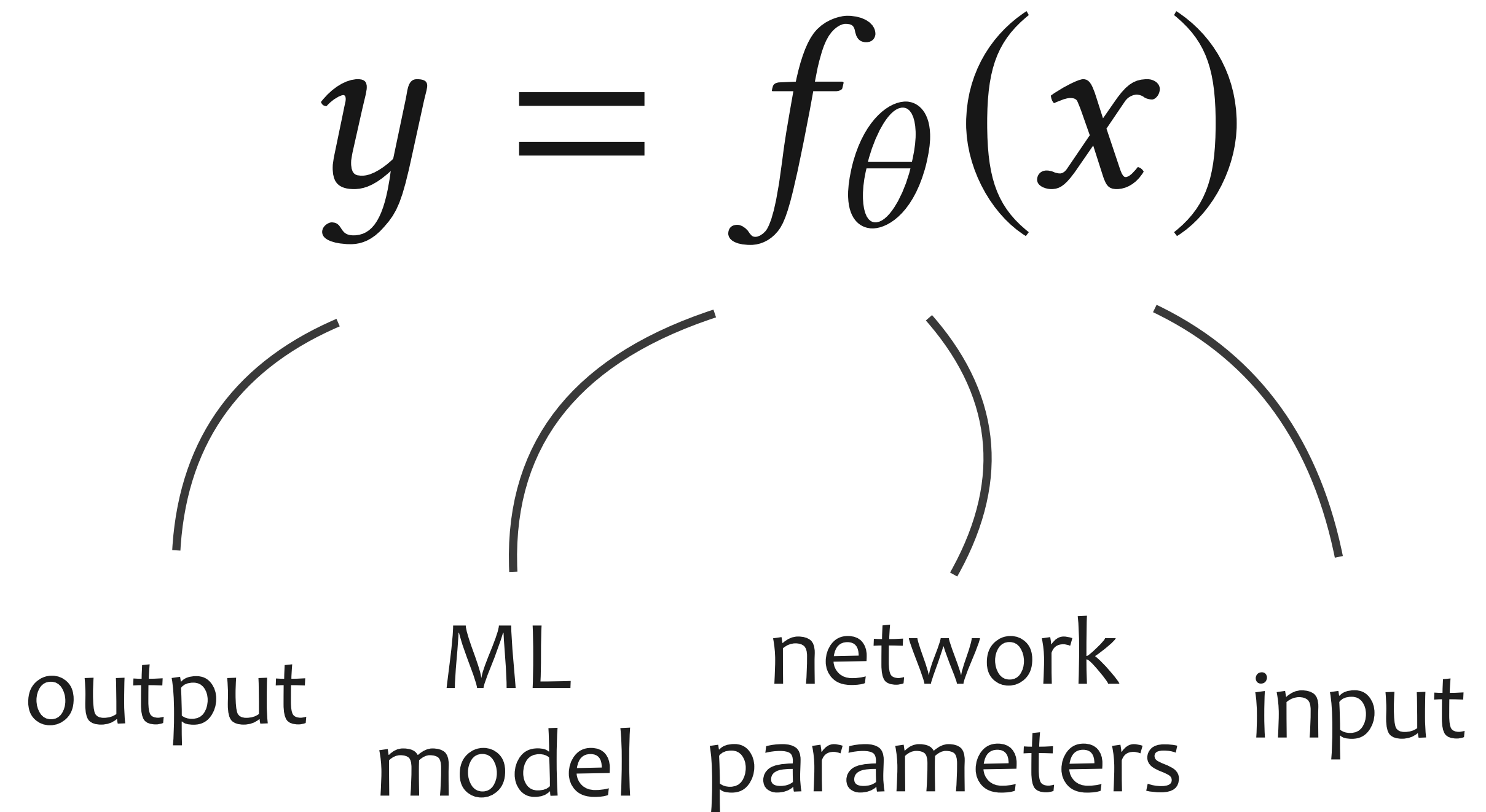
Alleviate Limitations



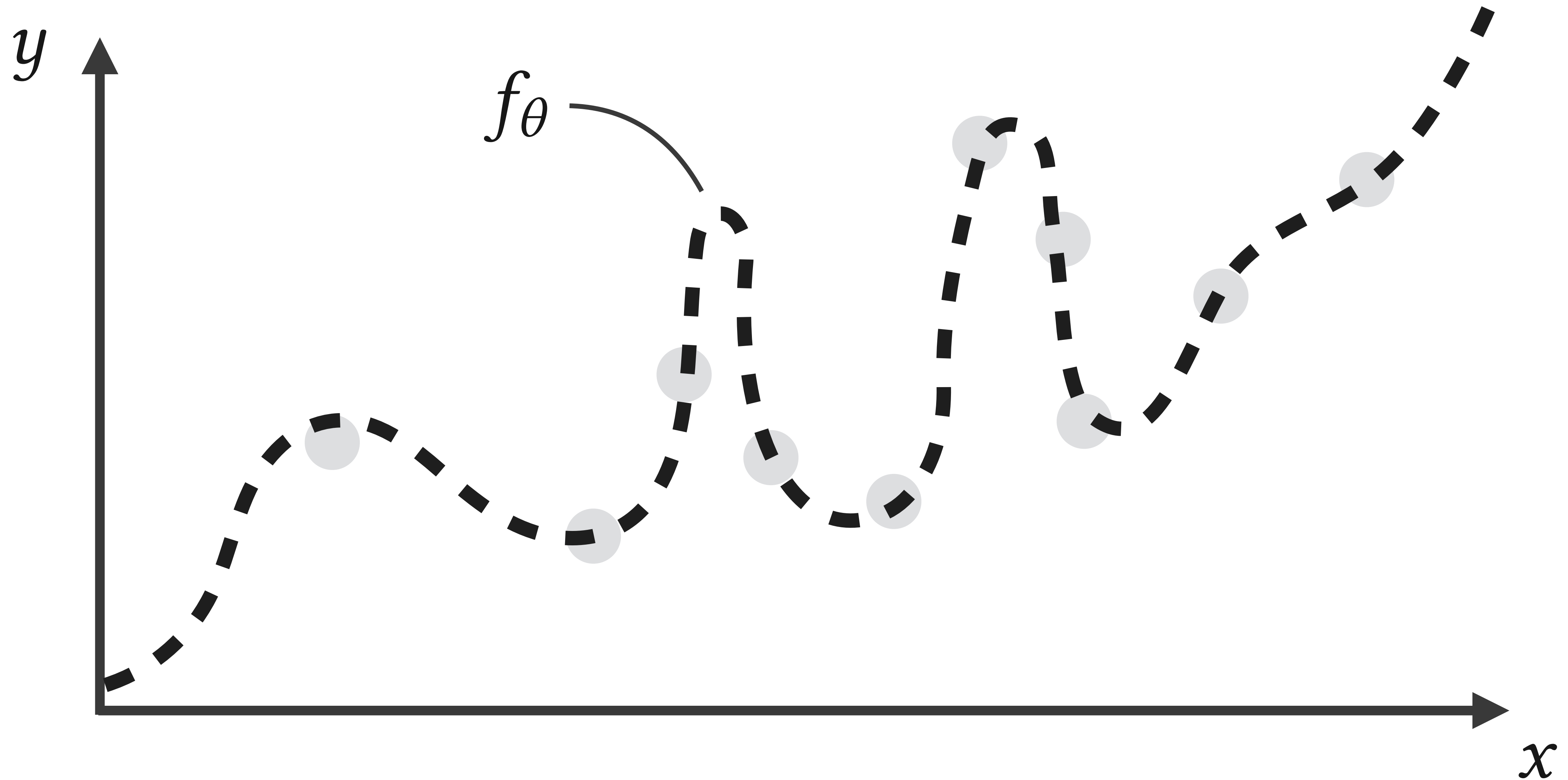


ROLES OF MACHINE LEARNING

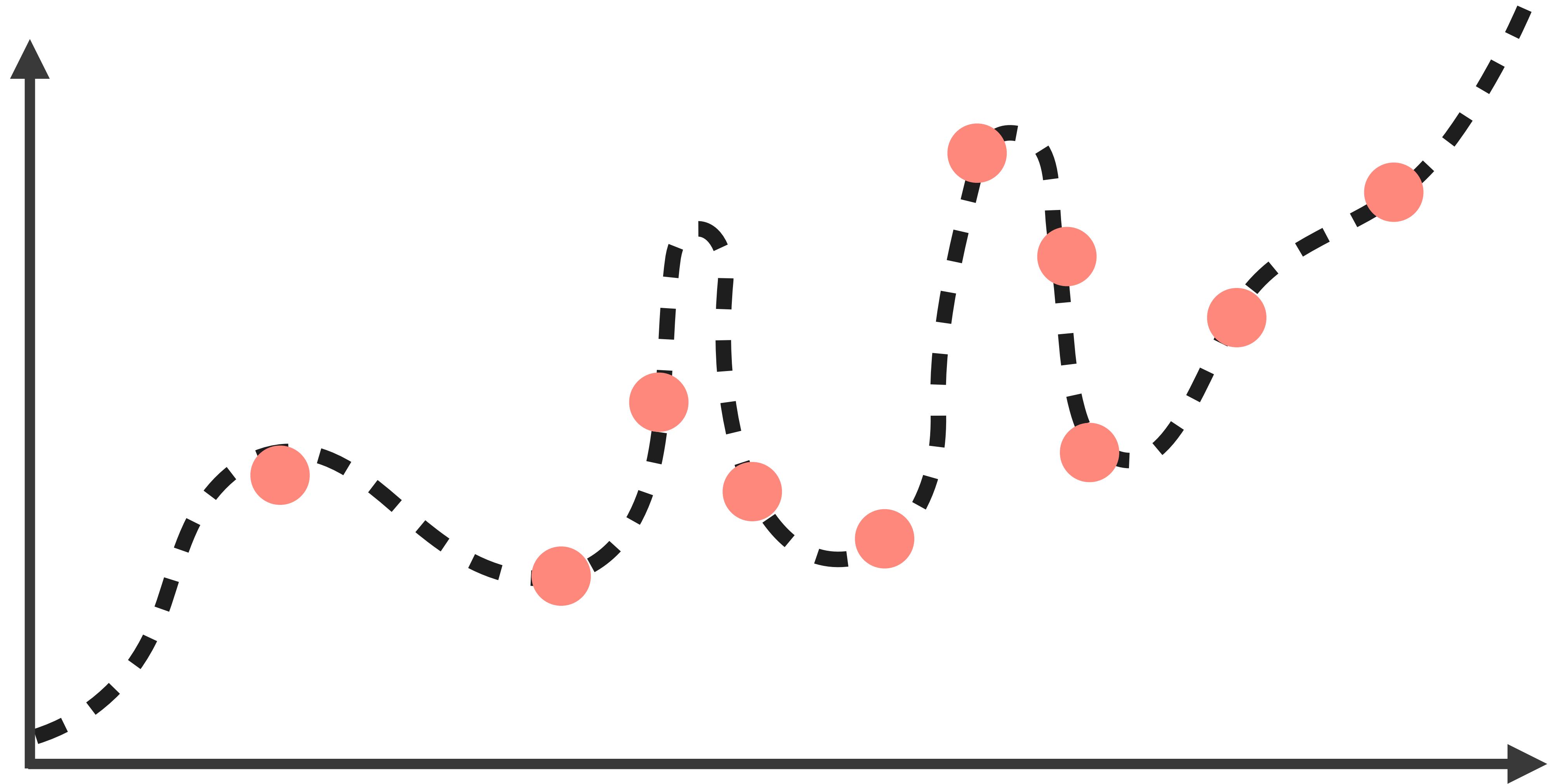
Non-linear Function Approximator



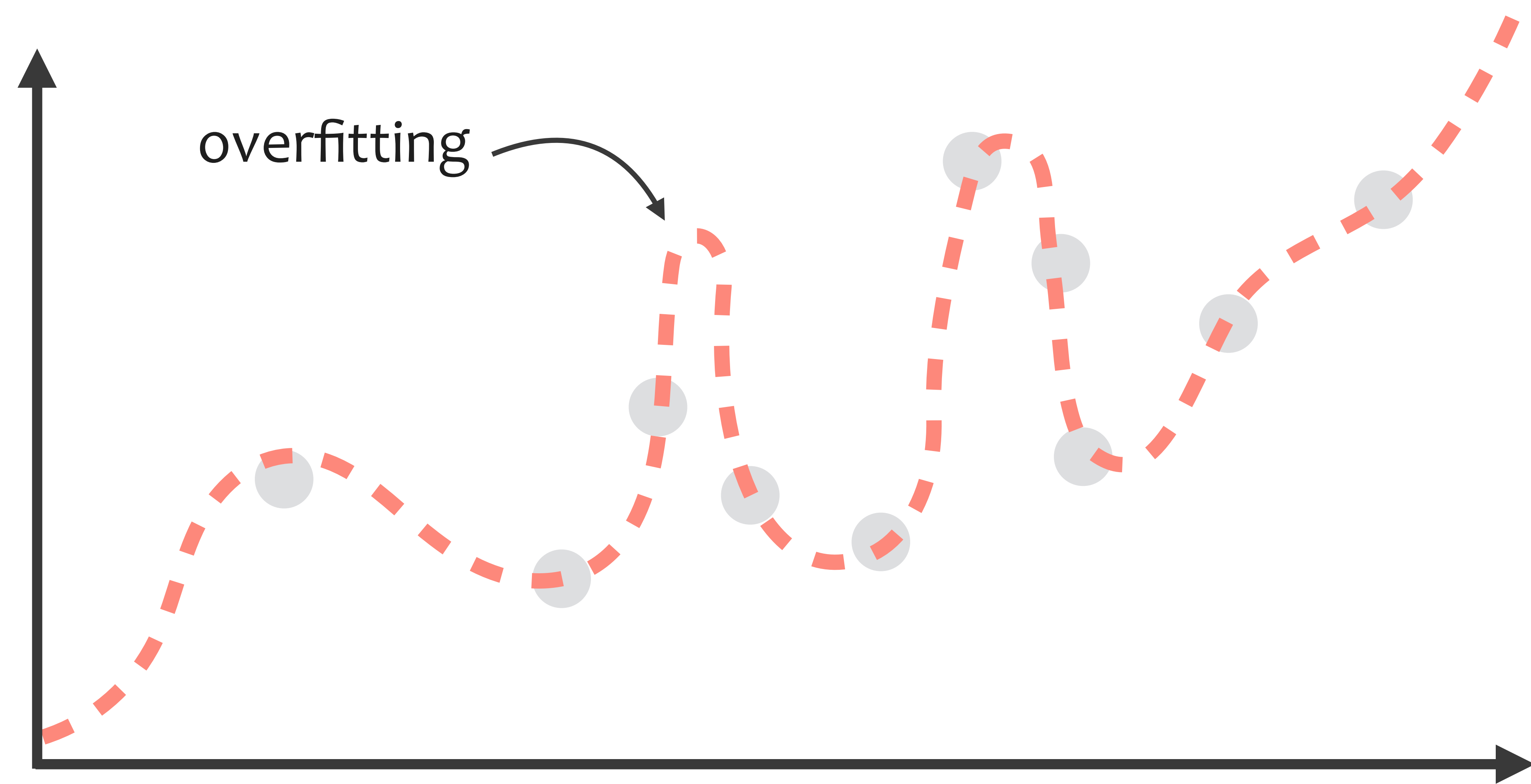
Non-linear Function Approximator



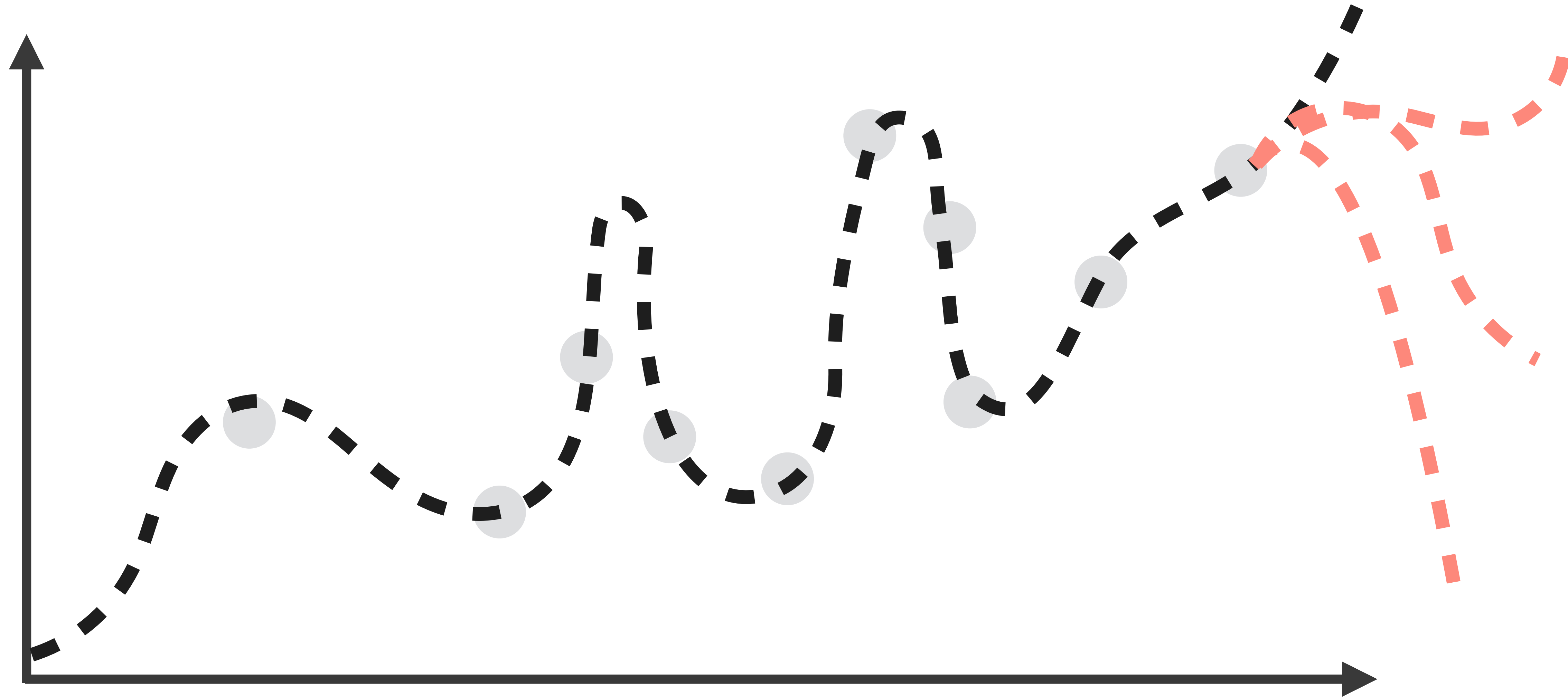
Need a lot of training data



May suffer from overfitting



Difficult to Generalize

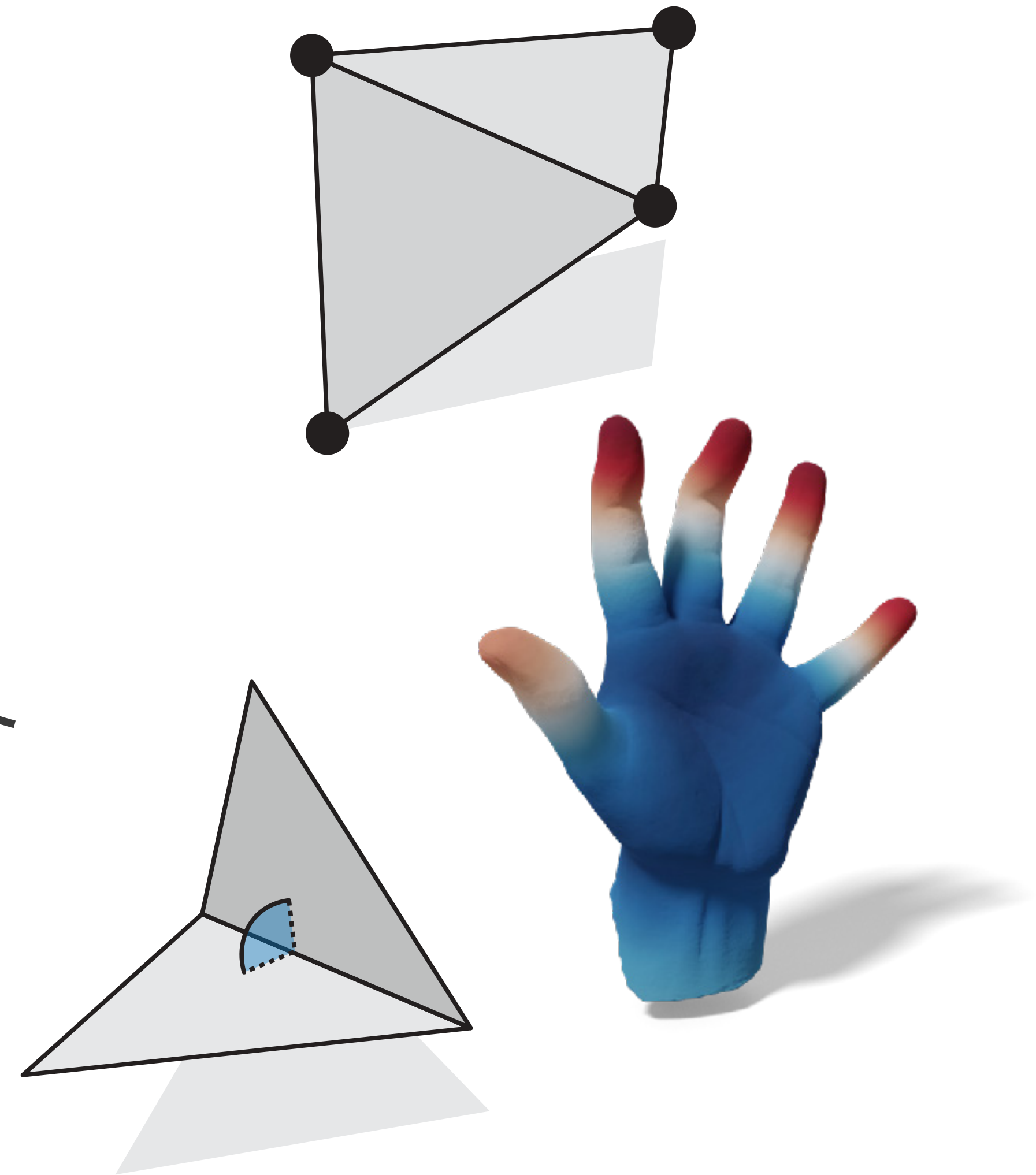


Machine learning as a feature extractor

Feature extractor



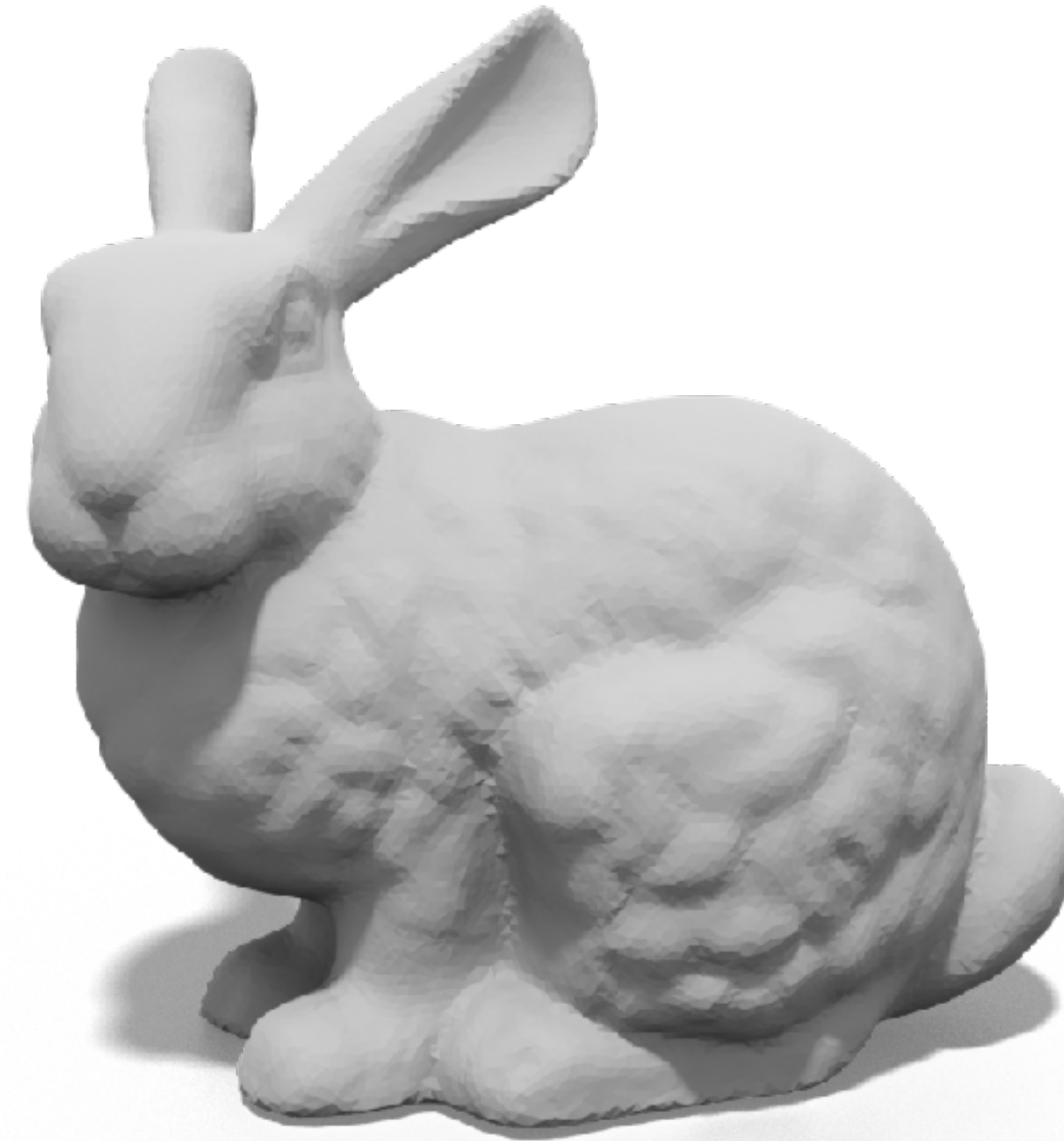
$$y = f_{\theta}(x)$$



Shape Classification



human

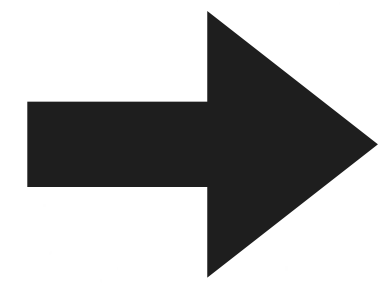


not human

Global Shape Descriptors



entire shape

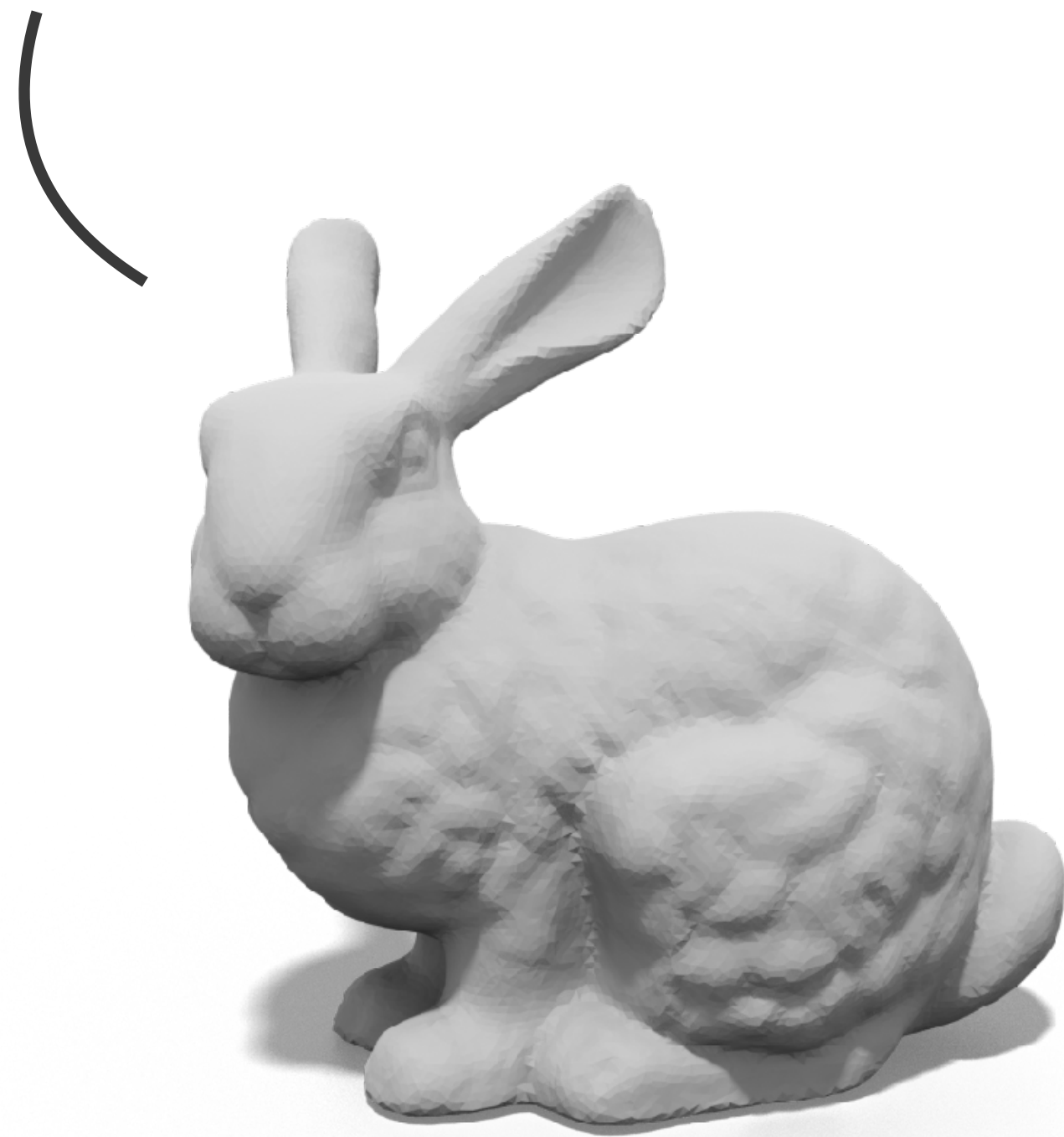
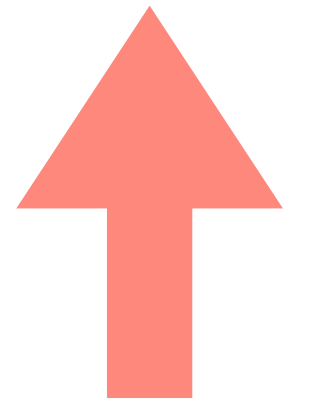


$$[a_1, a_2, \dots, a_n]$$

a fixed dimensional vector

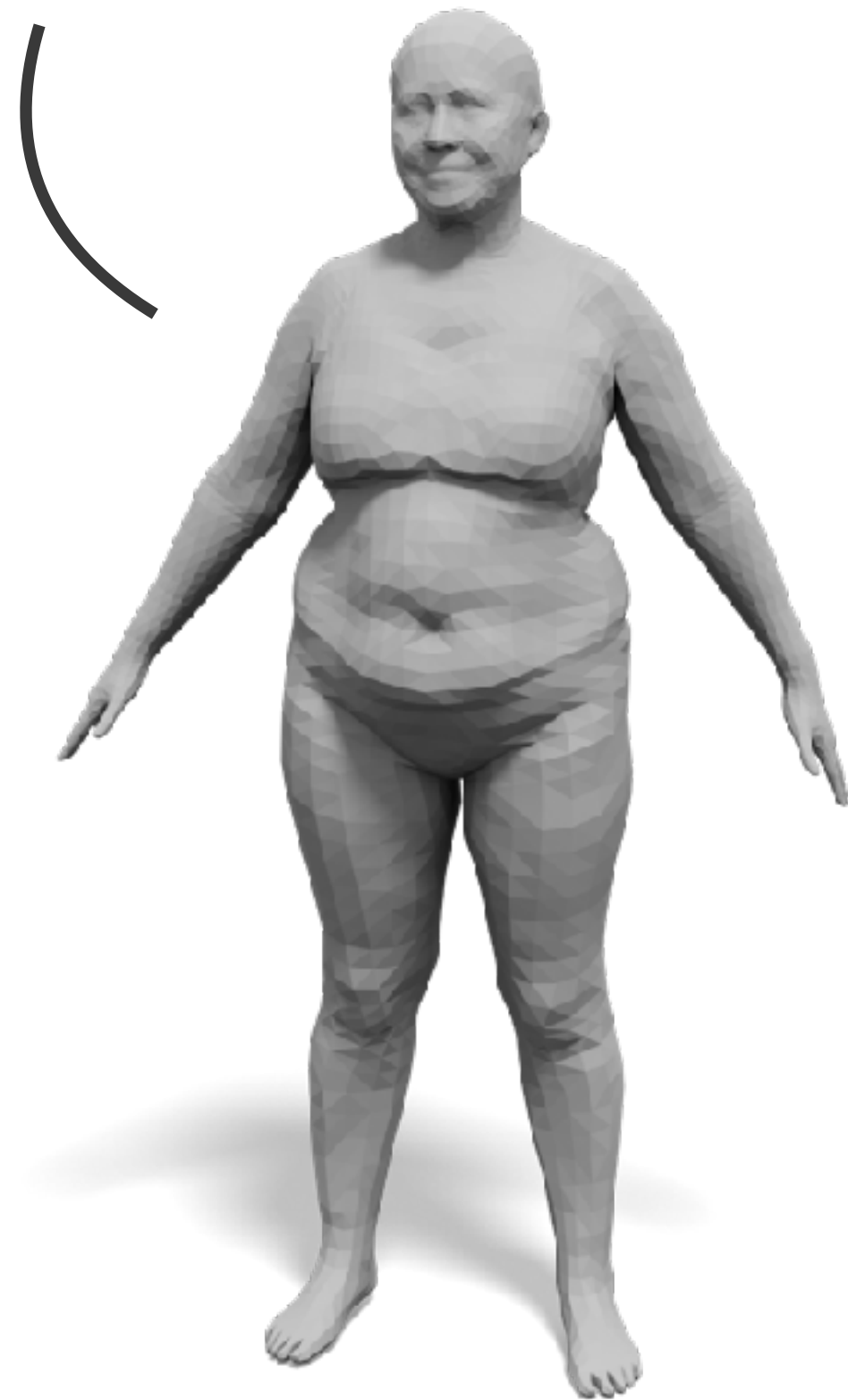
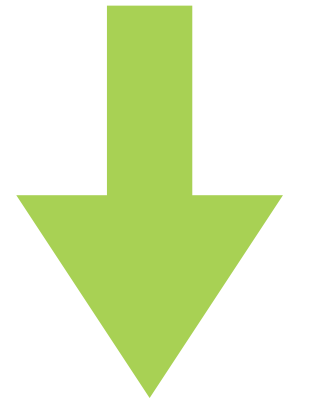
Measure Shape Difference

$$\| [a_1, a_2, \dots, a_n] - [b_1, b_2, \dots, b_n] \| =$$

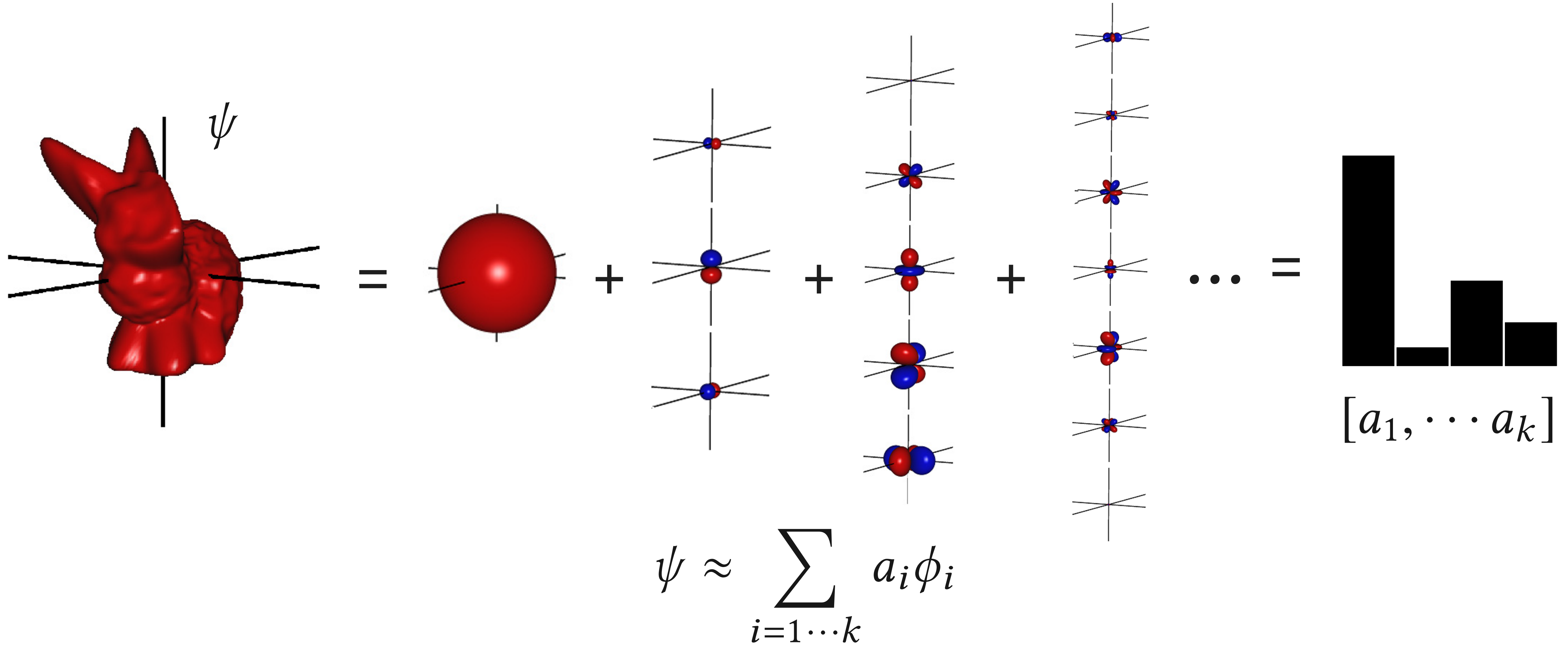


Measure Shape Difference

$$\| [c_1, c_2, \dots, c_n] - [b_1, b_2, \dots, b_n] \| =$$



E.g., Spherical Harmonics



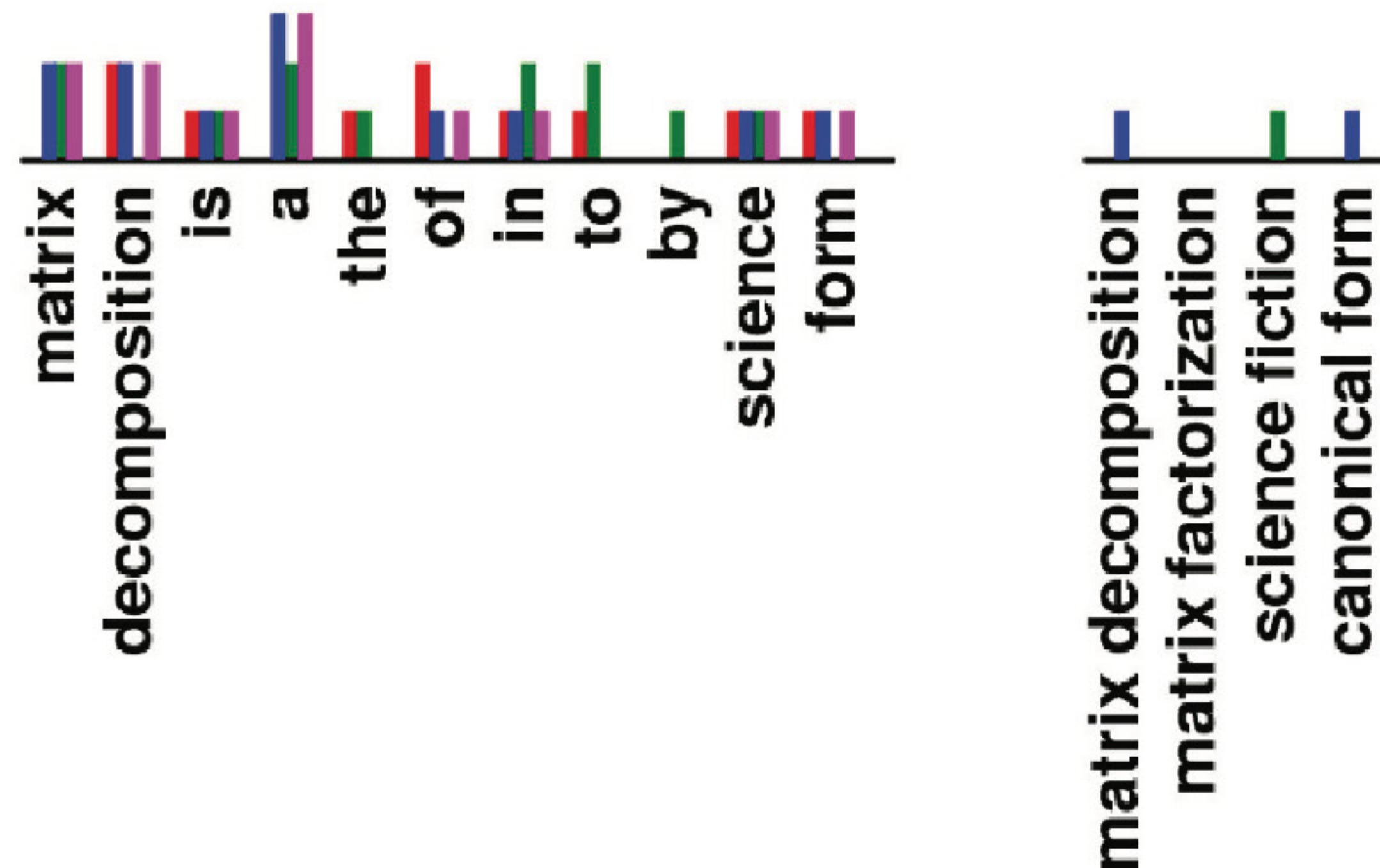
E.g., Bags of Words

in math science, matrix decomposition is a factorization of a matrix into some canonical form. each type of decomposition is used in a particular problem.

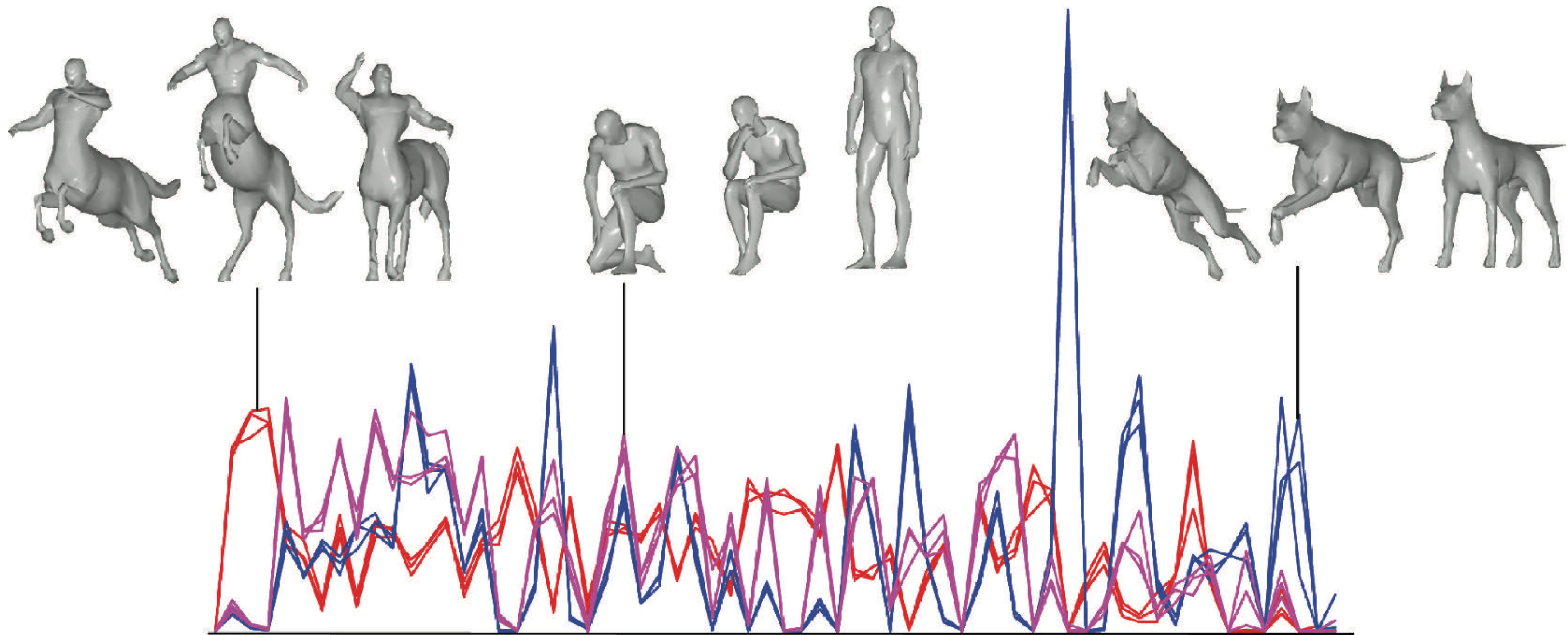
in particular matrix used type a some science decomposition form a factorization of is canonical matrix math decomposition is in a each problem into of

in biological science, decomposition is the process of organisms to break down into simpler form of matter. usually, decomposition occurs after death.

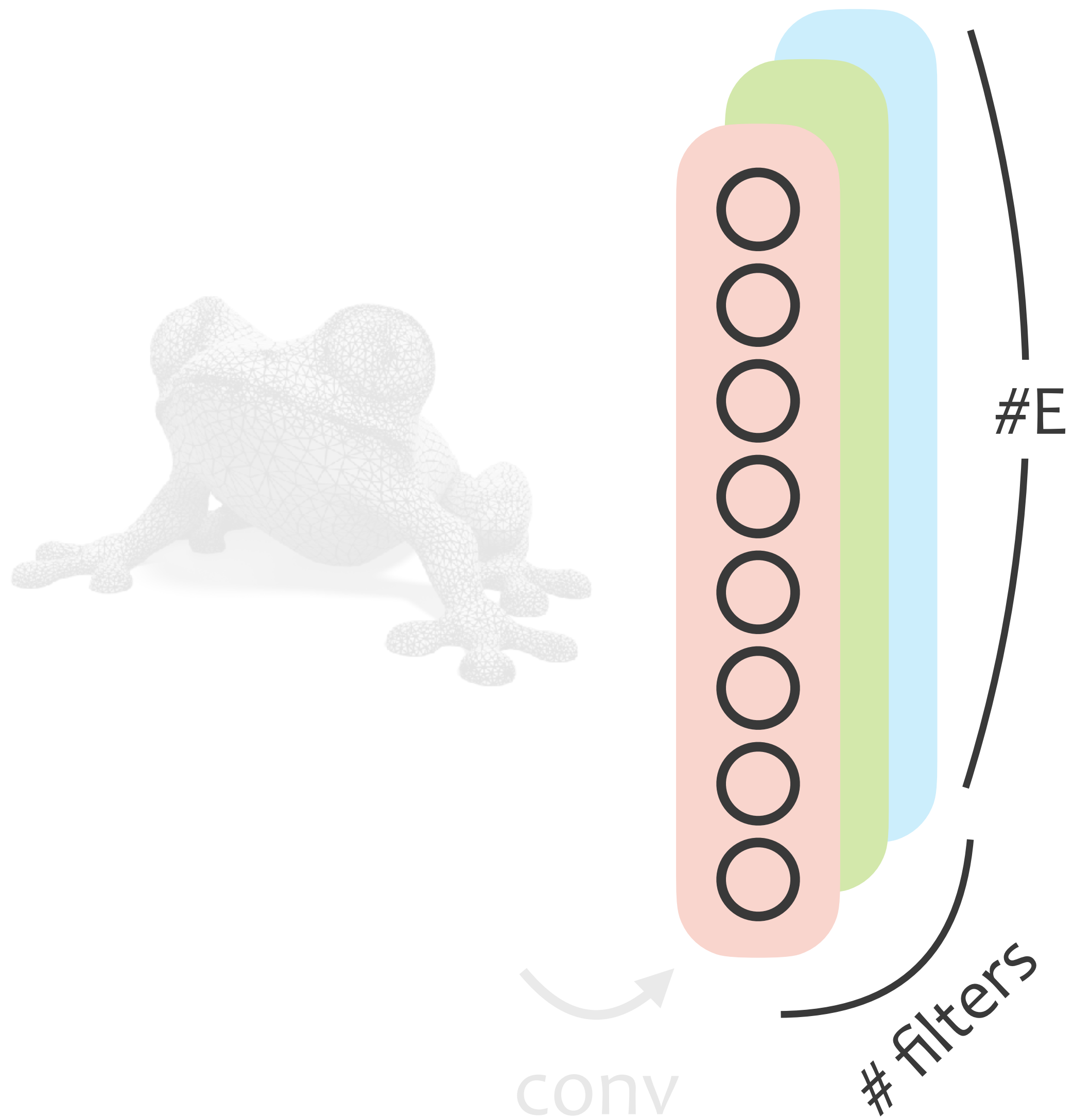
matrix is a science fiction movie released in 1999. matrix refers to a simulated reality created by machines in order to subdue the human population.



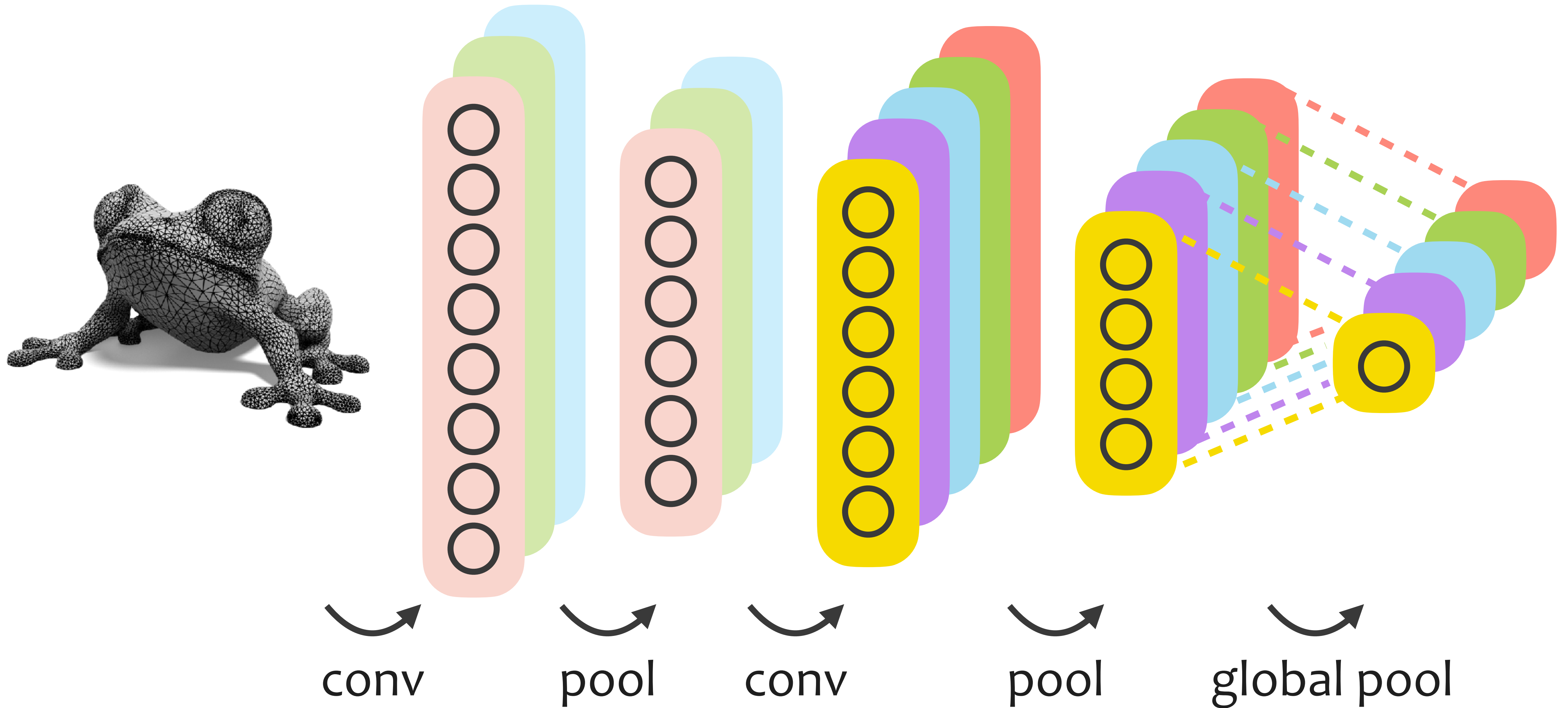
E.g., Bags of Features



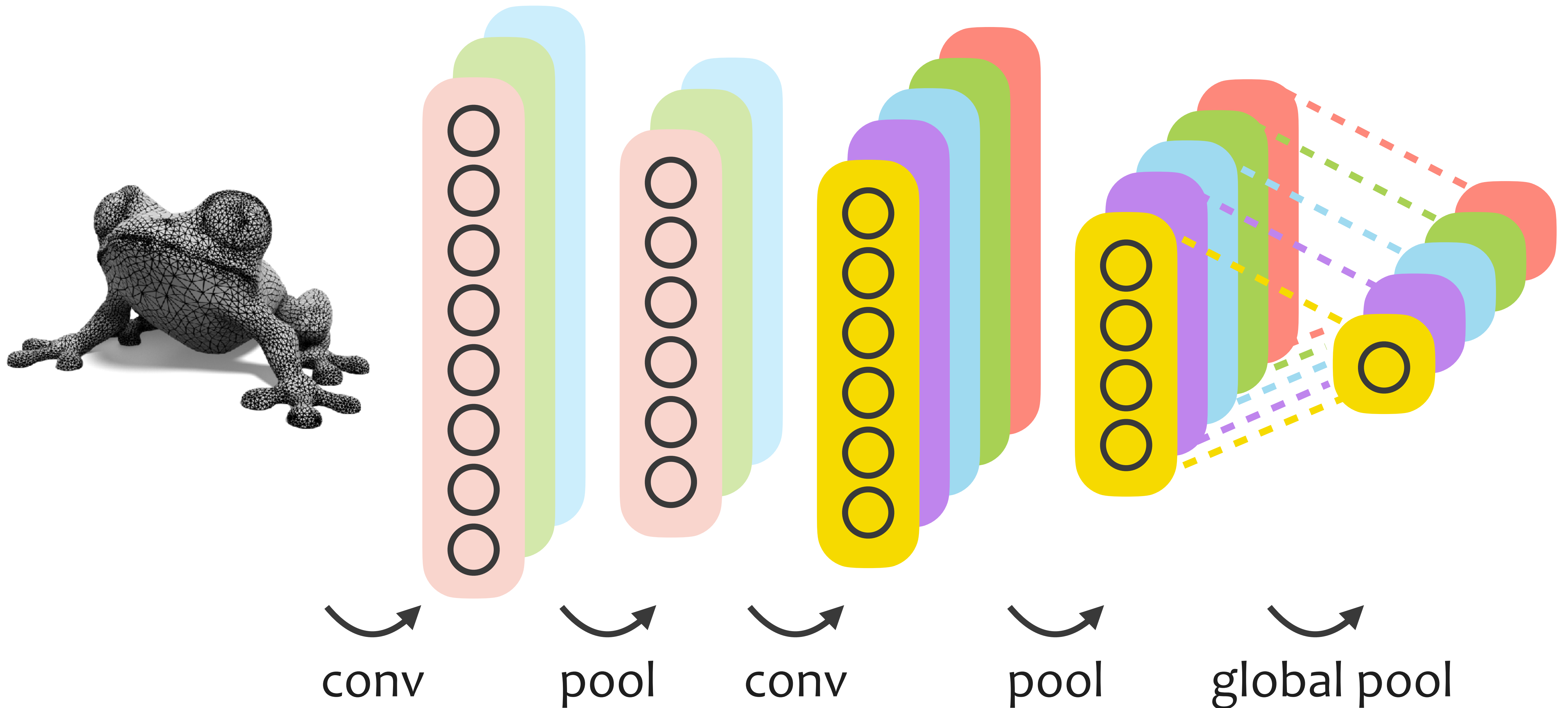
Learned Global Descriptors



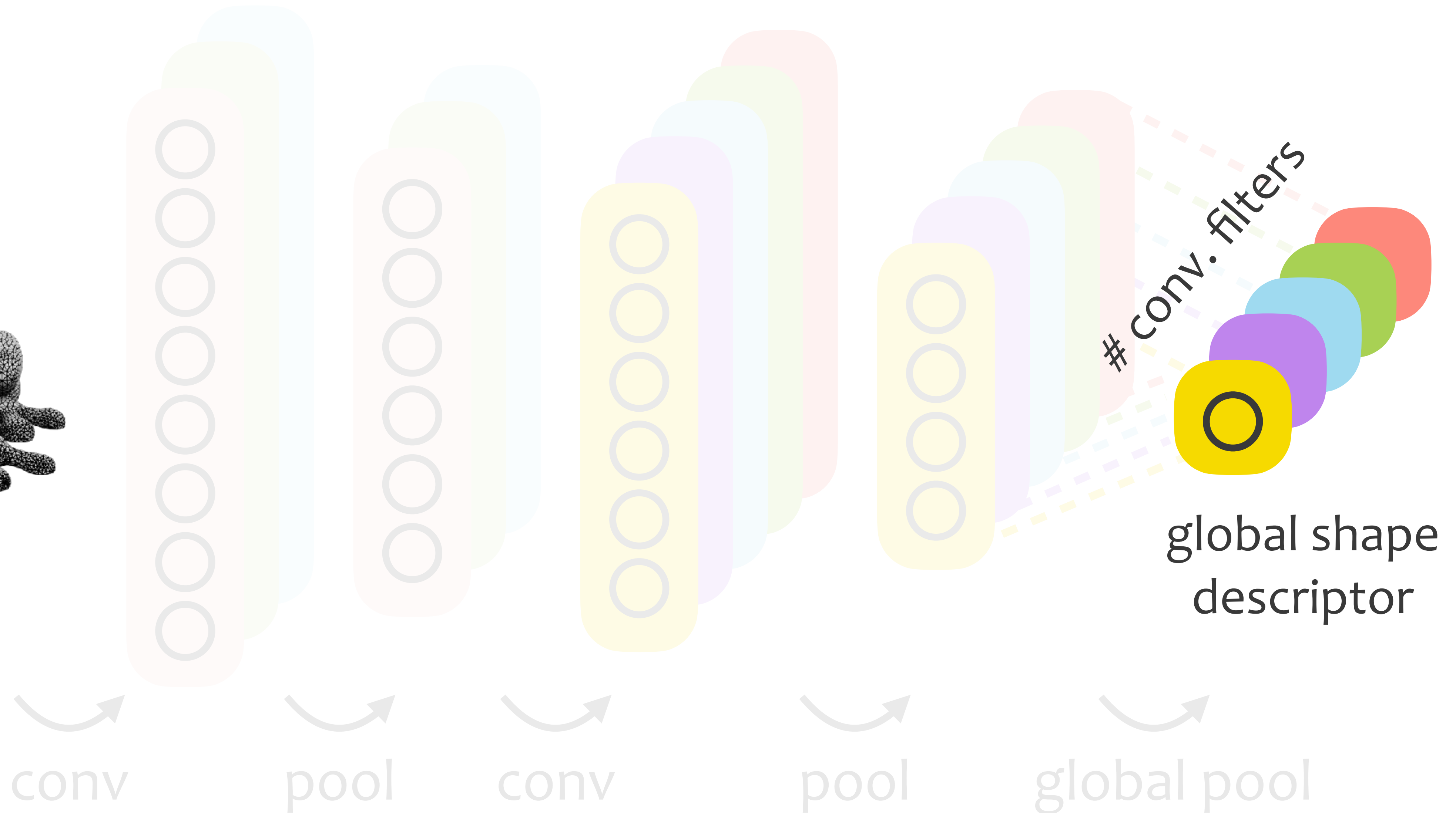
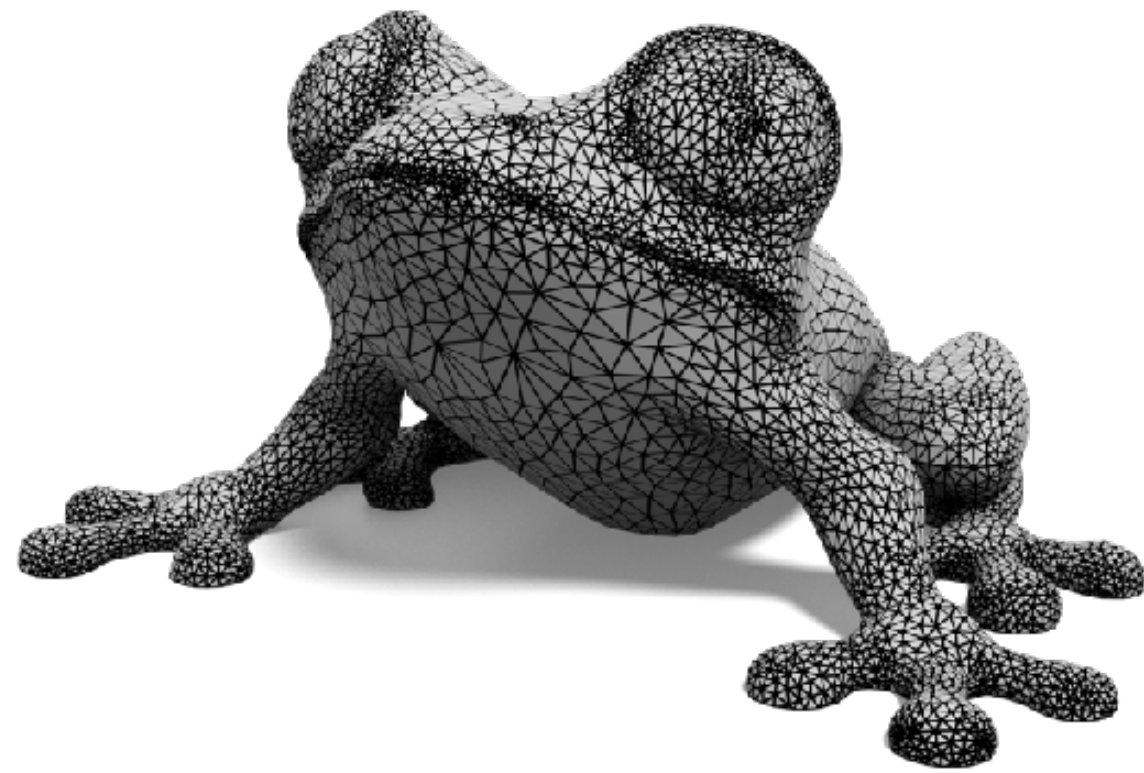
Learned Global Descriptors



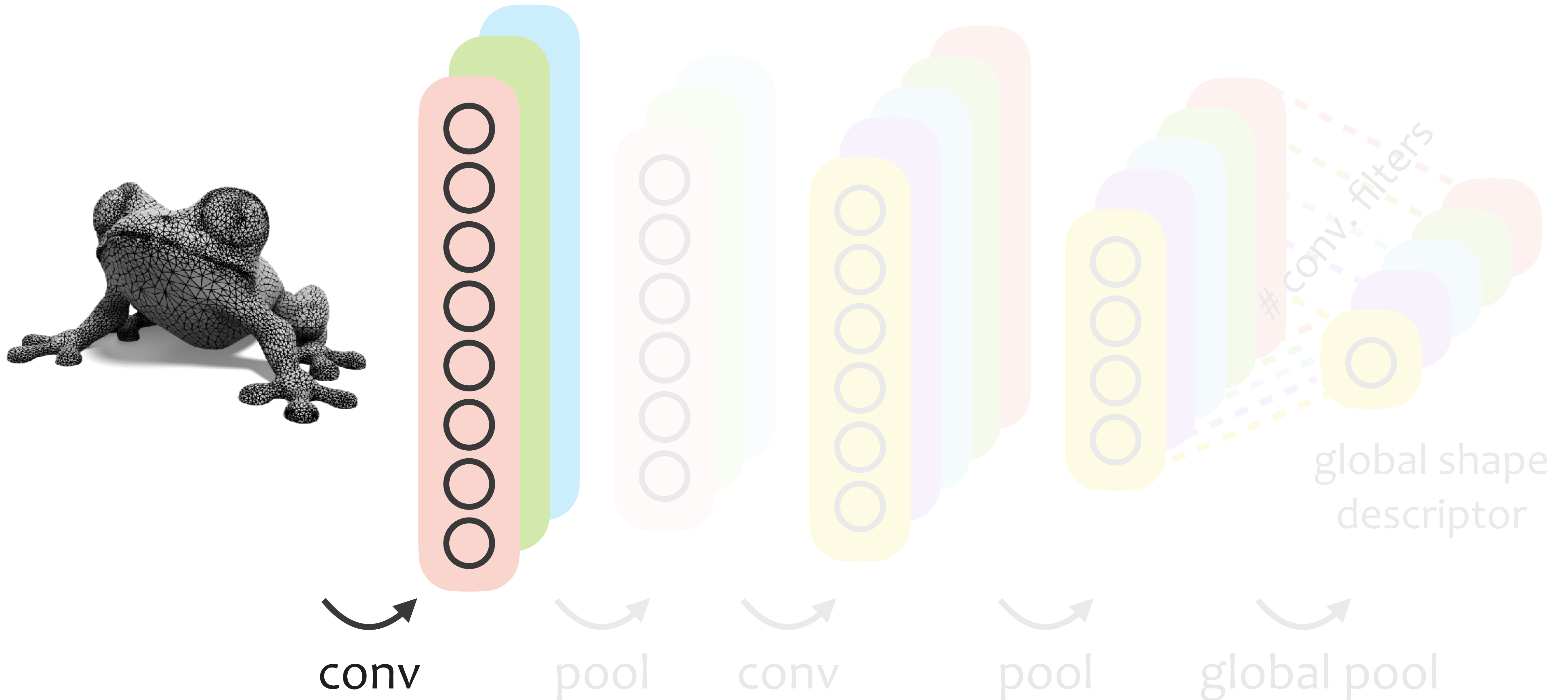
Learned Global Descriptors



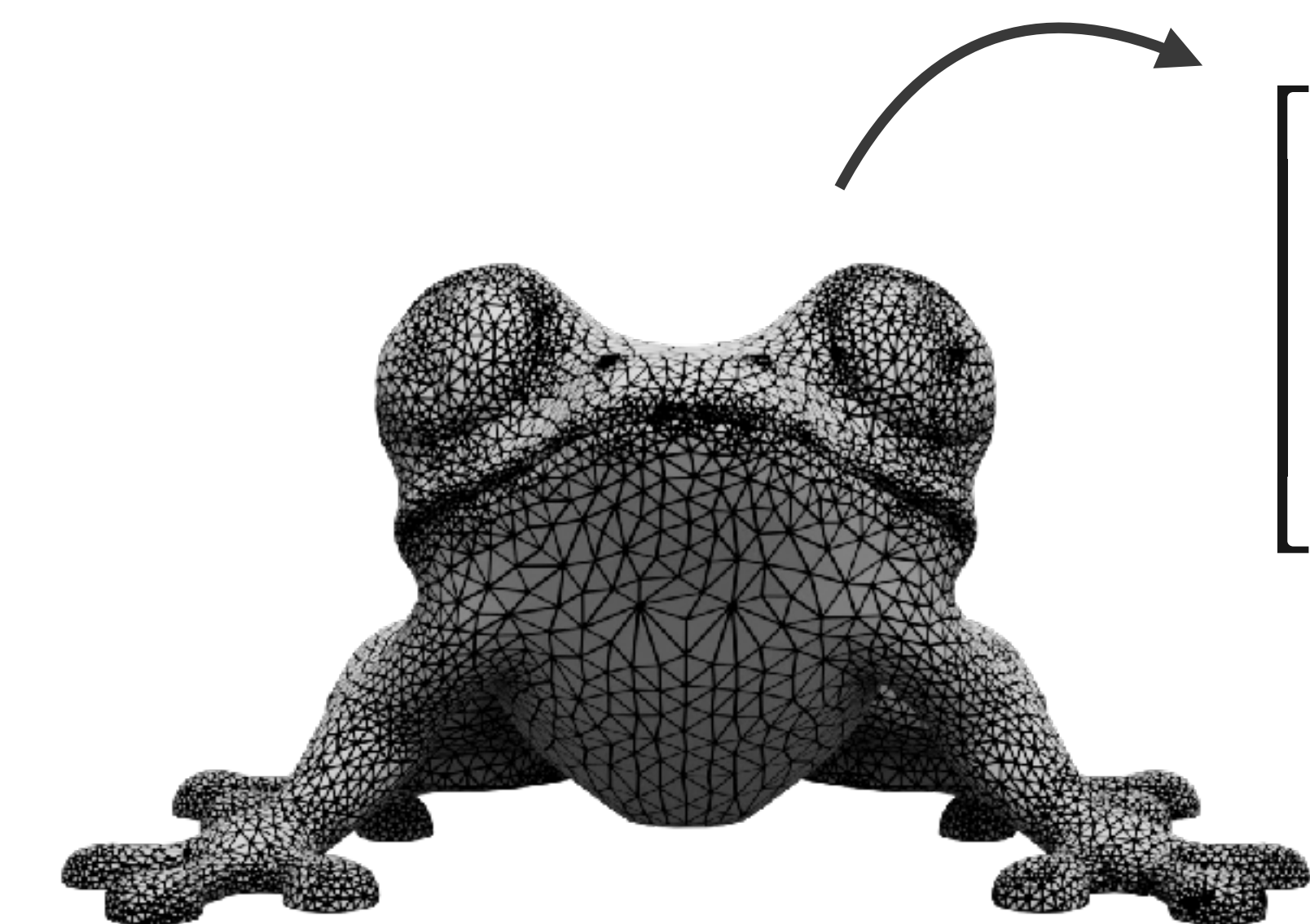
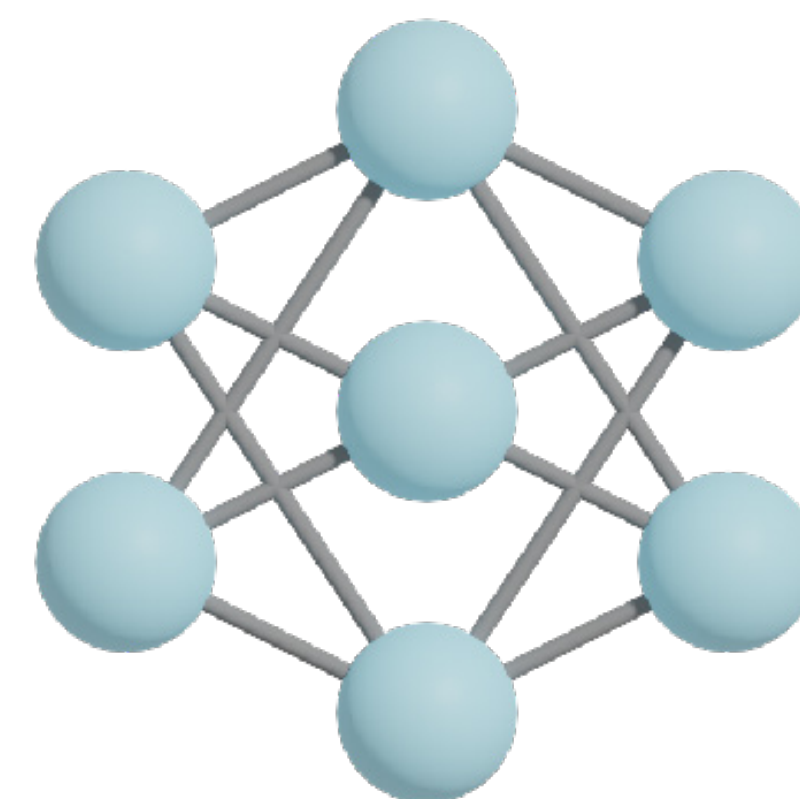
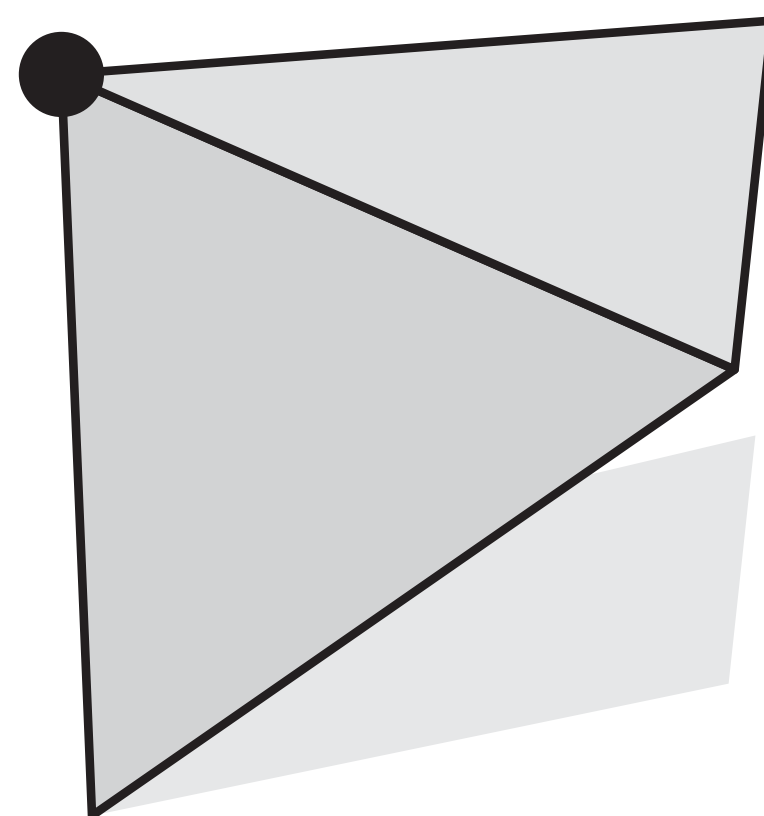
Learned Global Descriptors



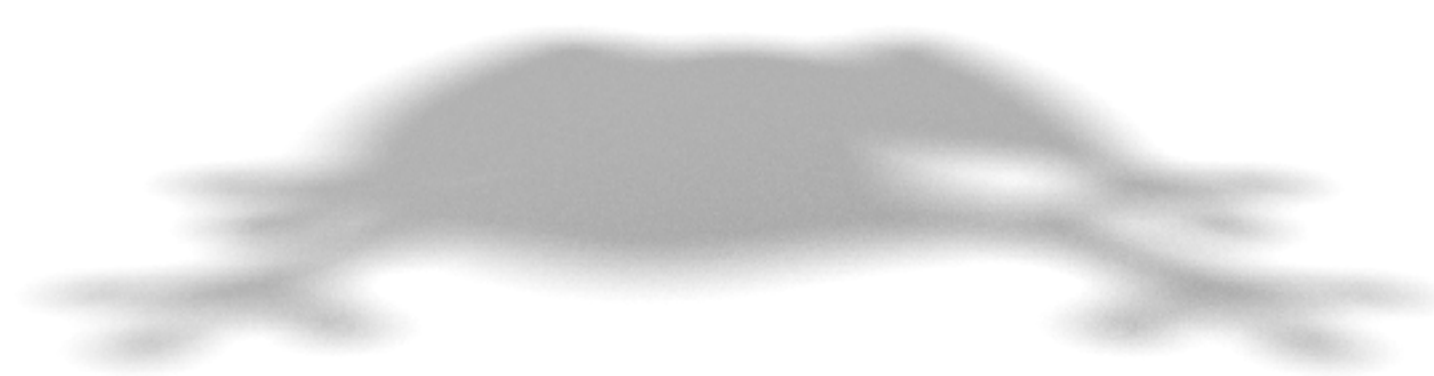
Inputs to the network



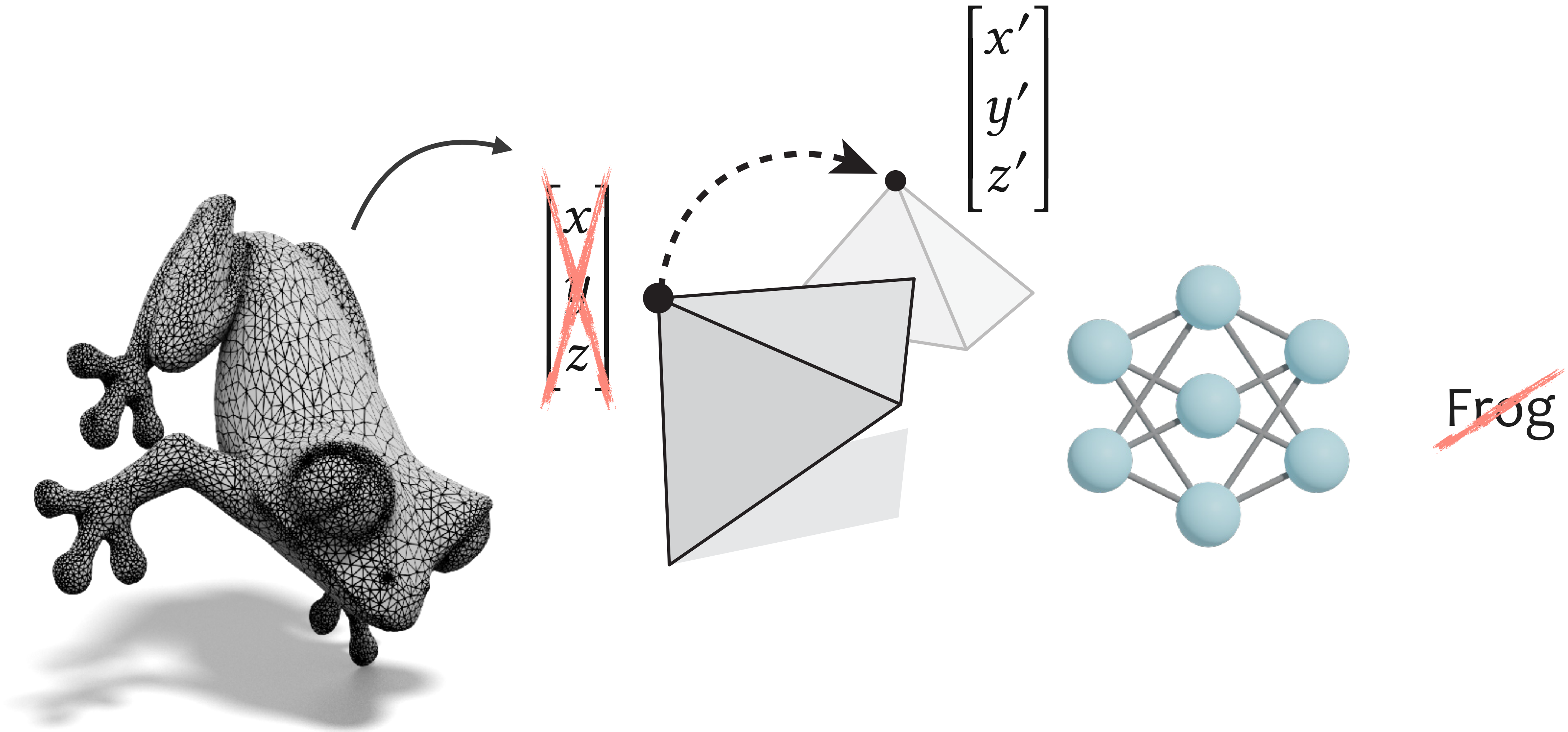
Not Orientation Invariant


$$\begin{bmatrix} x \\ y \\ z \end{bmatrix}$$


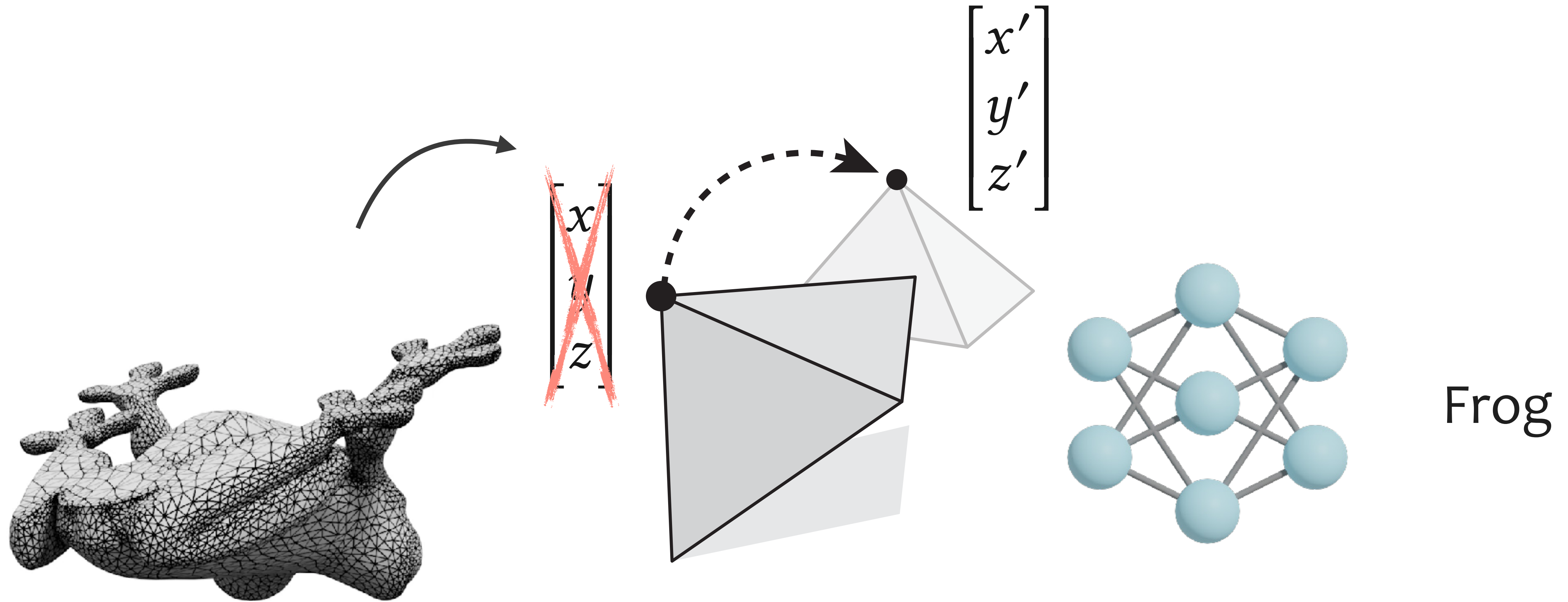
Frog



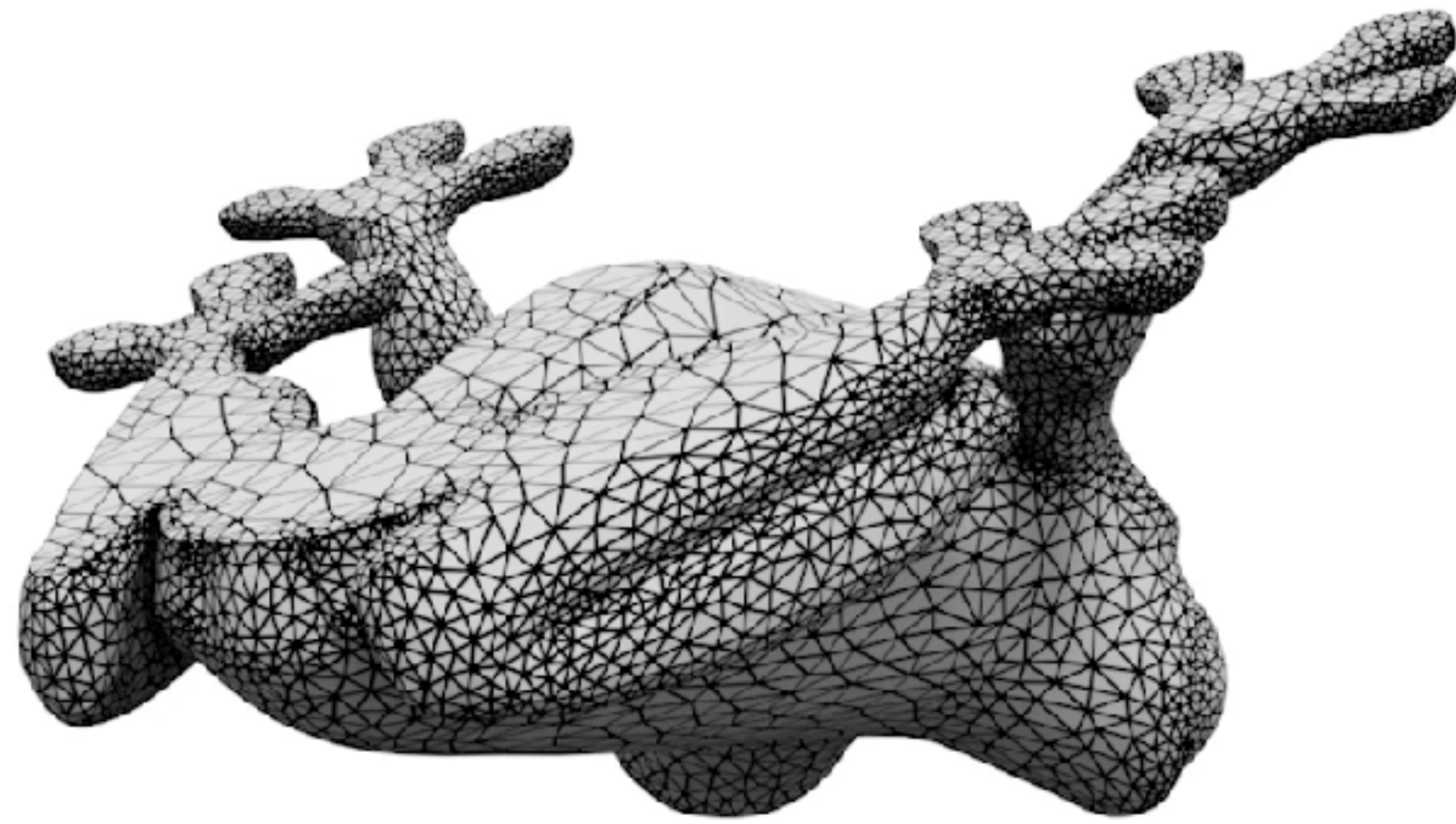
Not Orientation Invariant



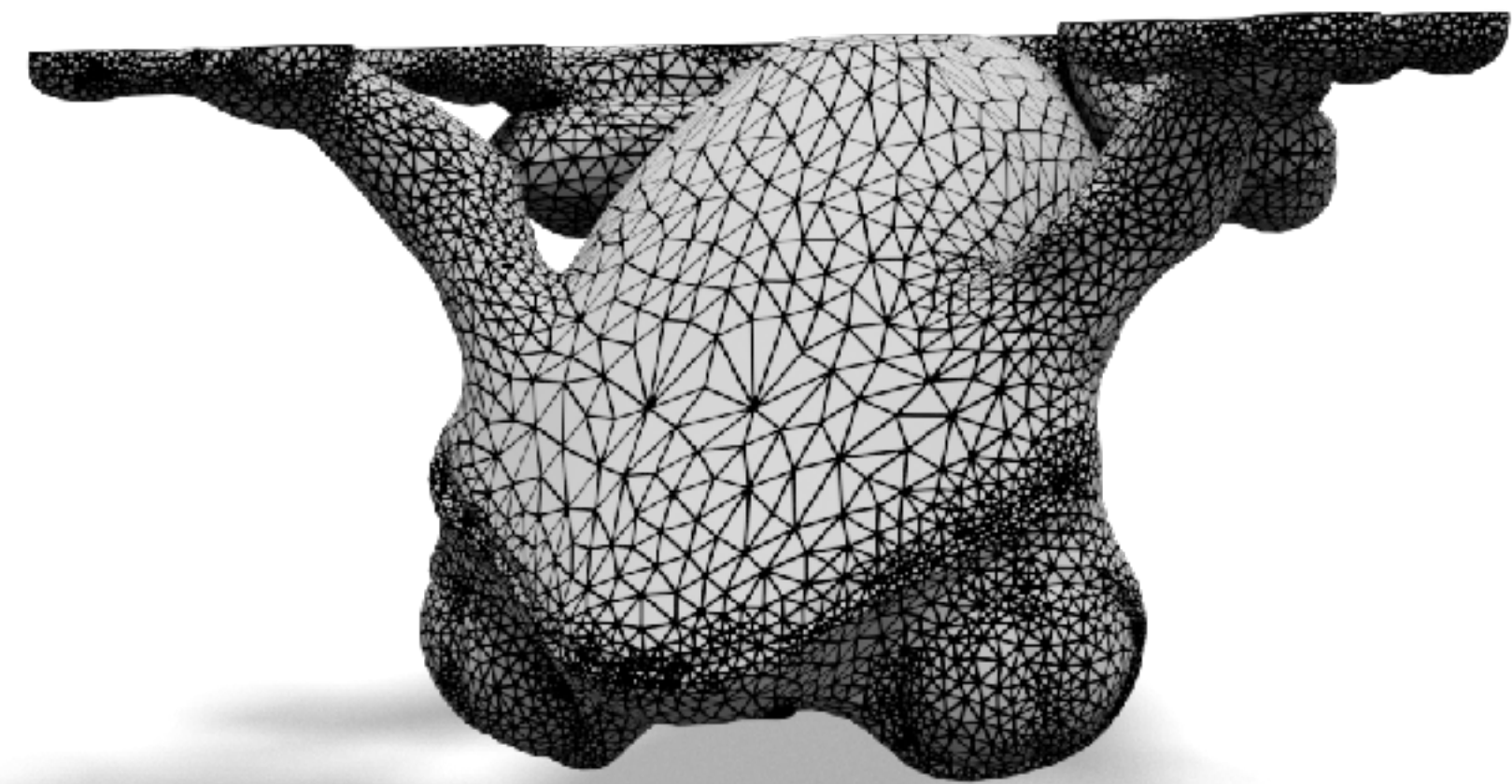
One Solution: Data Augmentation



It helps, but ...

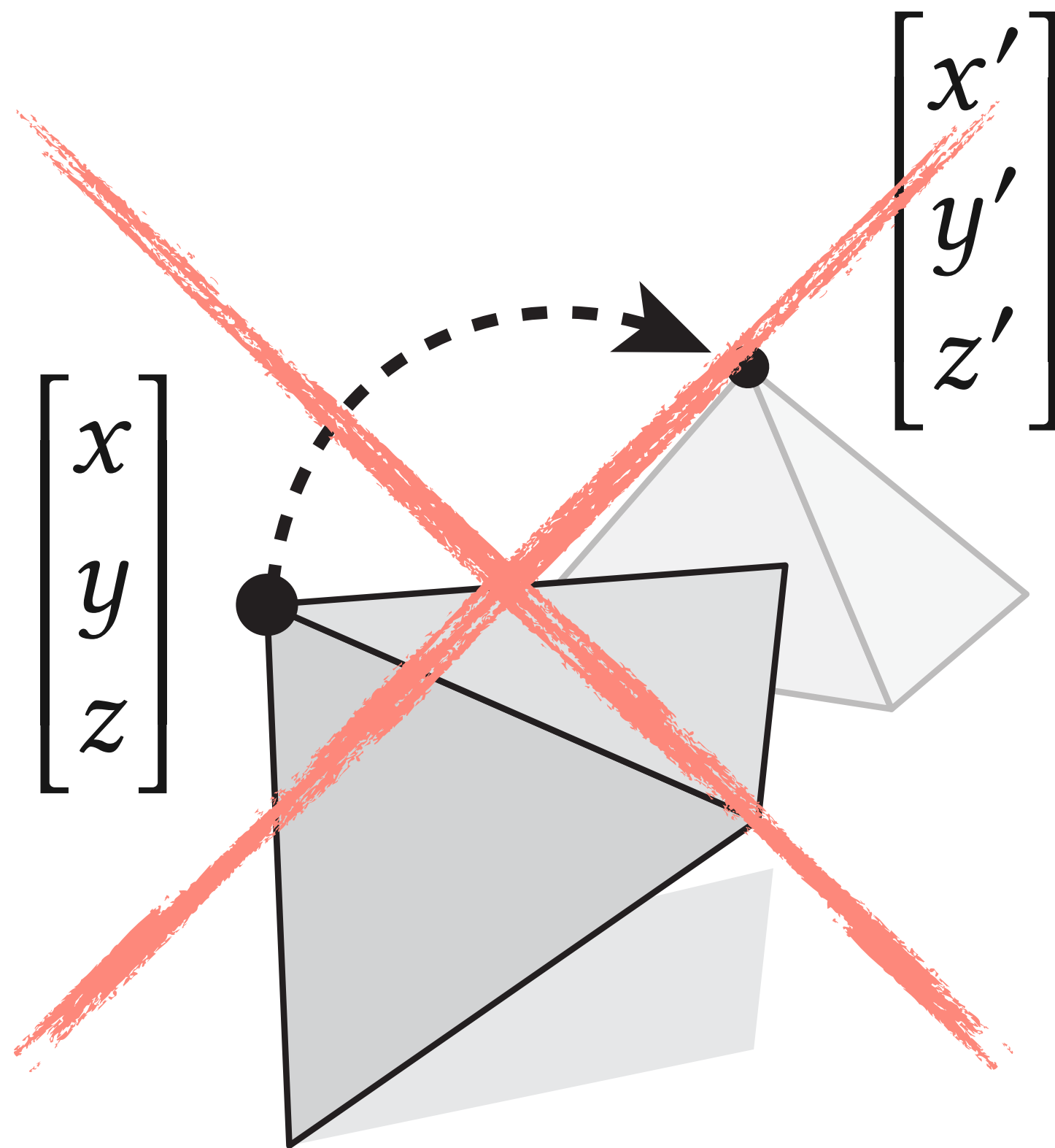


longer to train

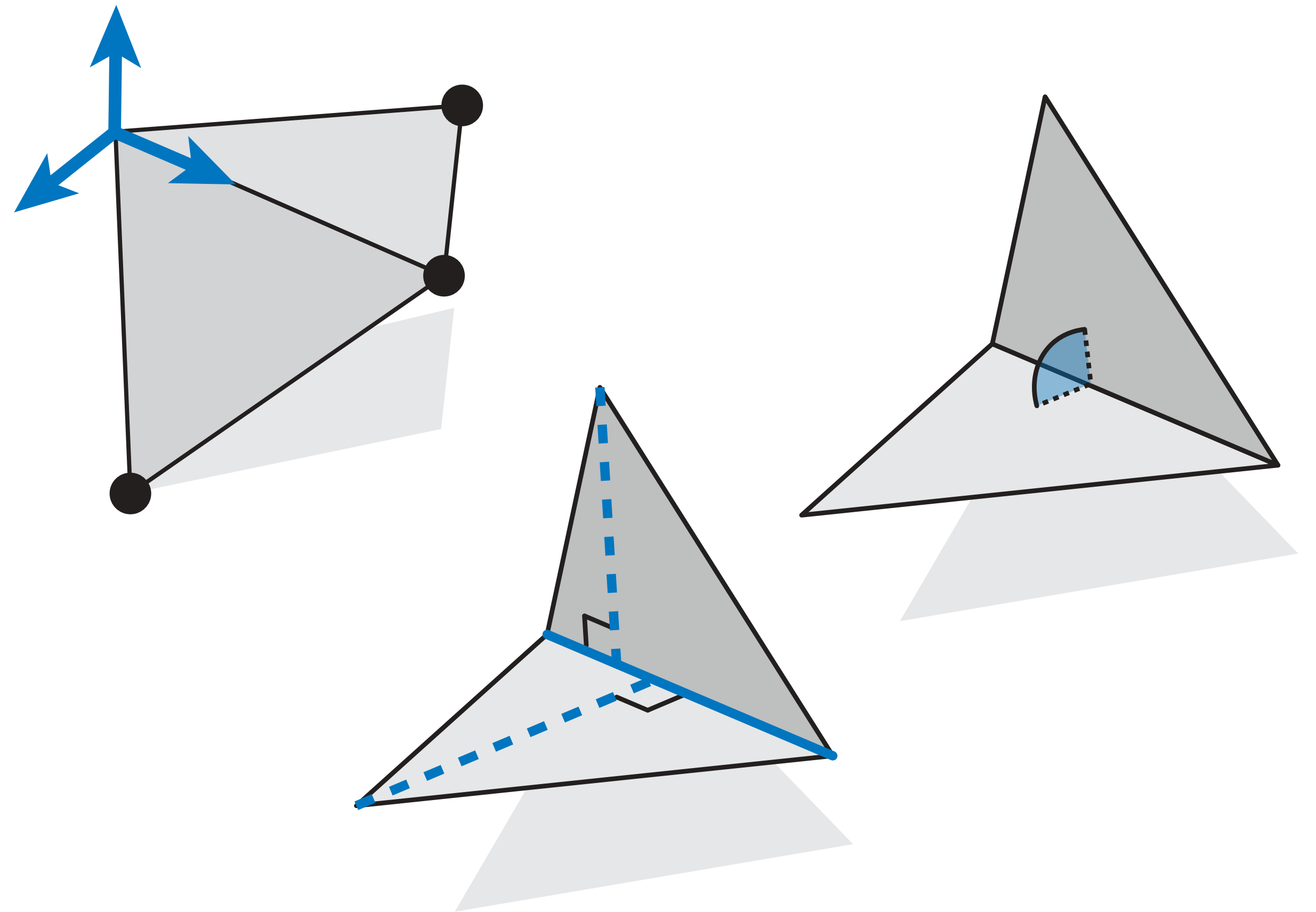


Adversarial attack

Leverage mesh structure

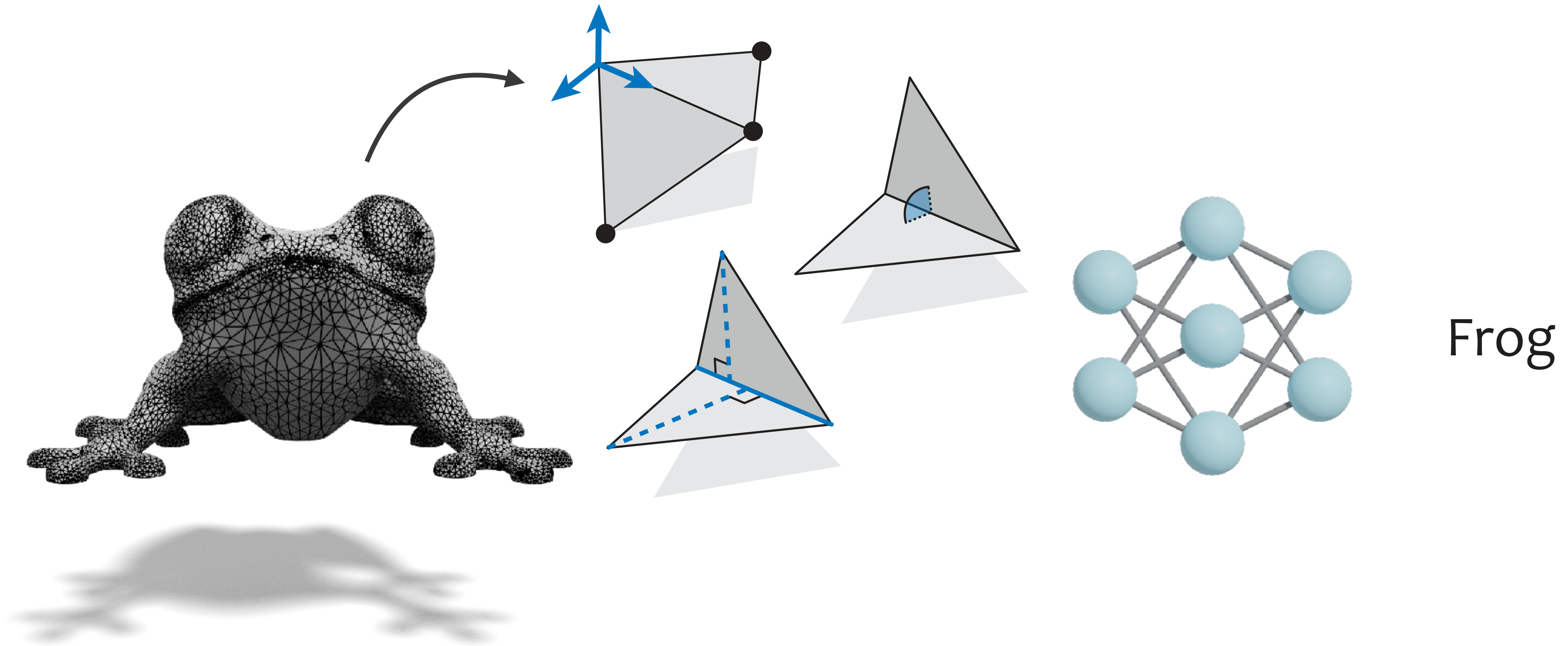


not invariant quantities



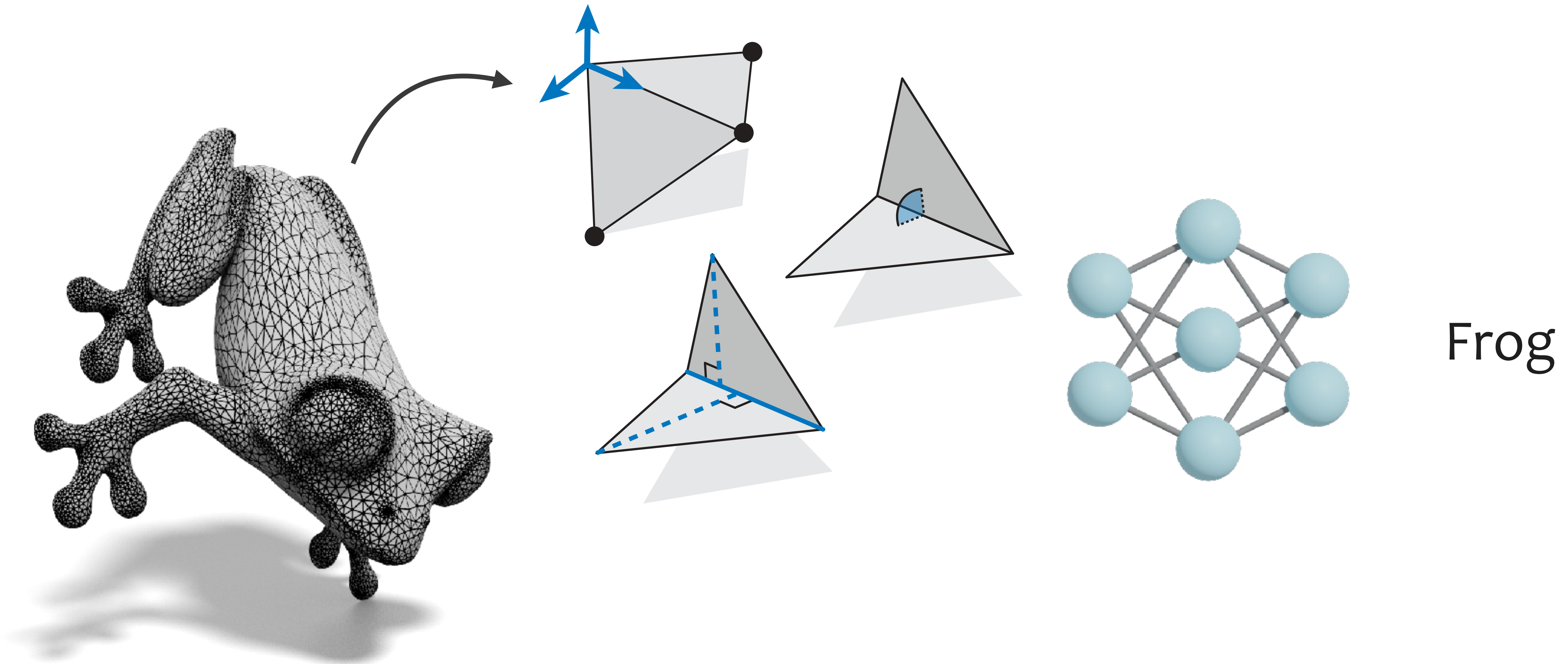
rotation invariant quantities

Orientation Invariant



Frog

Orientation Invariant



Push the limits

Classification SHREC		
Method	Split 16	Split 10
MeshCNN	98.6	91.0%
GWCNN	96.6%	90.3%
GI	96.6%	88.6%
SN	48.4%	52.7%
SG	70.8%	62.6%



Classic method
[Bronstein et al. 2011]

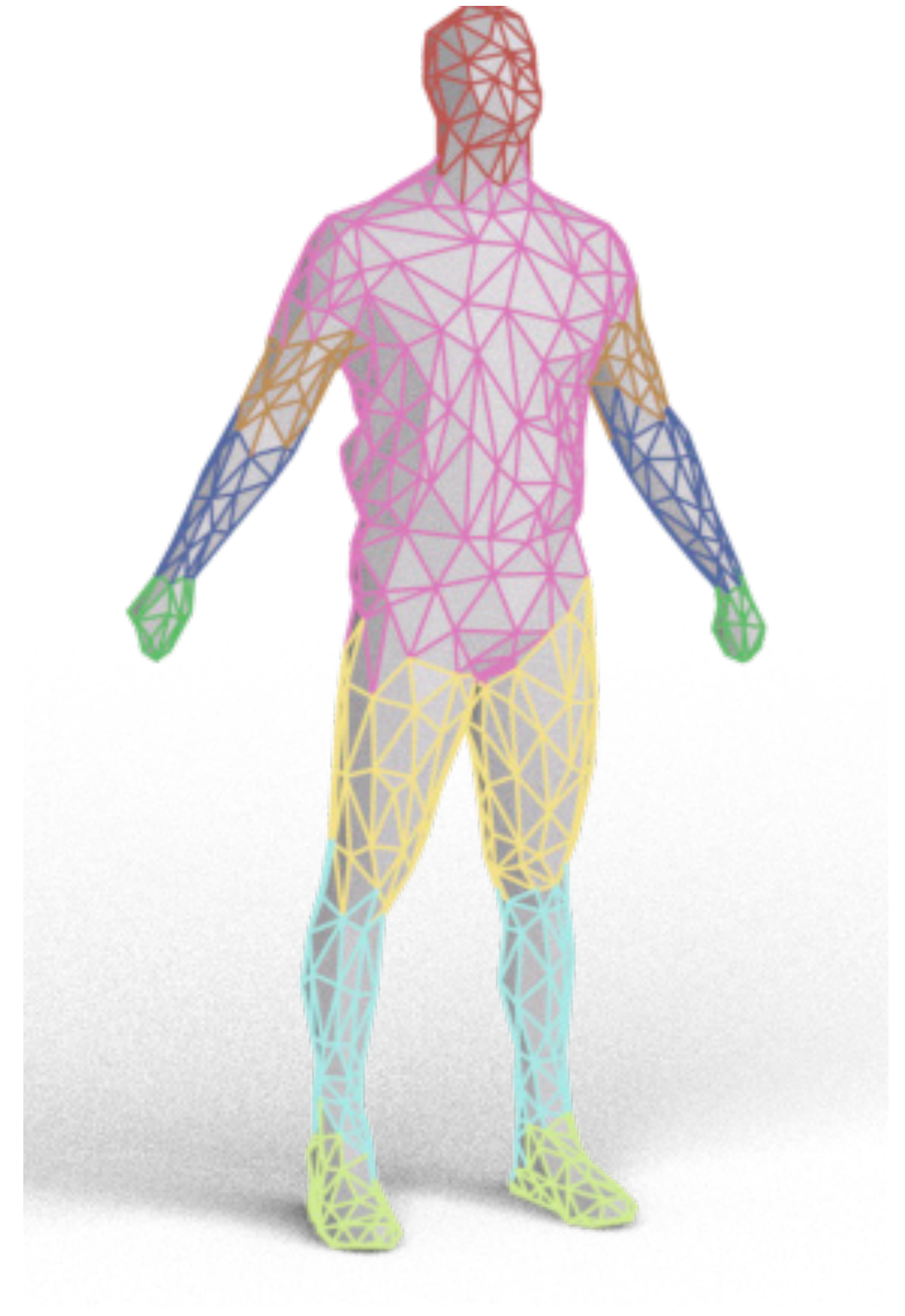
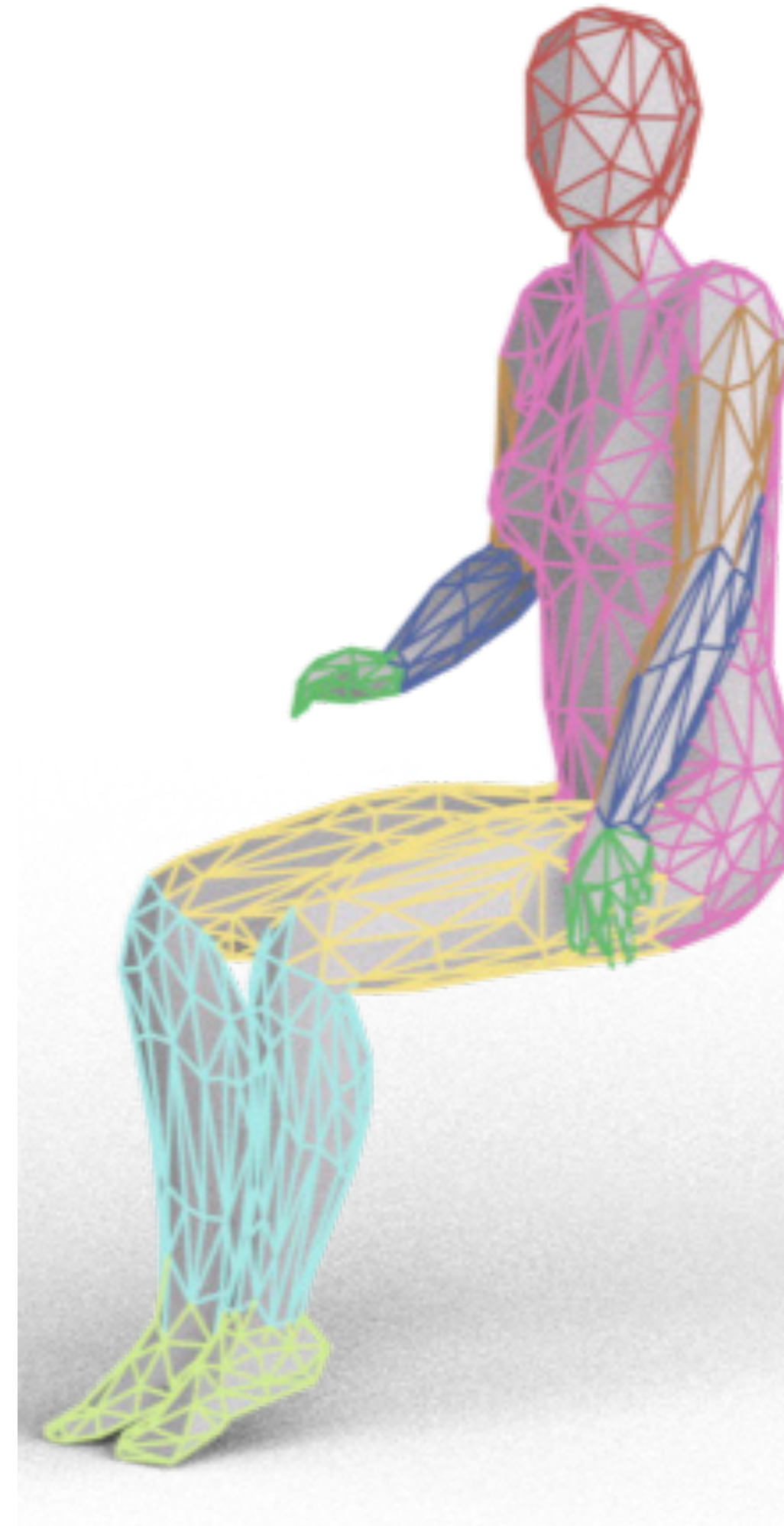
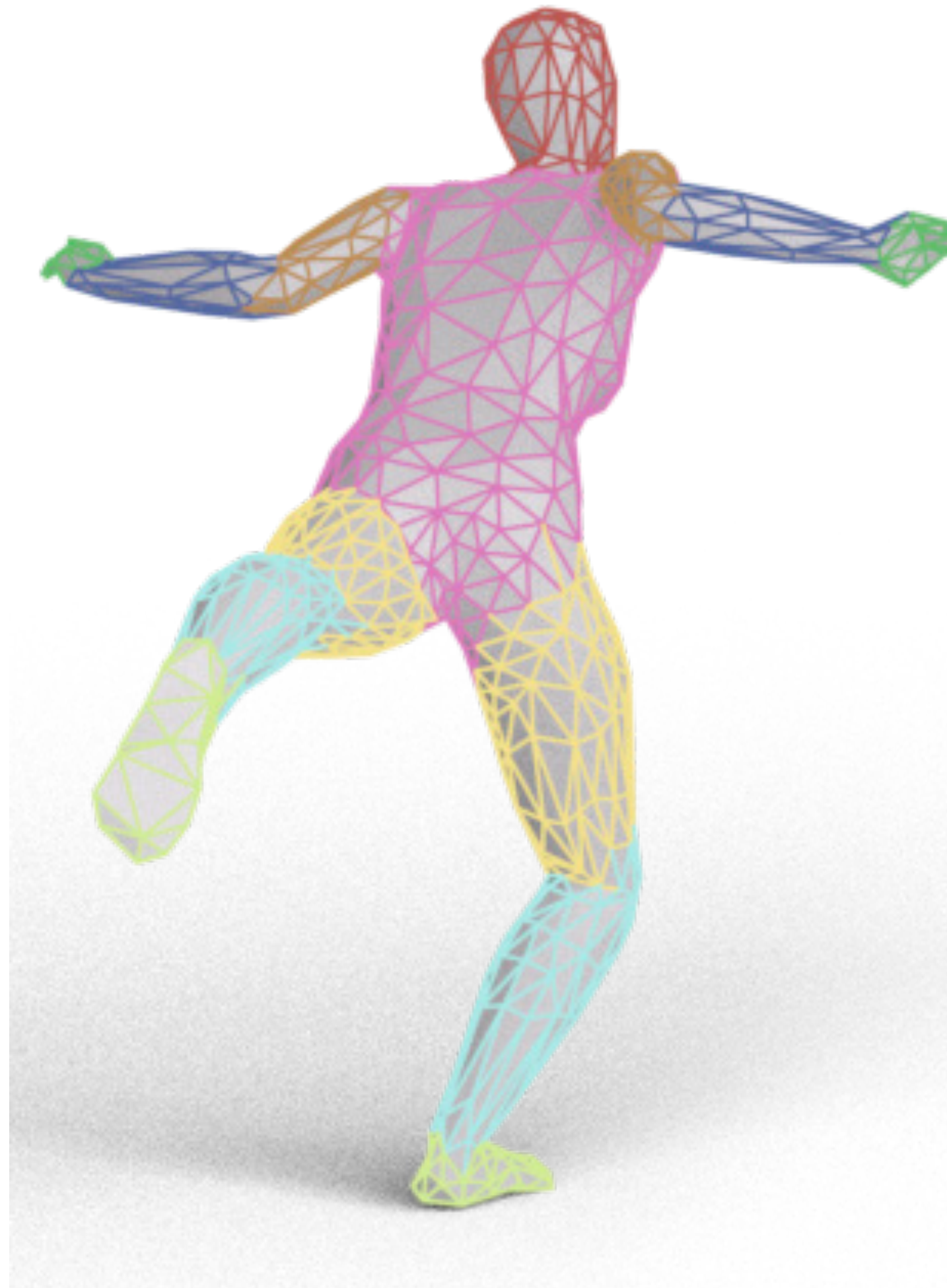
Push the limits

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GI	96.6%	88.6%
SN	48.4%	52.7%
SG	70.8%	62.6%

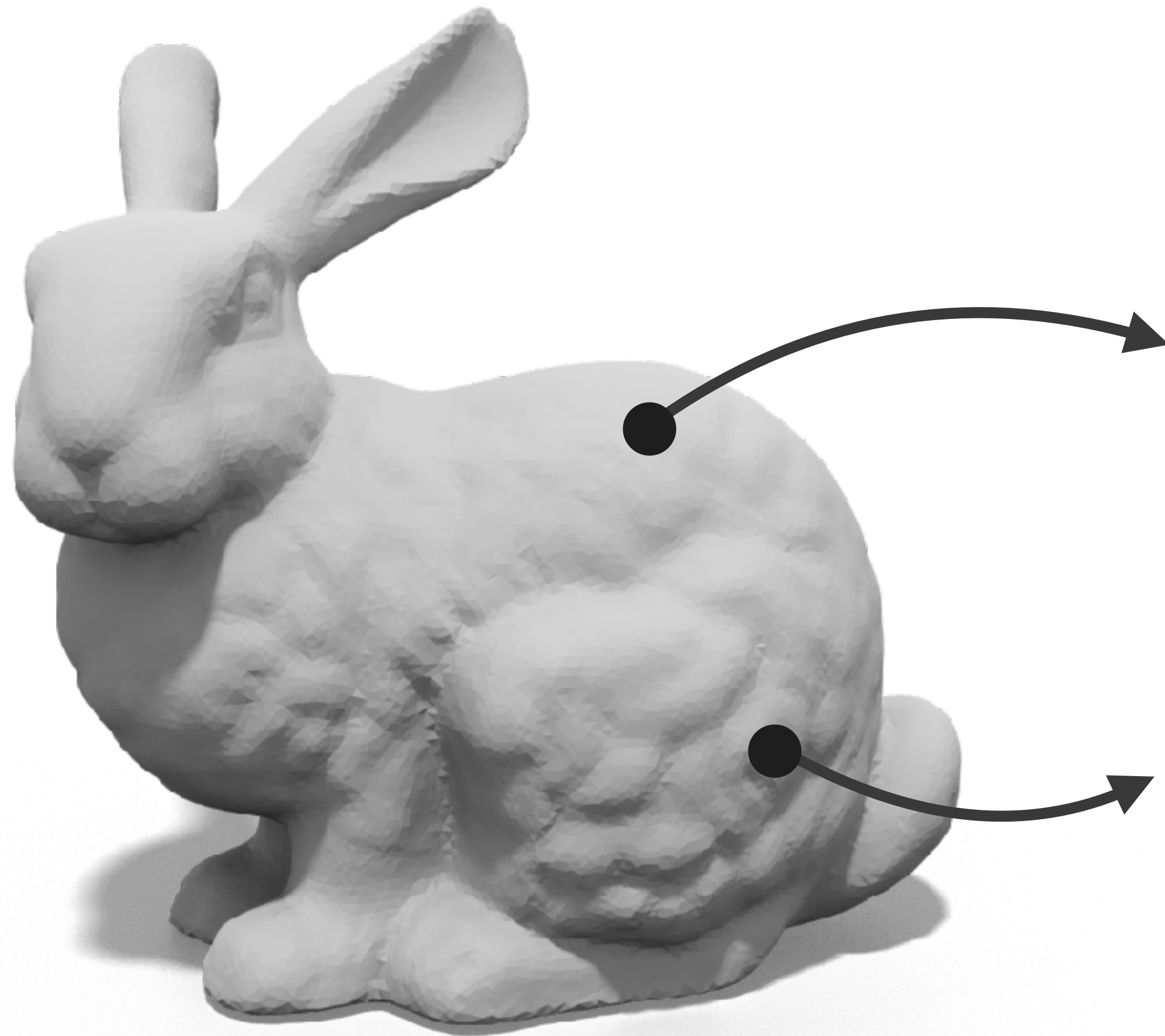


Classic method
[Bronstein et al. 2011]

Shape Segmentation



Local Shape Descriptors

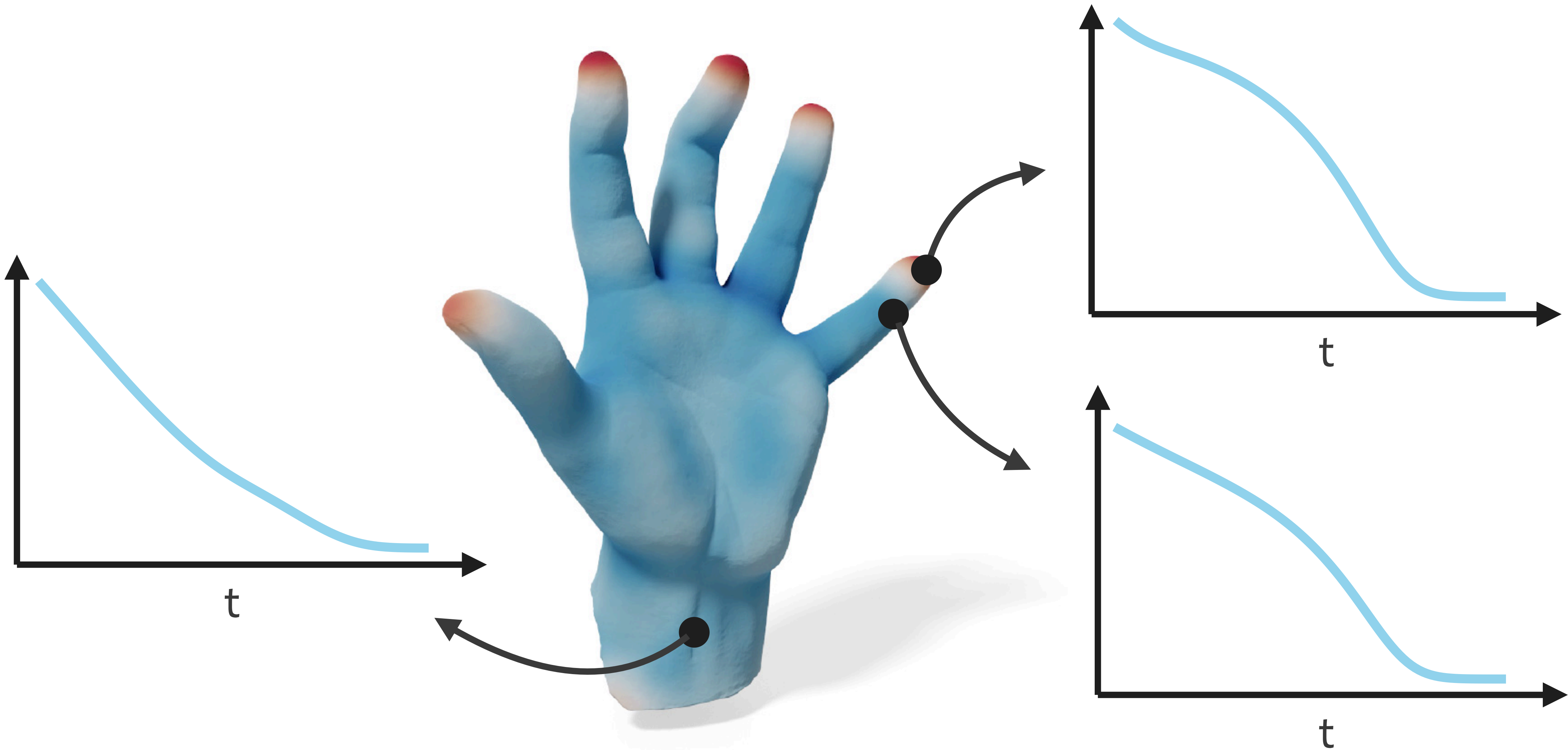


$$[a_1, a_2, \dots, a_n]$$

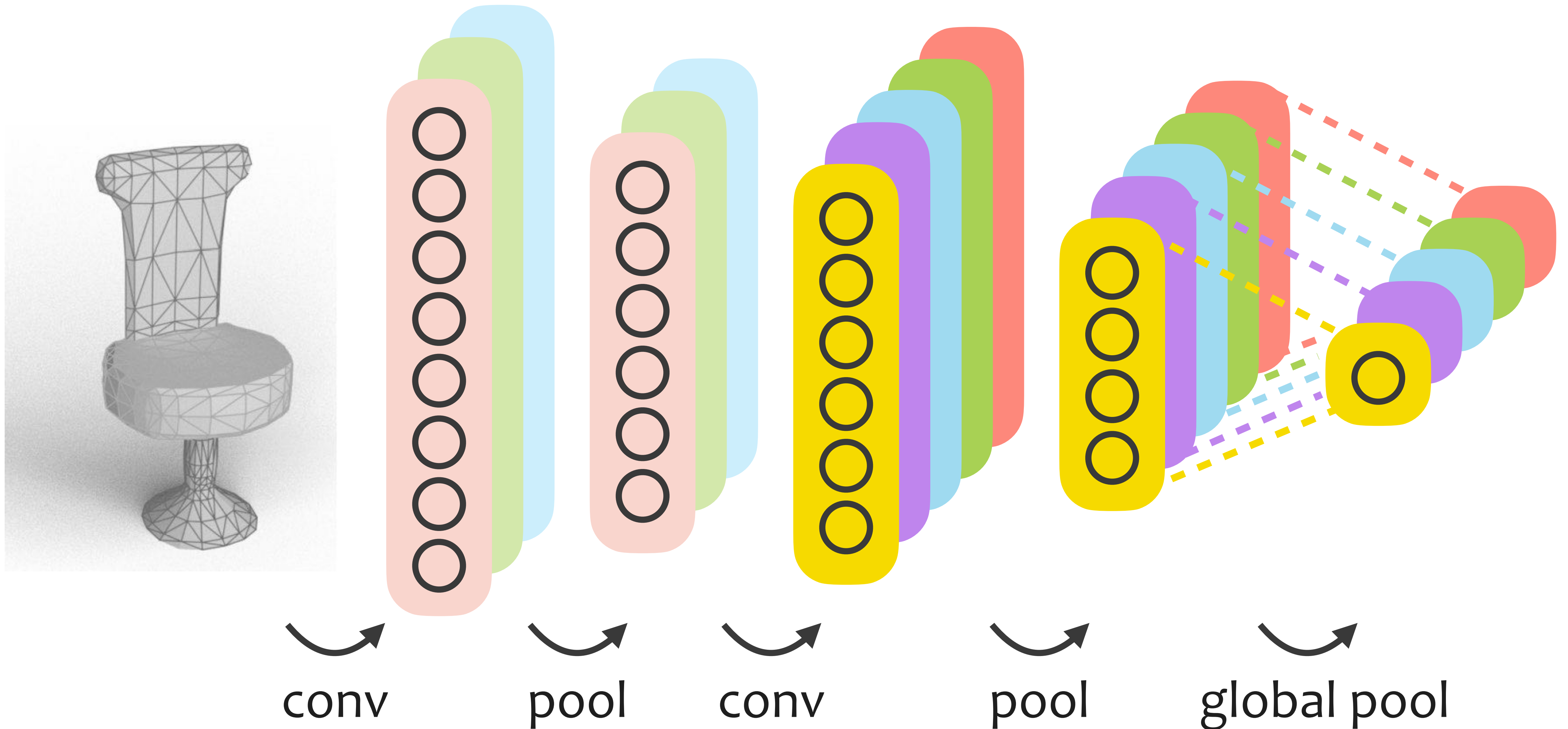
$$[b_1, b_2, \dots, b_n]$$

a fixed dimensional vector
per element

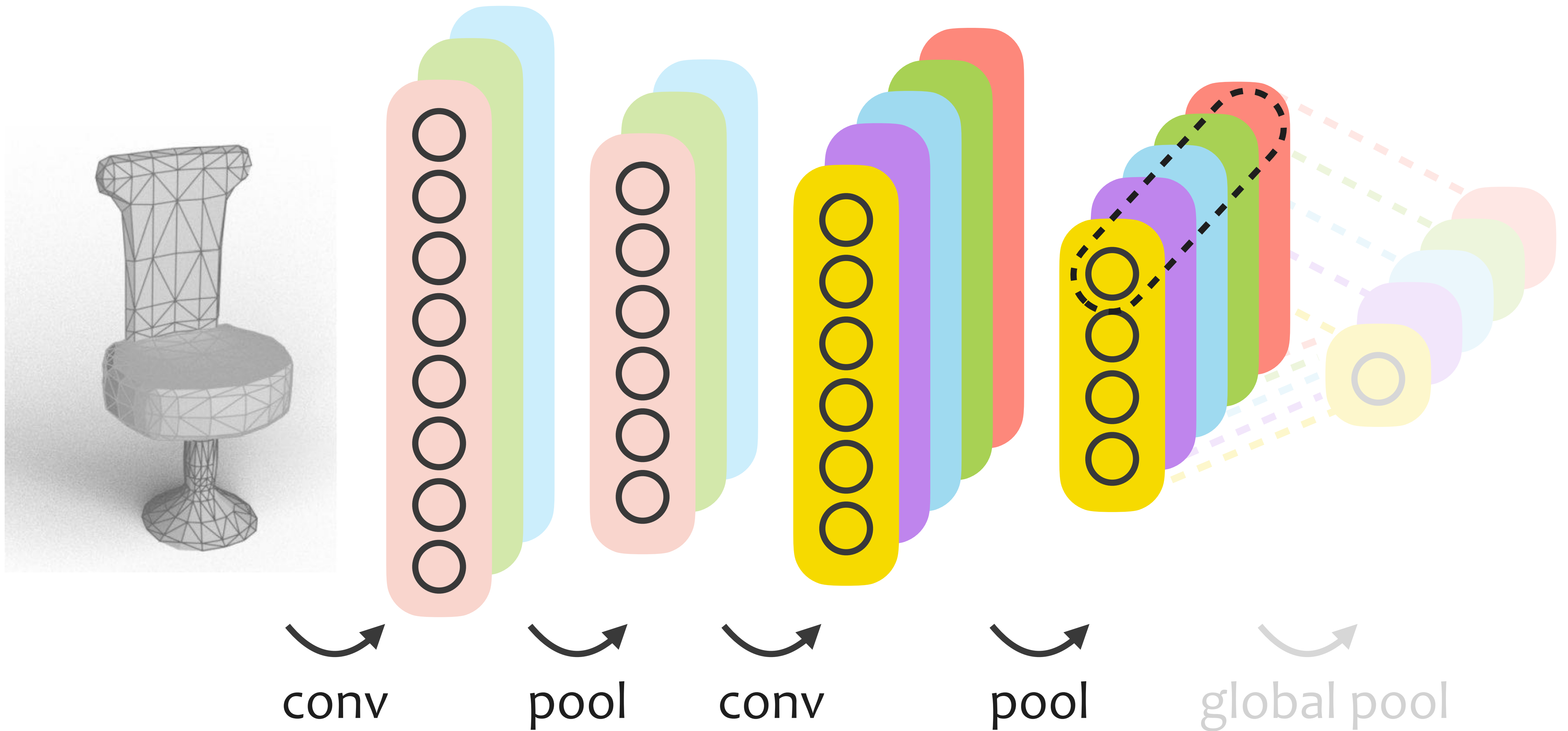
E.g., Heat Kernel Signature



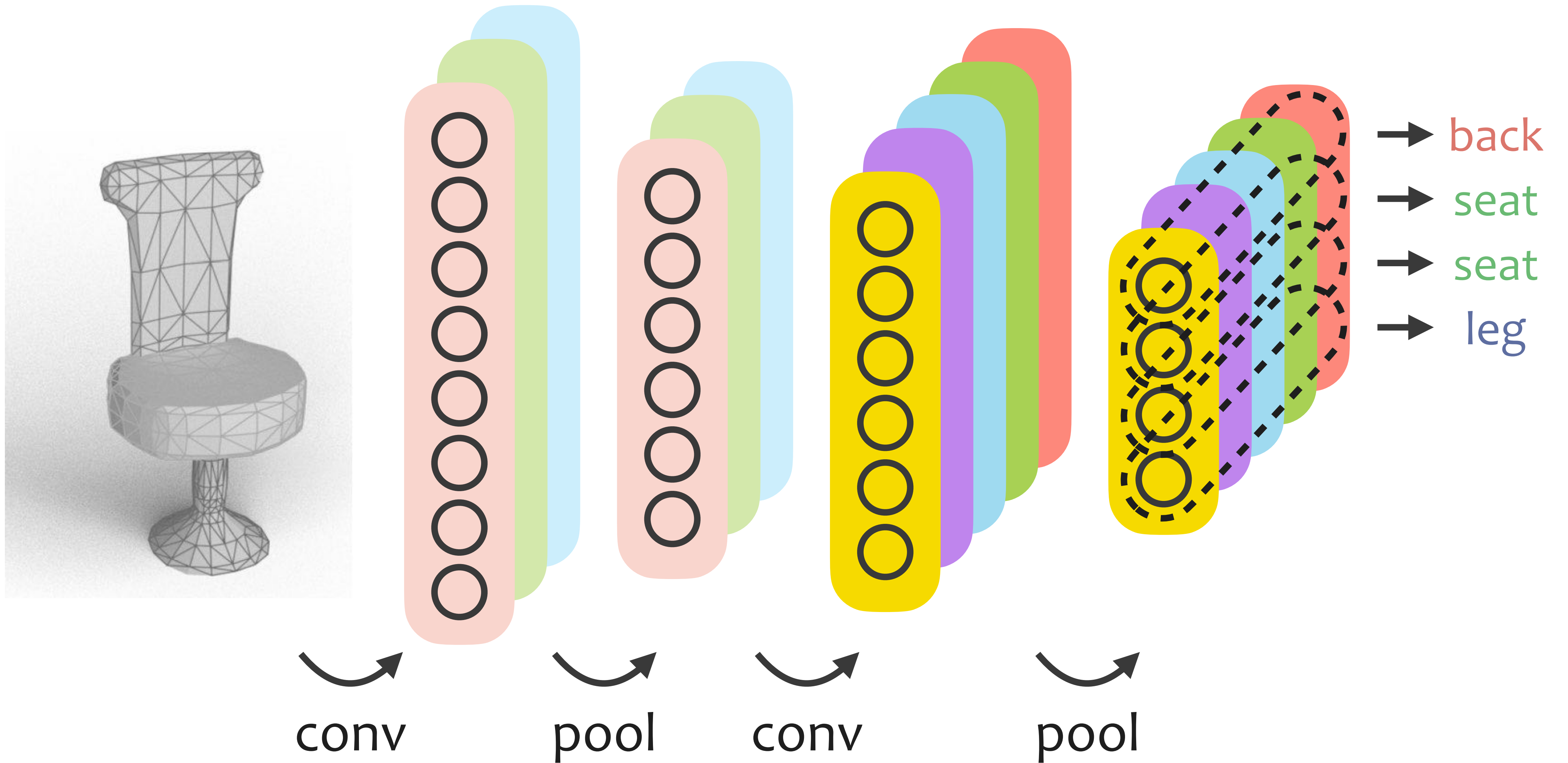
Learned Local Descriptors



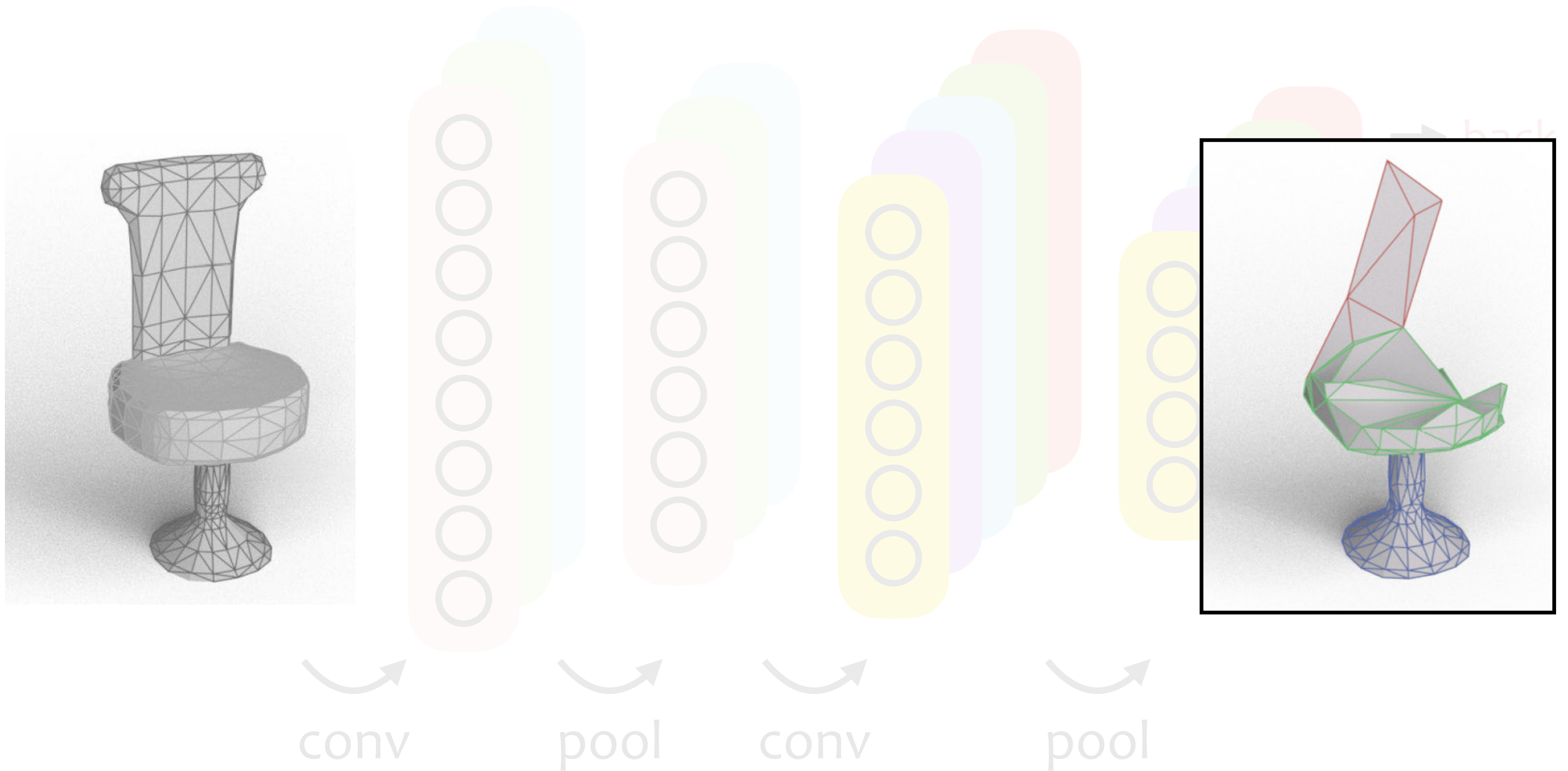
Learned Local Descriptors



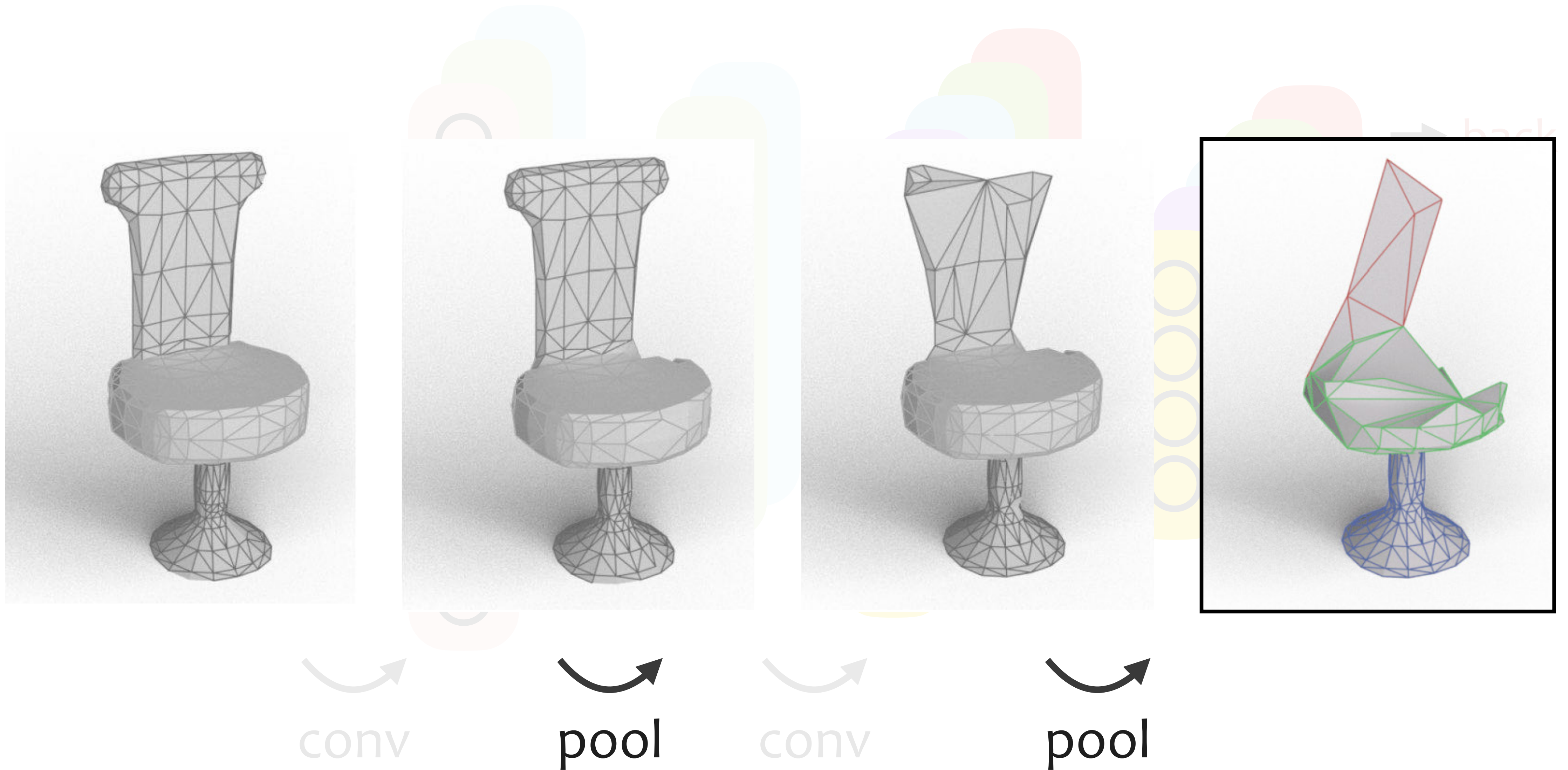
Learned Local Descriptors



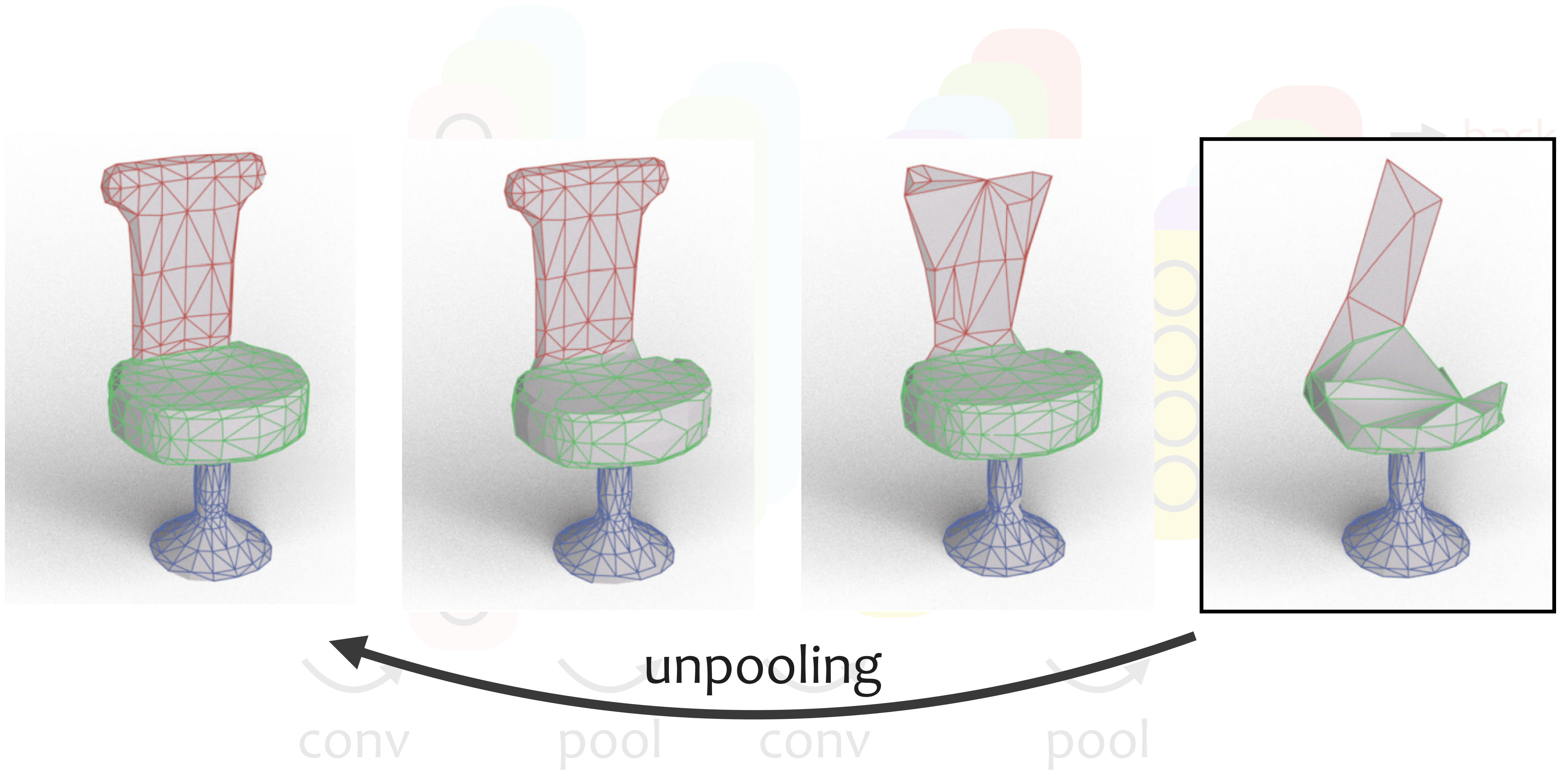
Machine Learning Segmentation



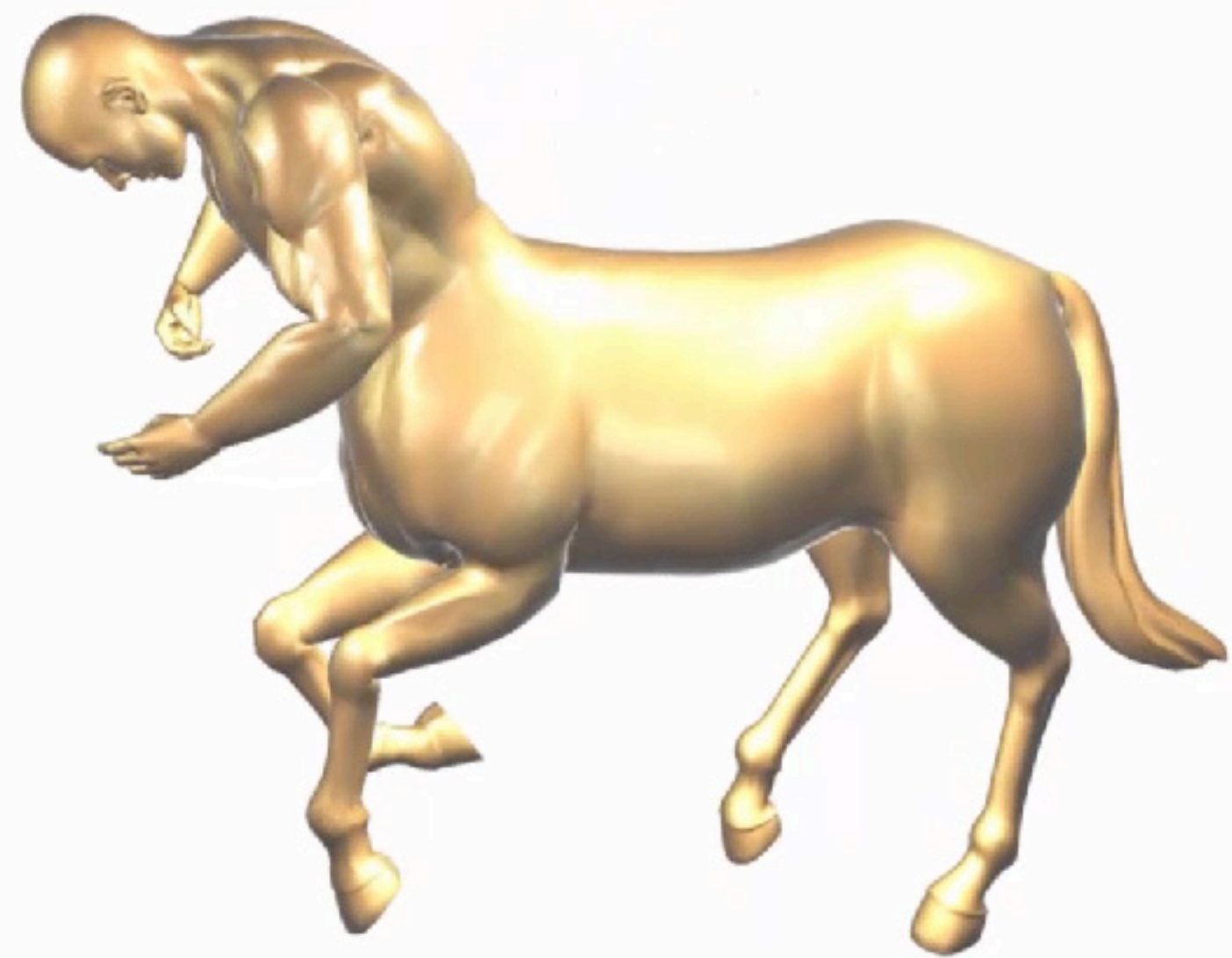
Machine Learning Segmentation



Machine Learning Segmentation



Handle Shape Variants



isometry

Handle Shape Variants

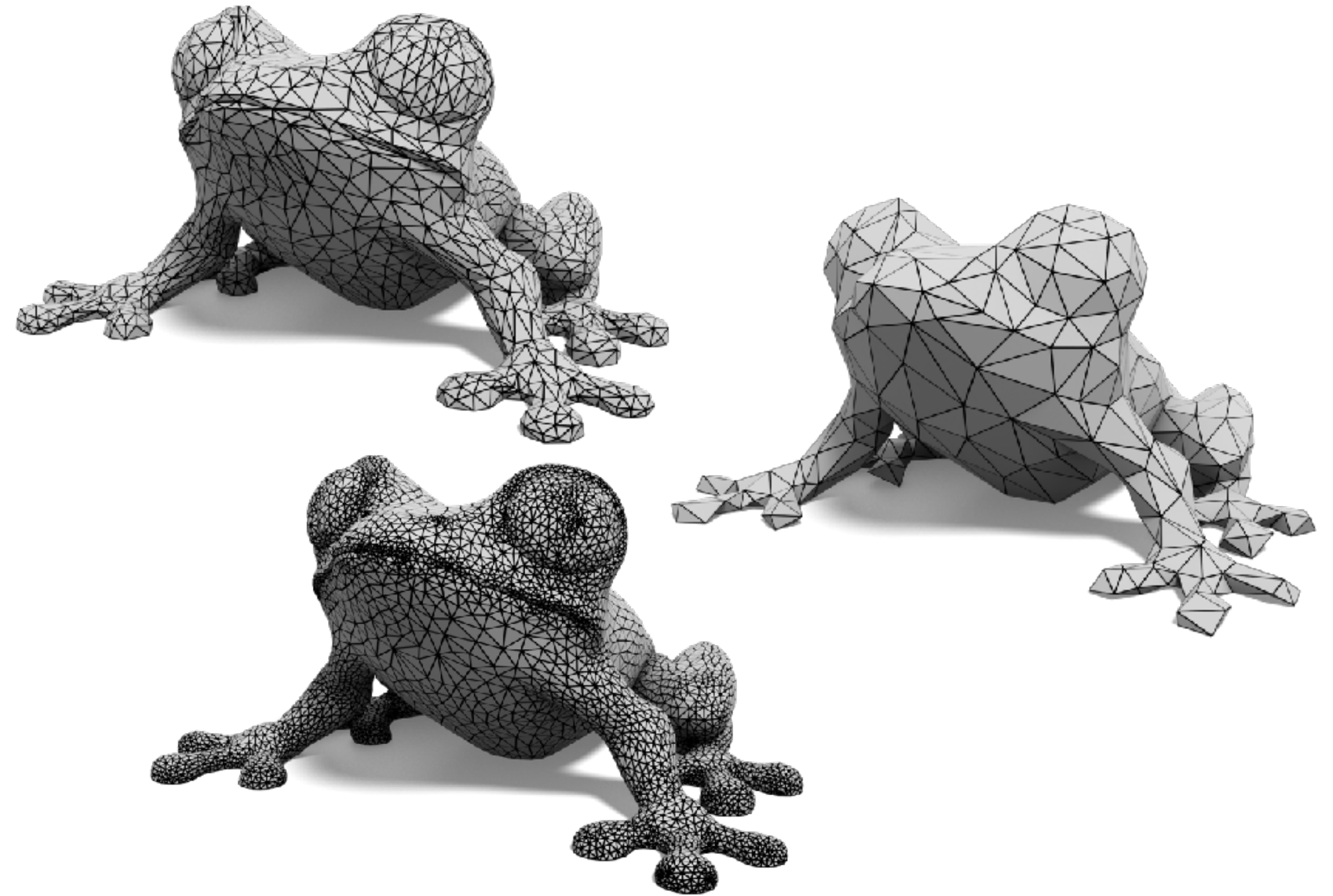


isometry invariant quantities

Handle Shape Variants



isometry invariant quantities



discretizations

Handle Shape Variants

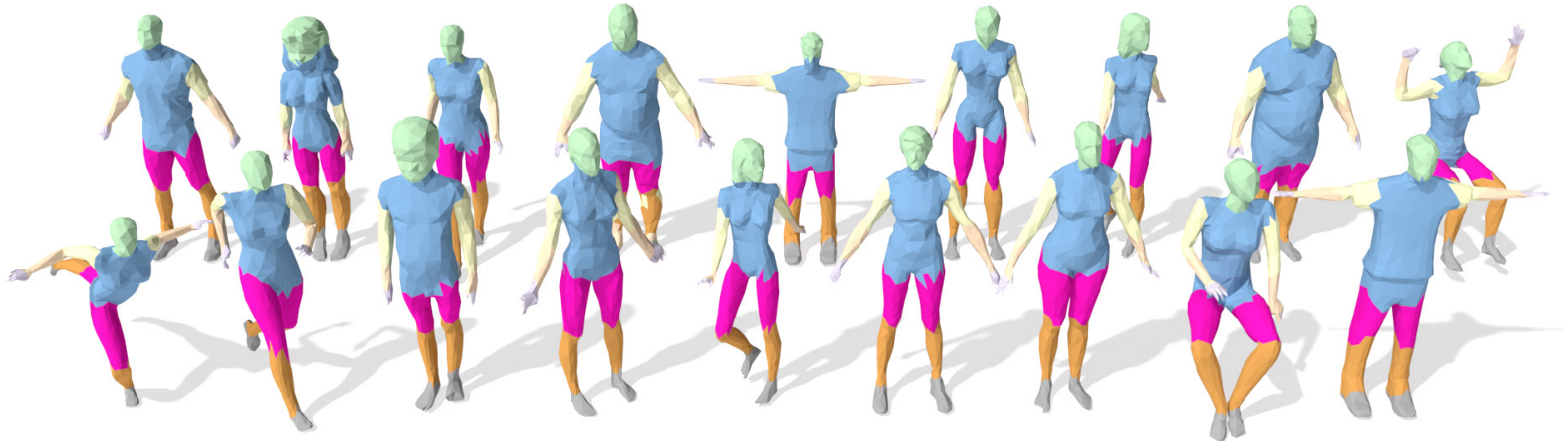


isometry invariant quantities

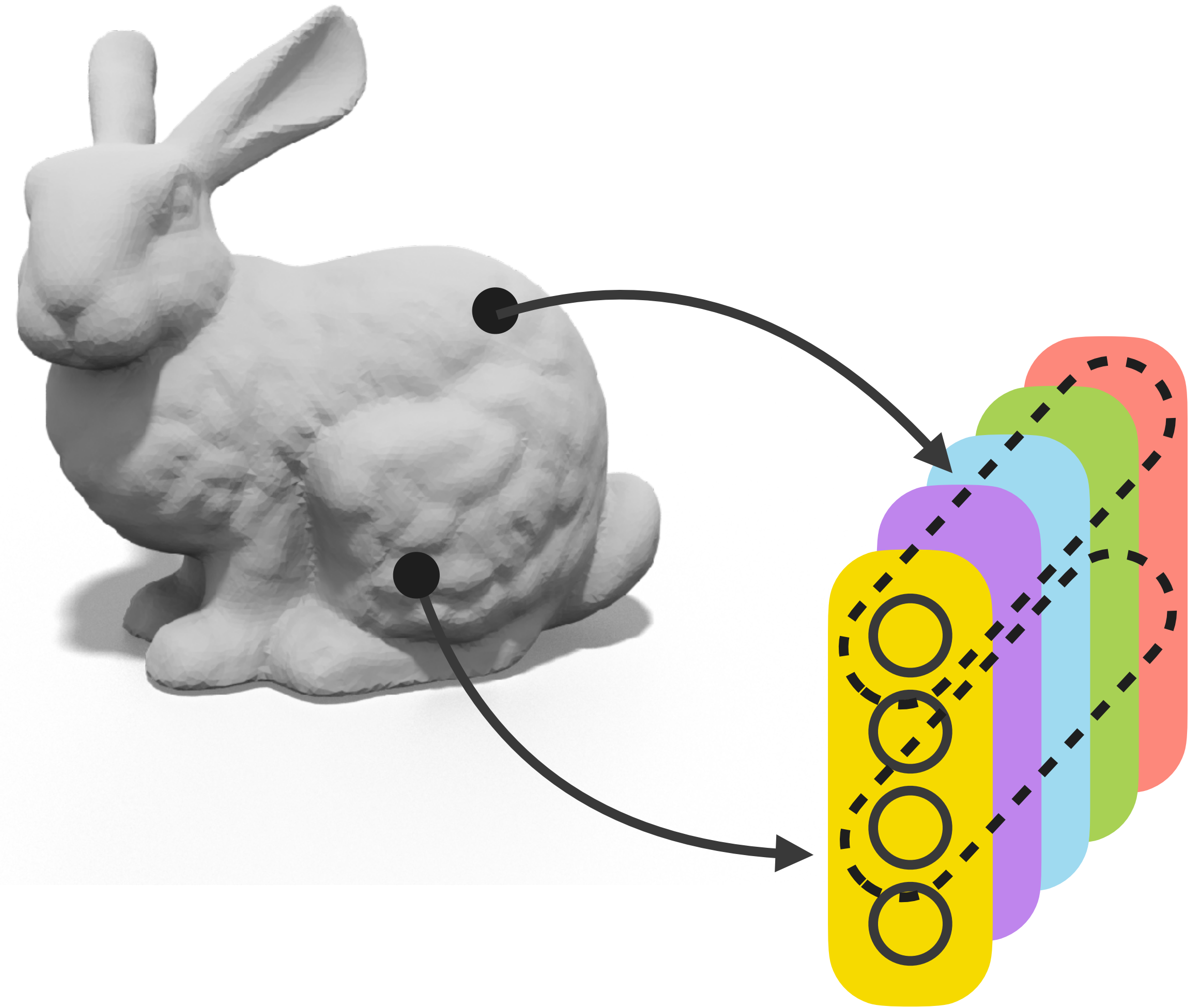
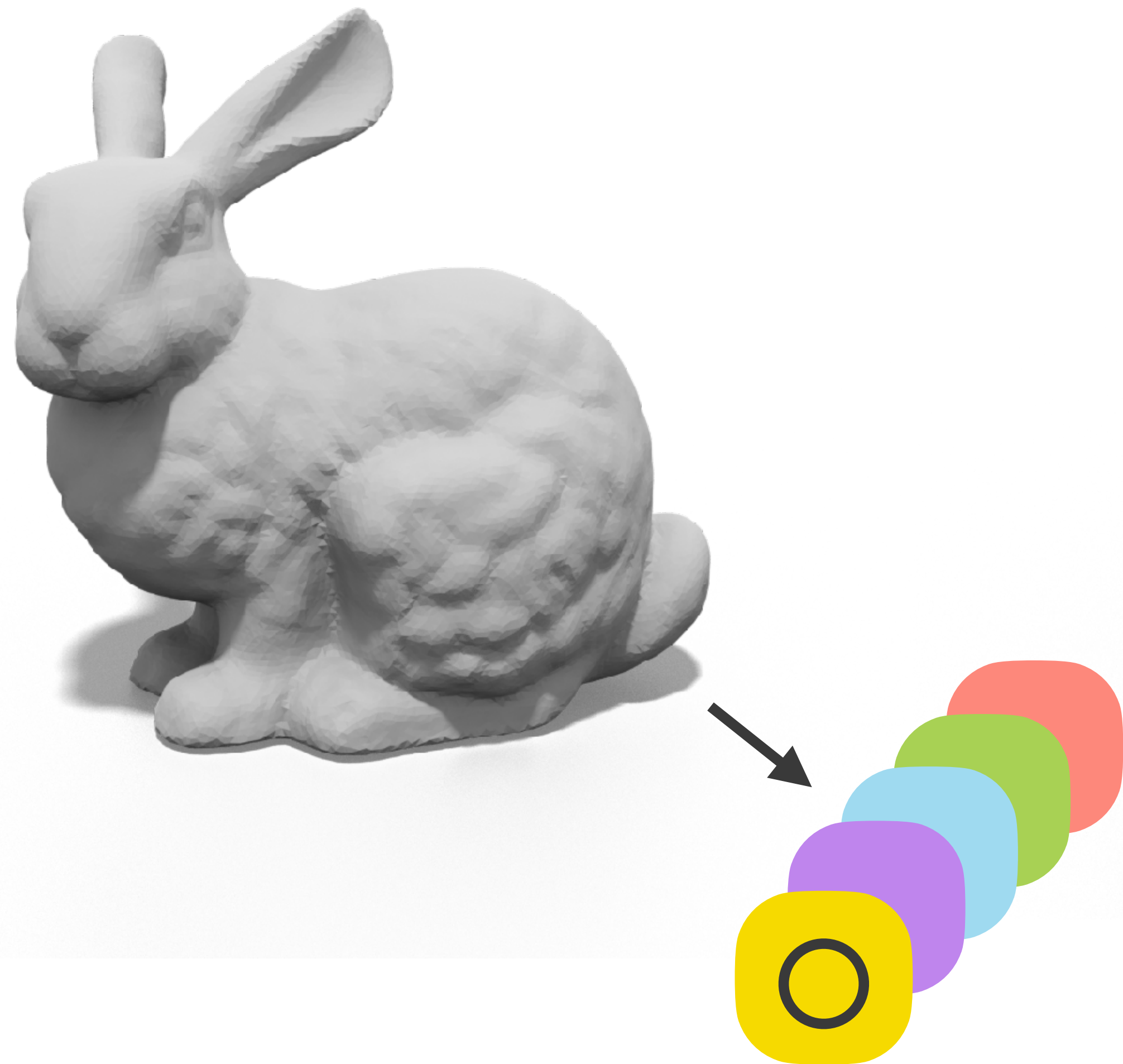


discretization agnostic convolution
(e.g., Sharp et al. 2021)

Segmentation

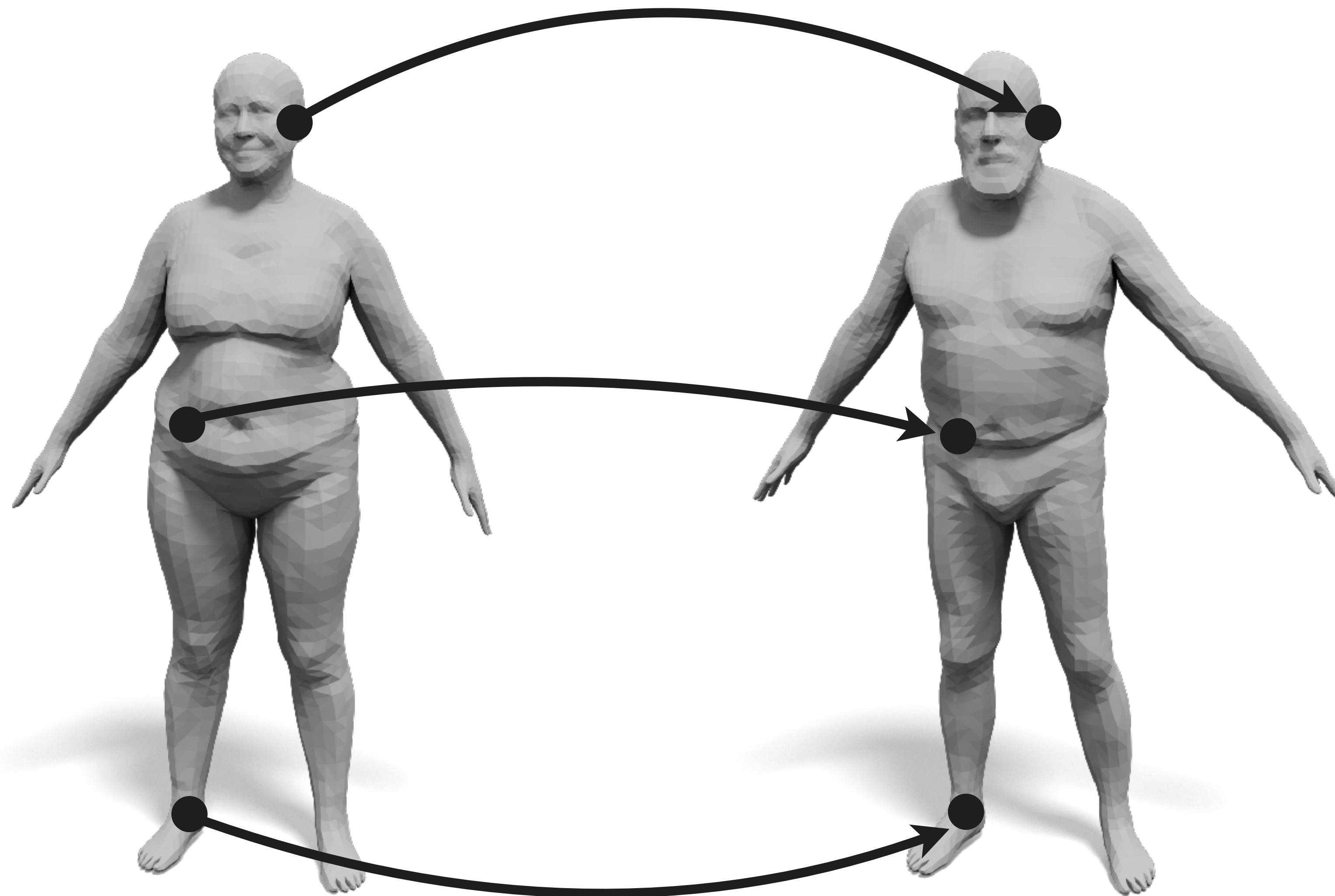


ML as Feature Extractors

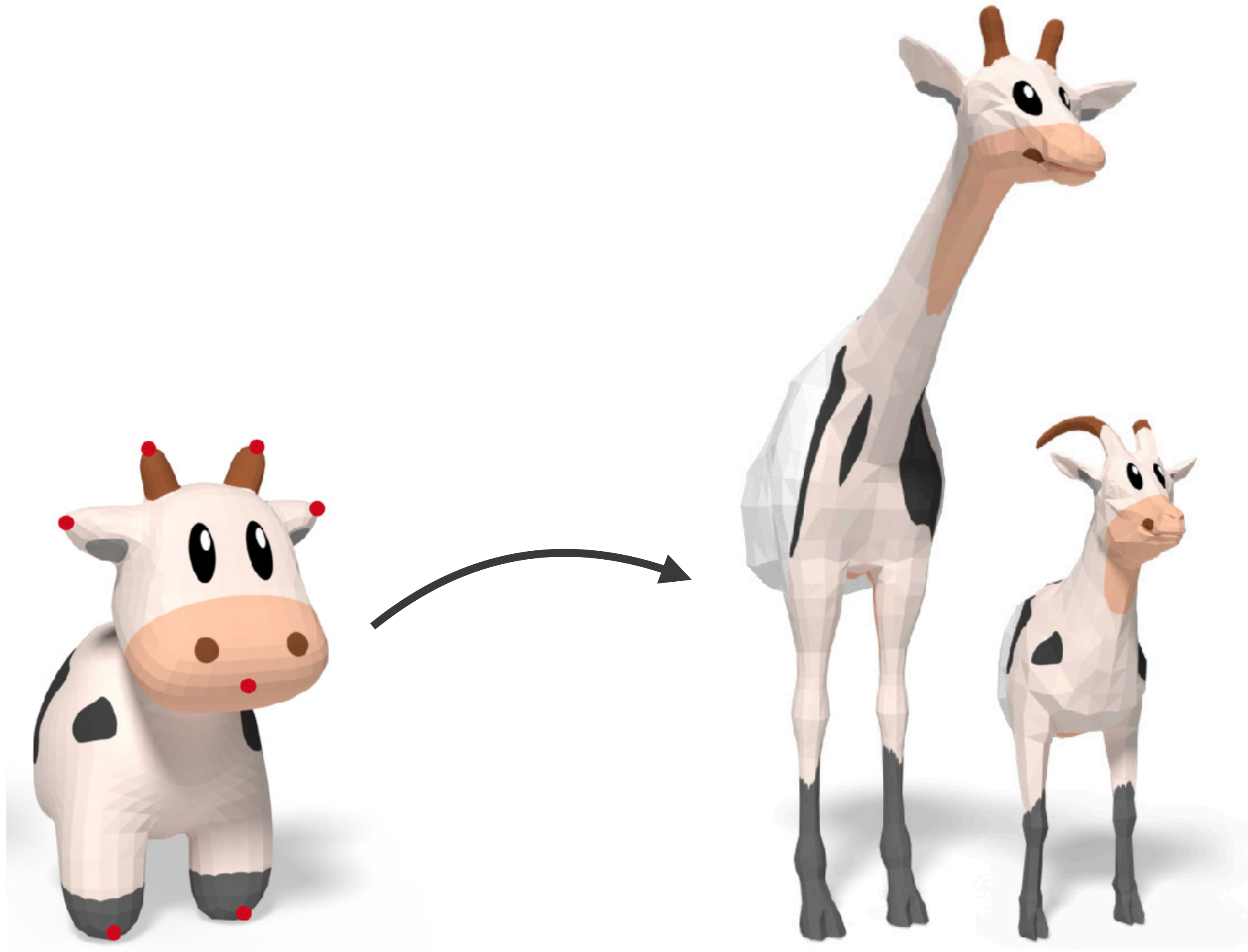


Applications of learned feature extractors
— combined with classic methods —

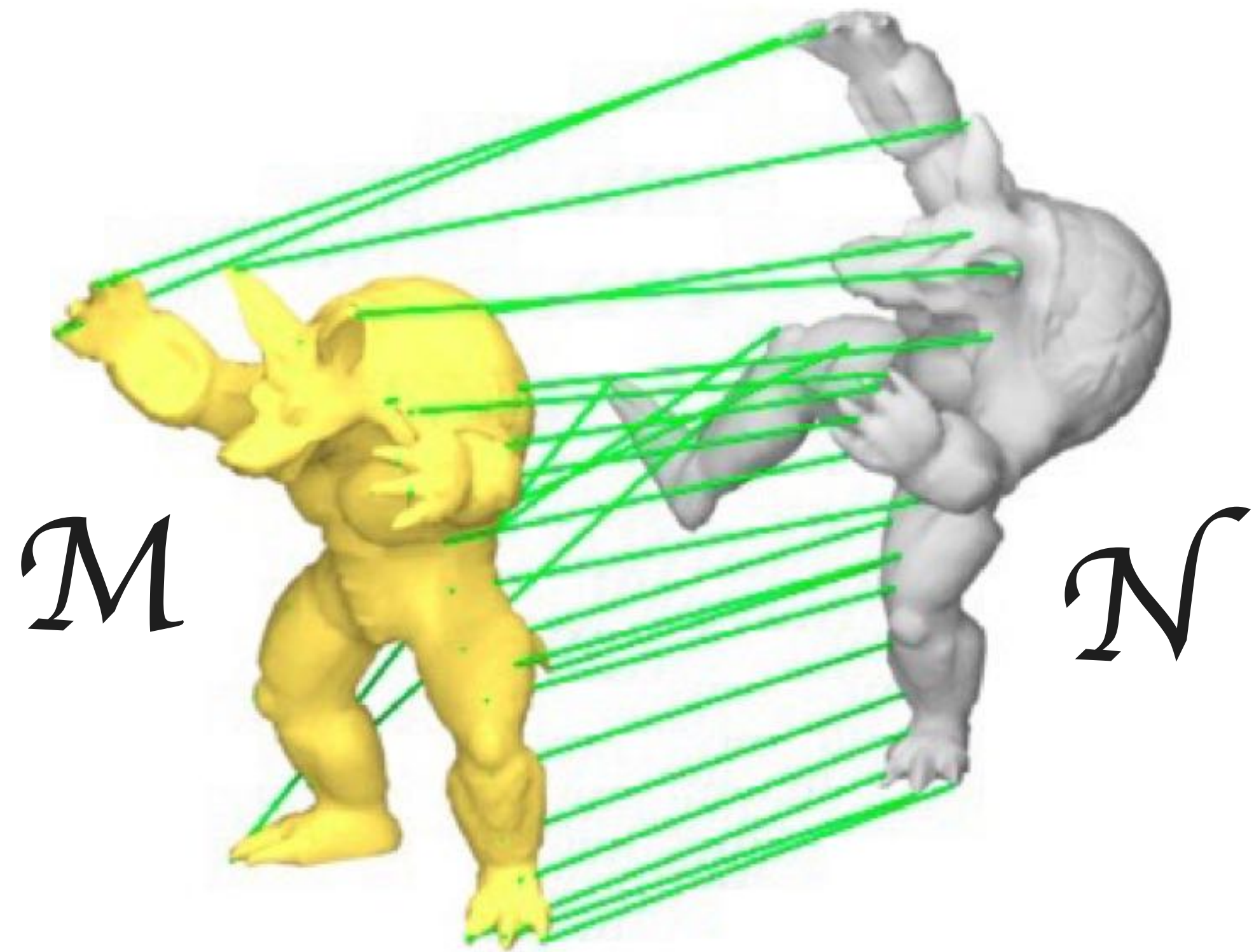
Example: Shape Matching



Texture Transfer

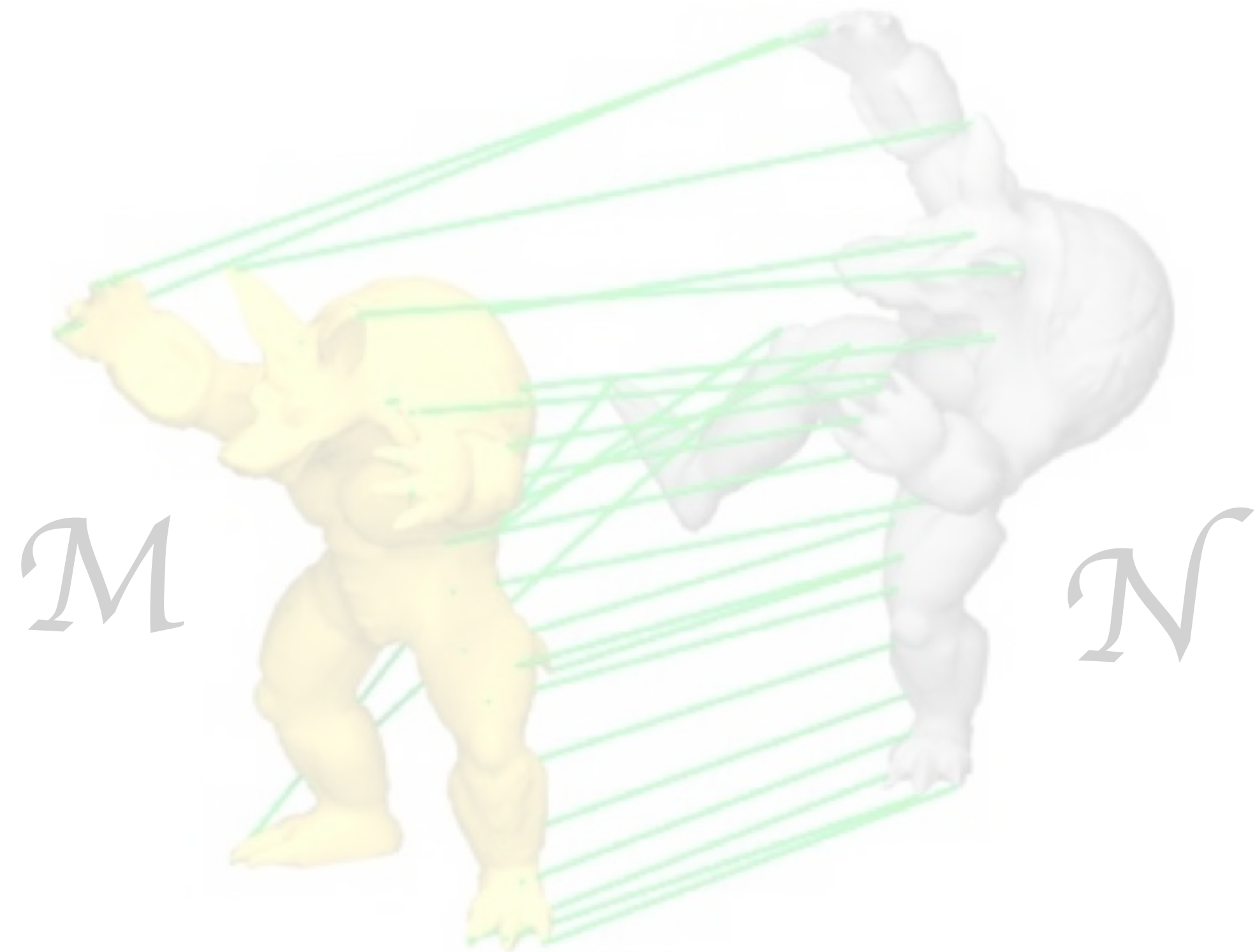


Point Maps



a point on \mathcal{M} \longrightarrow a point on \mathcal{N}

Functional Maps

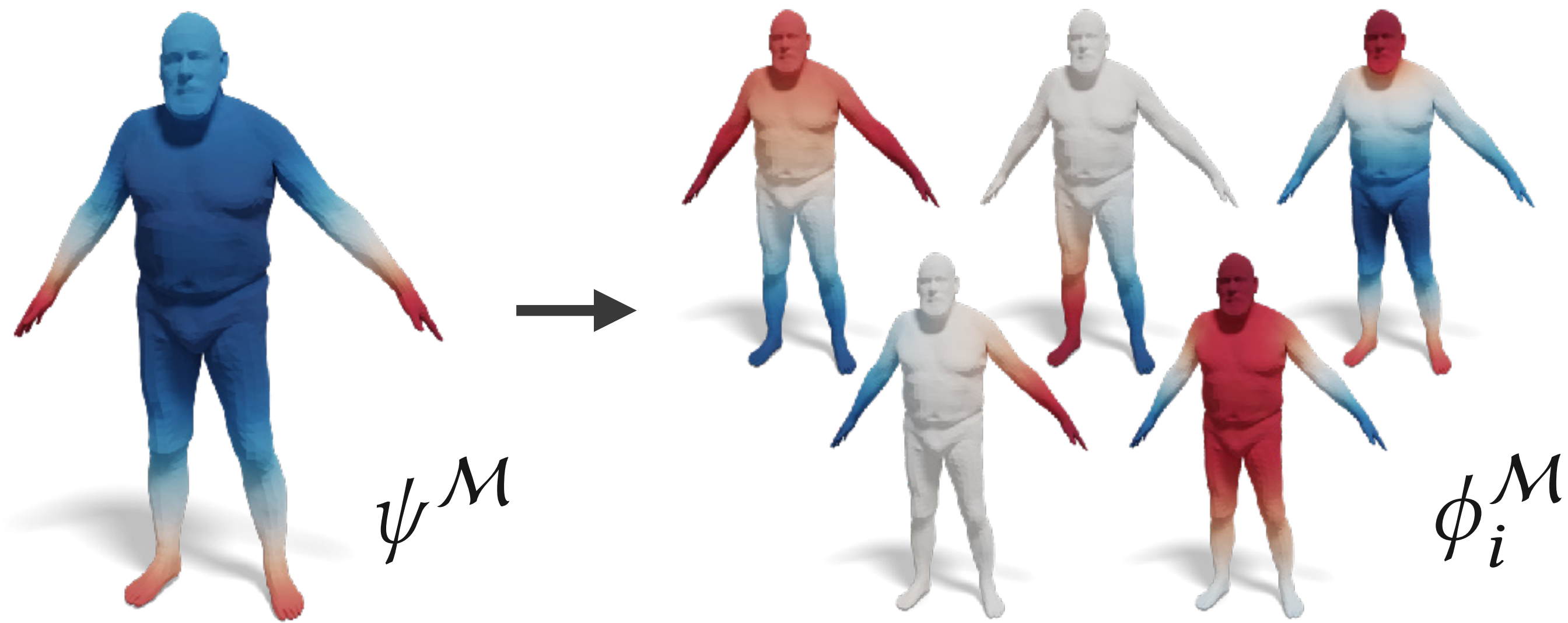


a point on \mathcal{M} \longrightarrow a point on \mathcal{N}

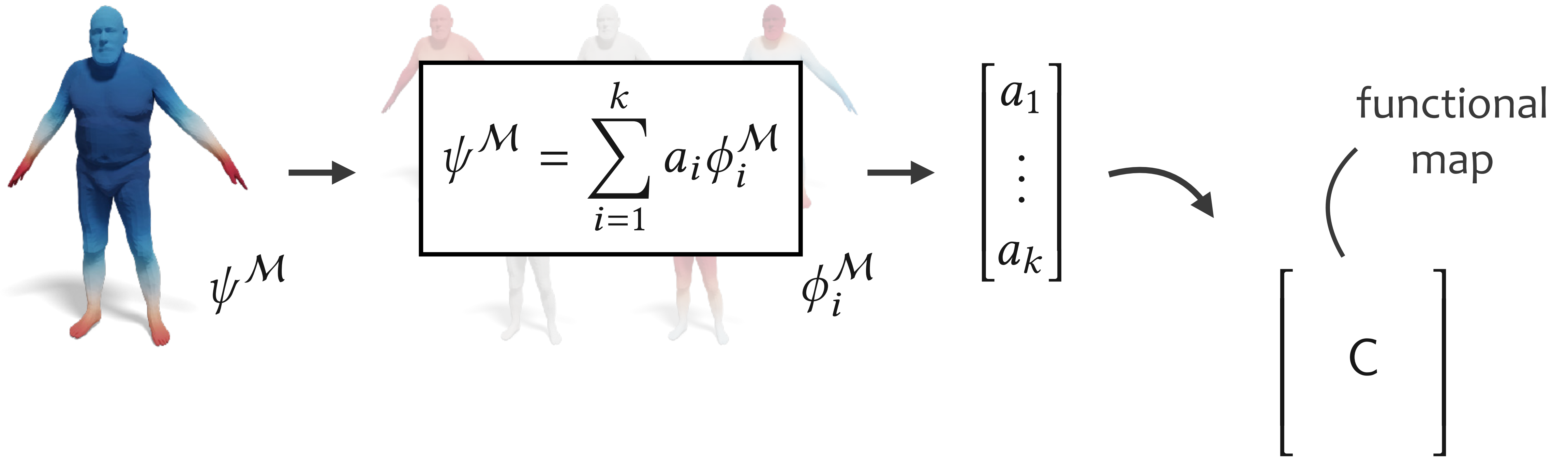


a function on \mathcal{M} \longrightarrow a function on \mathcal{N}

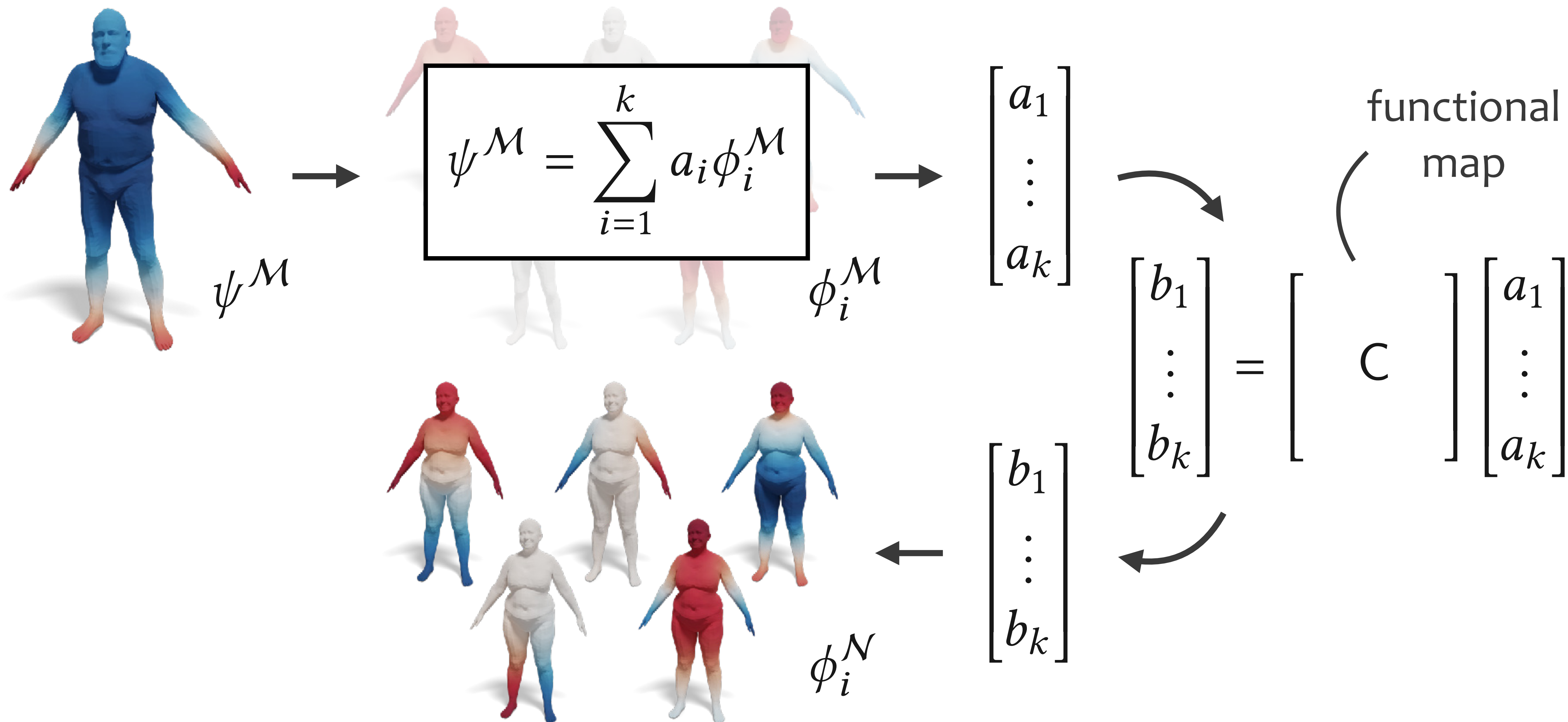
Functional Maps Overview



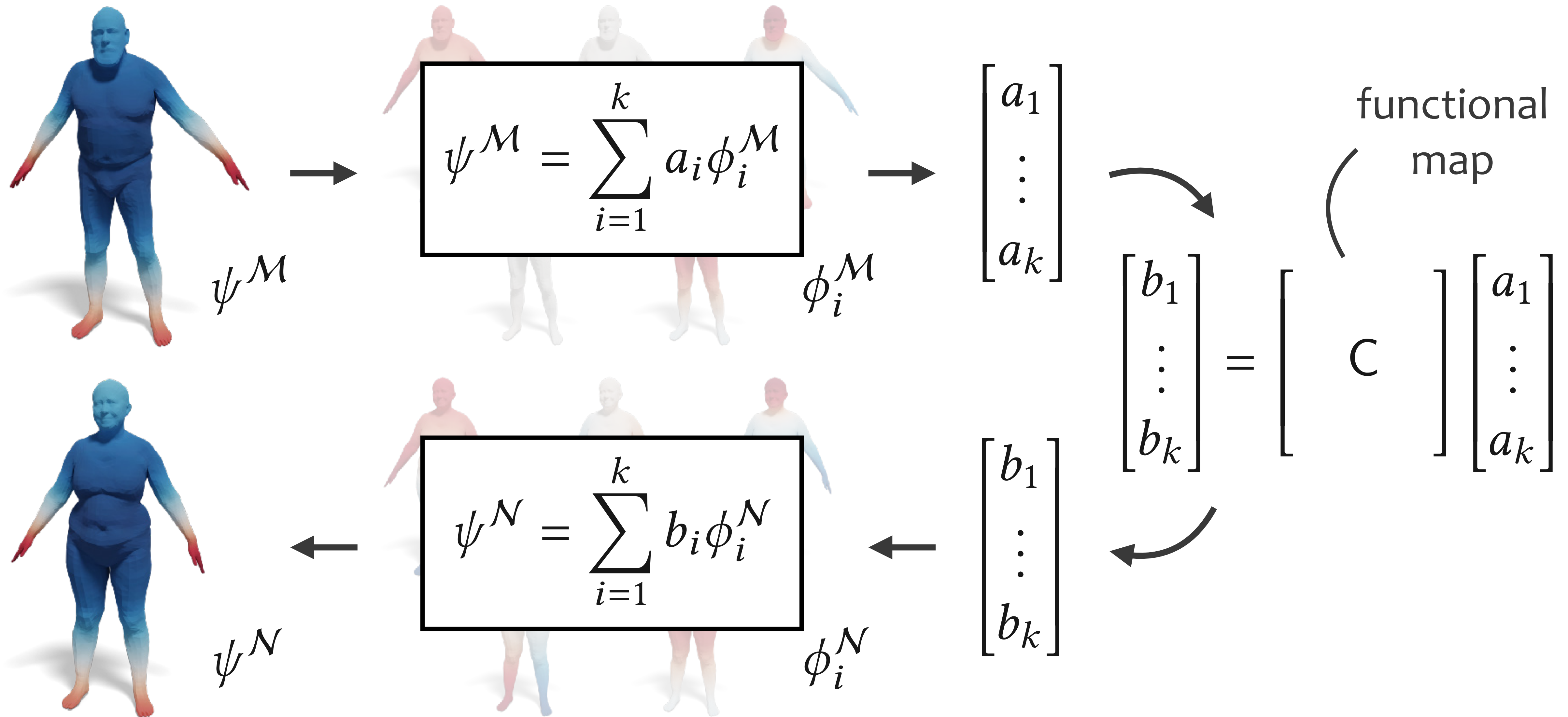
Functional Maps Overview



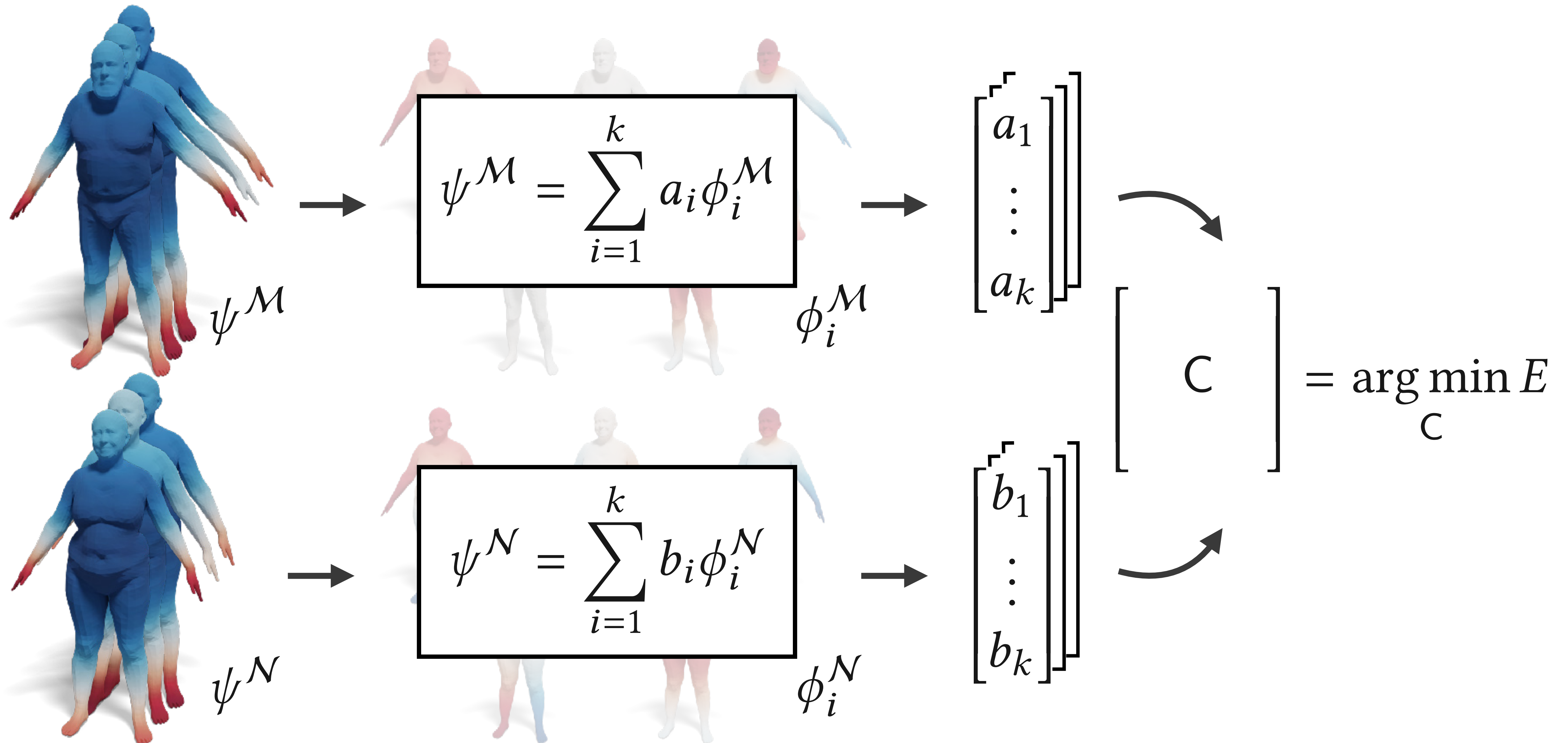
Functional Maps Overview



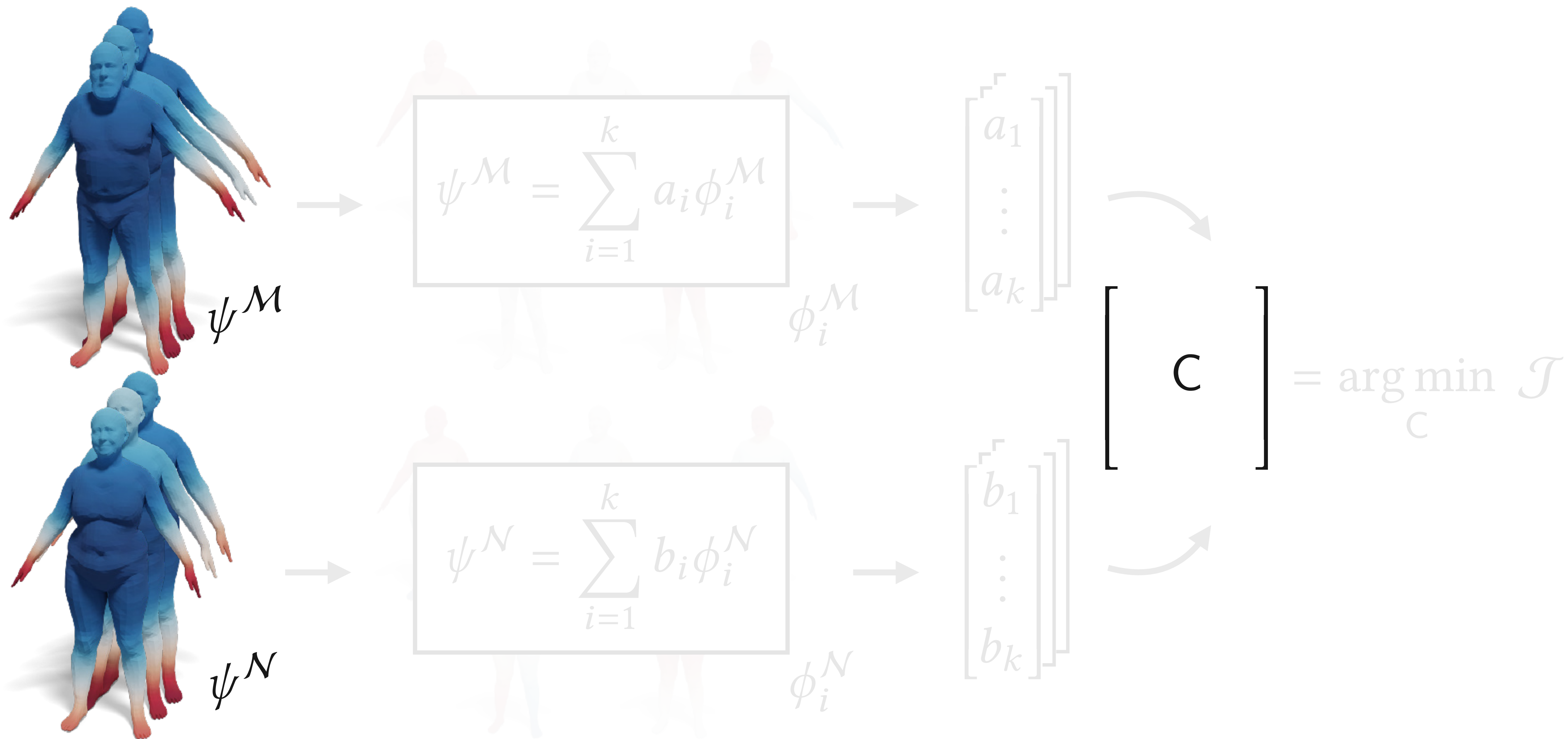
Functional Maps Overview



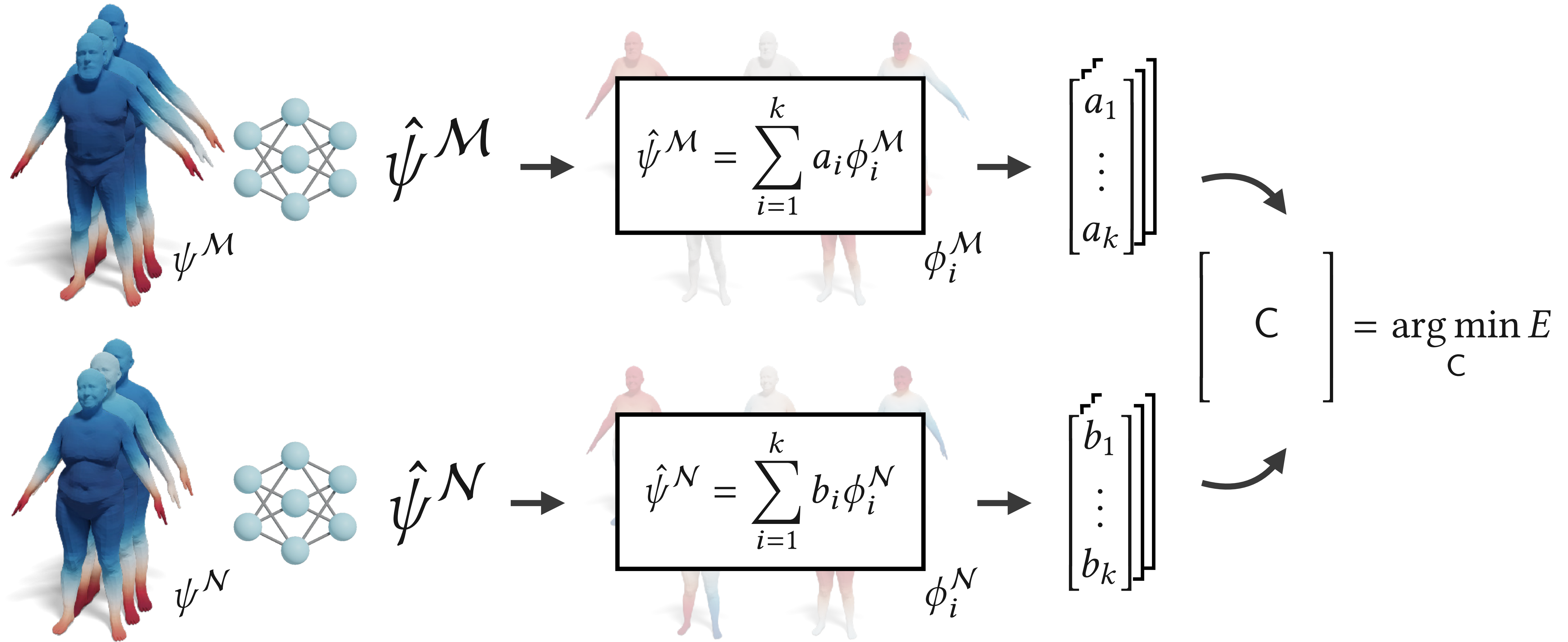
Computing Functional Maps



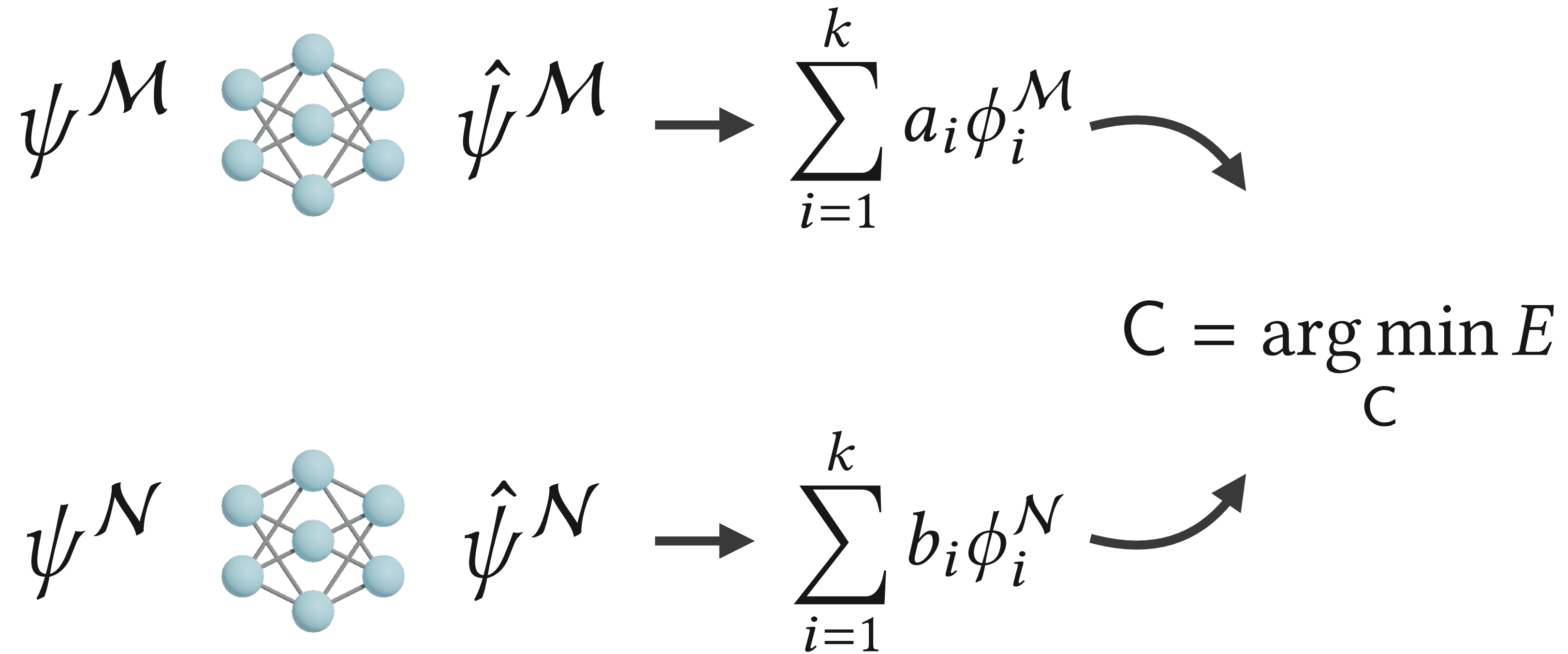
Computing Functional Maps



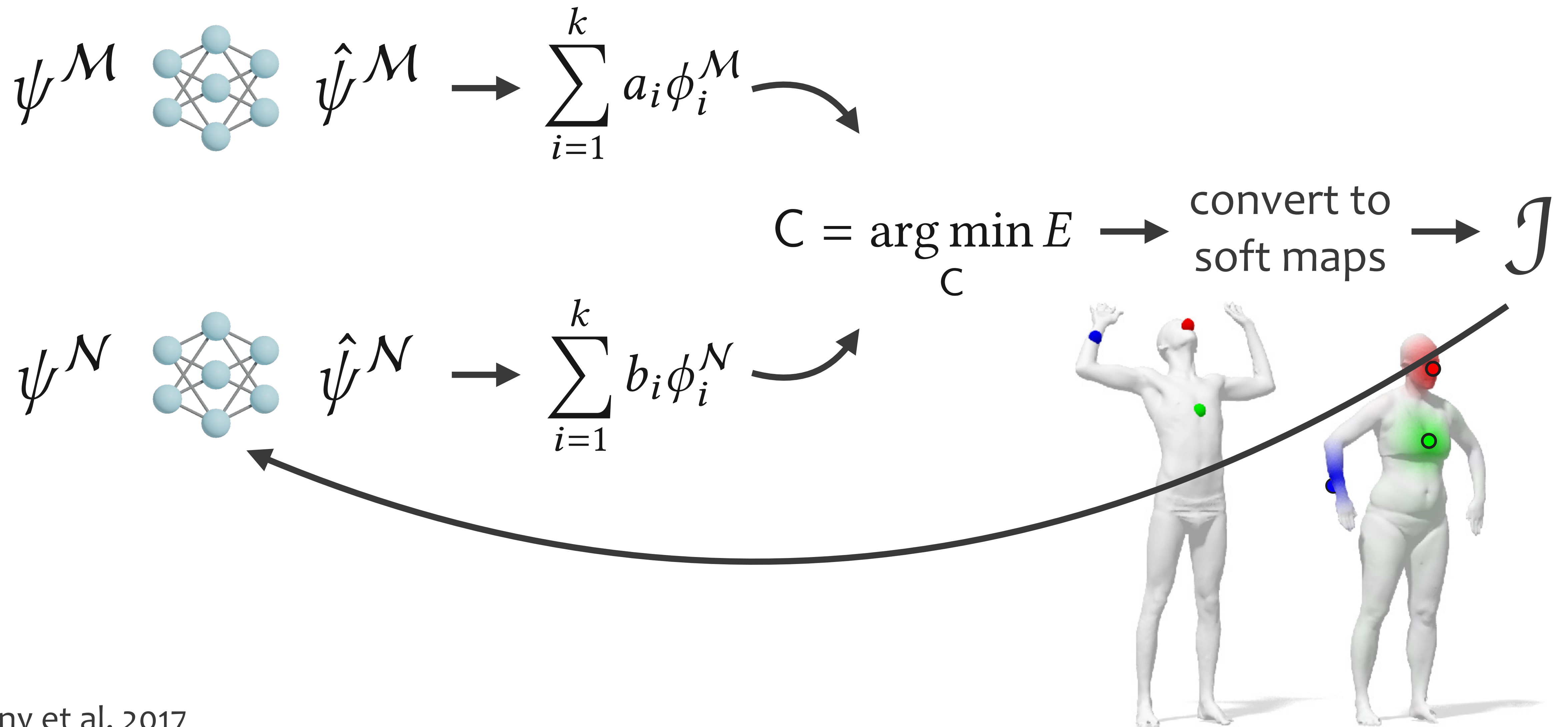
Deep Functional Maps



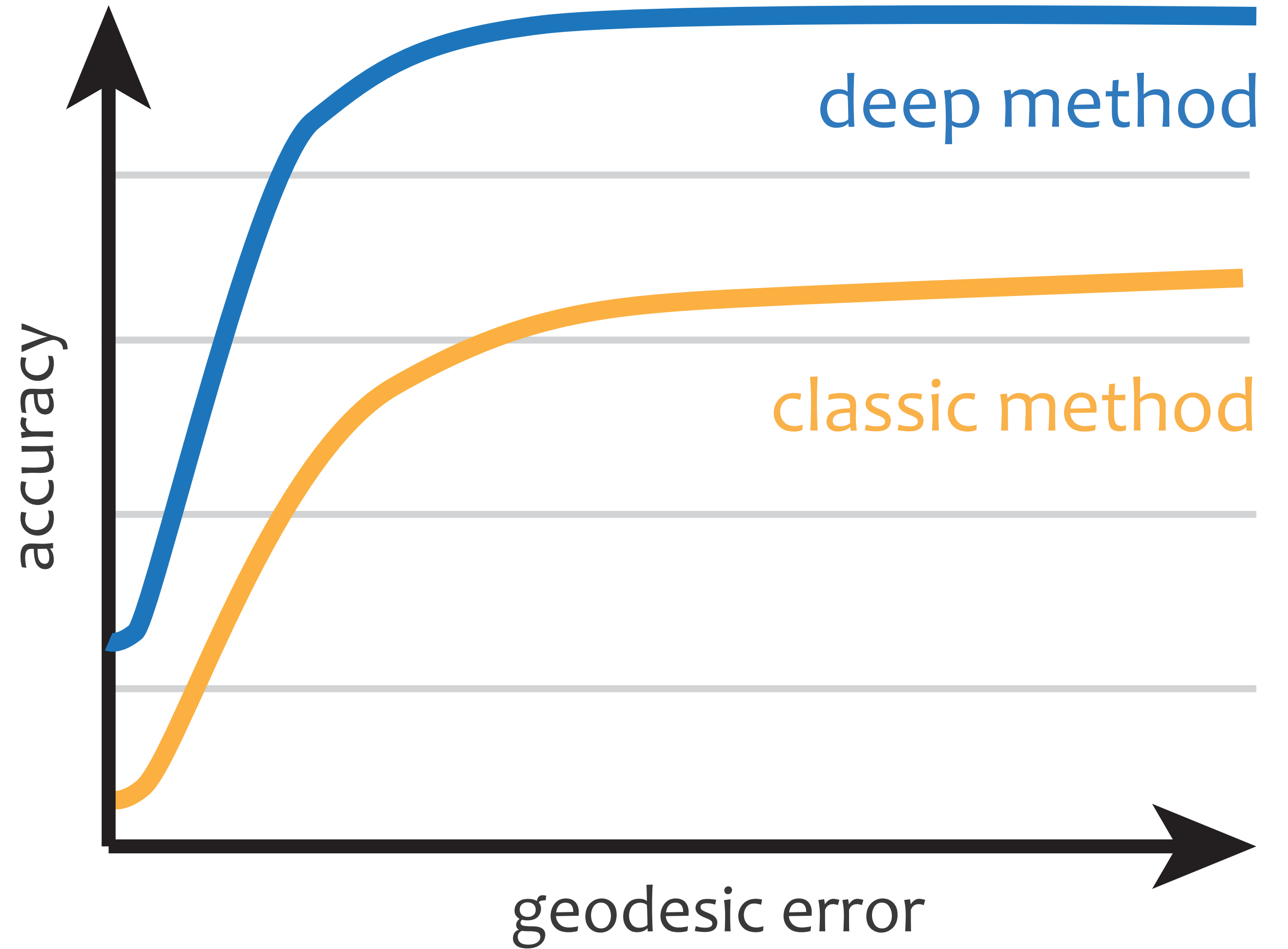
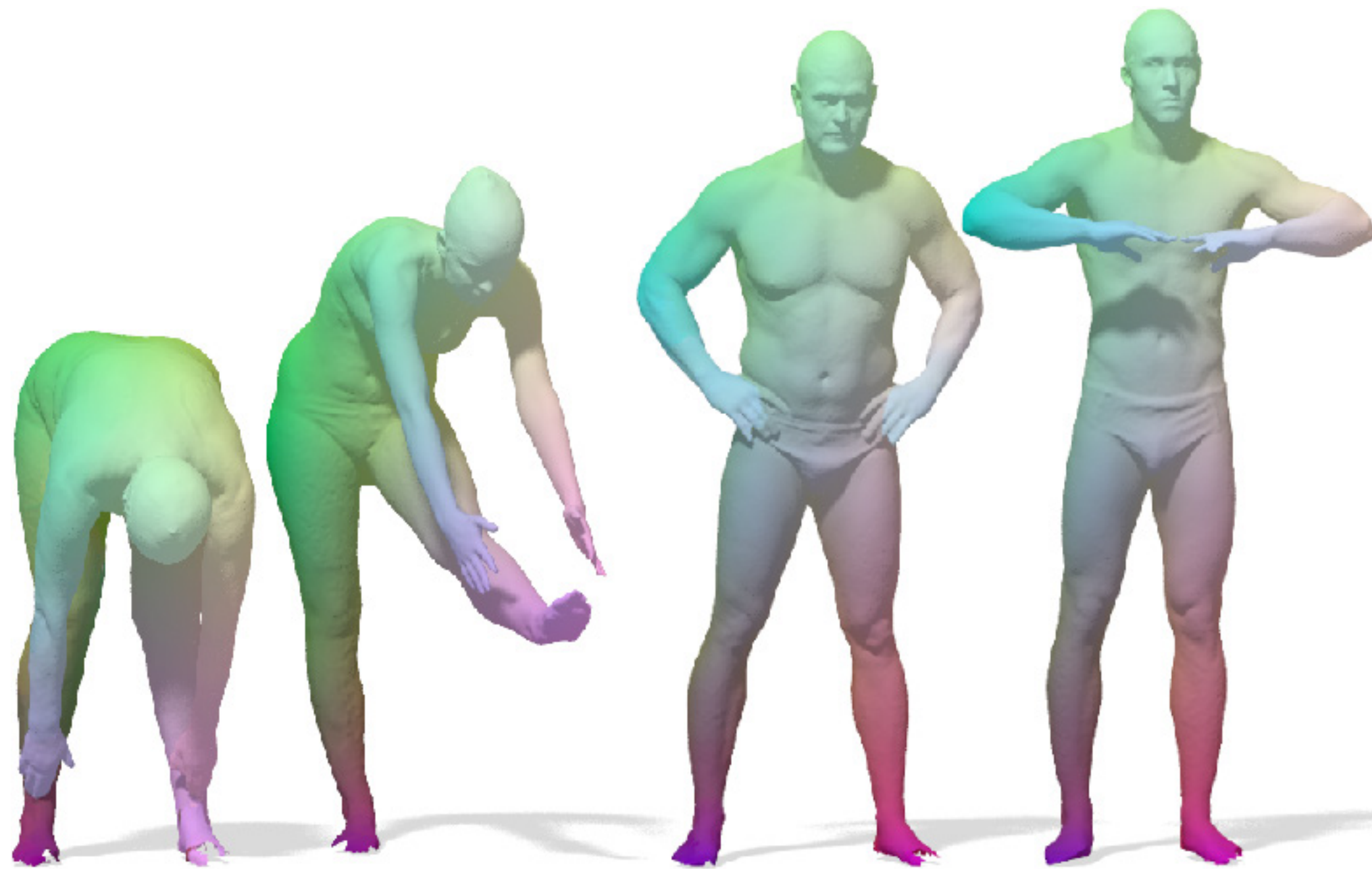
Deep Functional Maps



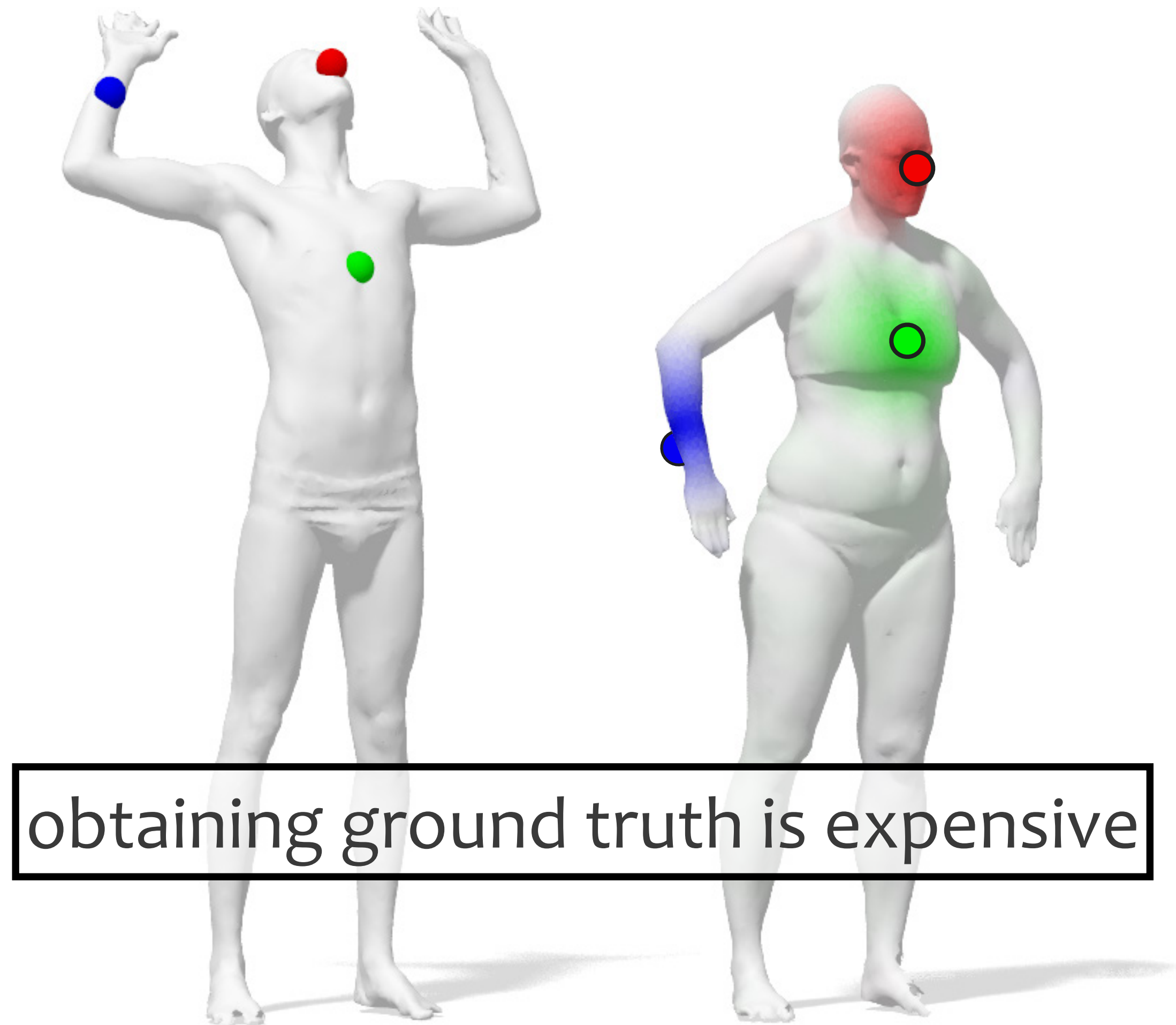
Deep Functional Maps



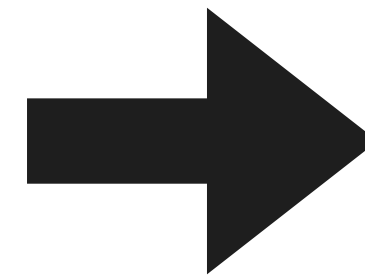
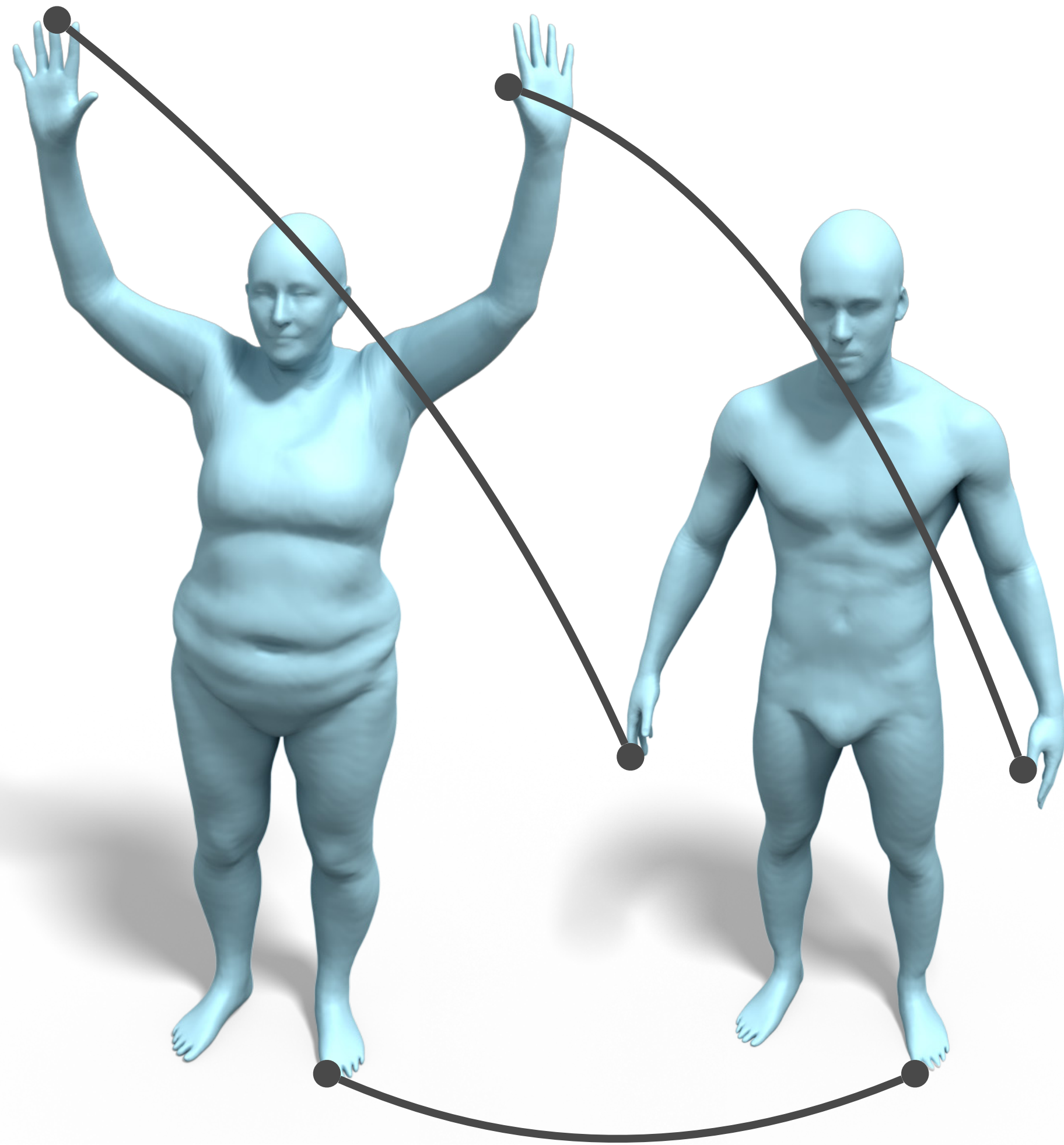
Push the limits



Requires Supervision



Classic Approaches

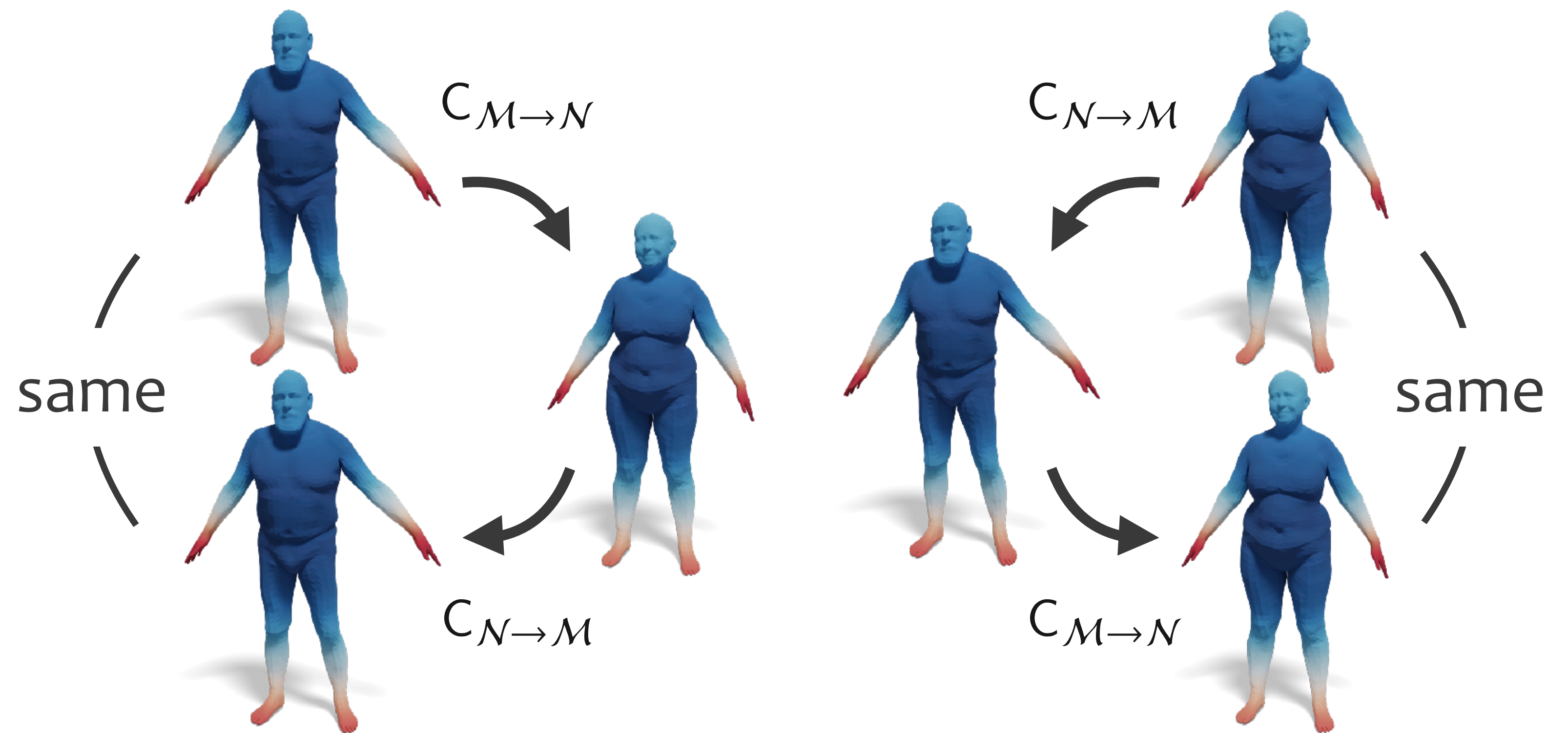


$$\arg \min_{\mathbf{C}} \mathcal{E}(\mathbf{C})$$

$$\mathcal{E}(\mathbf{C}) = \alpha_1 E_1(\mathbf{C}) + \alpha_2 E_2(\mathbf{C}) \\ + \alpha_3 E_3(\mathbf{C}) + \alpha_4 E_4(\mathbf{C})$$

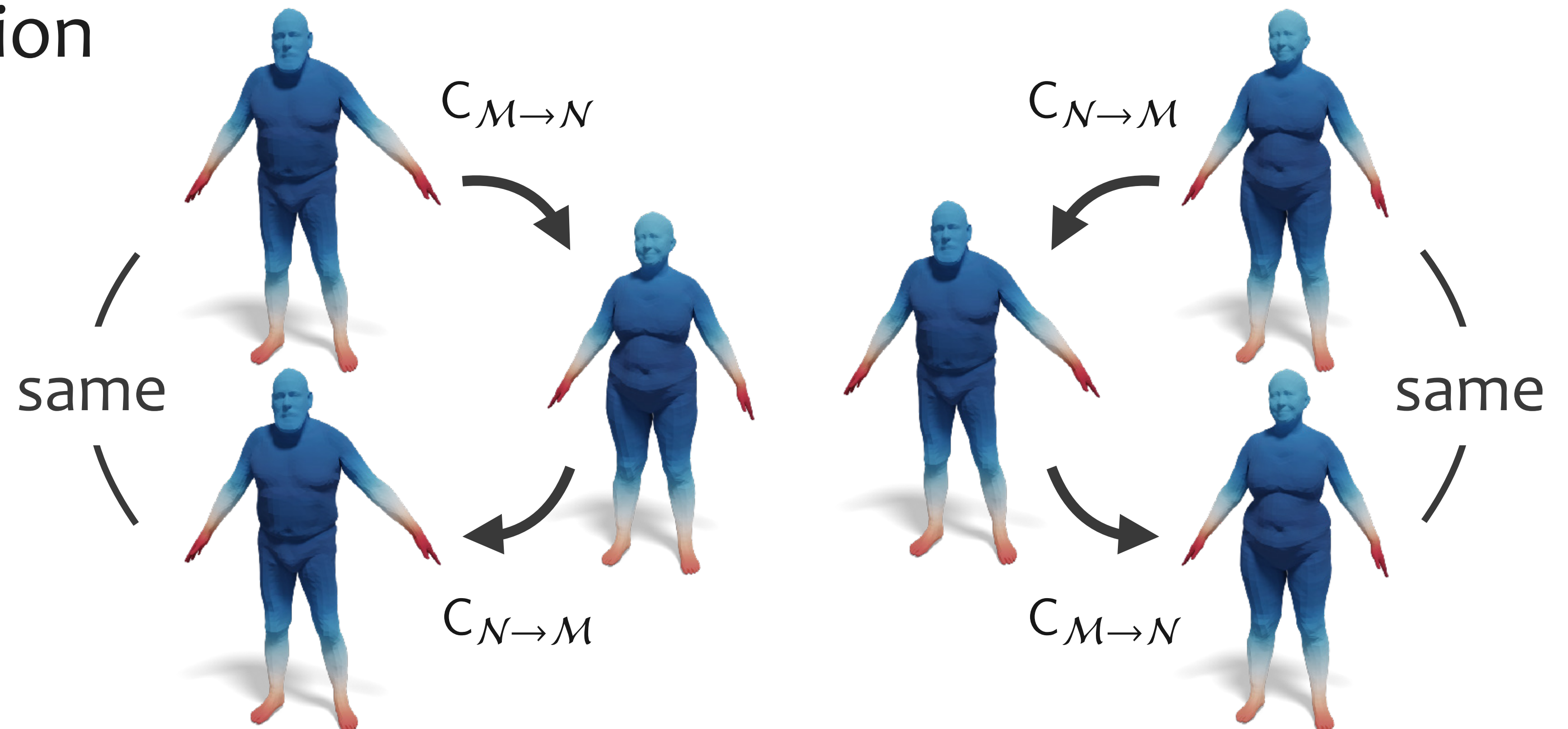
Desired Properties

- Bijectivity

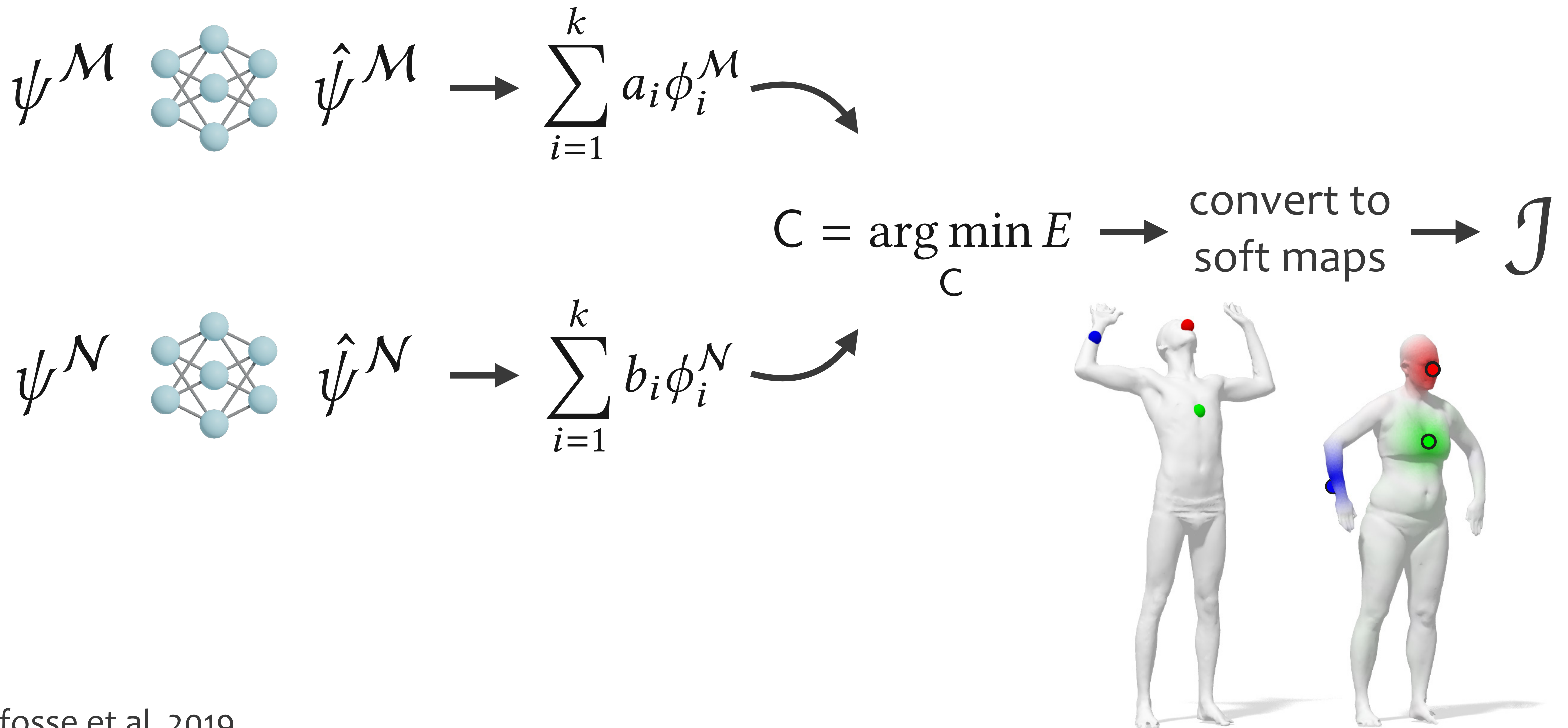


Desired Properties

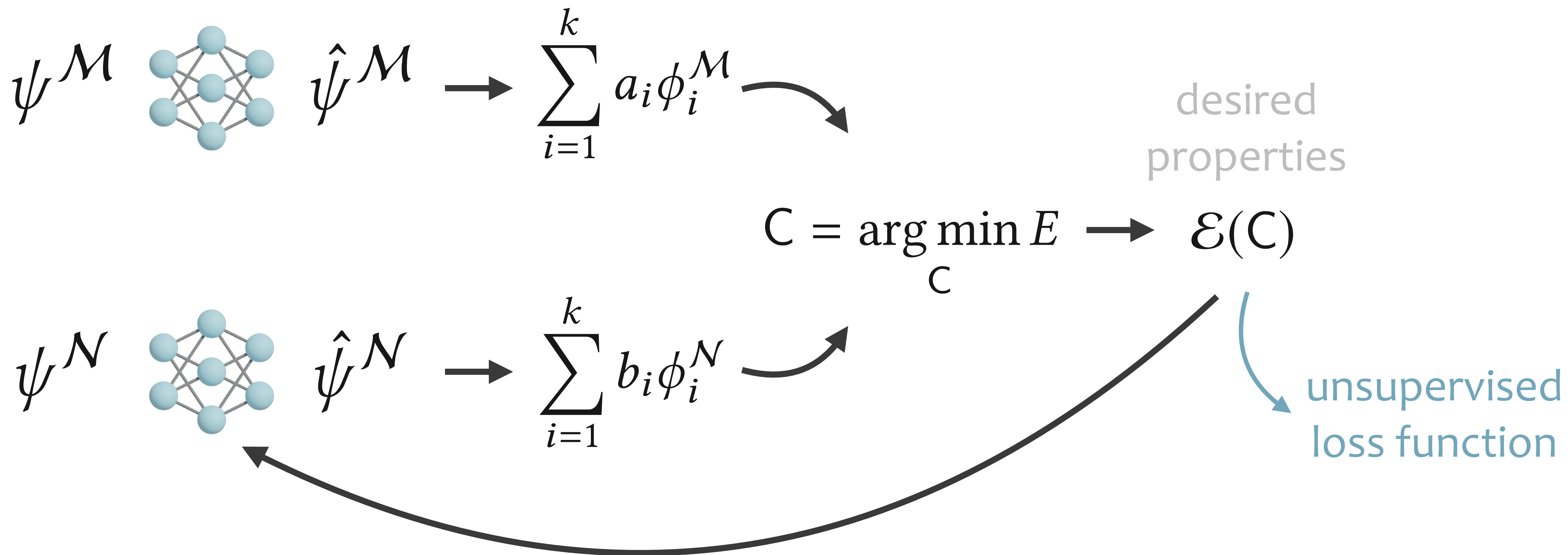
- Bijectivity
- Area preservation
- Laplacian commutativity
- Descriptor preservation
- ...



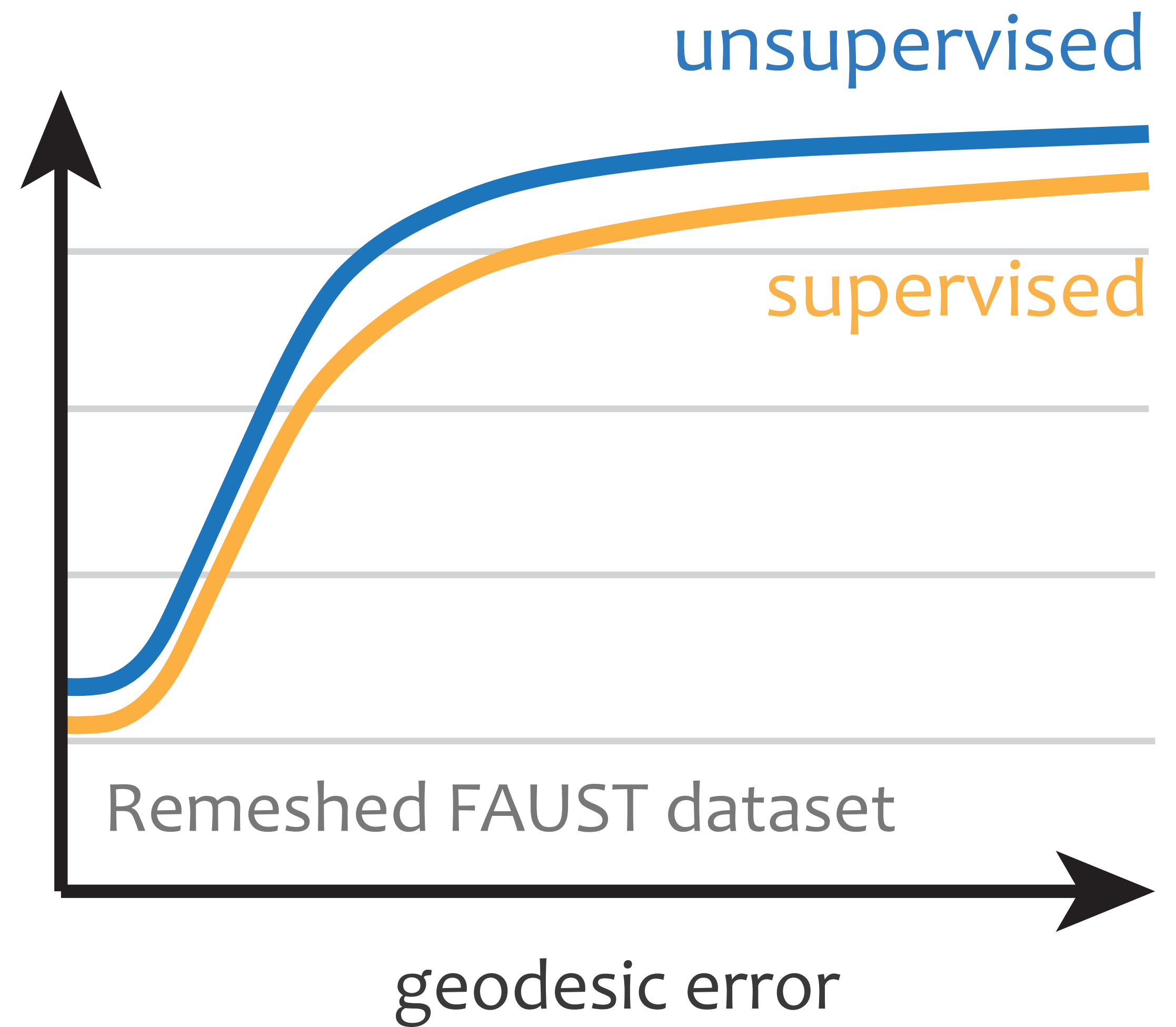
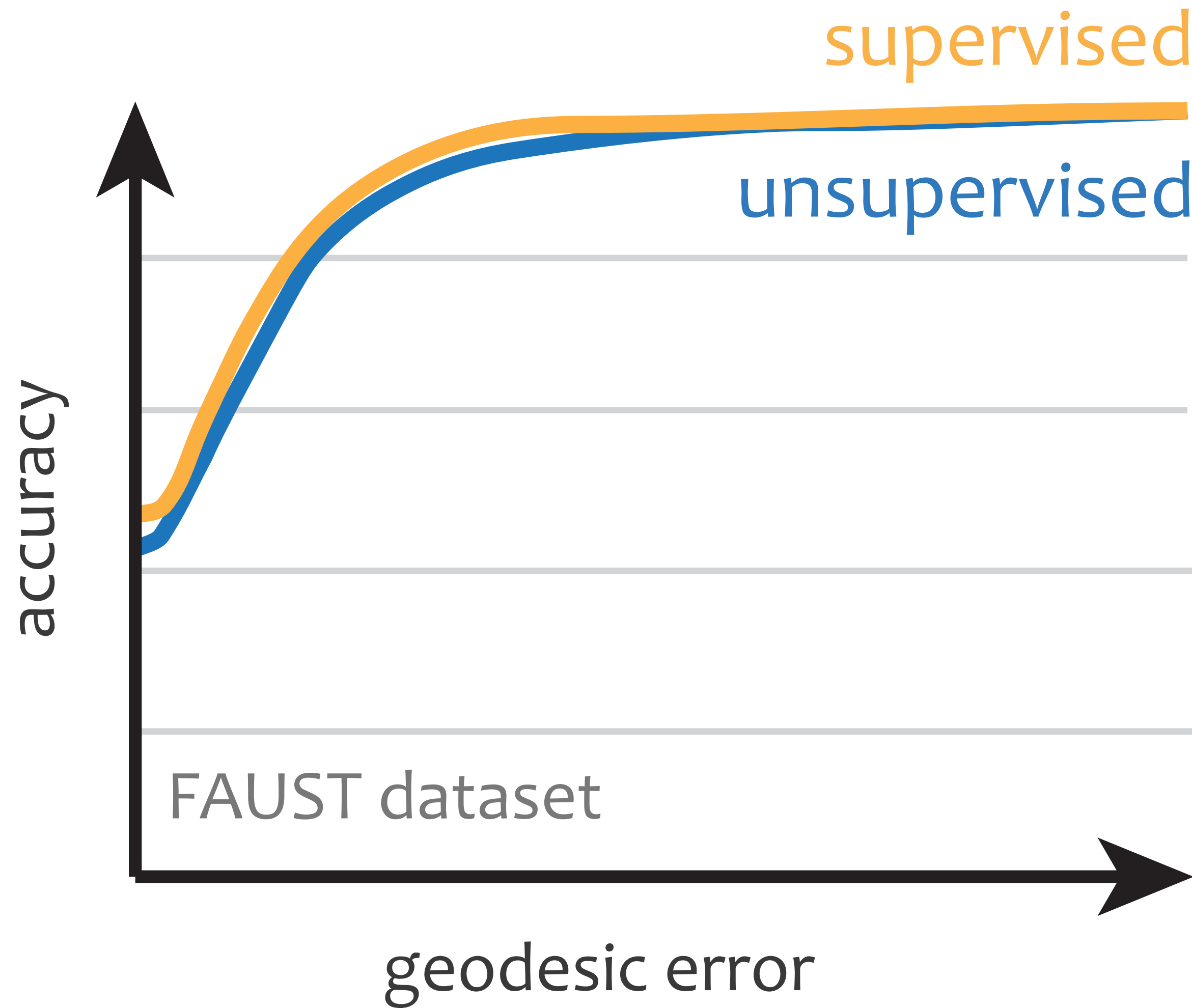
From Supervised to Unsupervised



From Supervised to Unsupervised



Comparable Results



Key Takeaways

good results, but not perfect

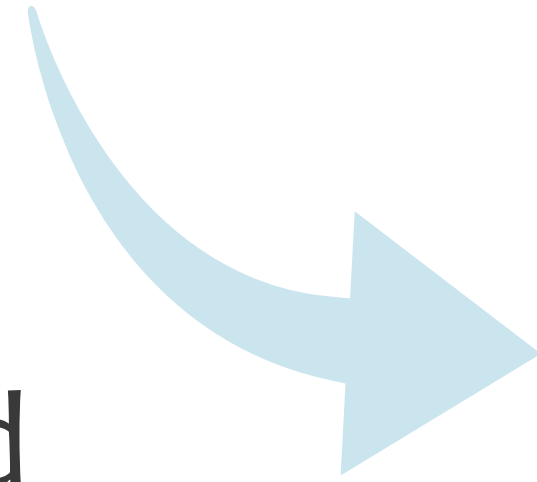
use machine learning



push the limit

require supervision

combine with classic method

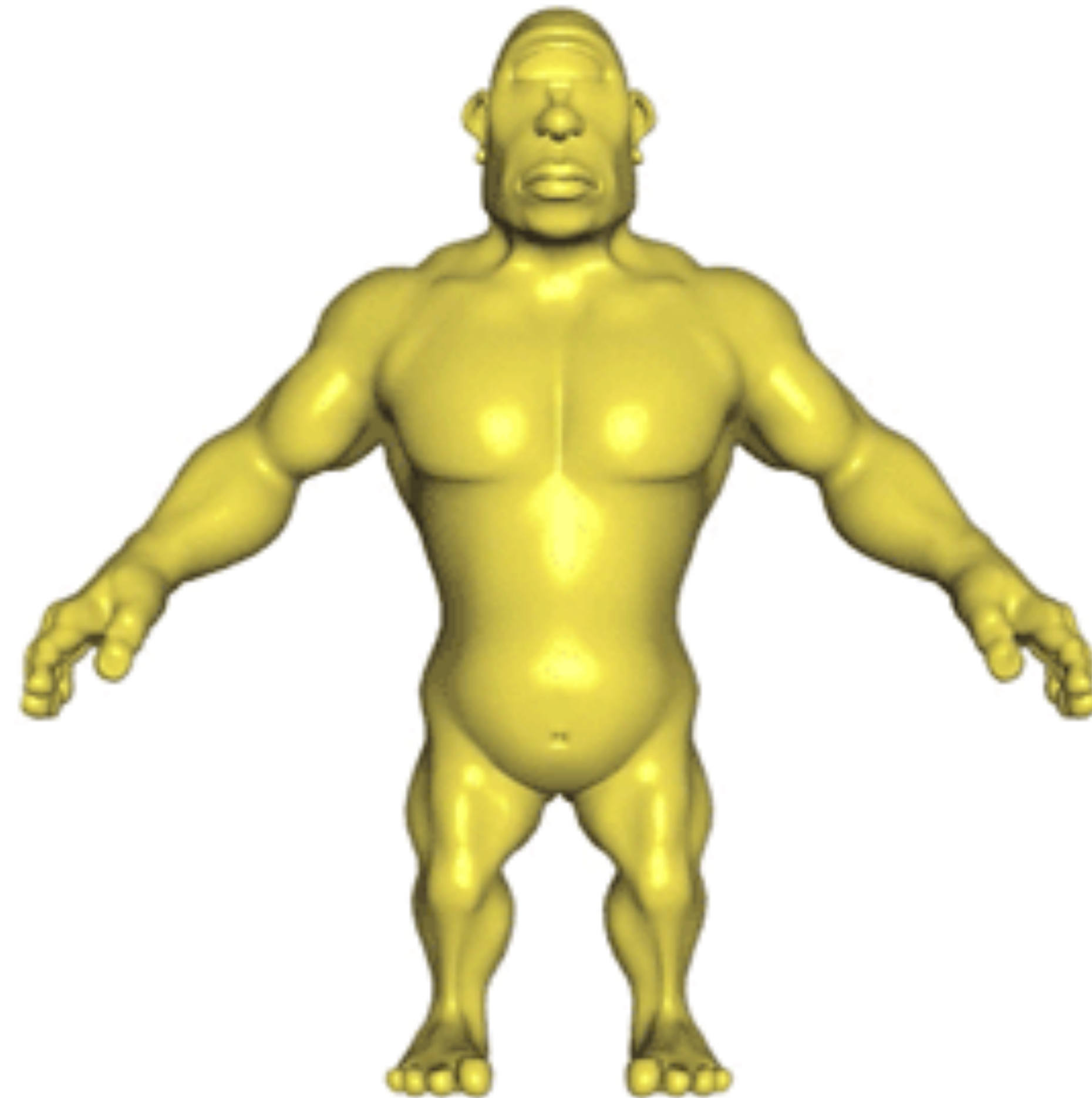


weak/no supervision

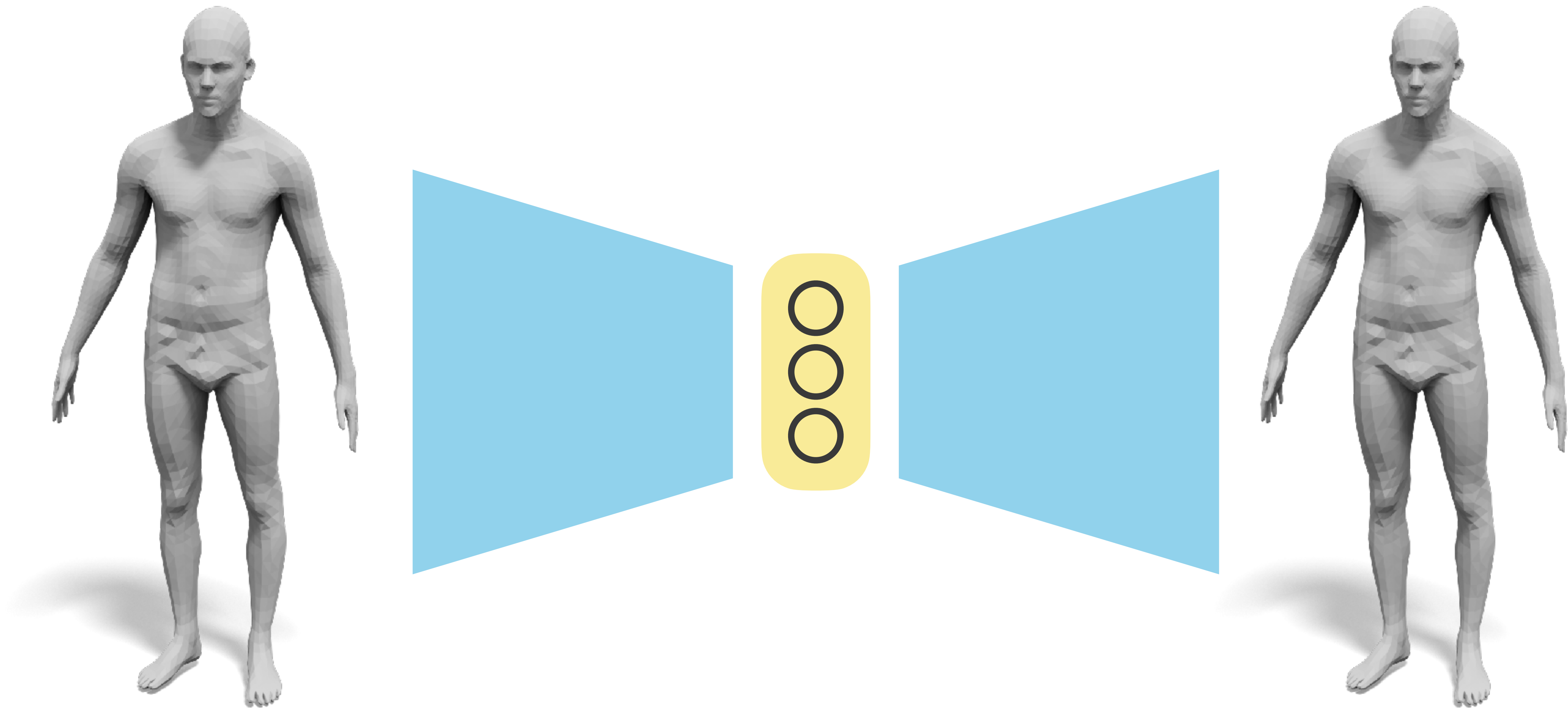
push the limit

open questions

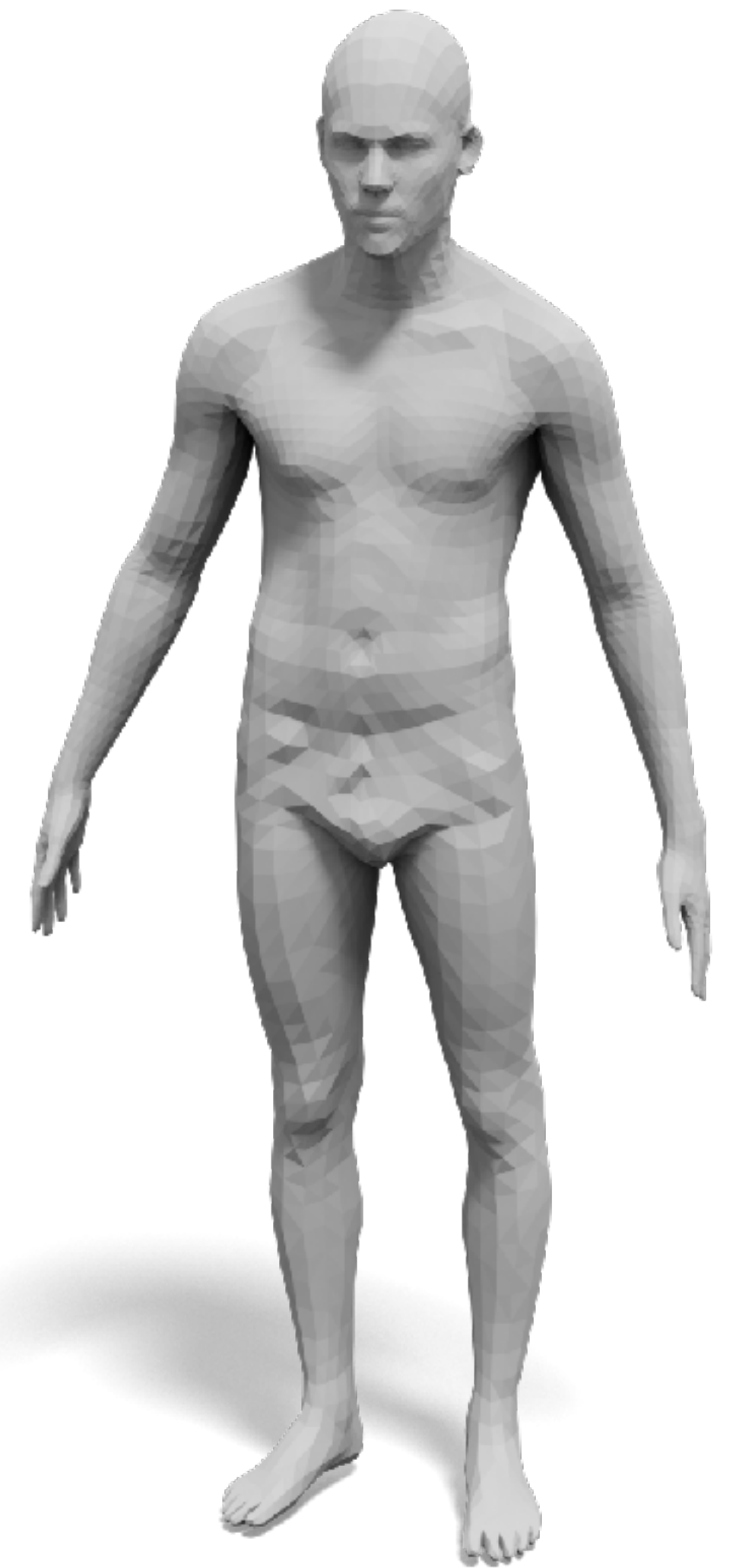
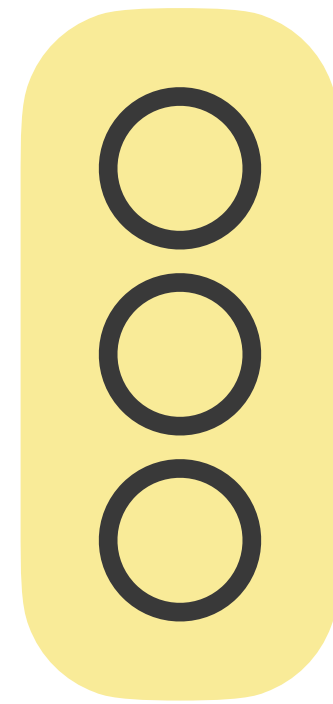
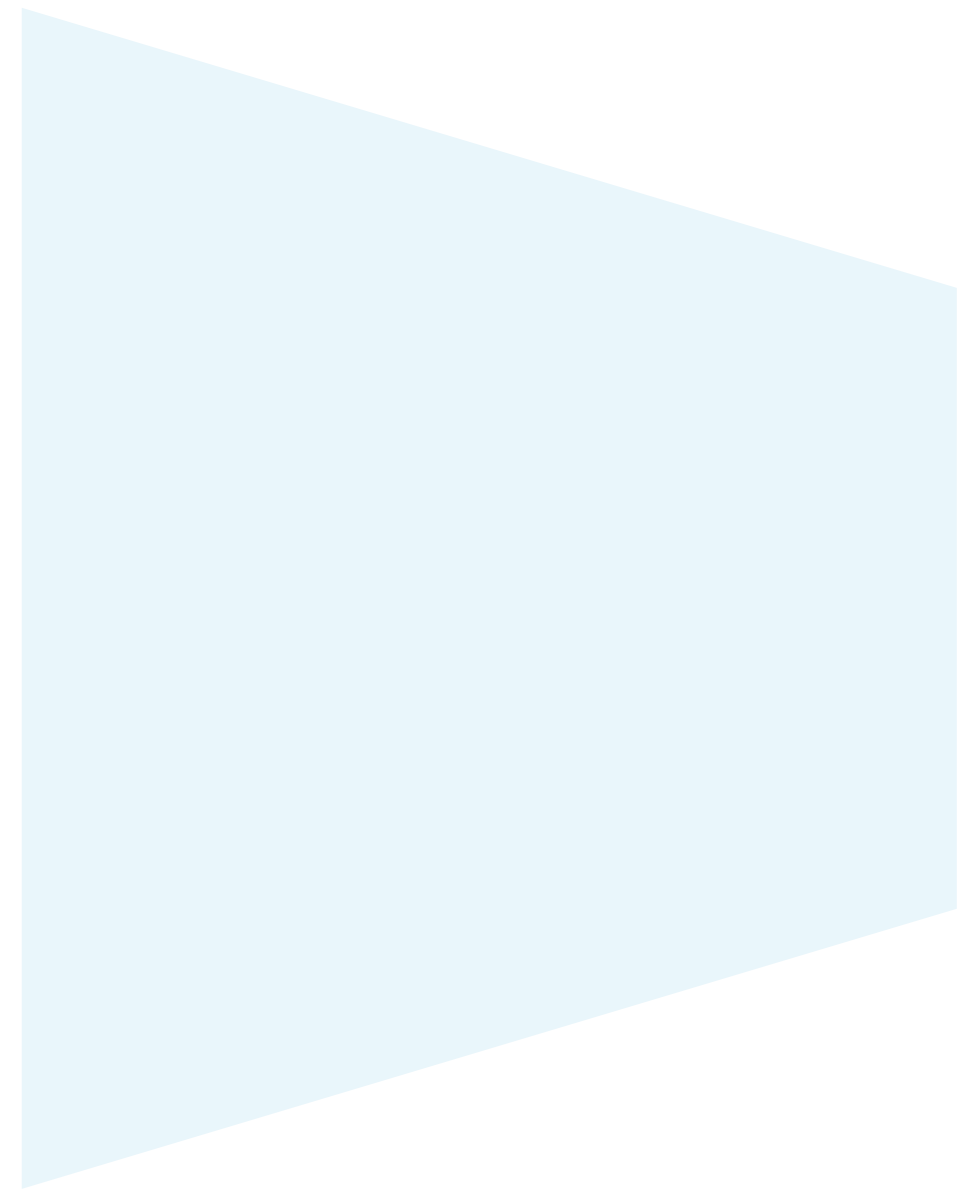
Example: Shape Deformation



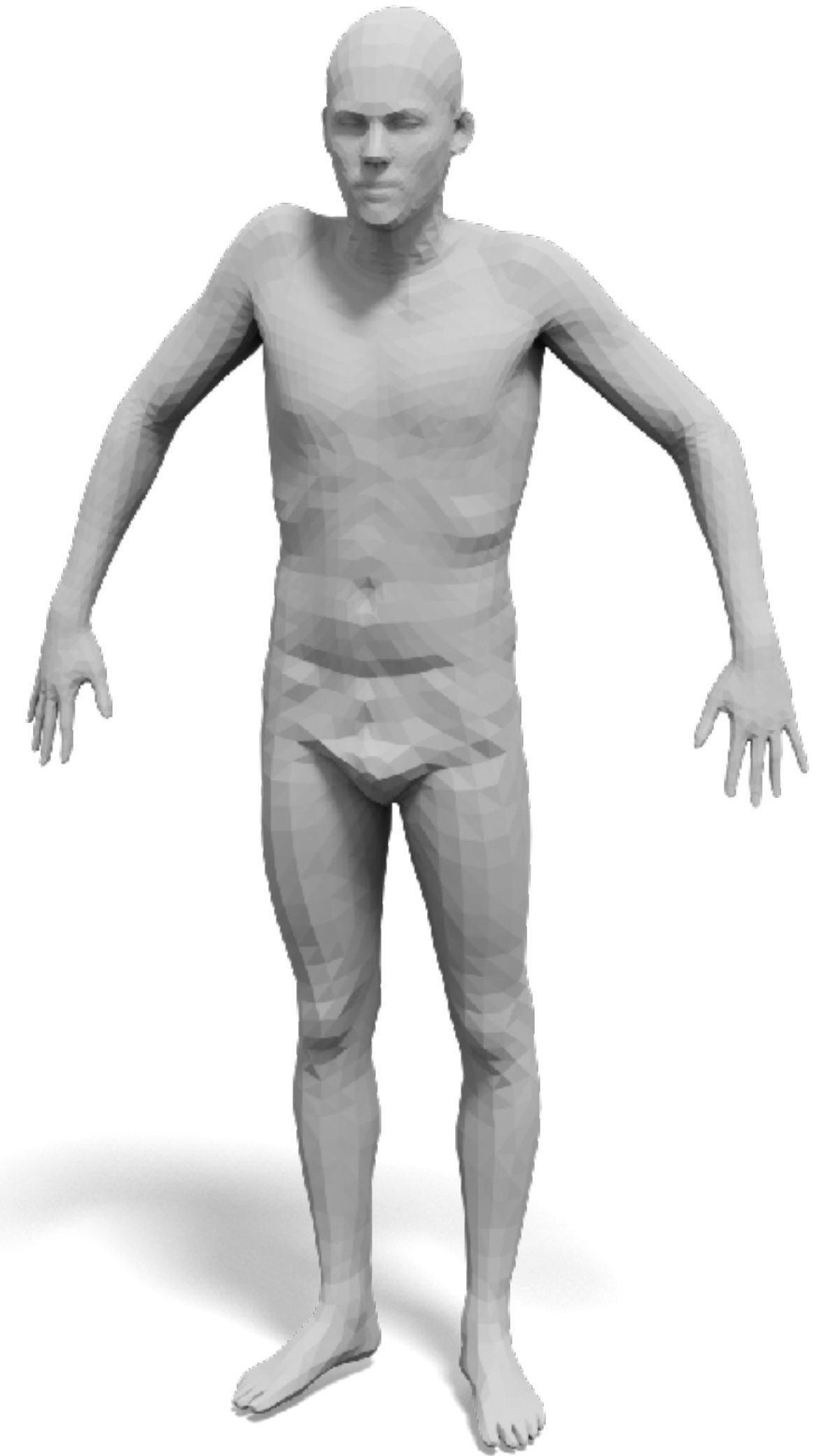
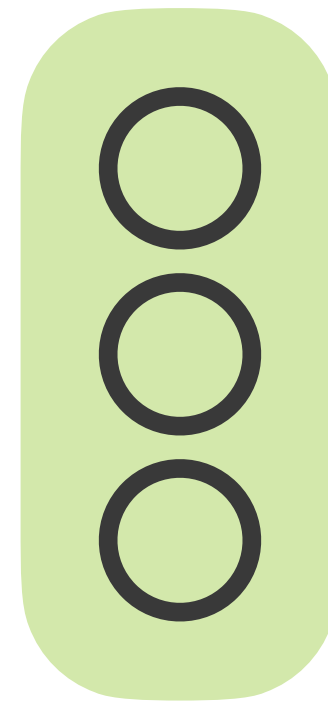
Learning Shape Deformation



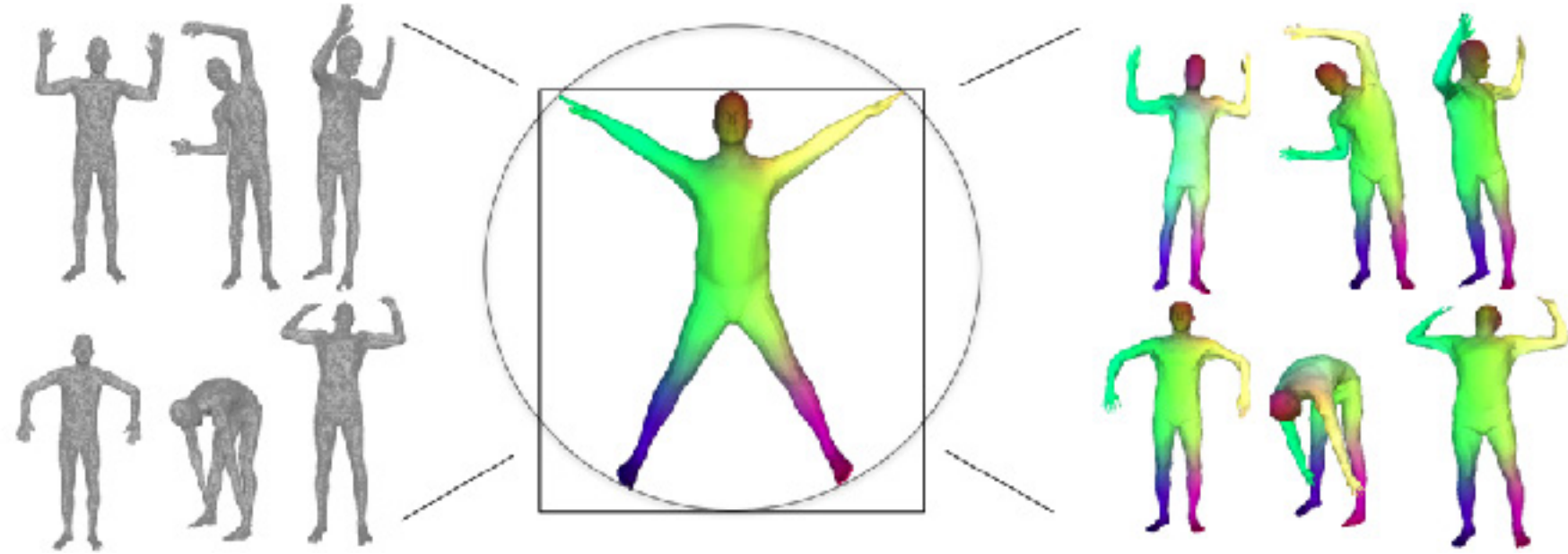
Learning Shape Deformation



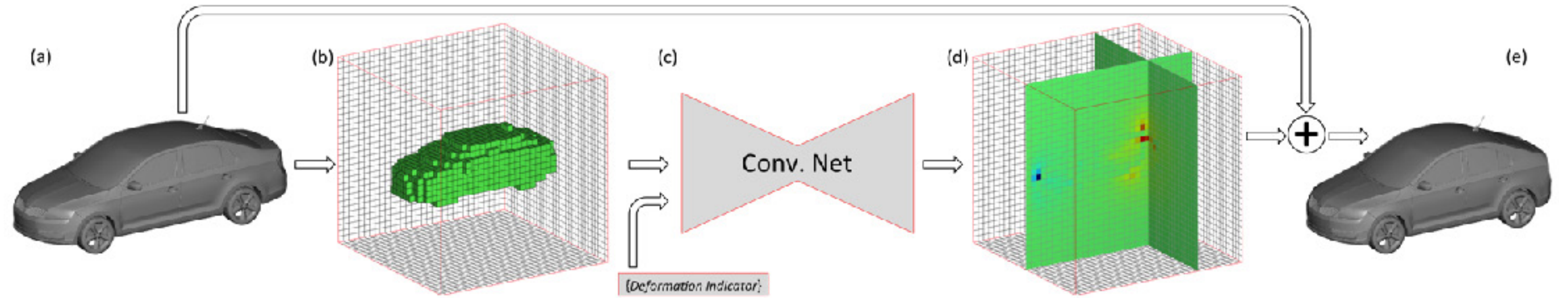
Learning Shape Deformation



Learning Shape Deformation



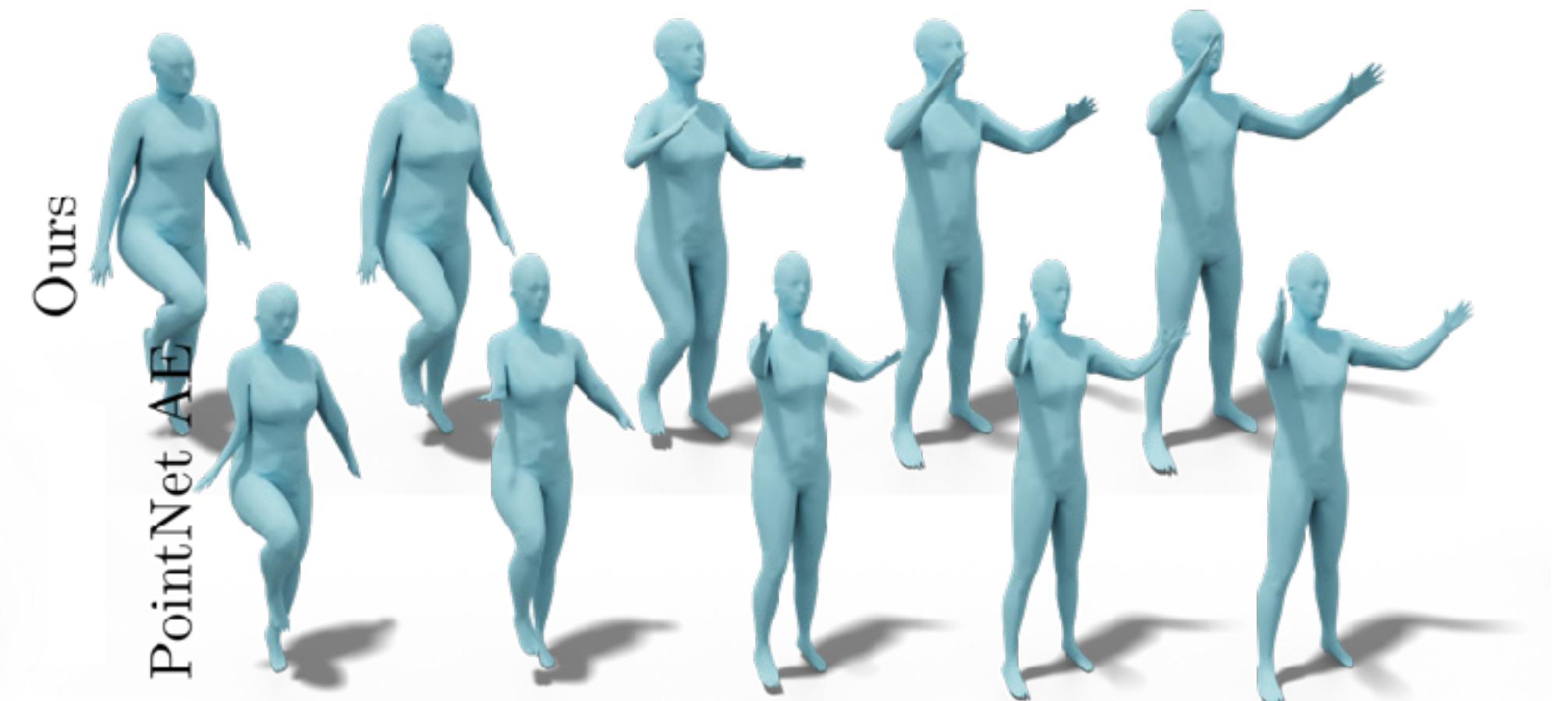
Groueix et al. 2018



Yumer & Mitra 2016

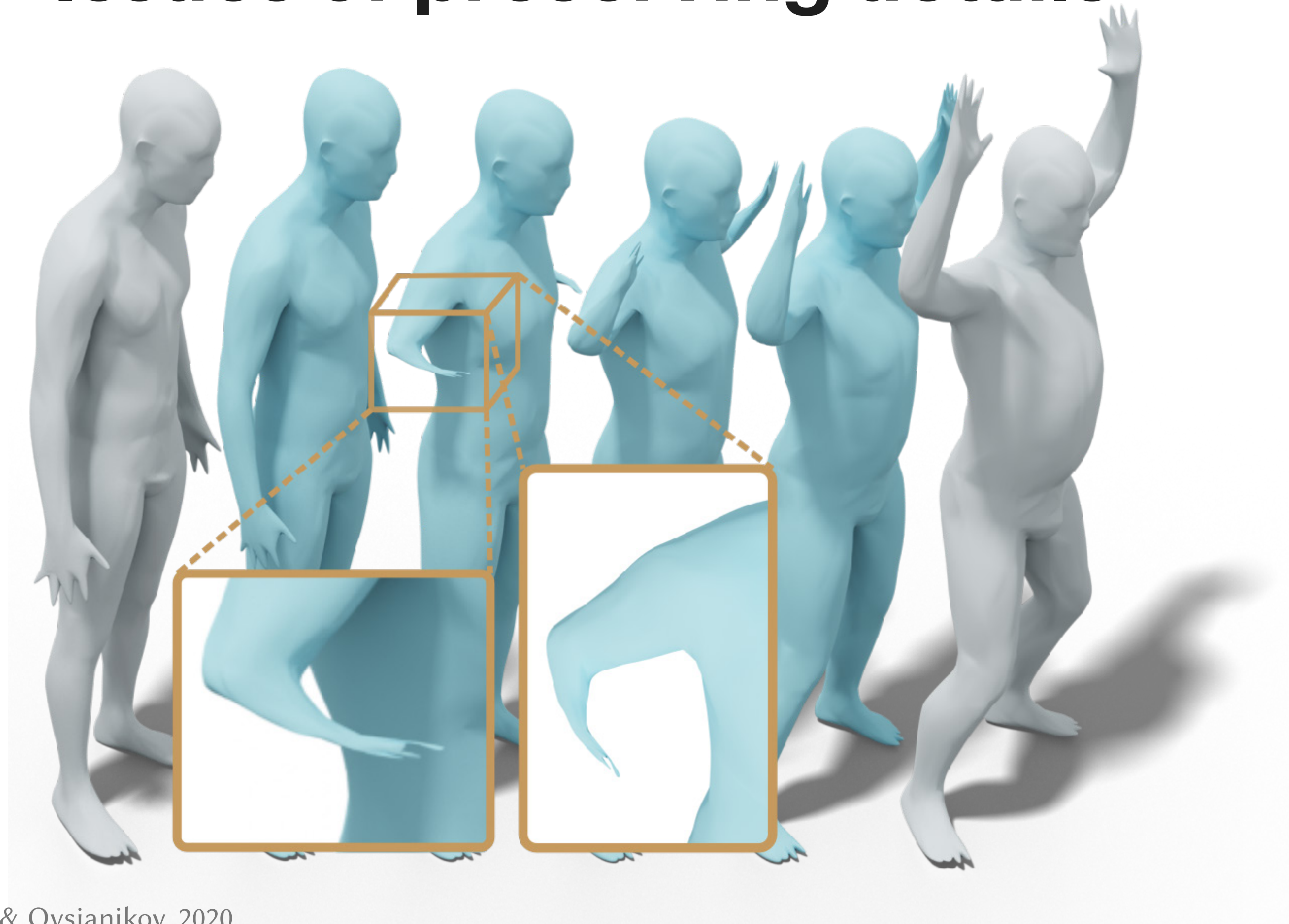


Gao et al. 2019



Rakotosaona & Ovsjanikov, 2020

Issues of preserving details



Linear Blend Skinning

new vertex locations

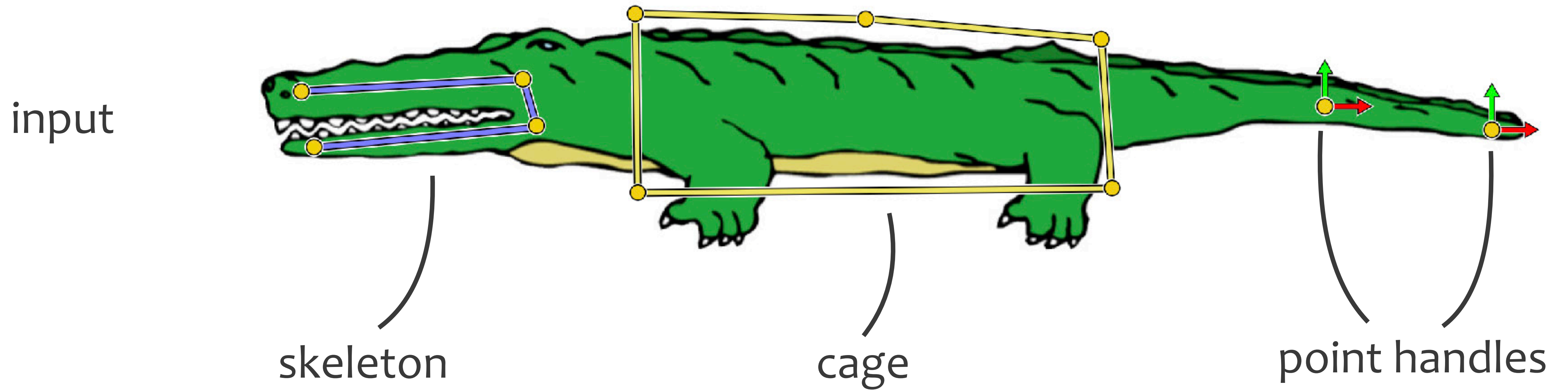
input vertex locations

$$v'_i = \sum_{j=1}^m w_{i,j} T_j v_i$$

weight

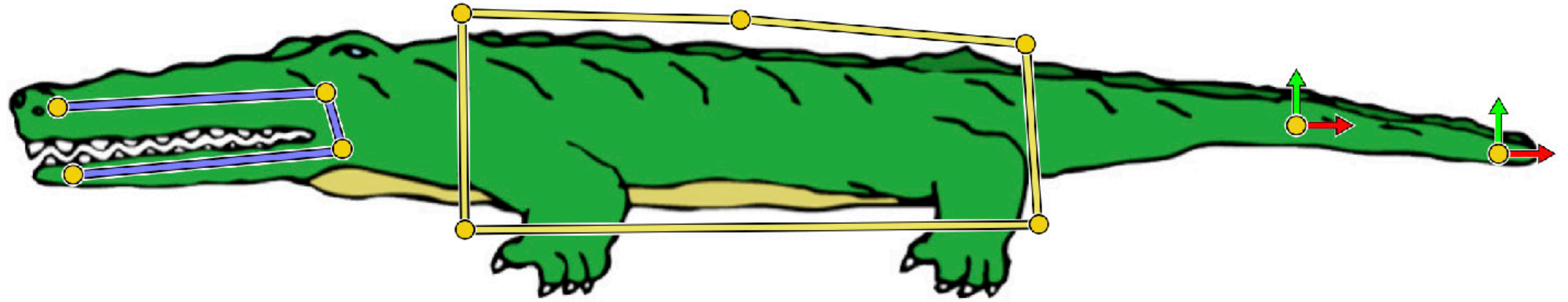
transformation of e.g., handles

Linear Blend Skinning

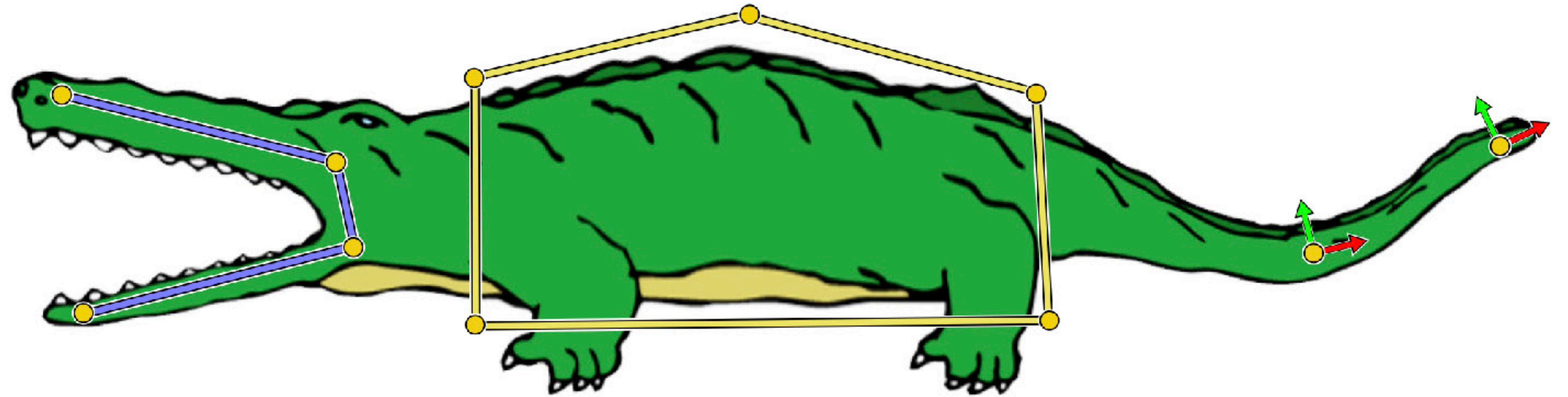


Linear Blend Skinning

input

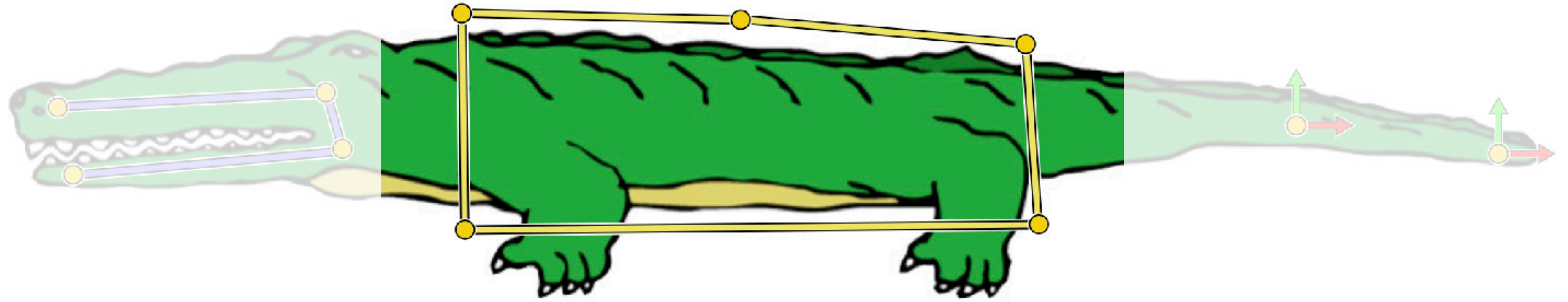


deformed

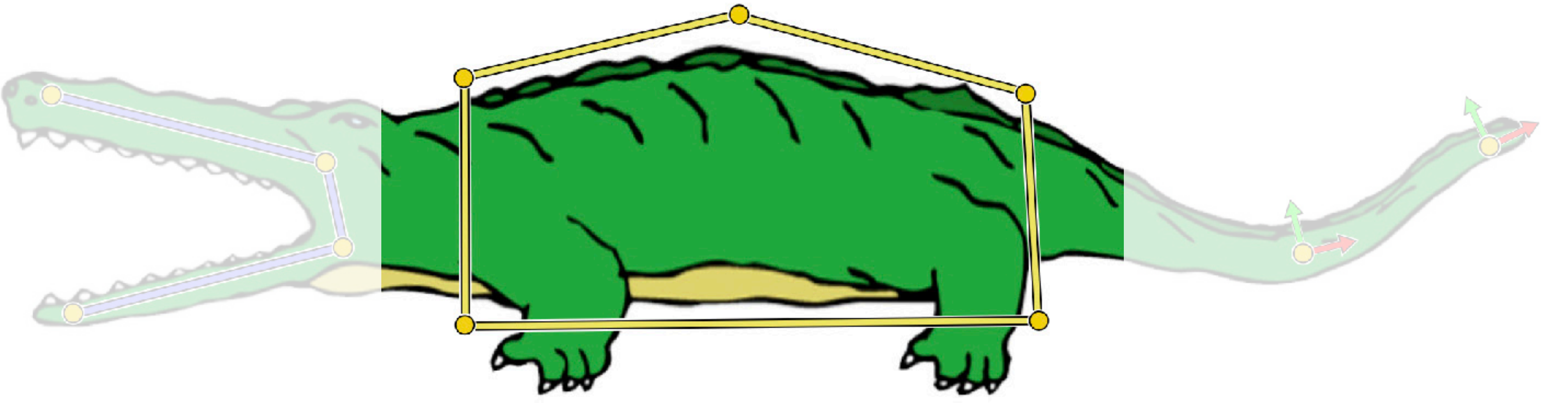


Linear Blend Skinning

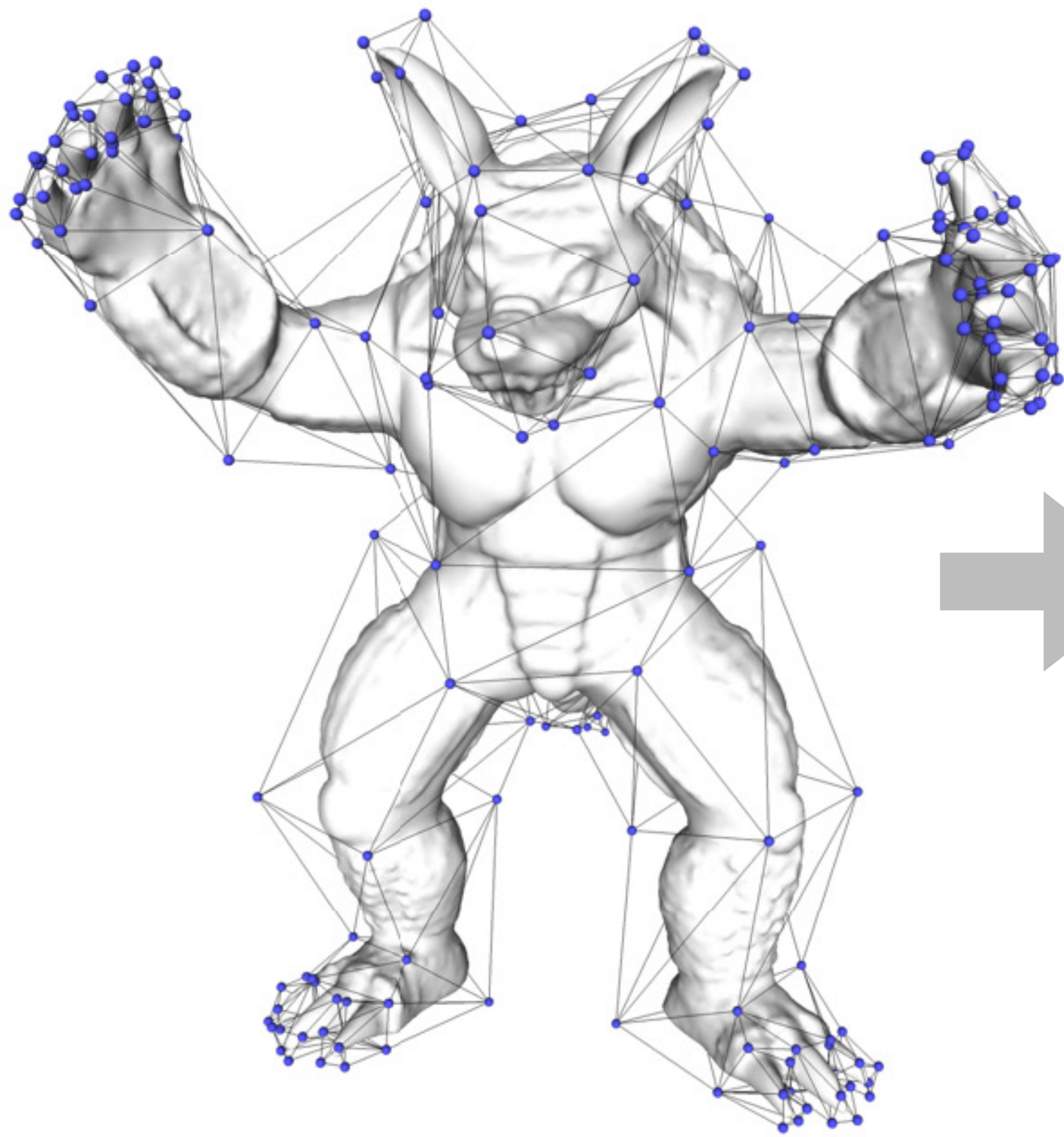
input



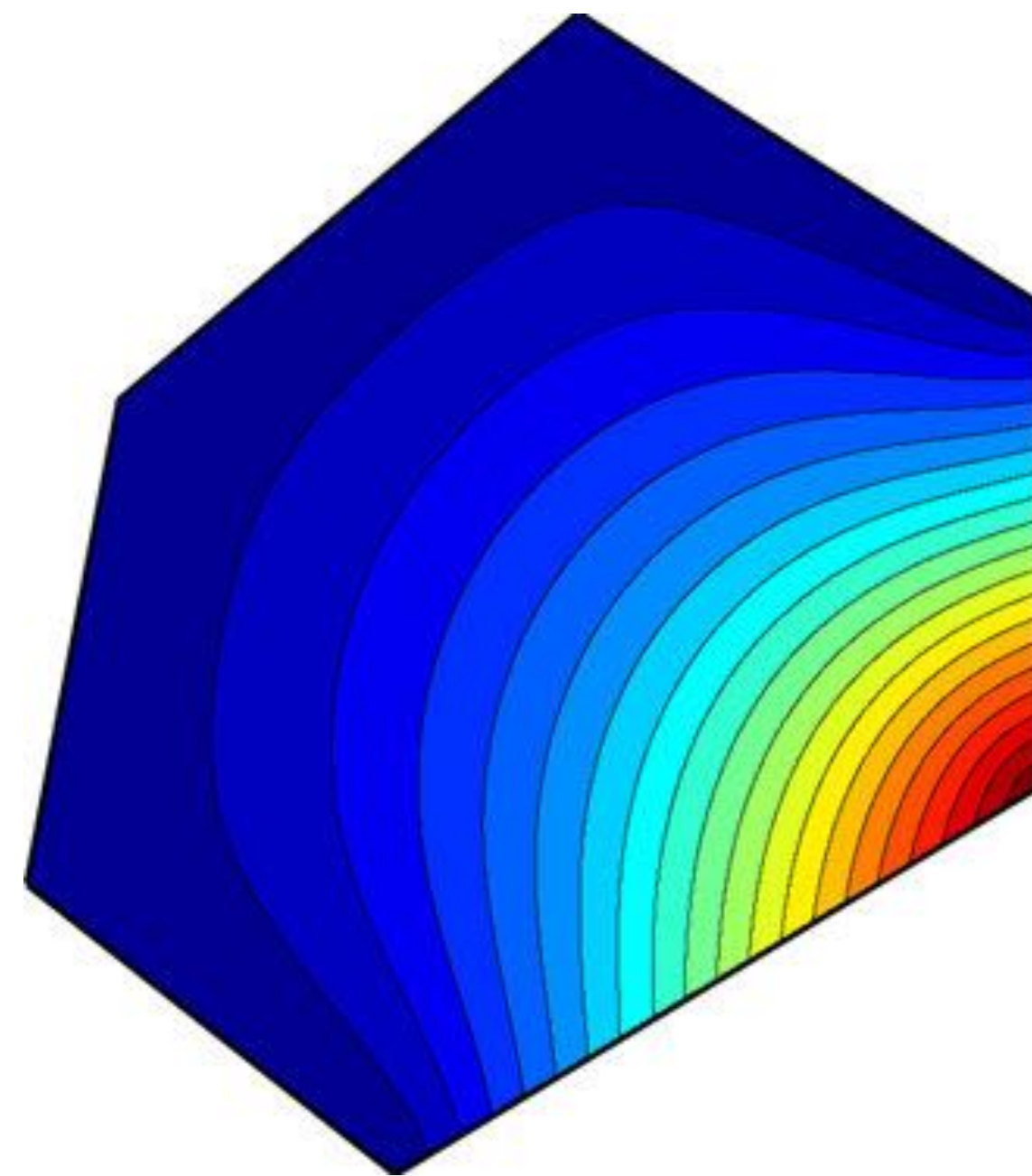
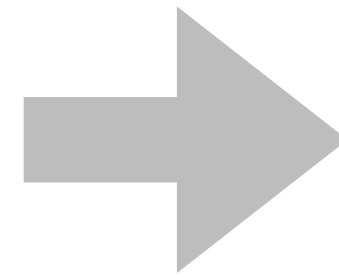
deformed



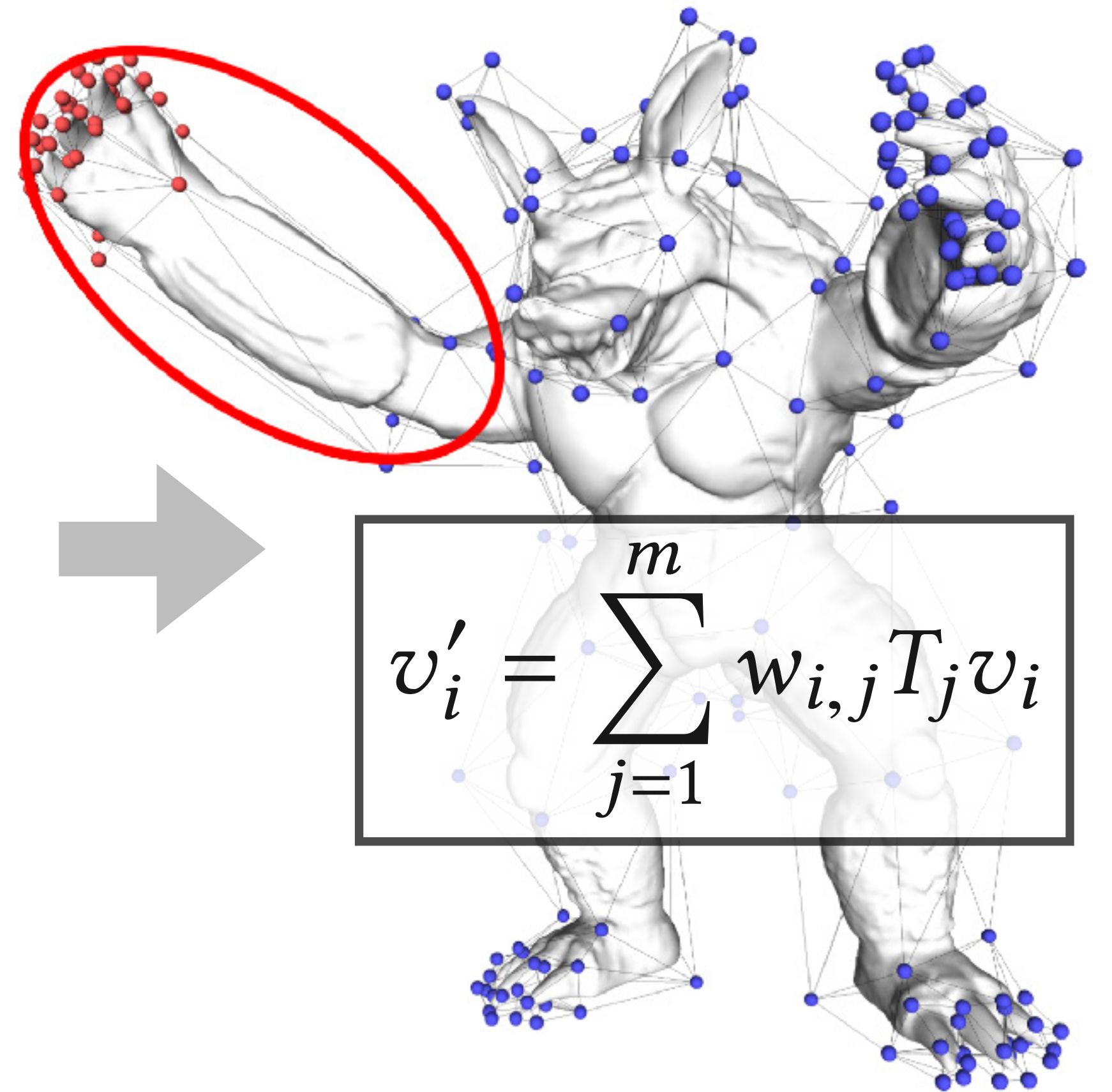
Cage-Based Deformation



construct a cage



compute cage weights



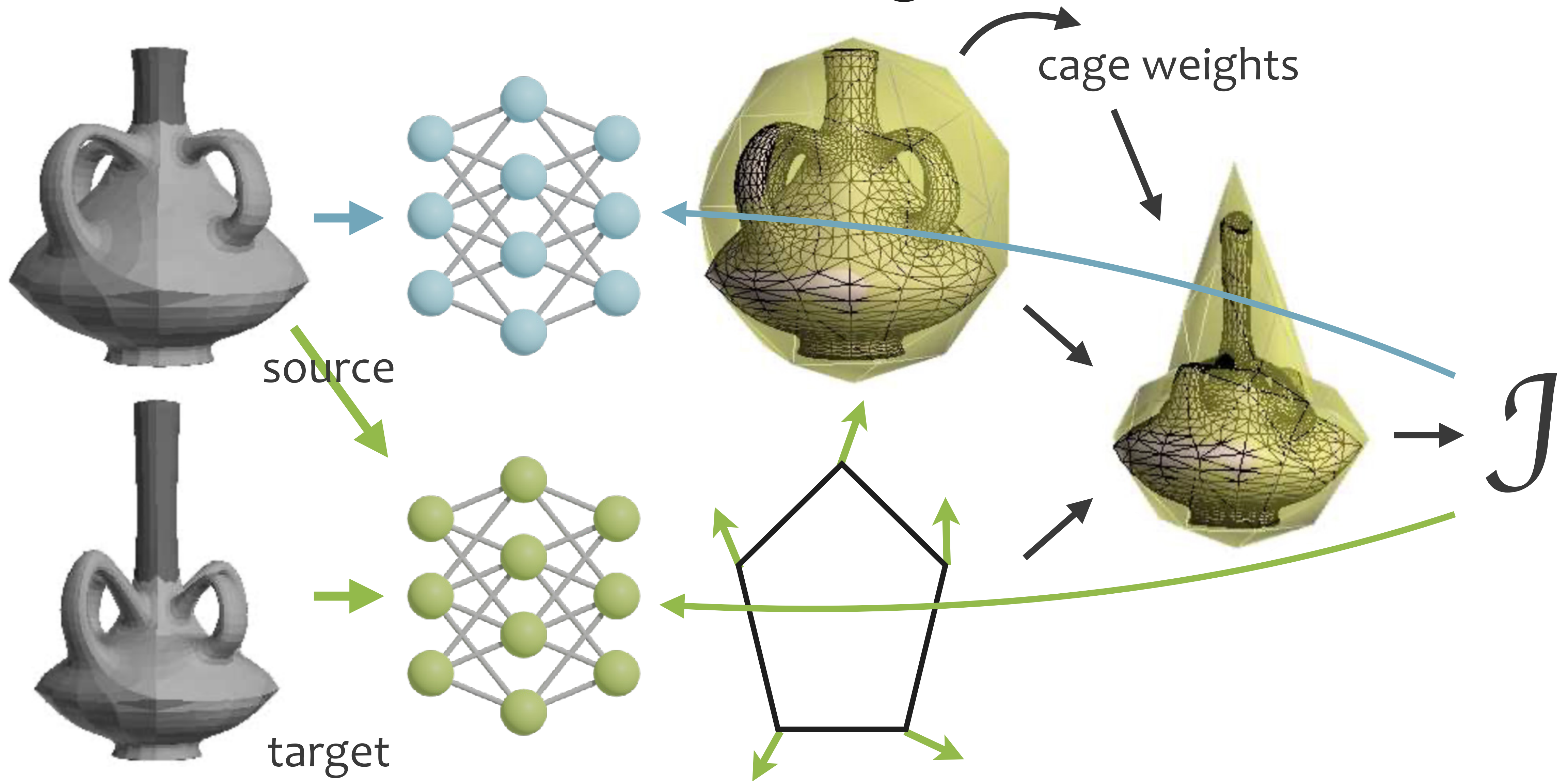
deform the model

$$v'_i = \sum_{j=1}^m w_{i,j} T_j v_i$$

Neural Cages



Neural Cages



Loss Function

$$\mathcal{J} = w_1 \mathcal{L}_{MVC} + w_2 \mathcal{L}_{\text{align}} + w_3 \mathcal{L}_{\text{shape}}$$

“nice” cage
(e.g., not self-overlap)

positive cage weights

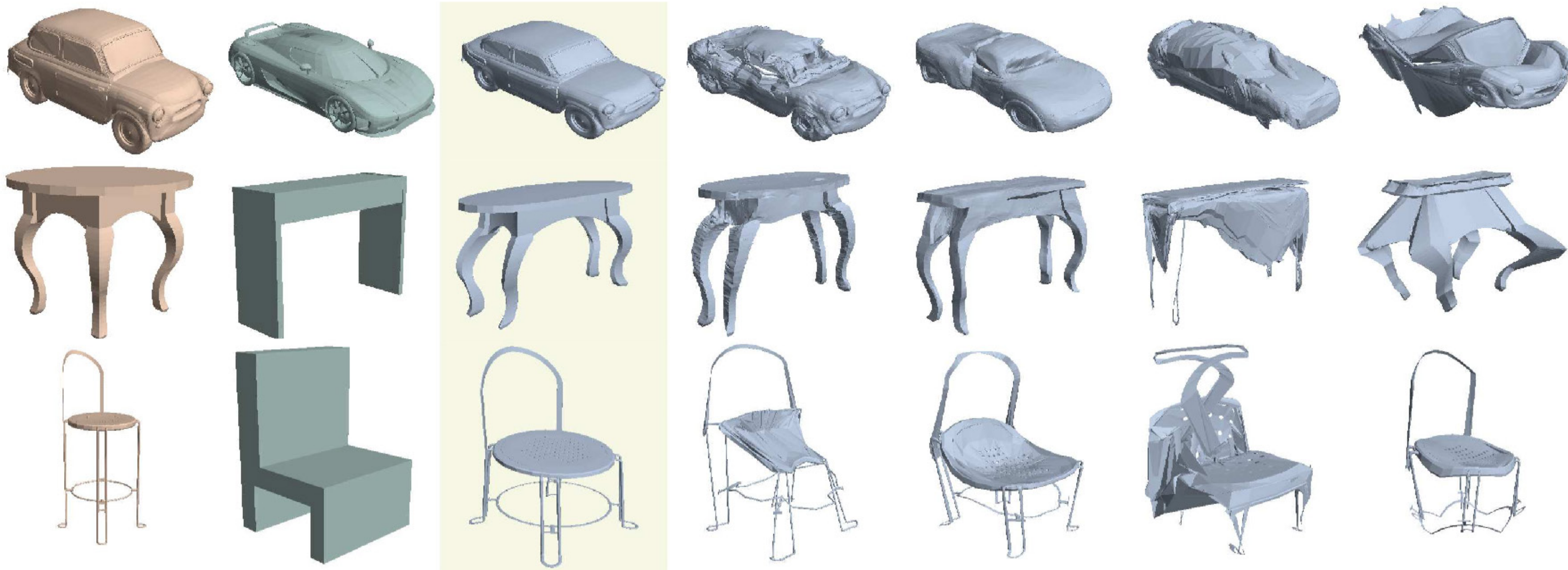
align with target

Chamfer

preserve input
shapes

e.g., preserve normals

Detail-Preserving Deformation



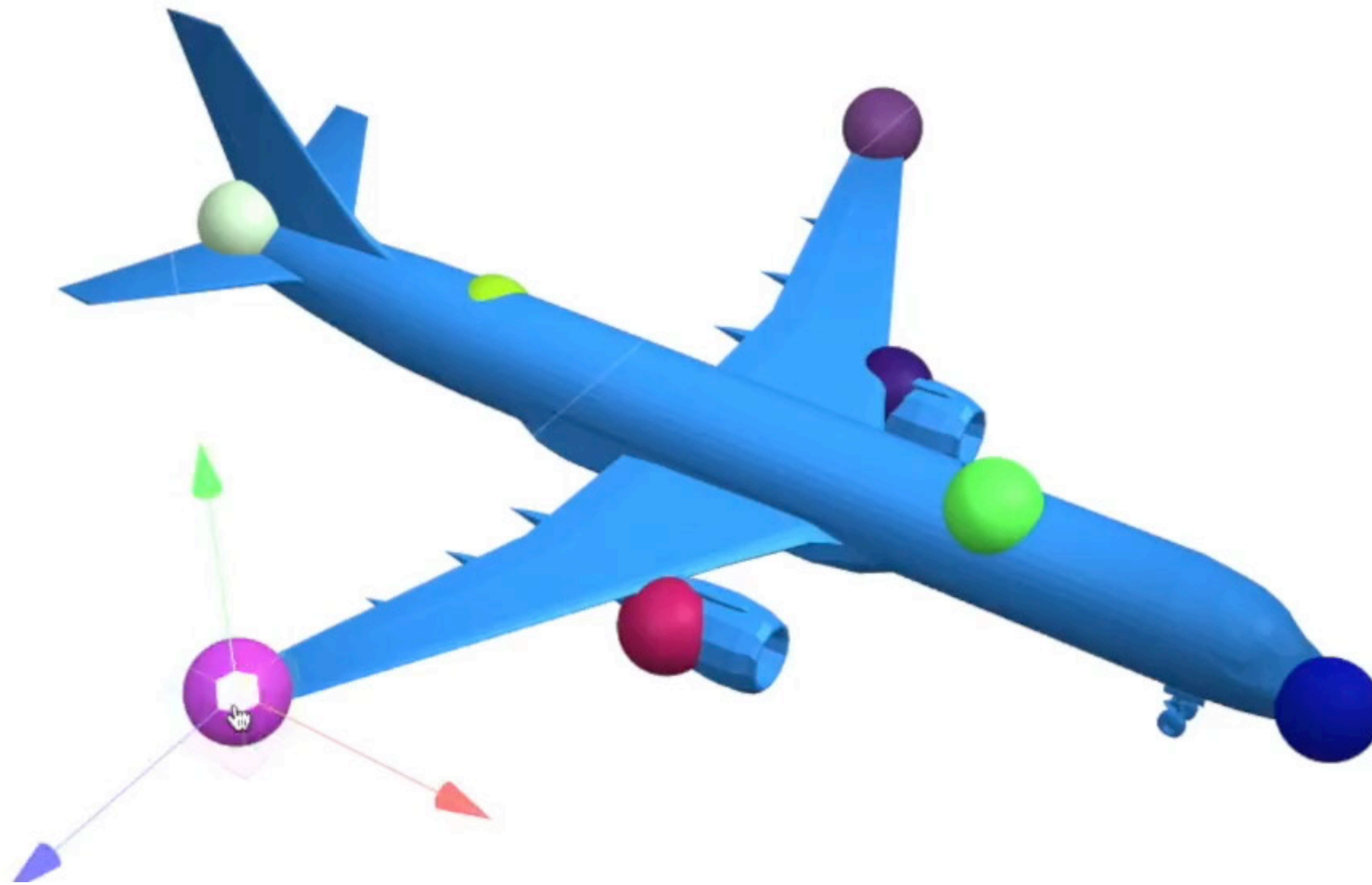
input

target

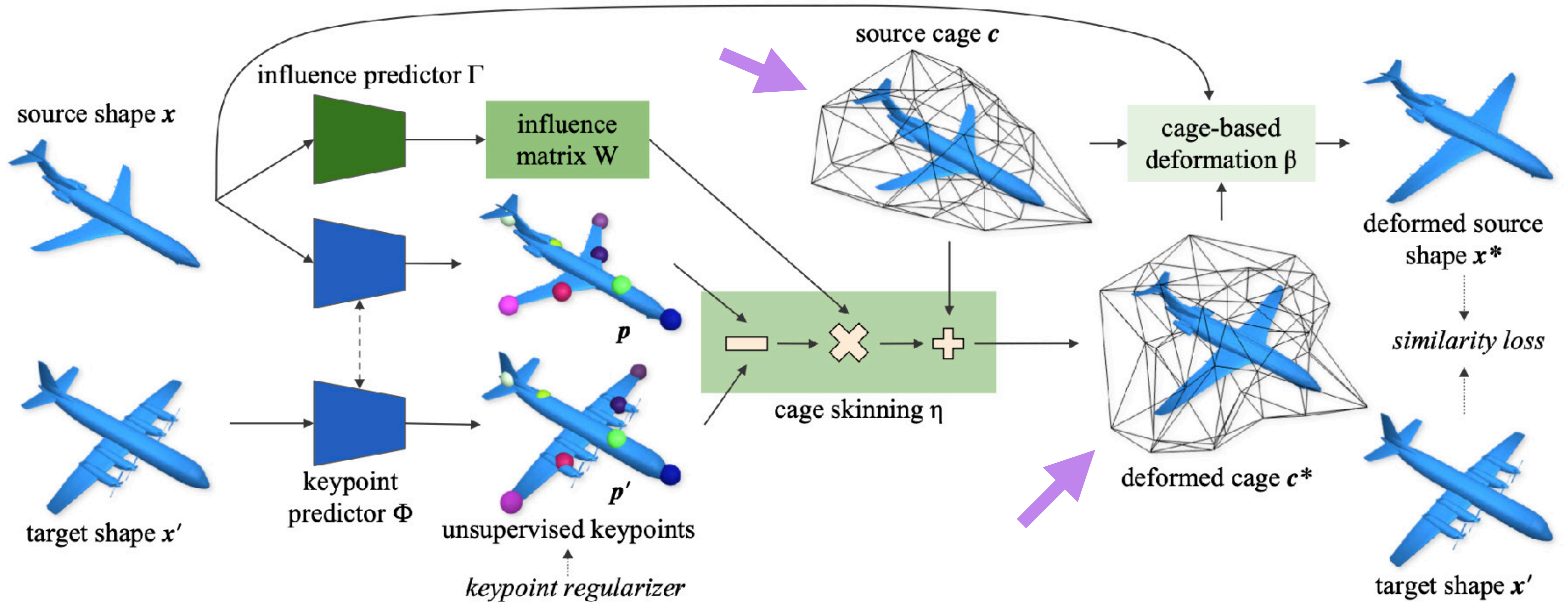
output

previous methods

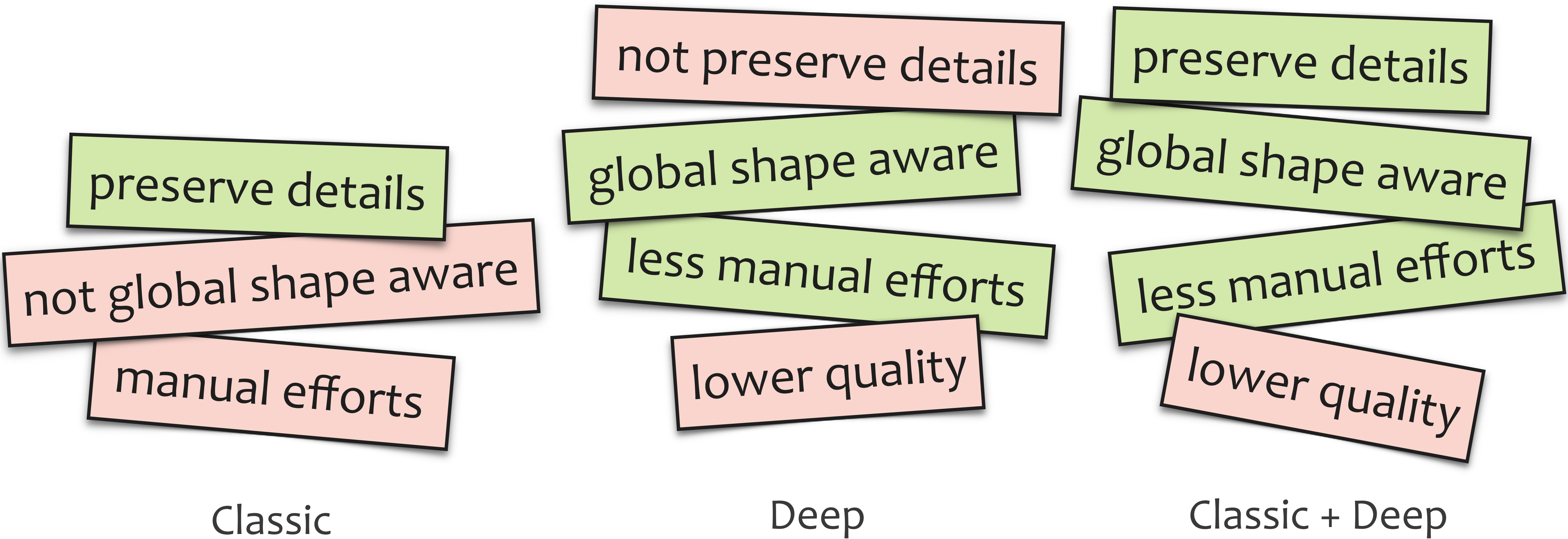
Keypoint Deformer



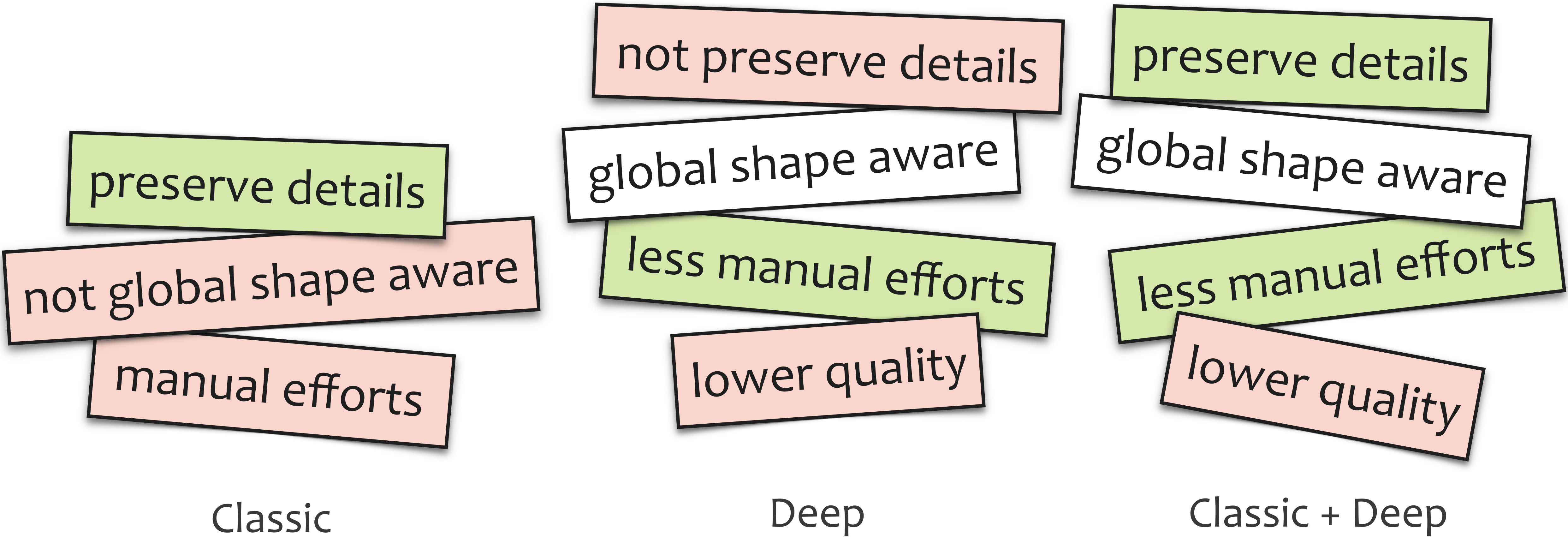
Keypoint Deformer



Key Takeaways

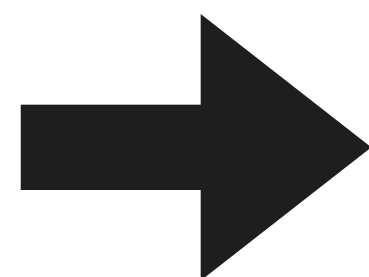
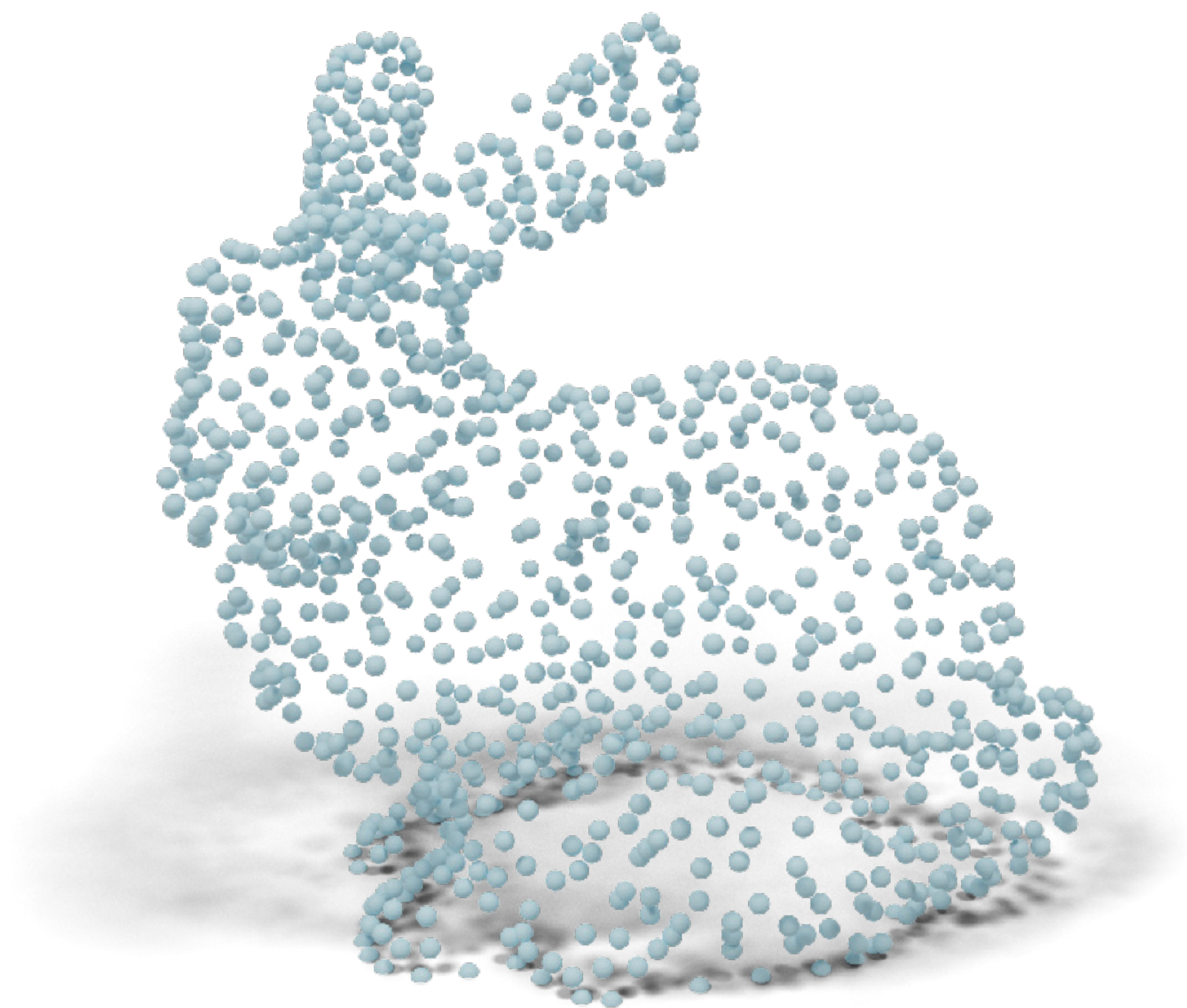


Key Takeaways

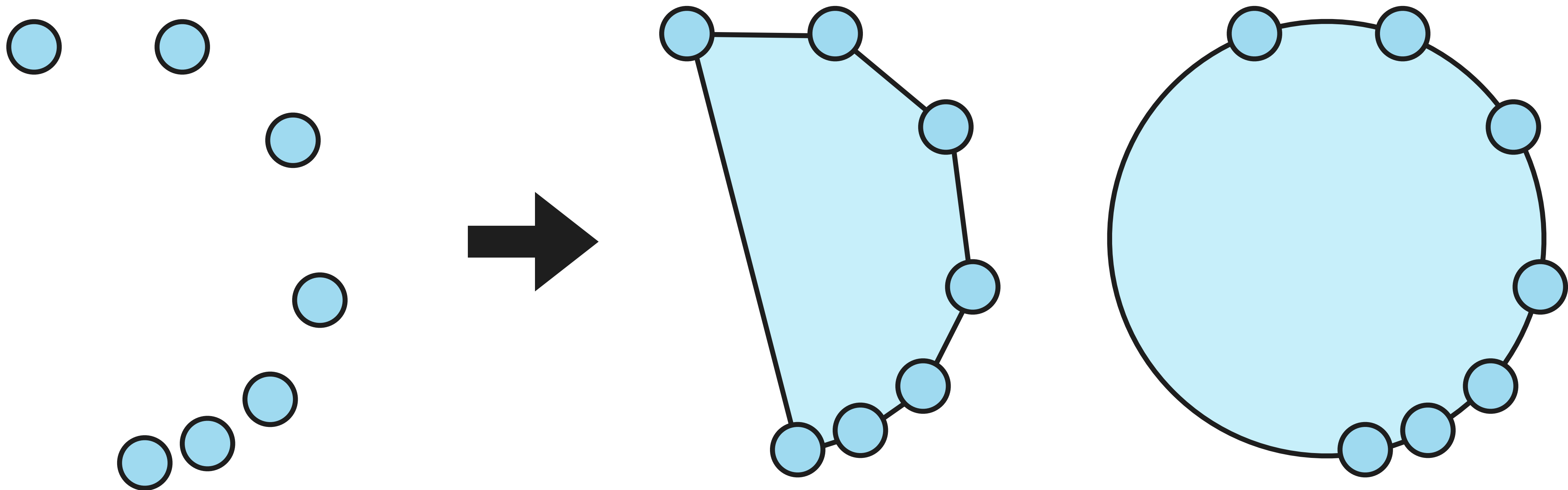


Machine learning as geometric prior

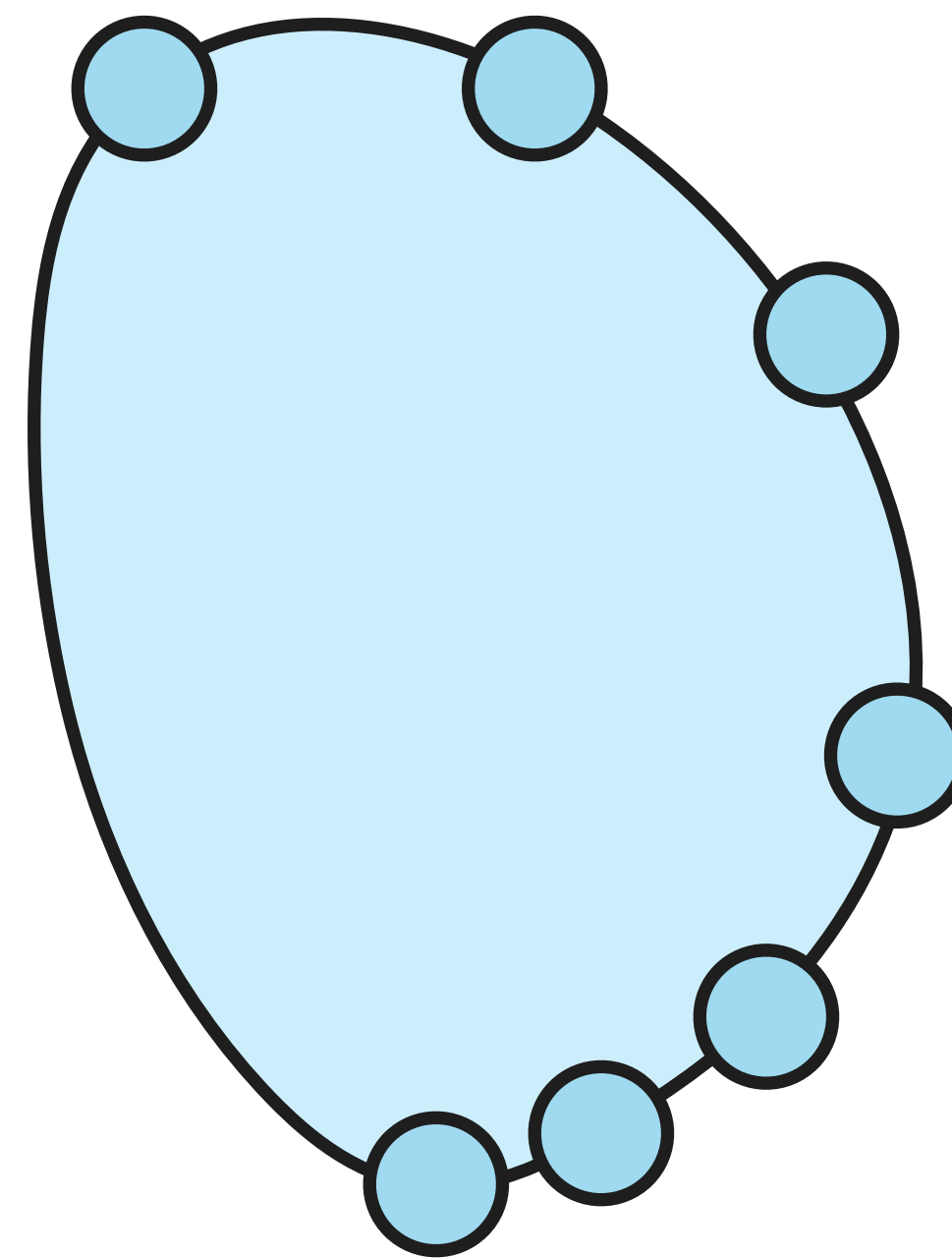
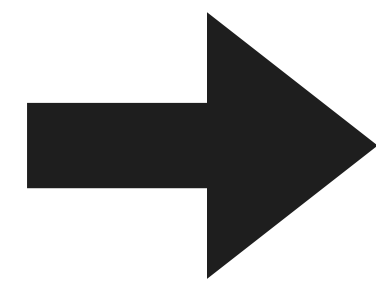
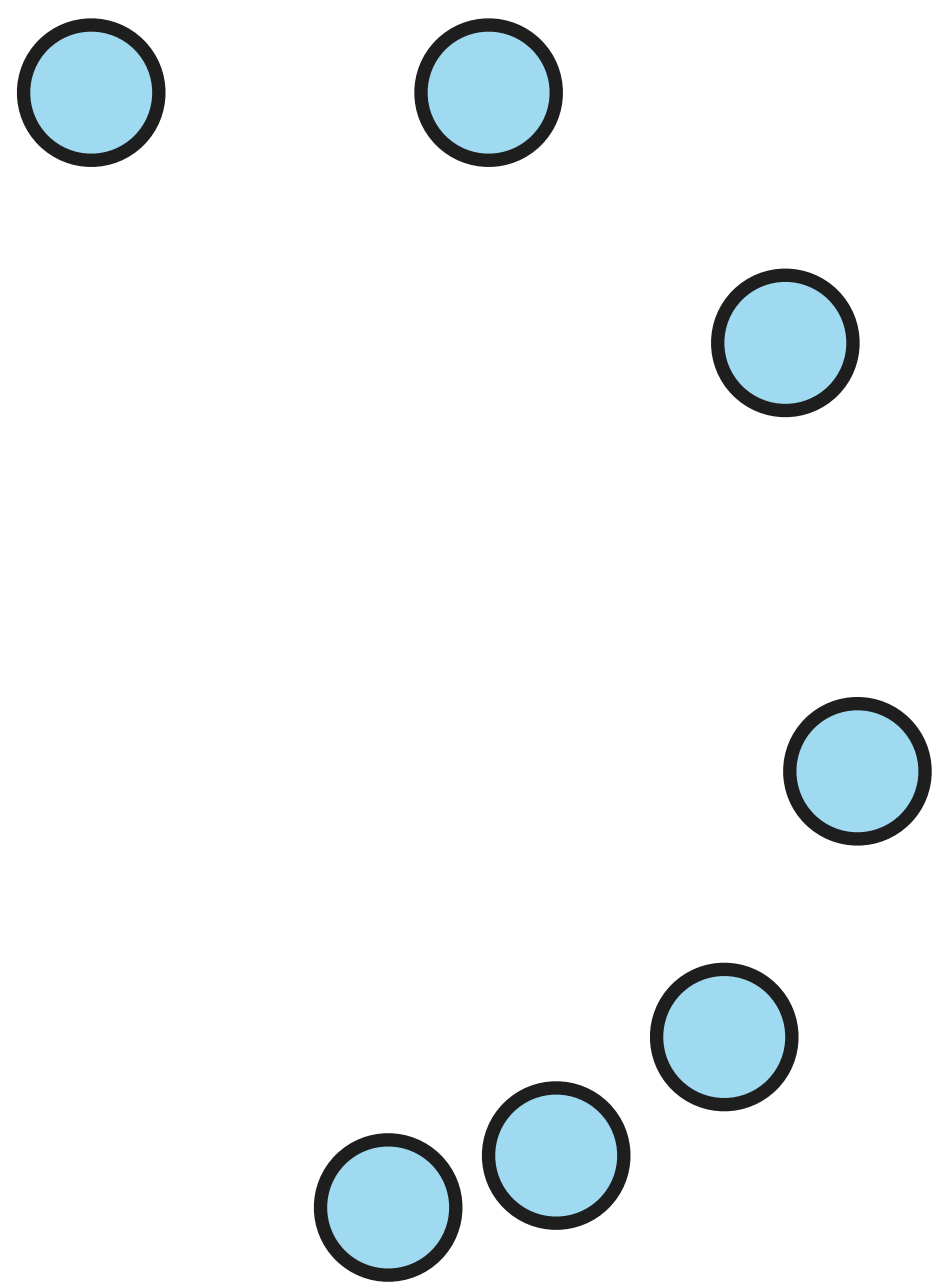
Surface Reconstruction



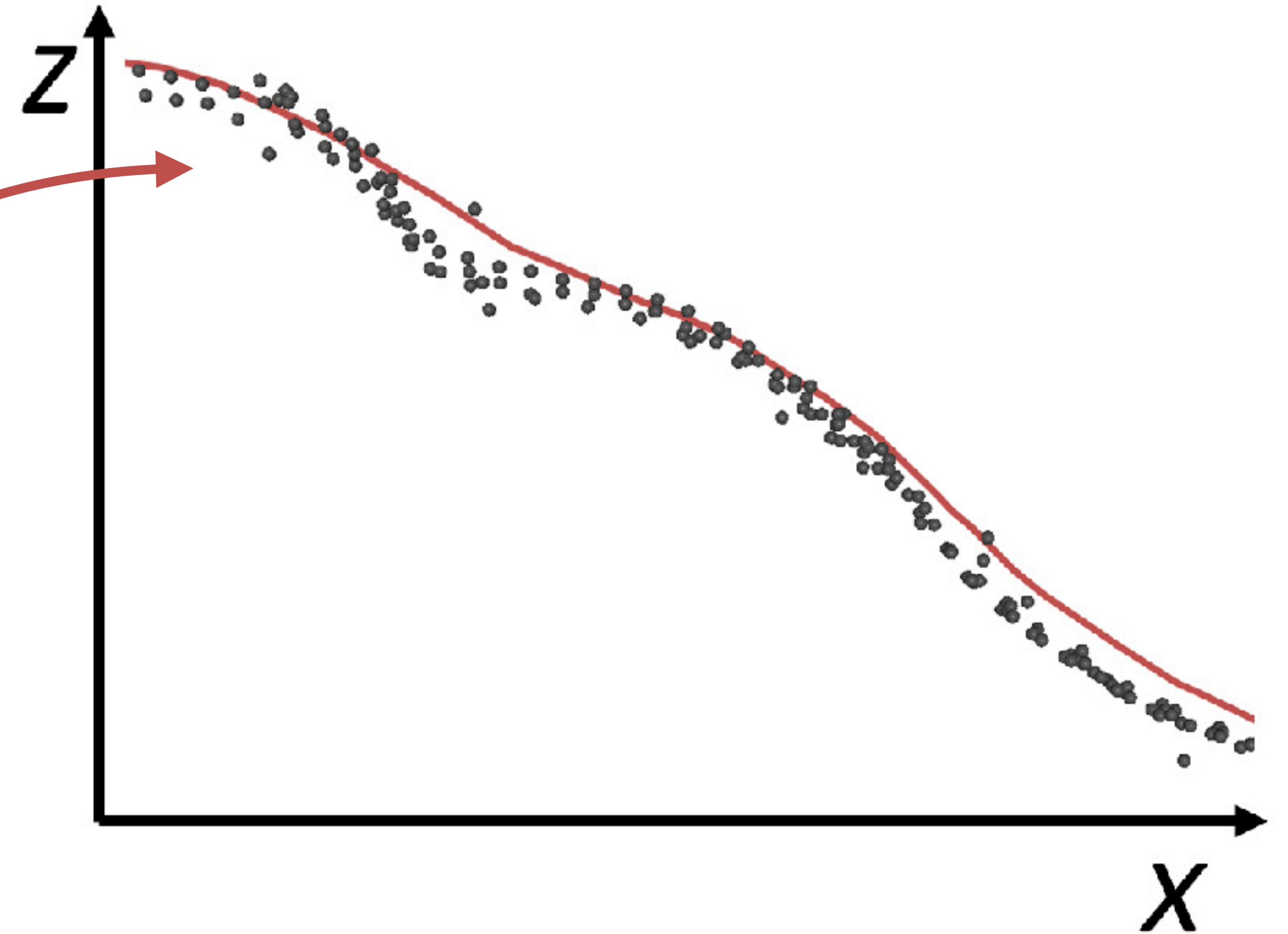
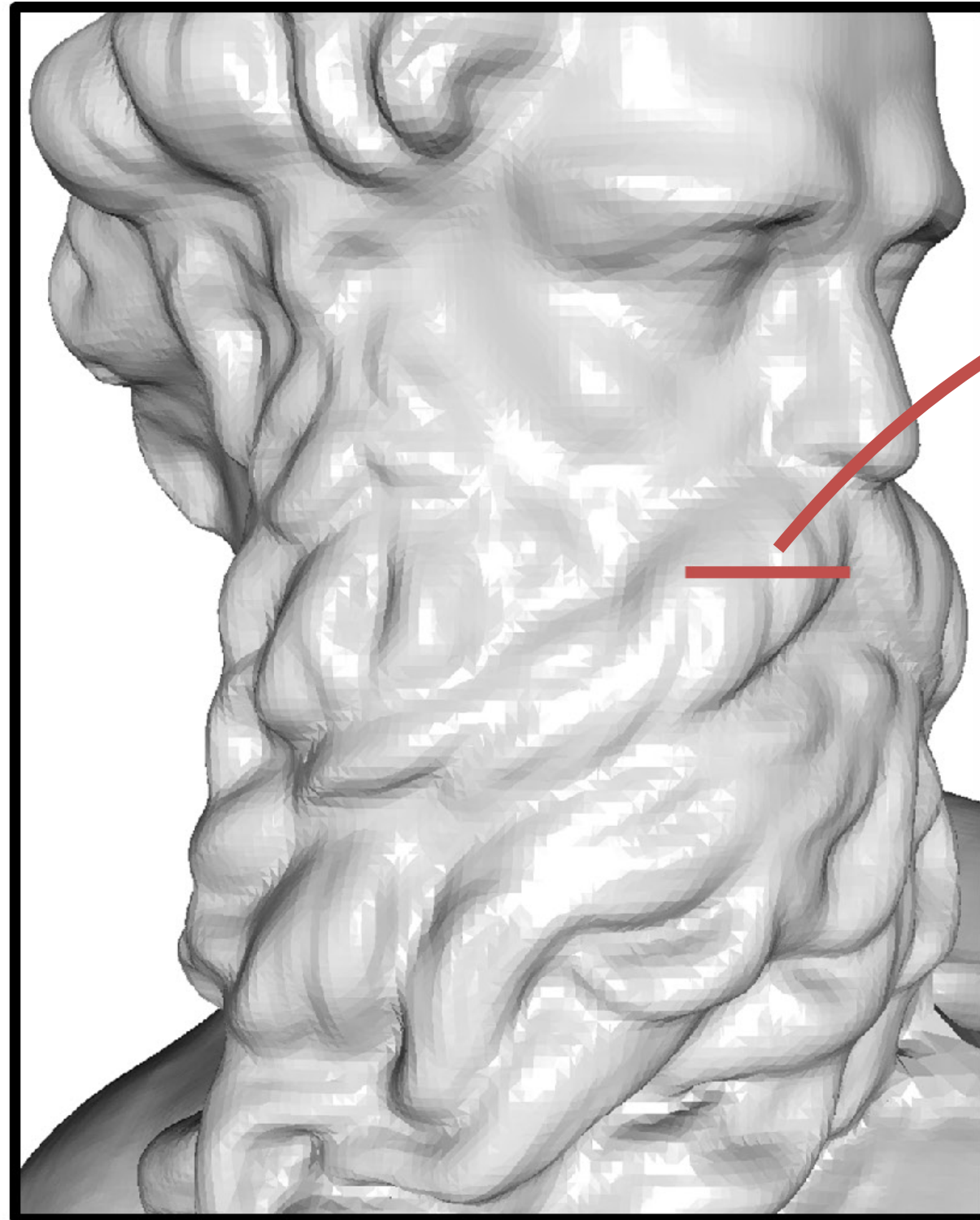
An ill-posed problem



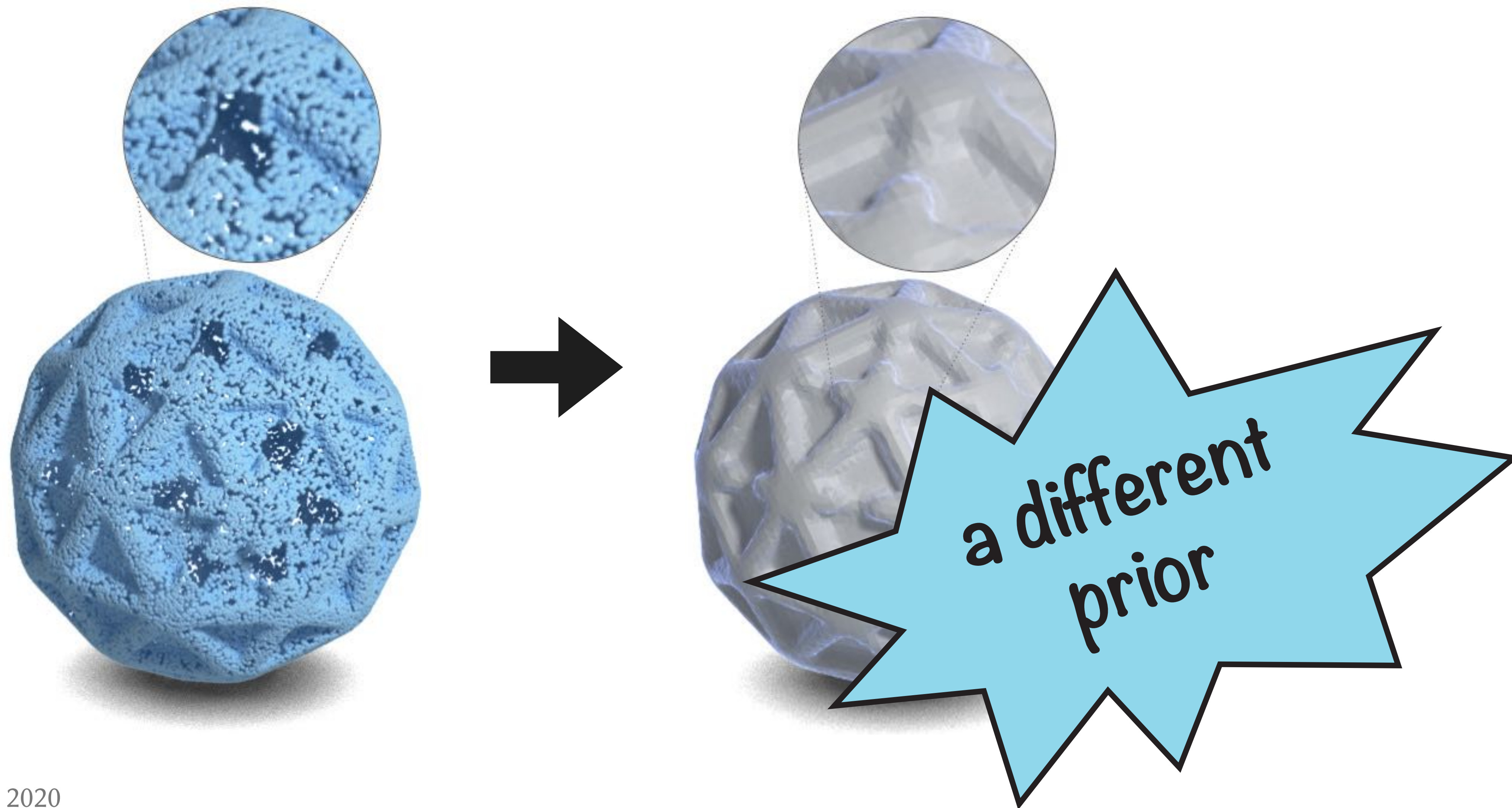
A Smooth Solution



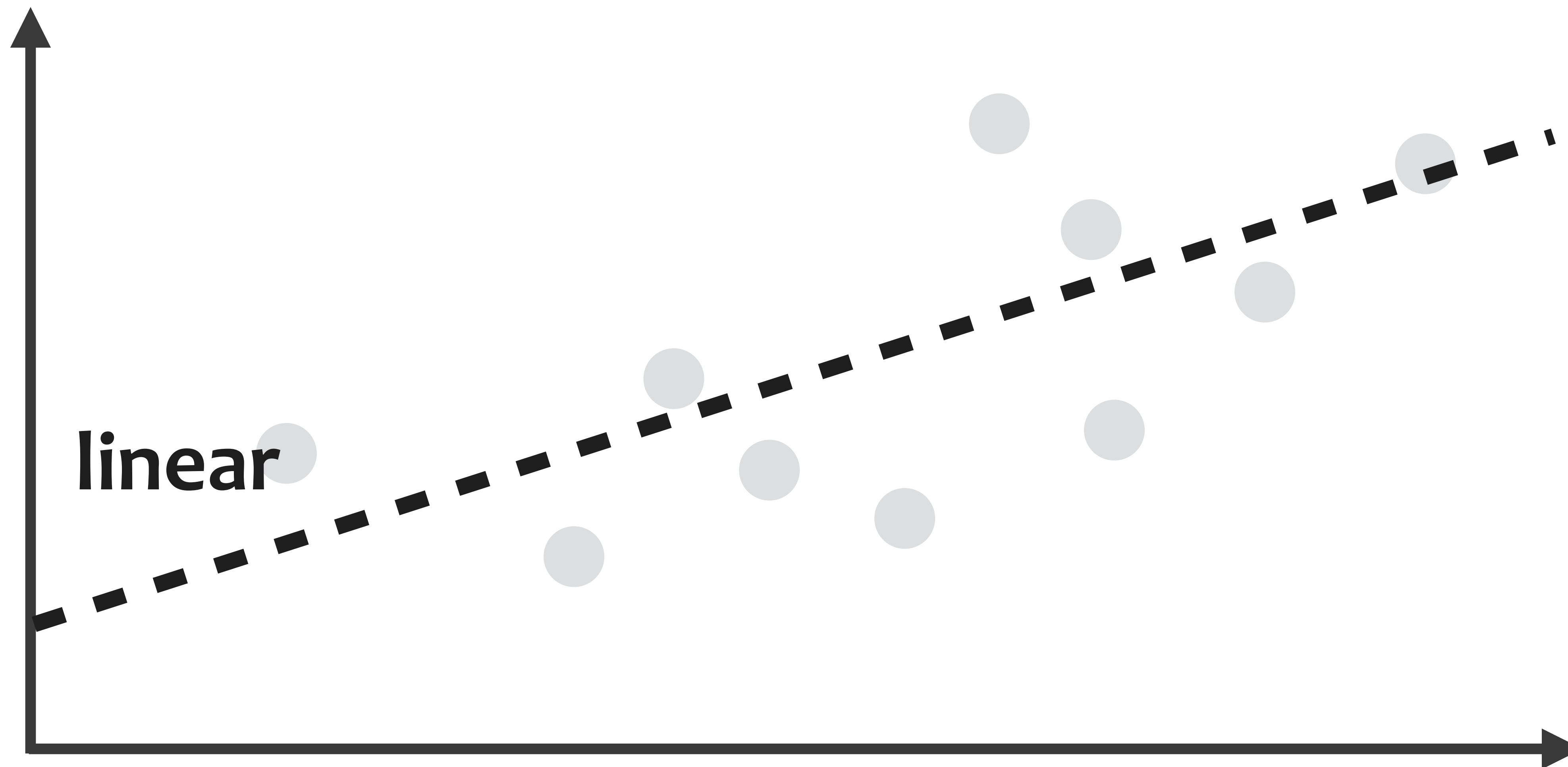
Classic Smoothness Prior



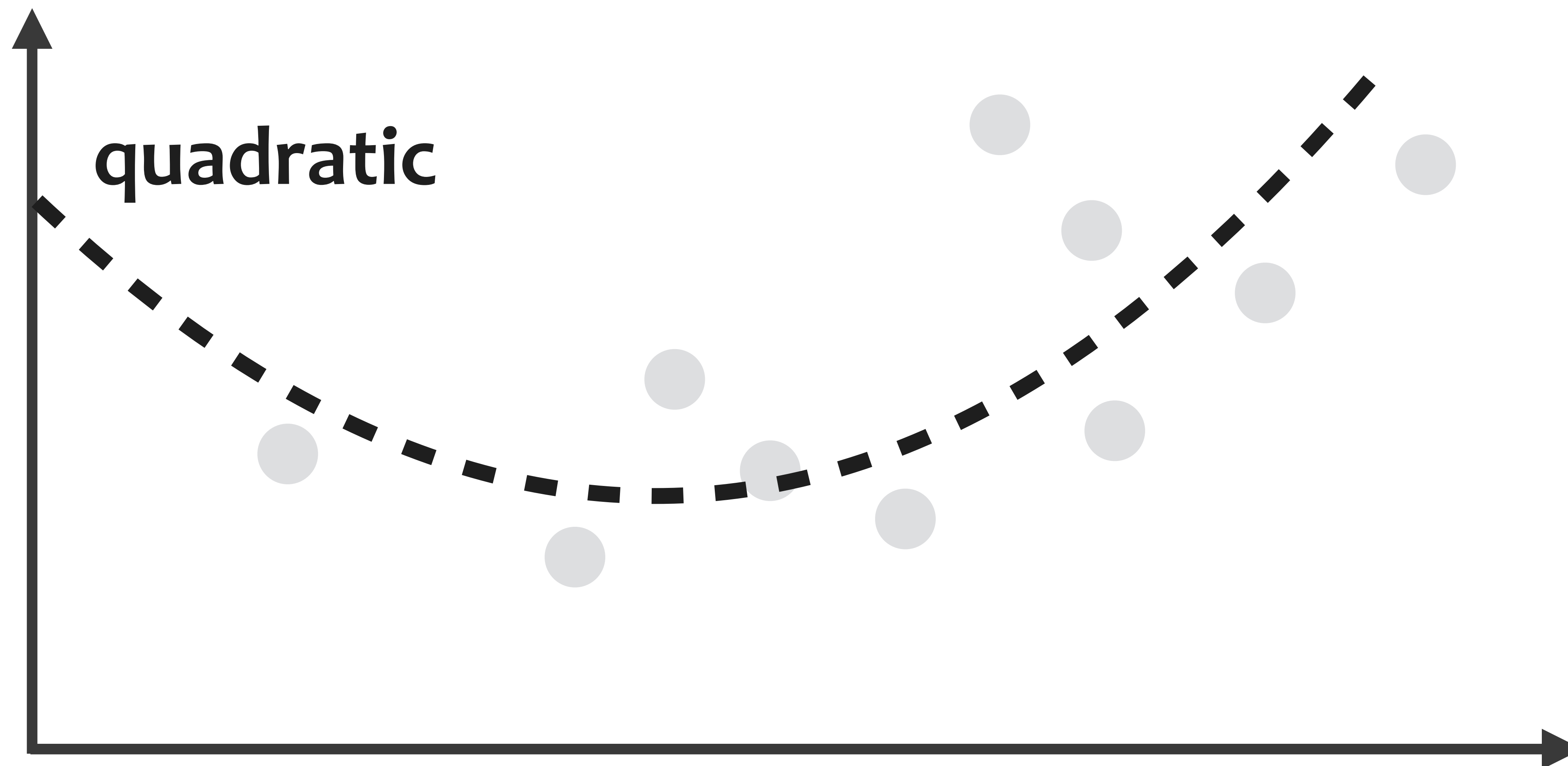
Smoothness is not always good



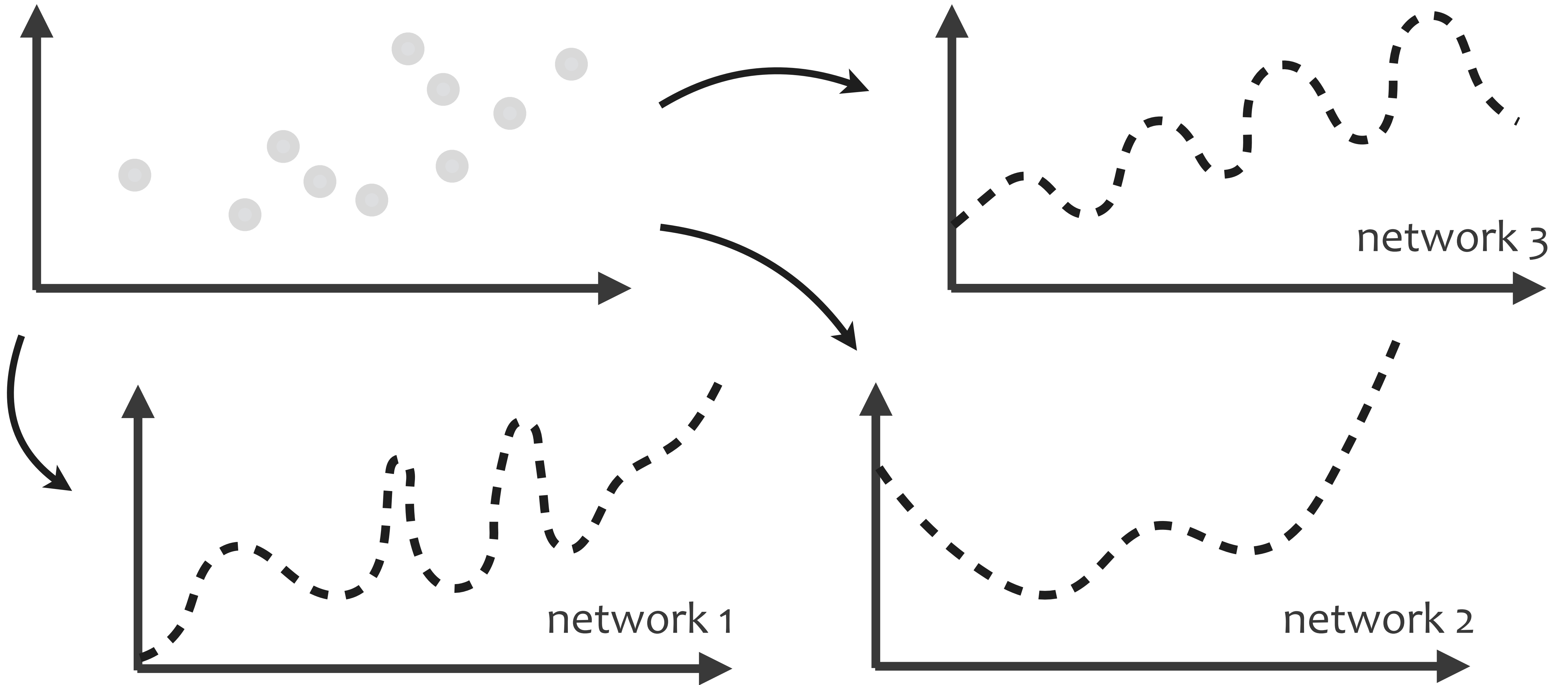
Inductive Bias as Prior



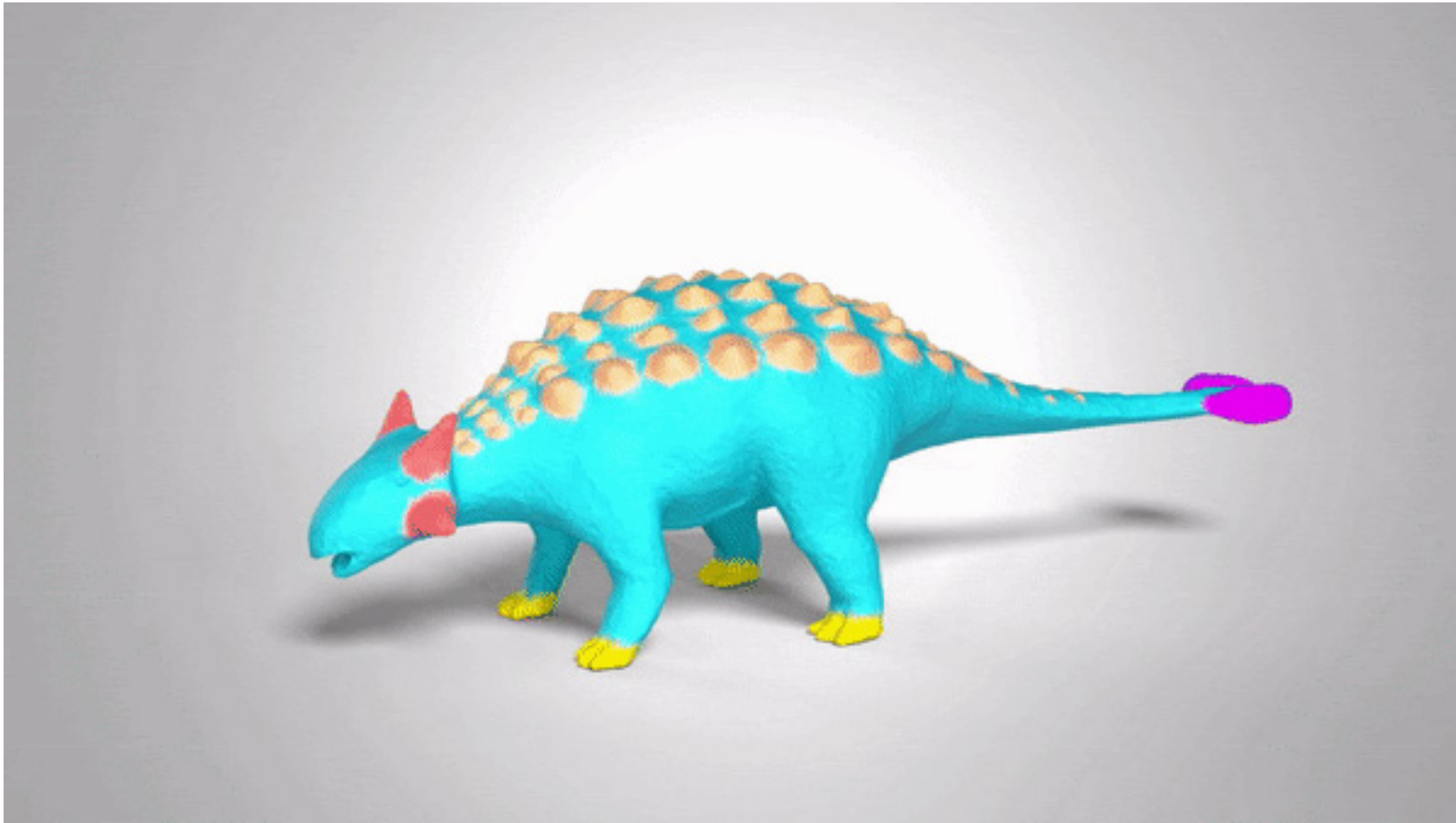
Inductive Bias as Prior



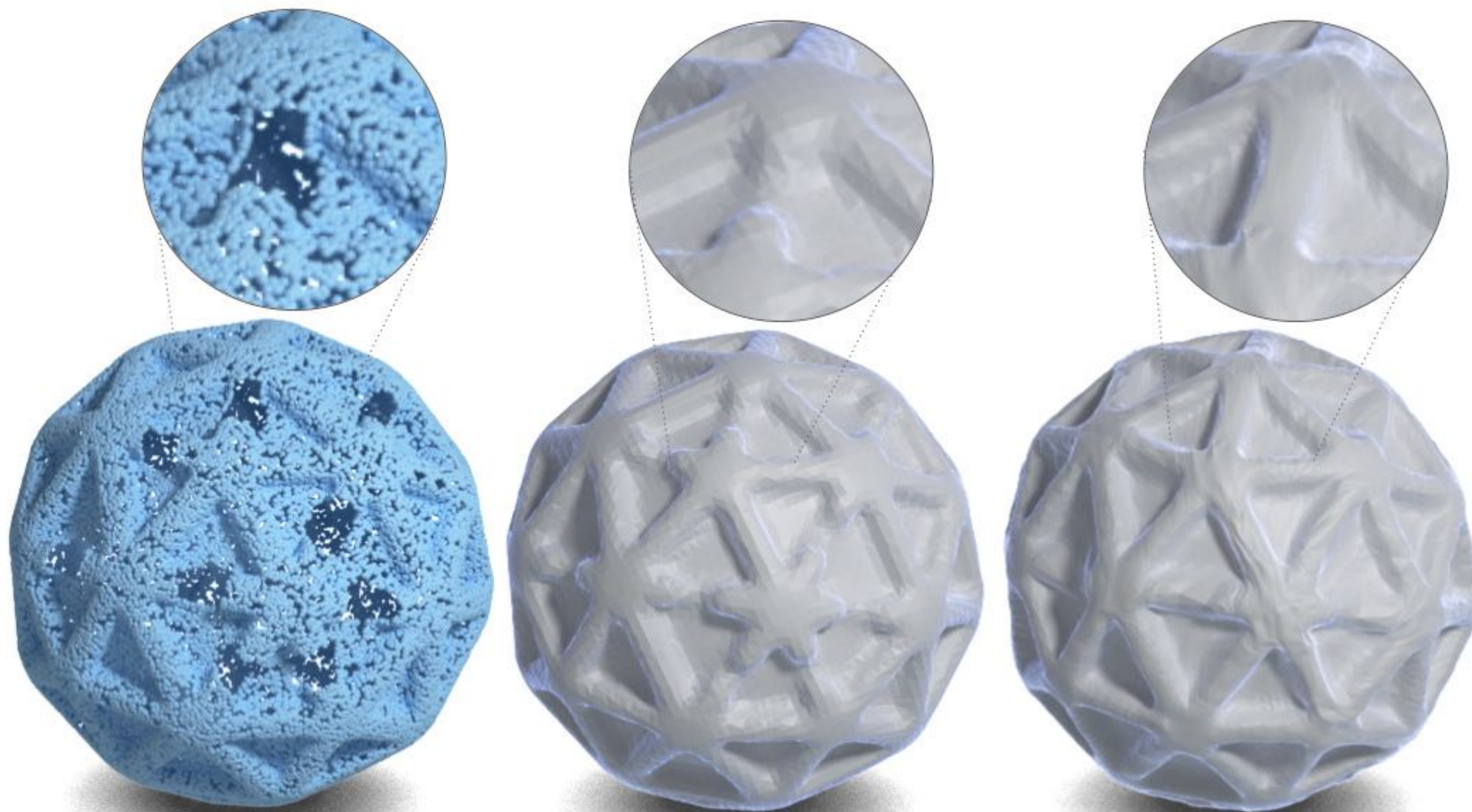
Deep Network Biases



New Possibilities : Self-Prior



Results of Self-Prior

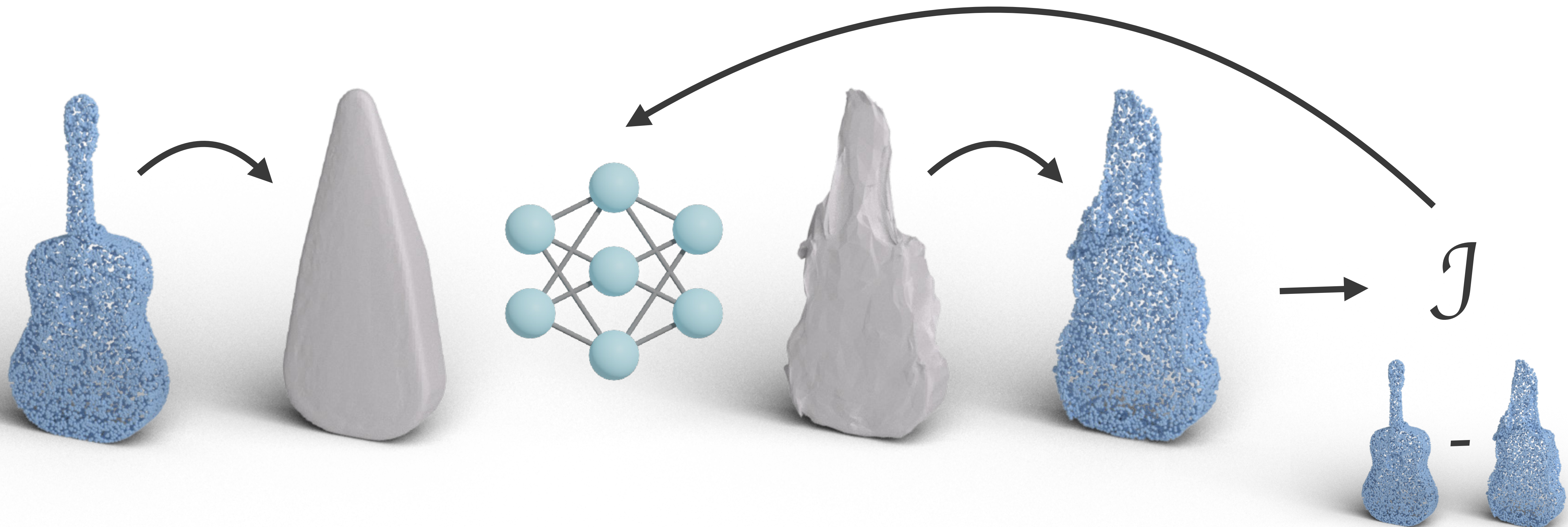


input

Smoothness

Self-prior

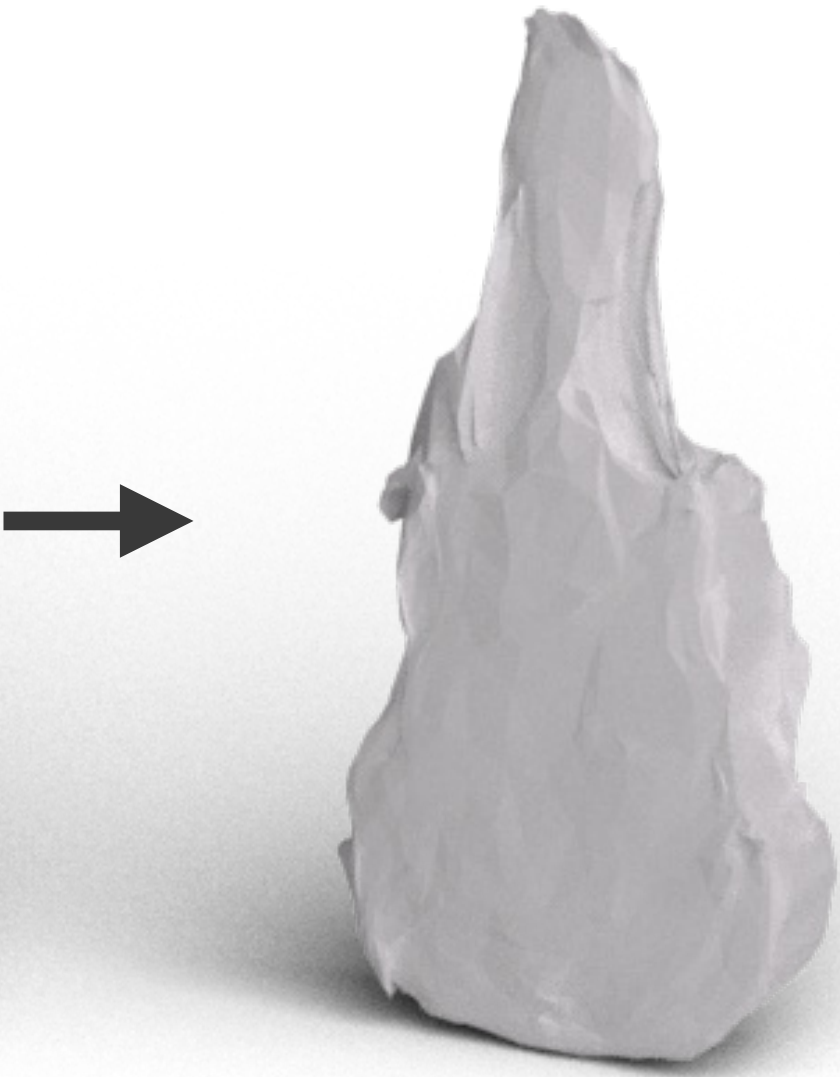
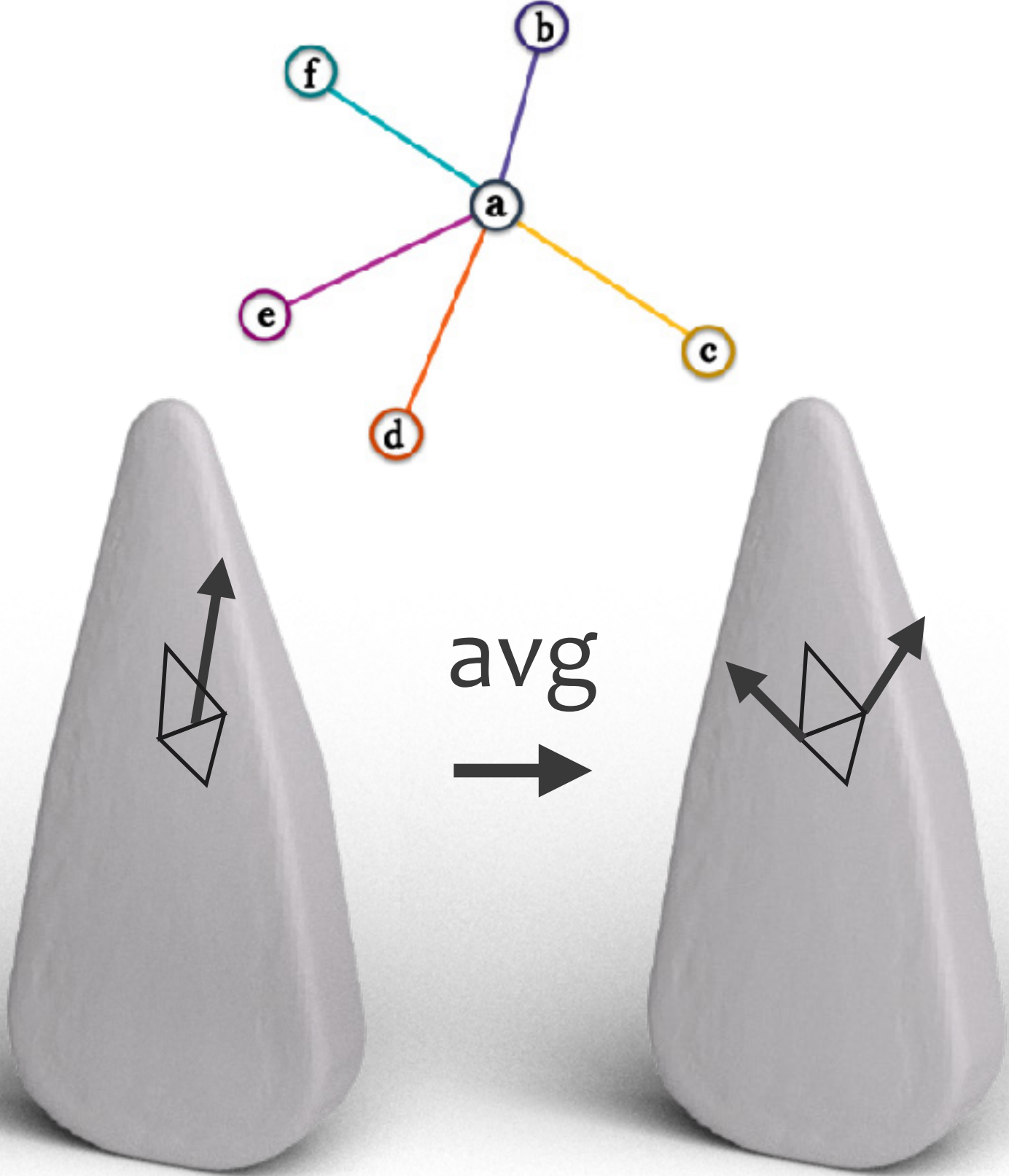
Point2Mesh Overview



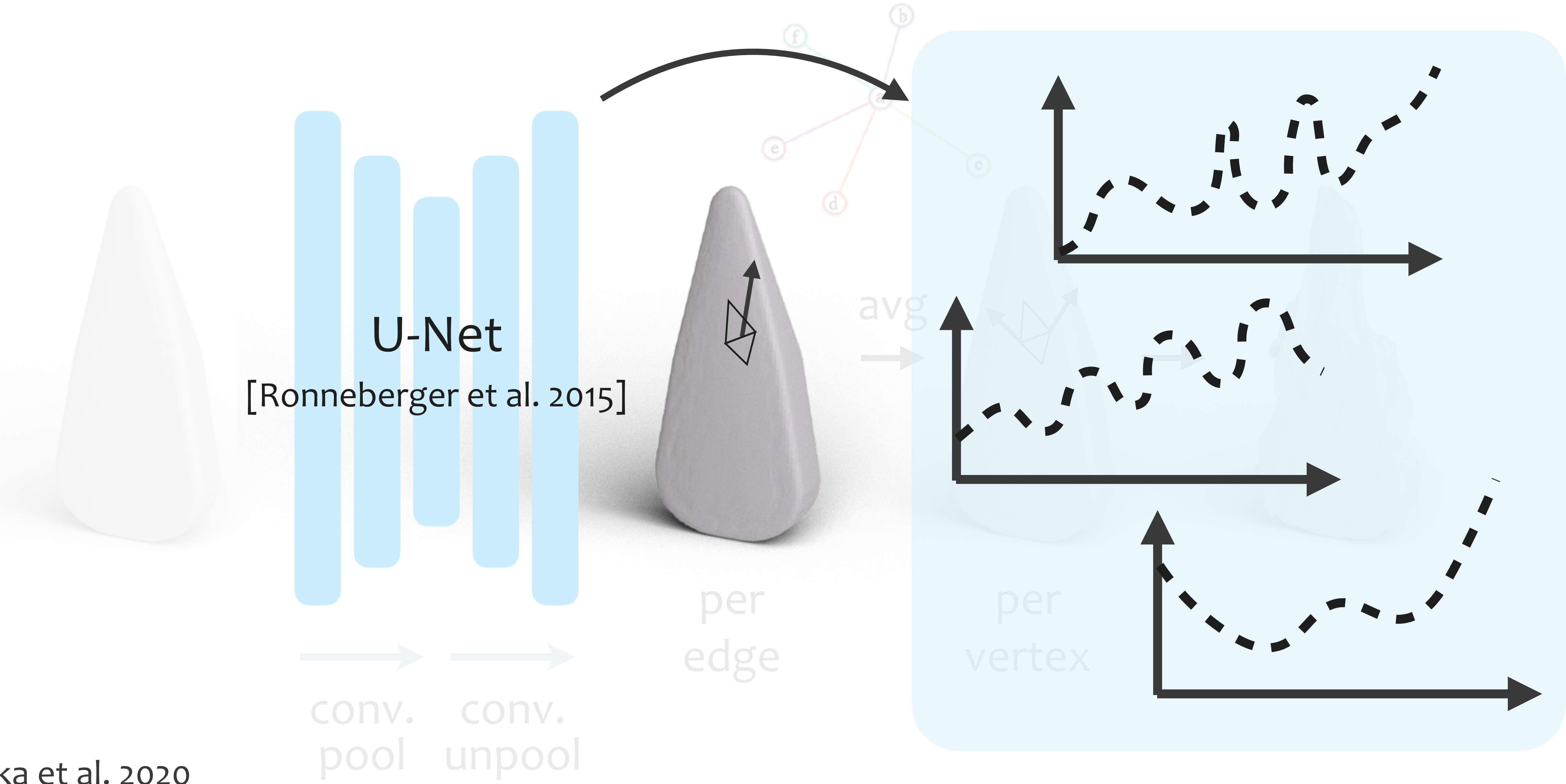
Point2Mesh Overview



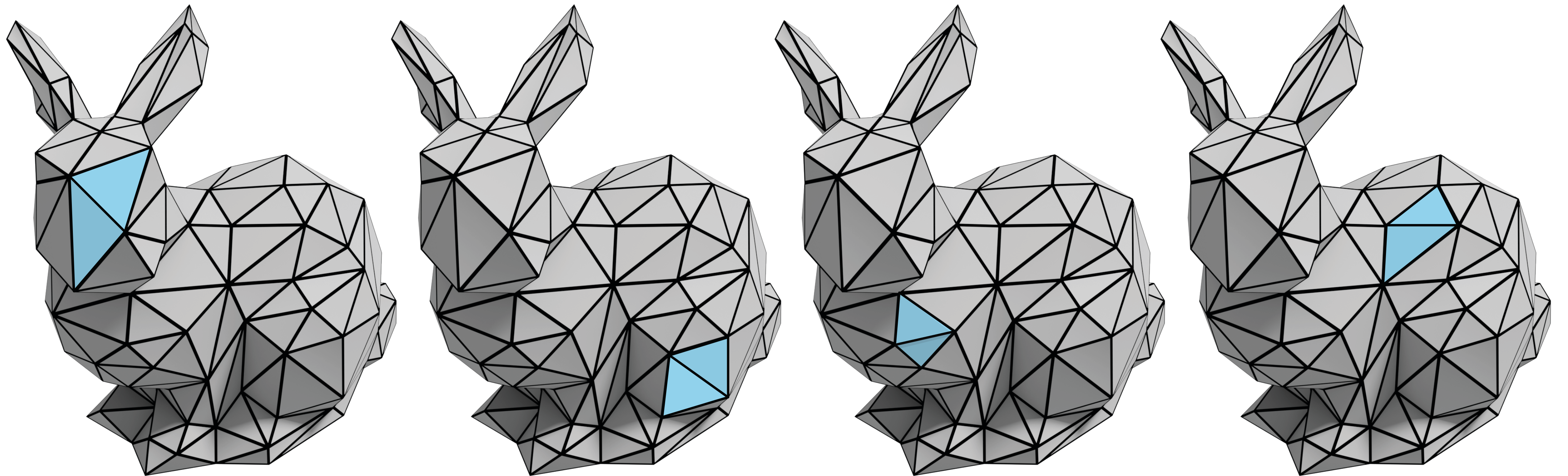
conv. pool conv. unpool



Point2Mesh Overview



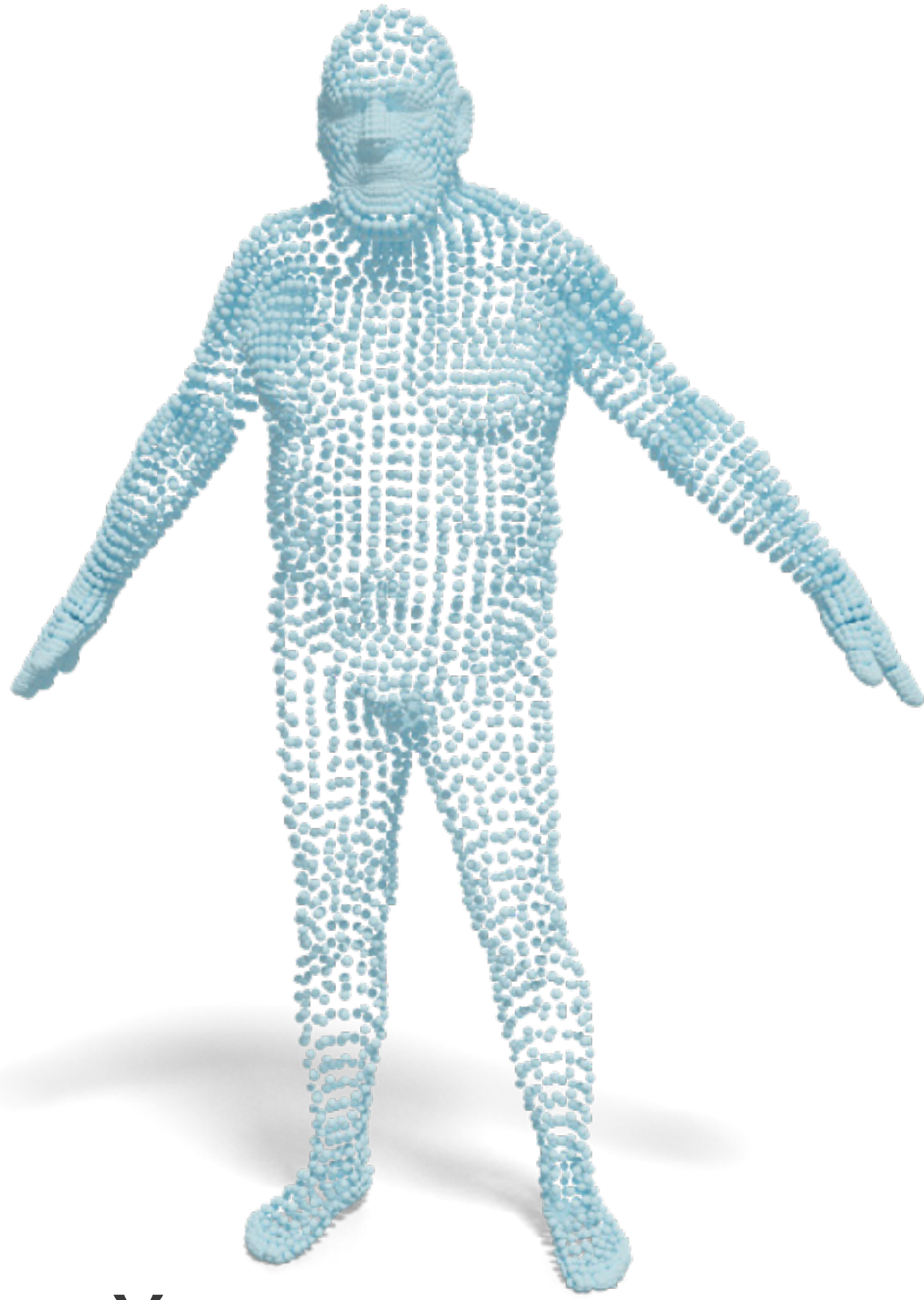
CNN filters are shared



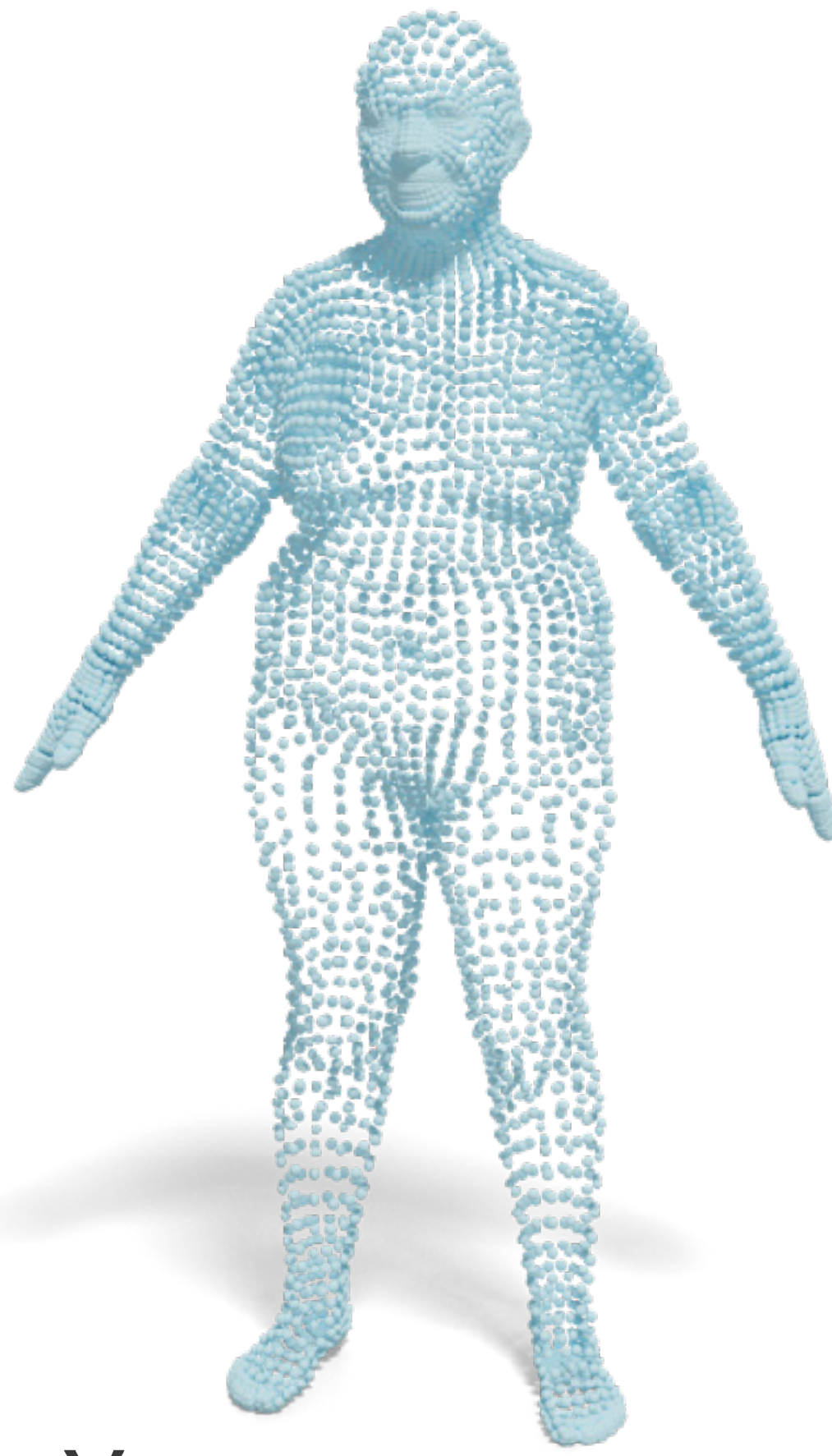
Point2Mesh Overview



Loss Function: Chamfer Distance

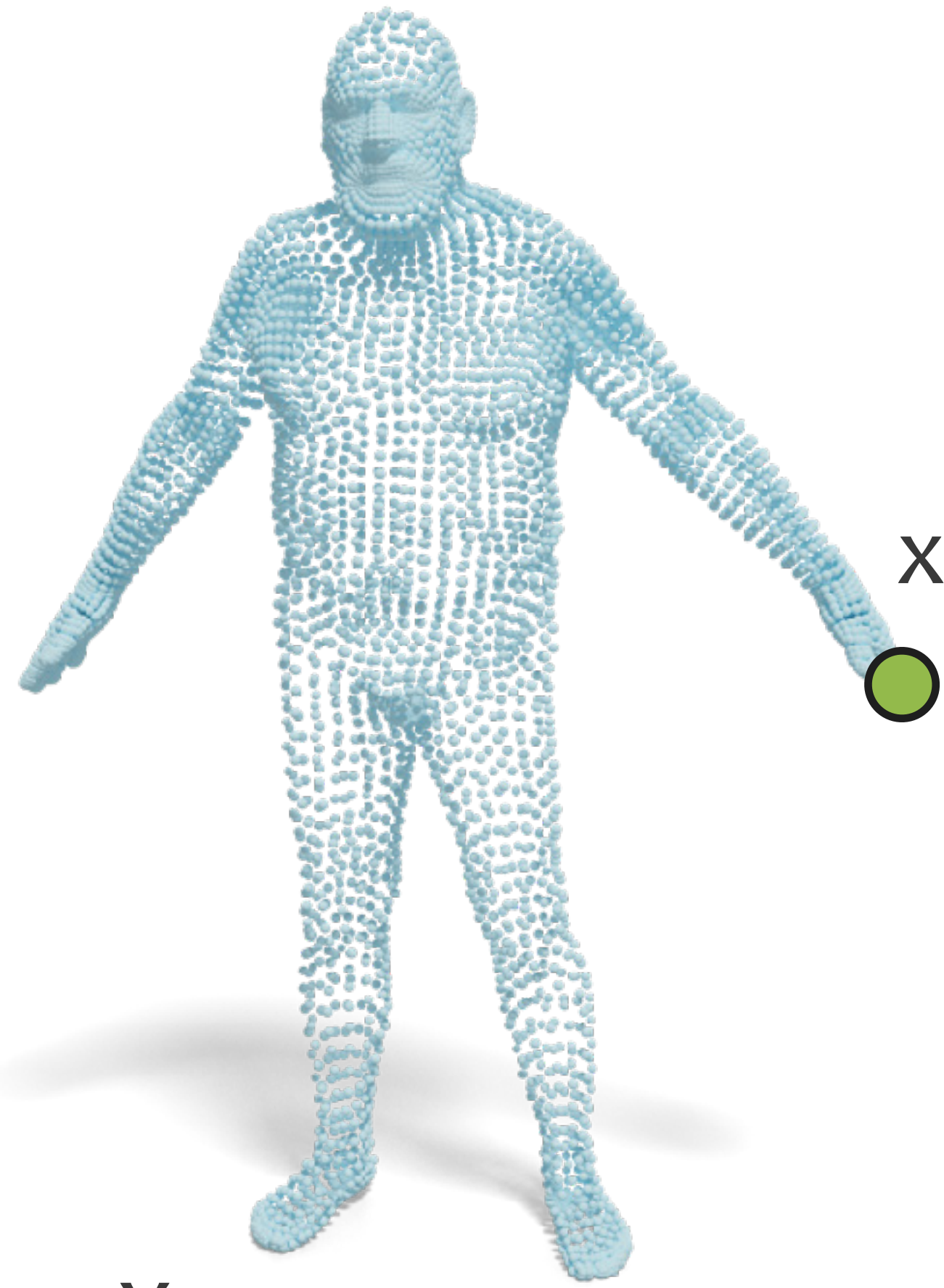


X

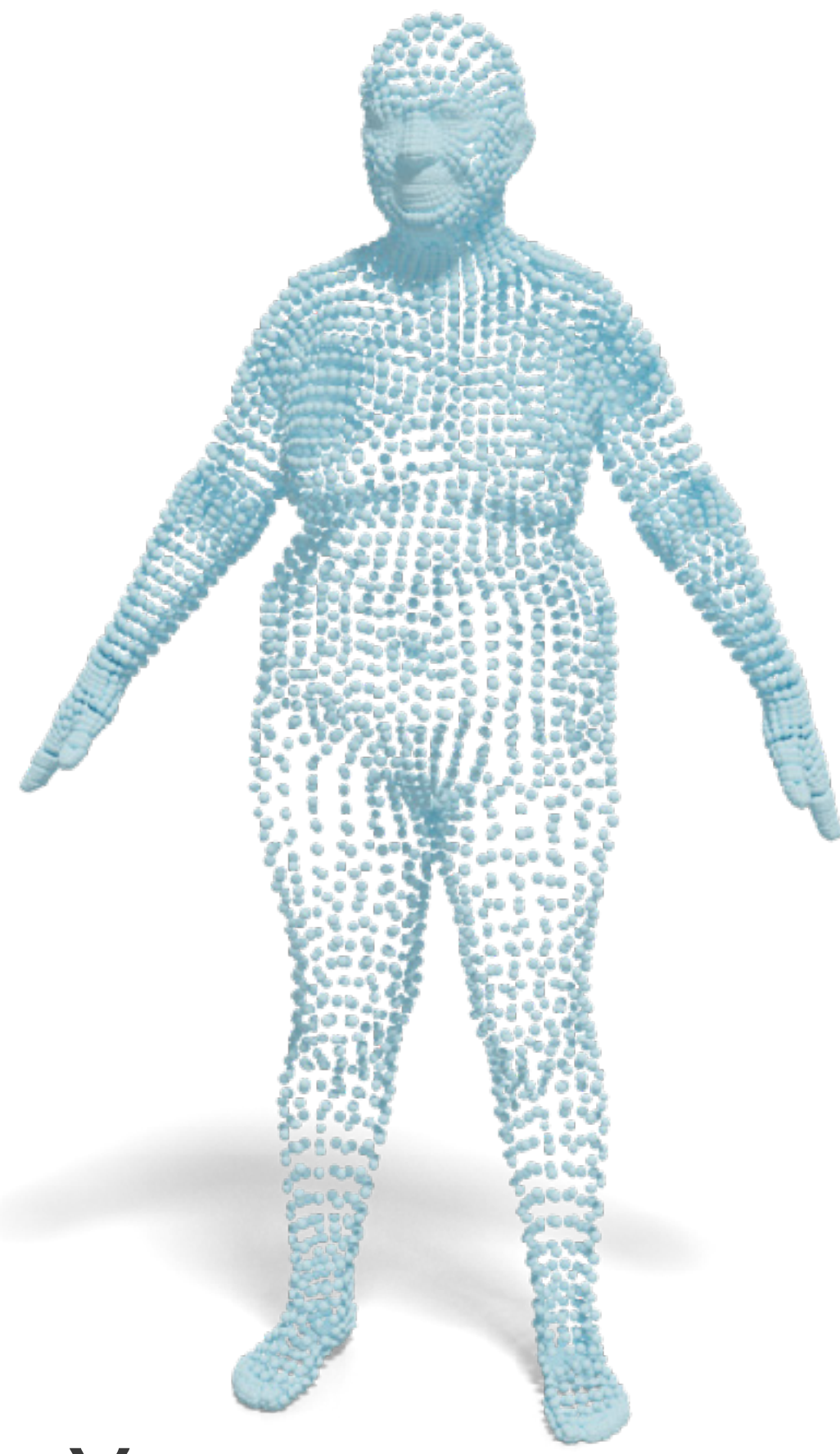


Y

Loss Function: Chamfer Distance



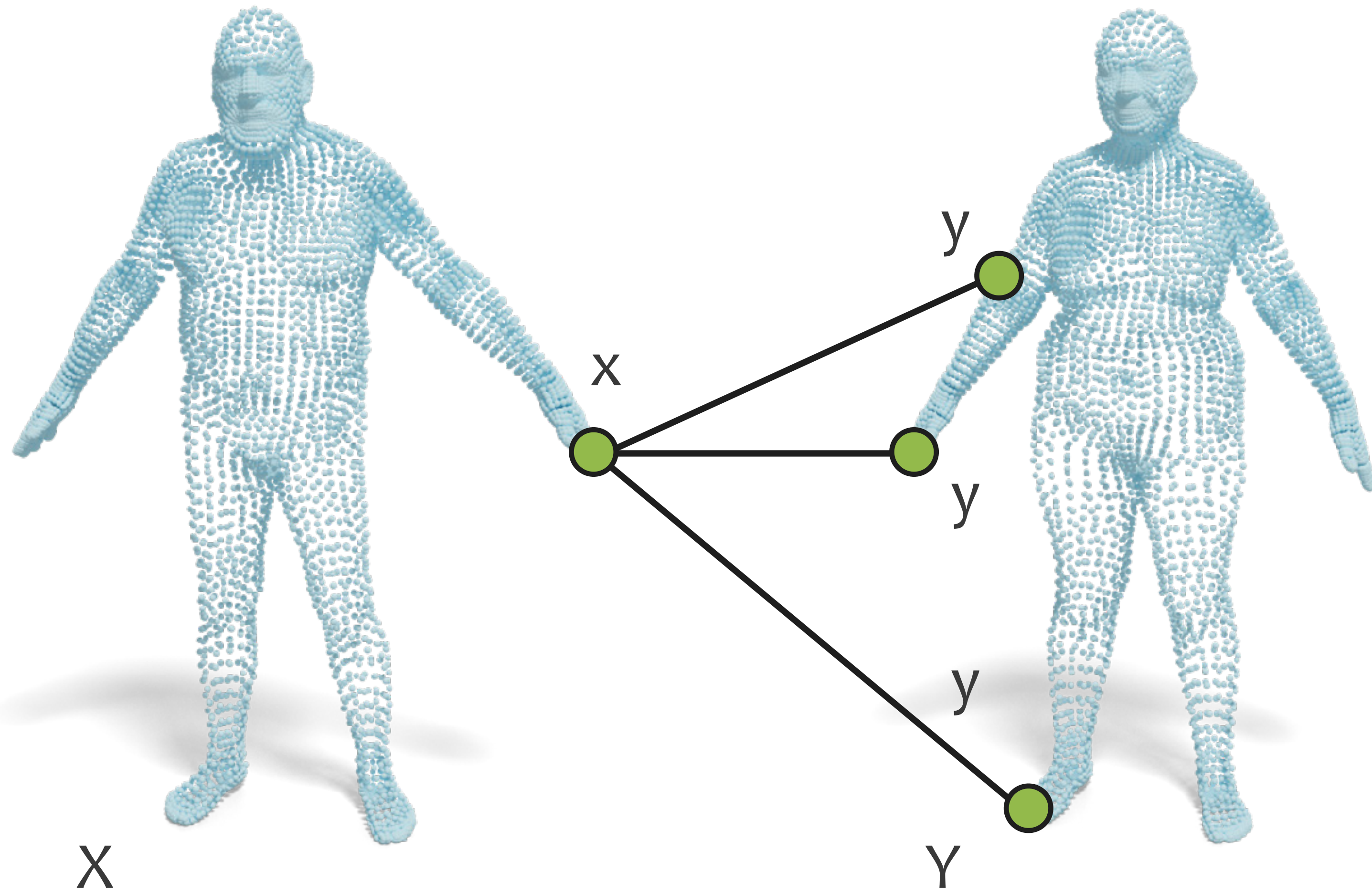
X



Y

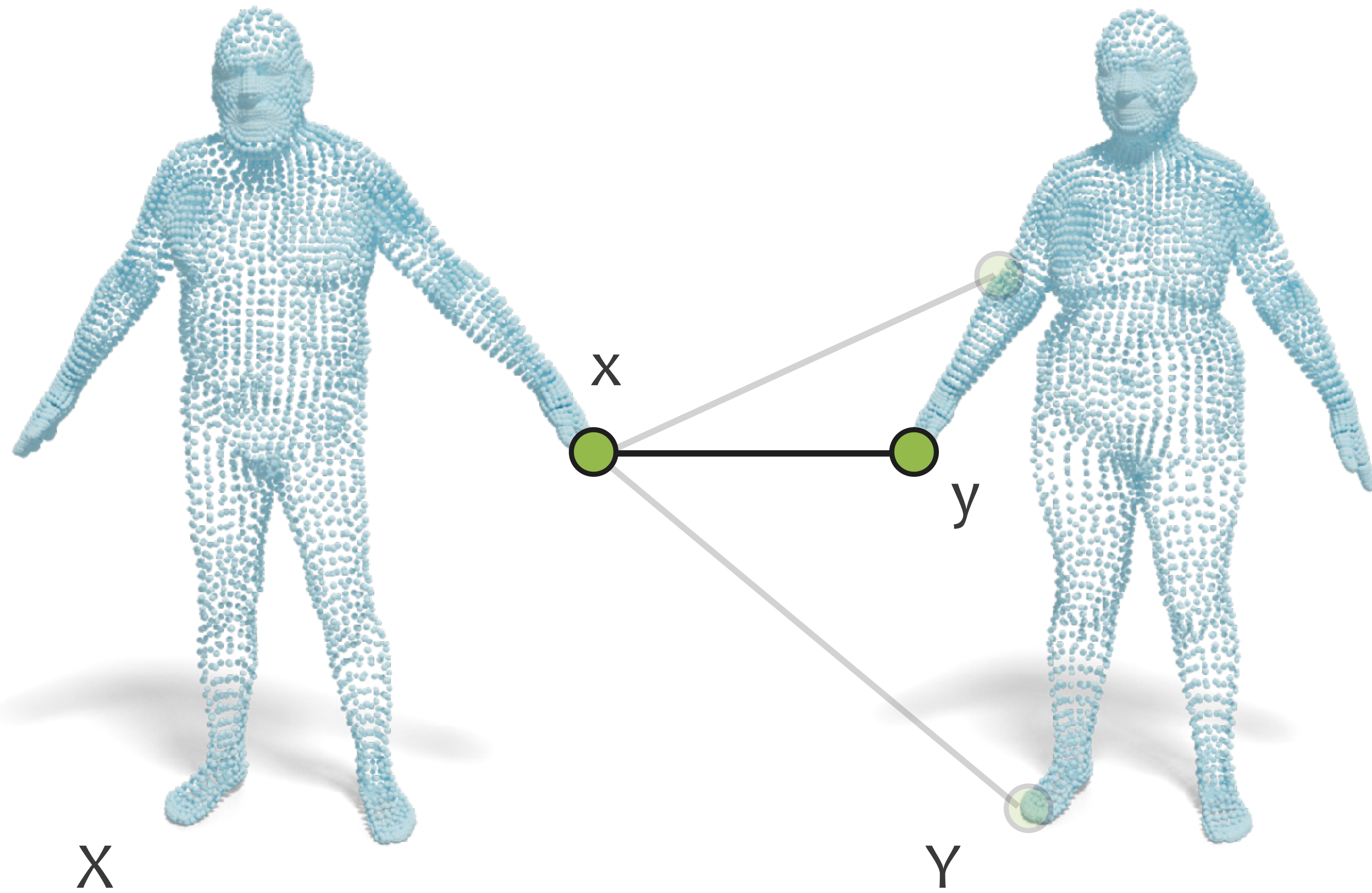
$$\mathcal{J}(X, Y) = \sum_x x$$

Loss Function: Chamfer Distance



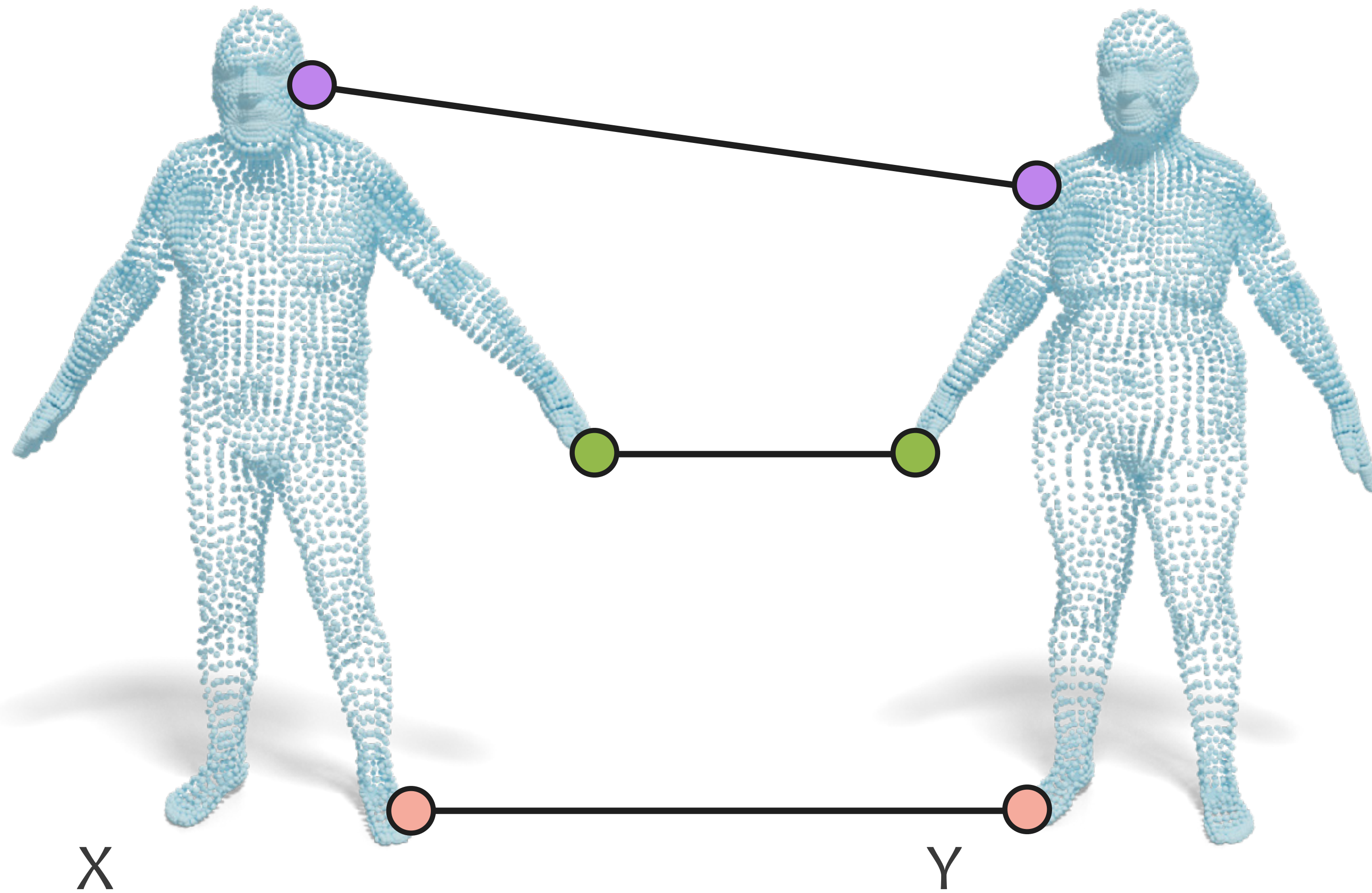
$$\mathcal{J}(X, Y) = \|x - y\|^2$$

Loss Function: Chamfer Distance



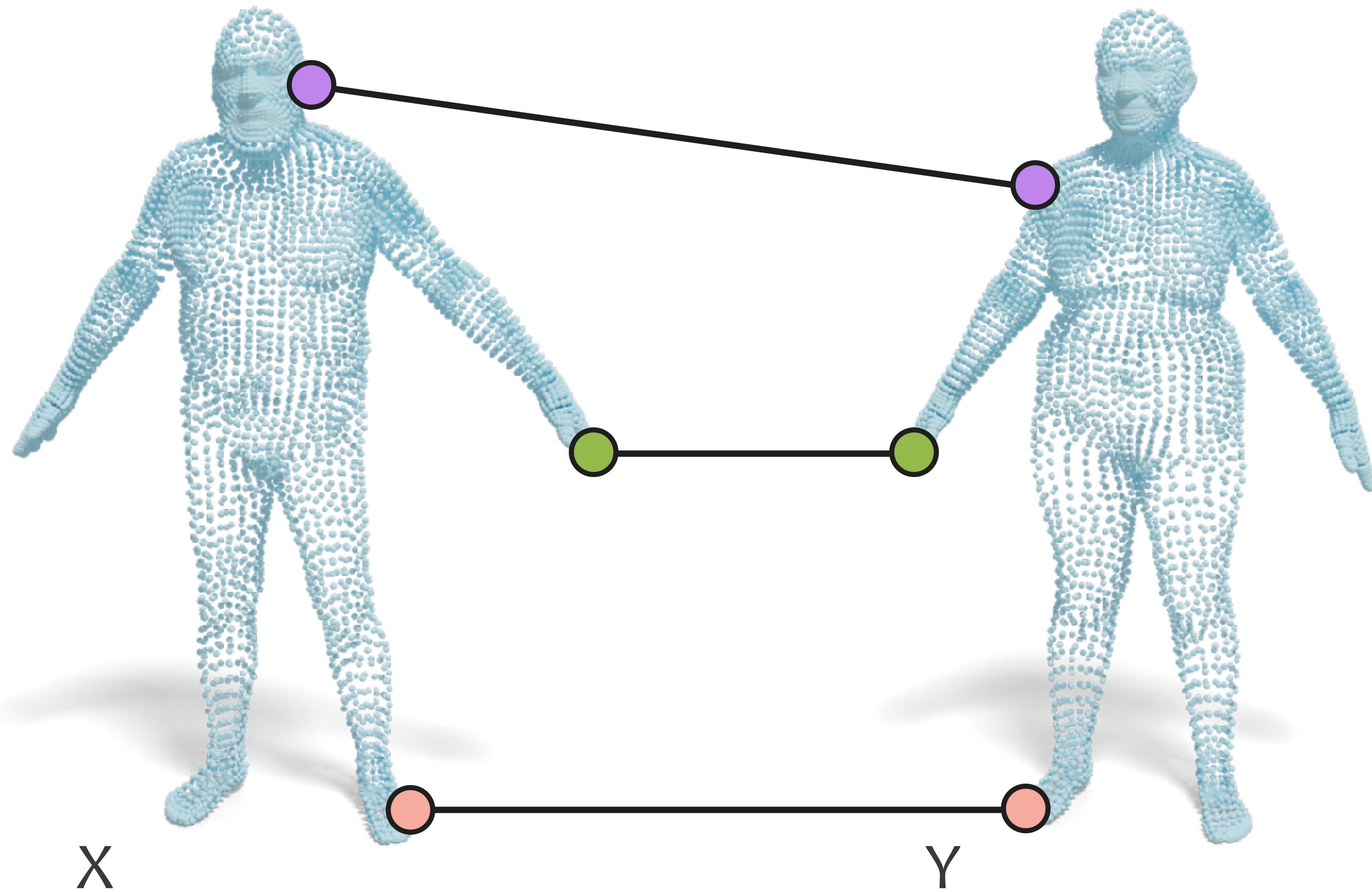
$$\mathcal{J}(X, Y) = \min_{y \in Y} \|x - y\|^2$$

Loss Function: Chamfer Distance



$$\mathcal{J}(X, Y) = \sum_{x \in X} \min_{y \in Y} \|x - y\|^2$$

Loss Function: Chamfer Distance



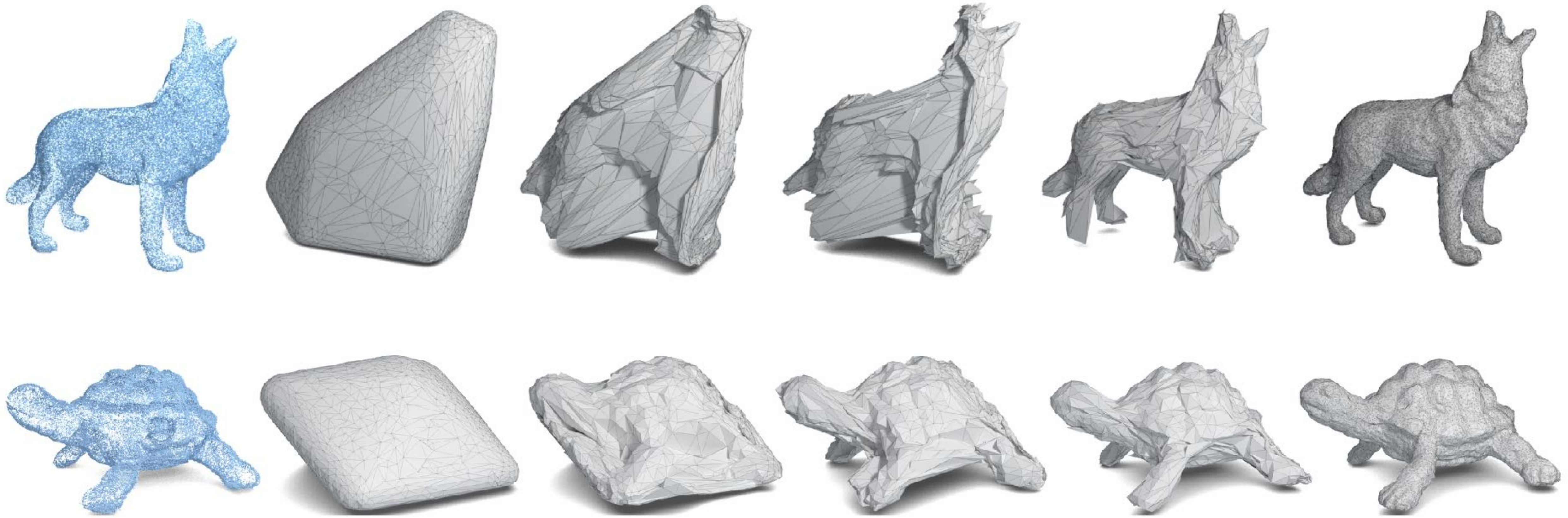
$$\mathcal{J}(X, Y) = \sum_{x \in X} \min_{y \in Y} \|x - y\|^2 + \sum_{y \in Y} \min_{x \in X} \|y - x\|^2$$

bidirectional Chamfer

Optimization

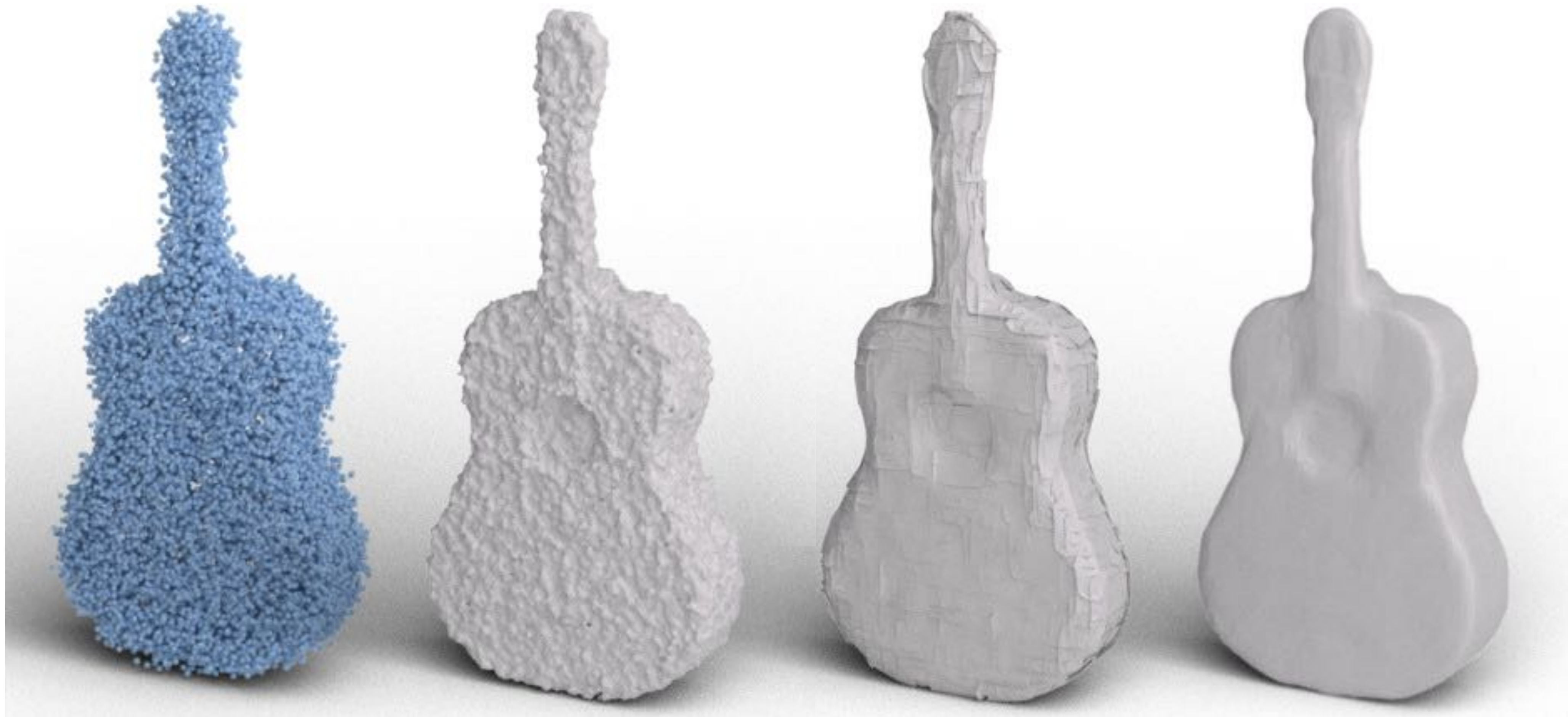


Results



iterations

Denosing



smoothness
prior

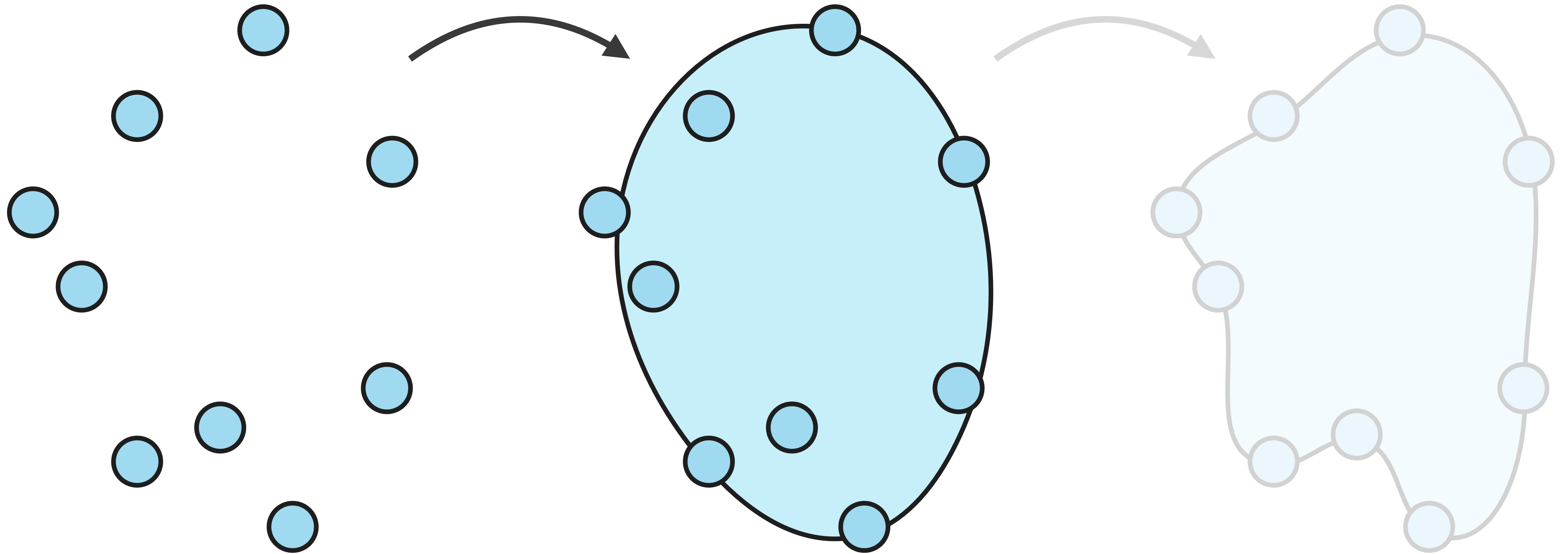
deep
geometric prior

self-prior

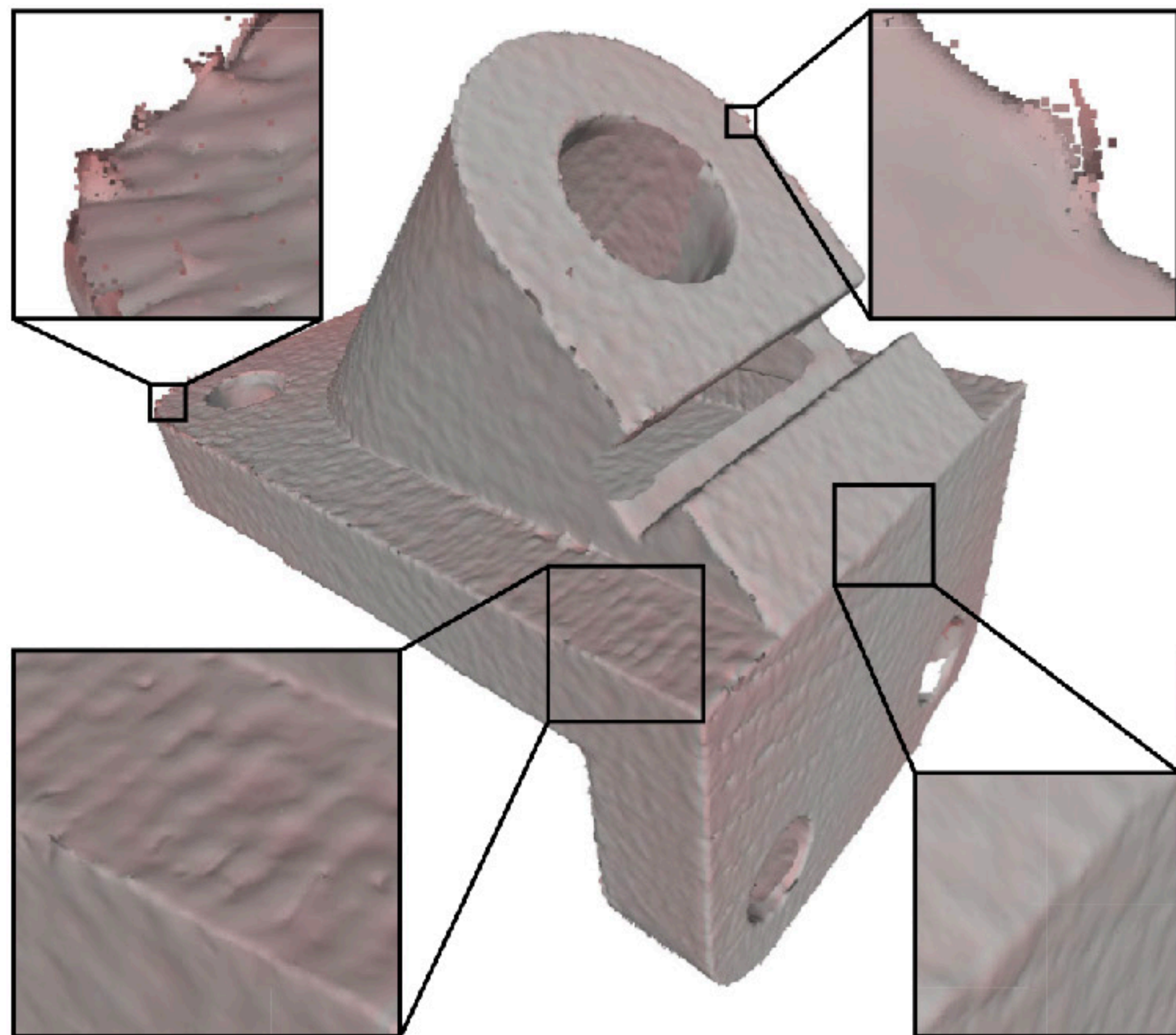
Early-stop as a regularization

train for a while

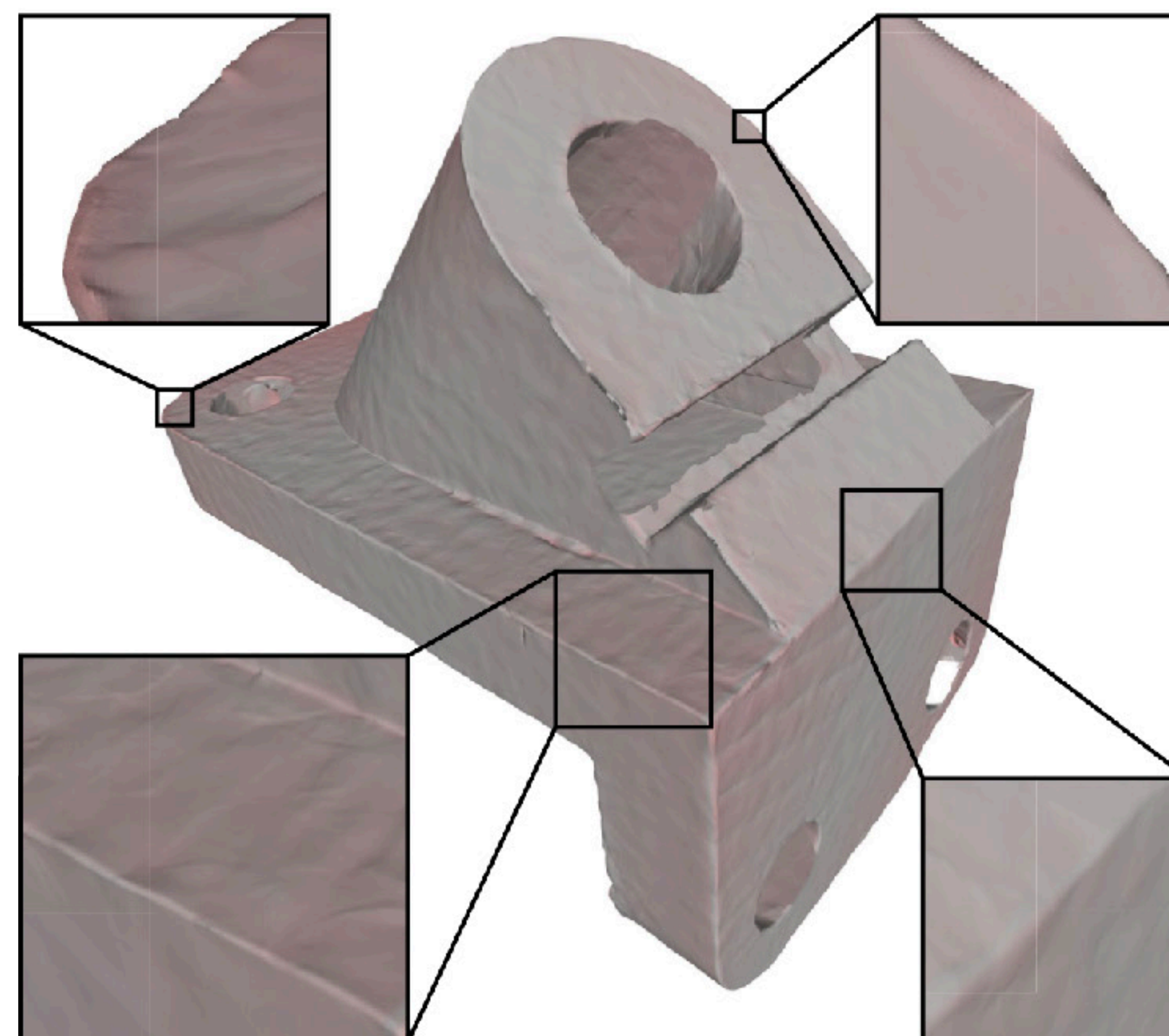
train until converge



Early-Stop Regularization

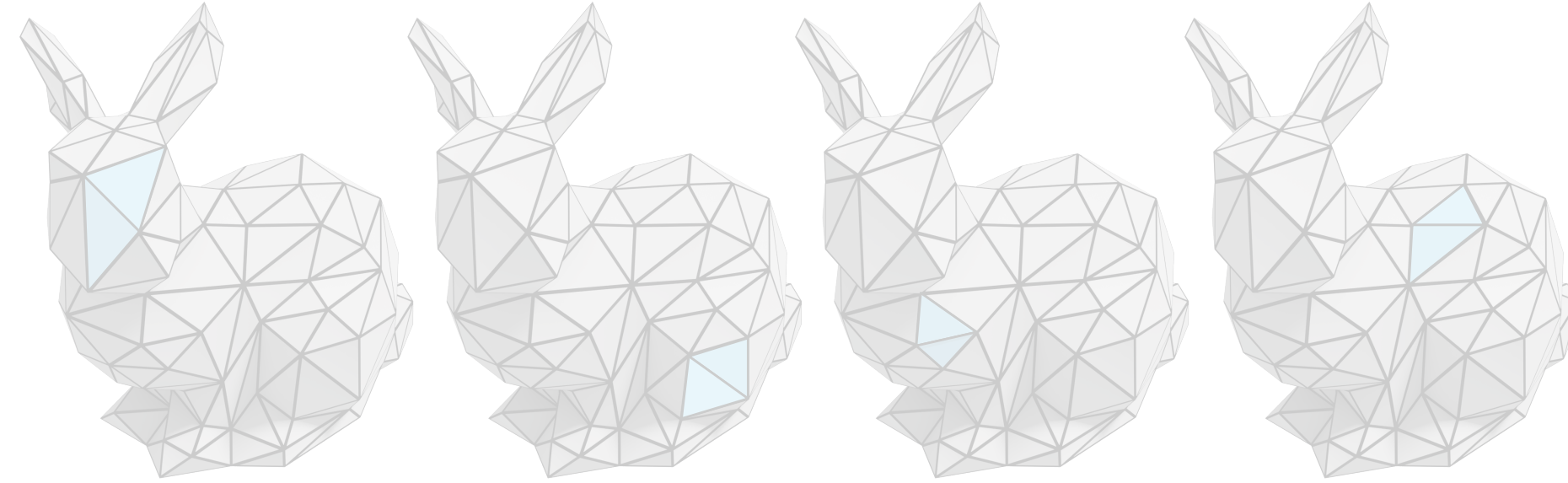


Classic



deep geometric prior

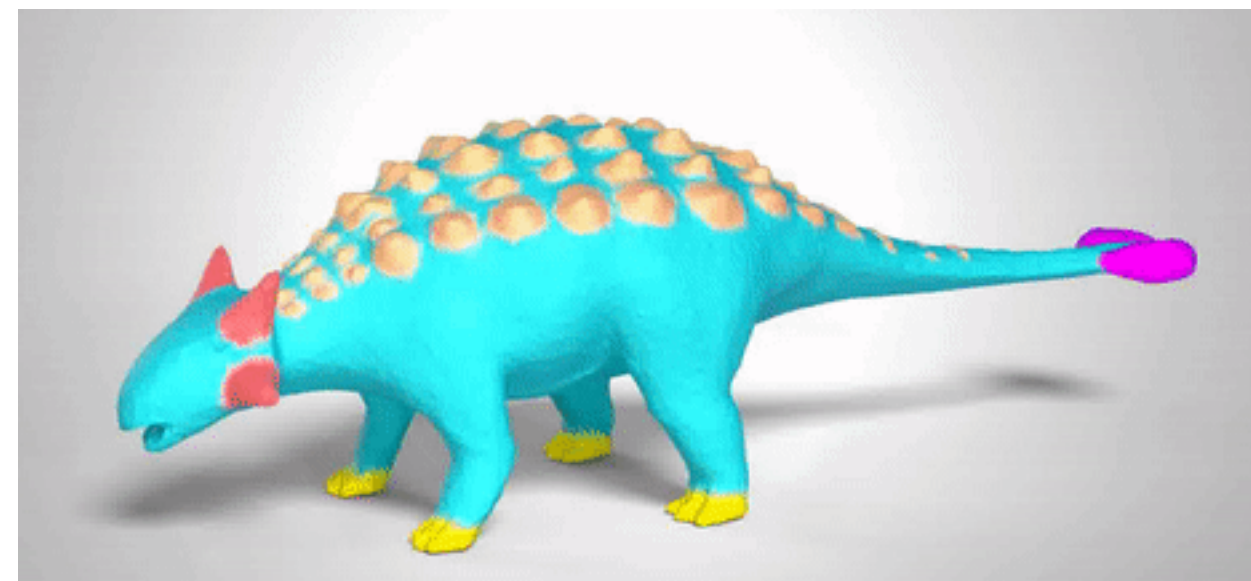
Mesh Convolutional Neural Networks



Machine Learning & Geometry Processing



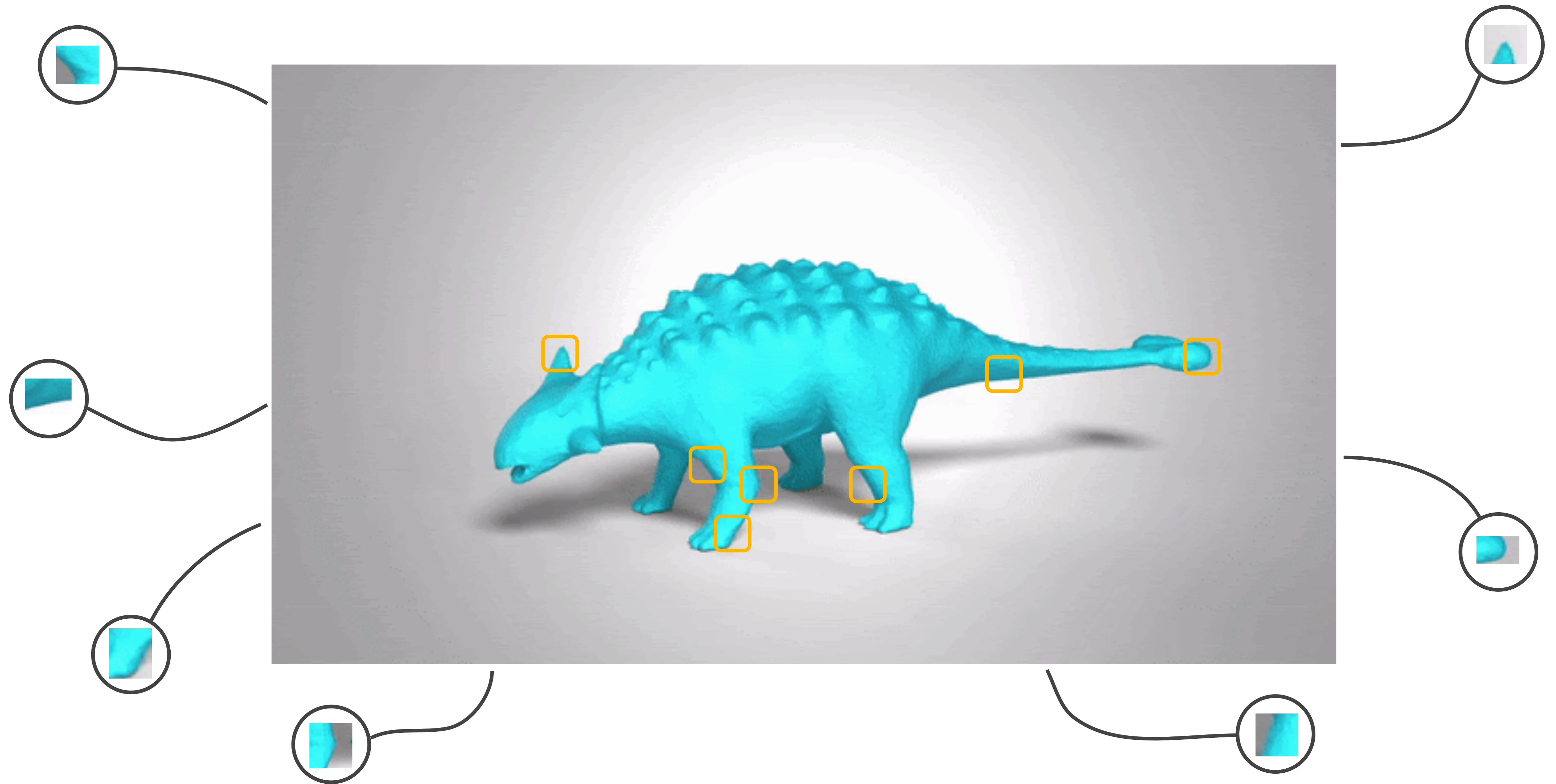
Learning from a Single Mesh



Learning from external data



Learning from internal data



Example: Mesh Upsampling

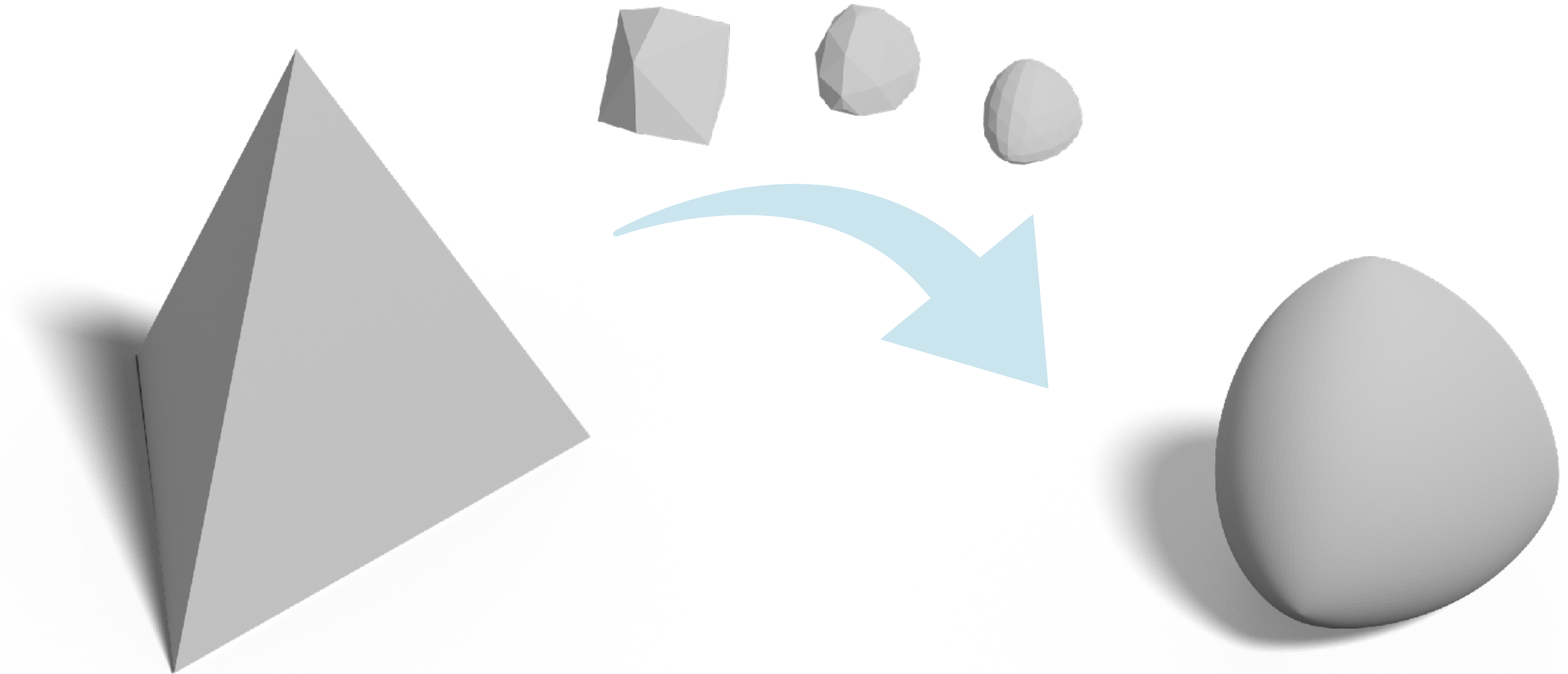


Image Upsampling

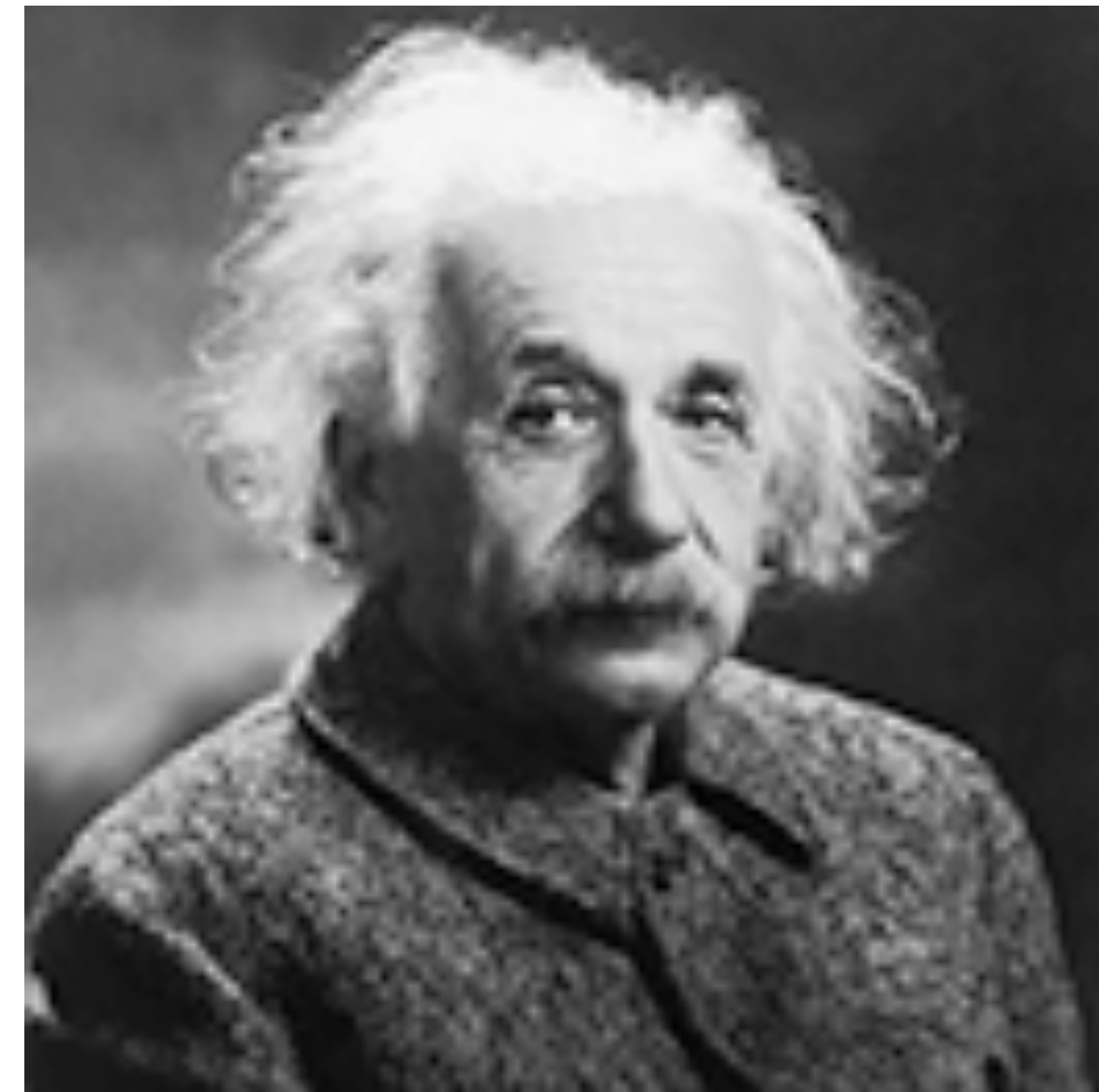
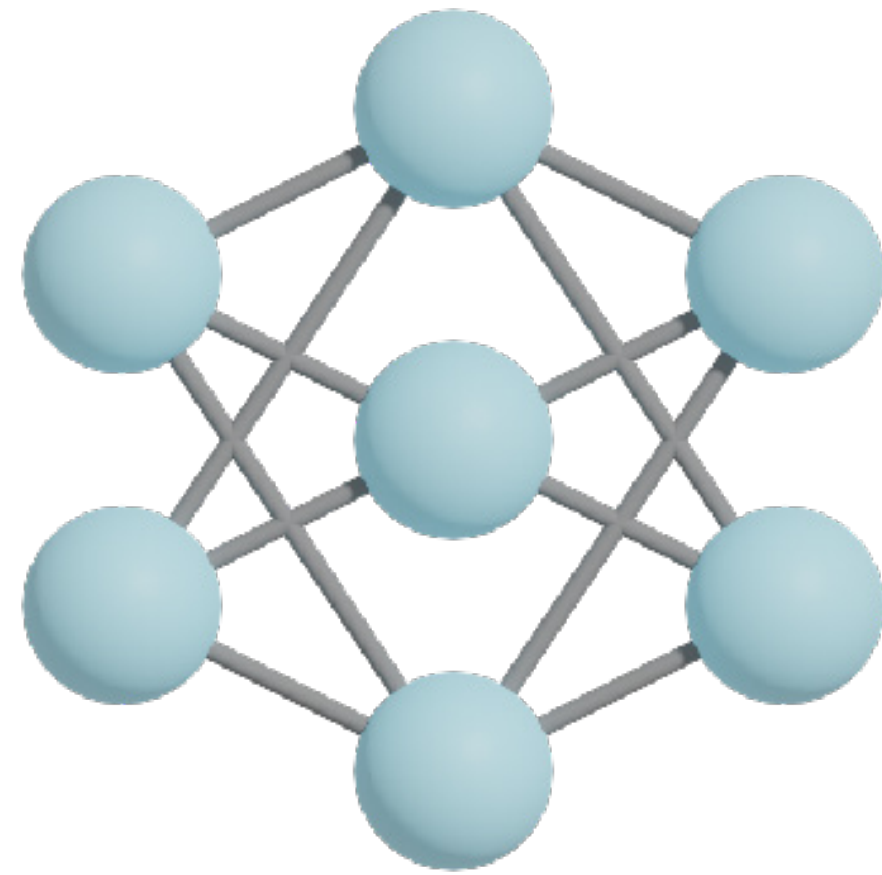
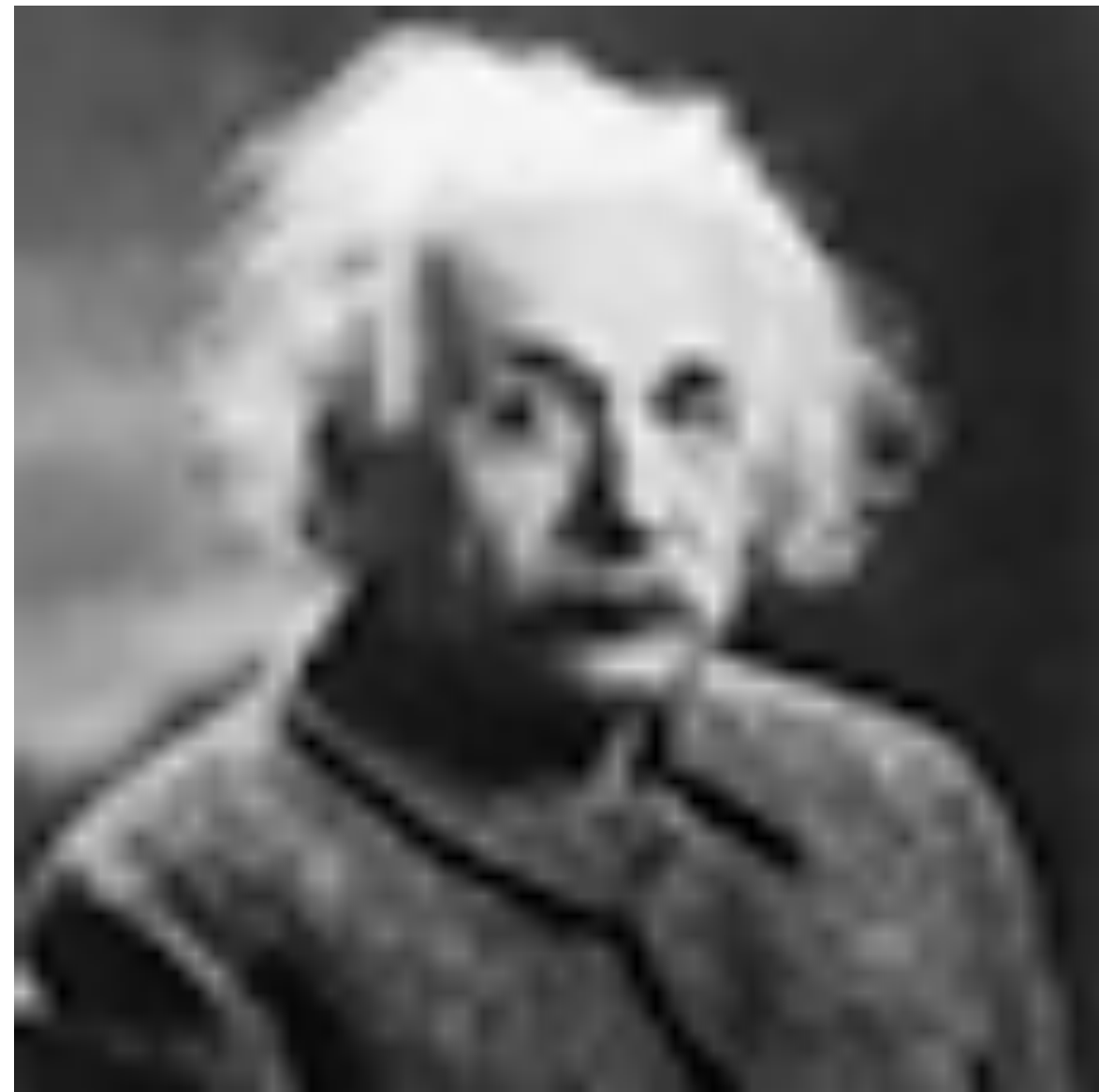
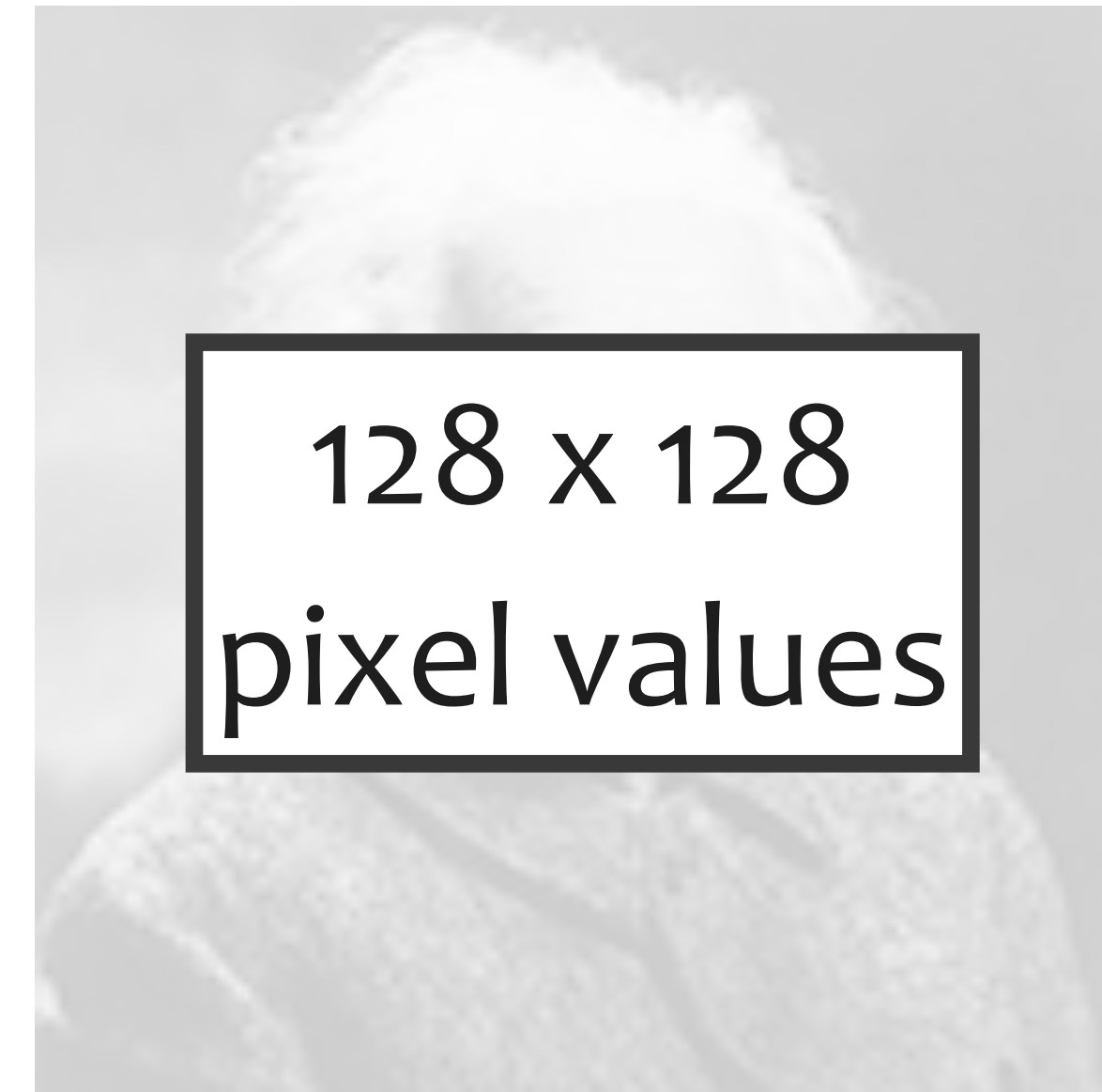
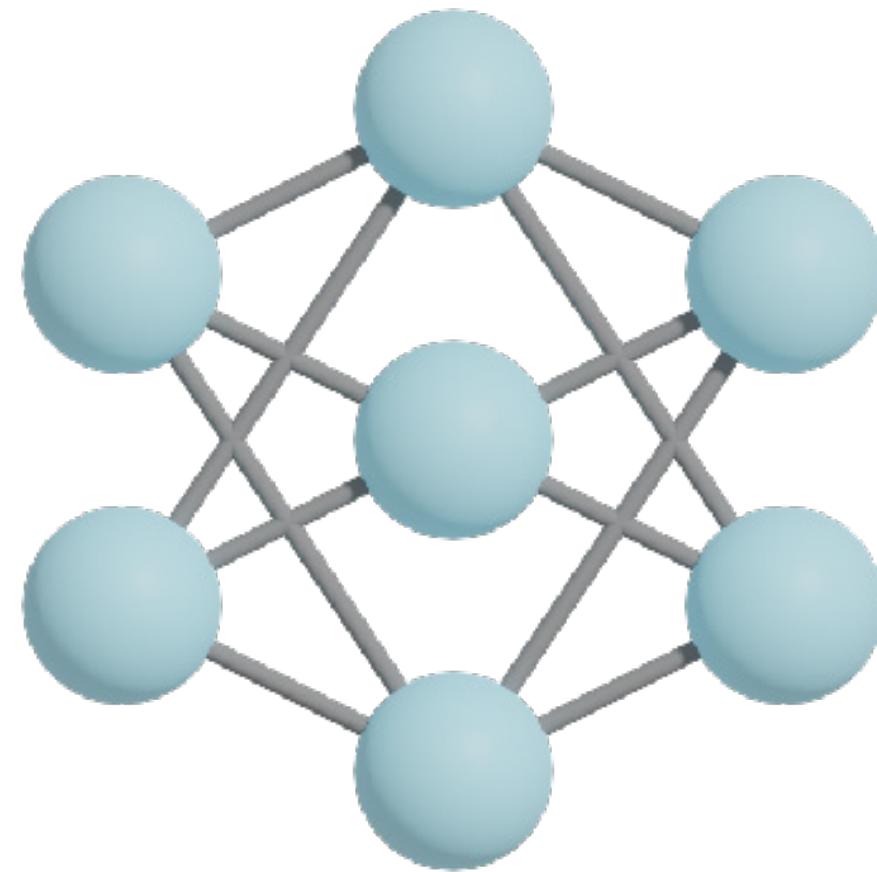
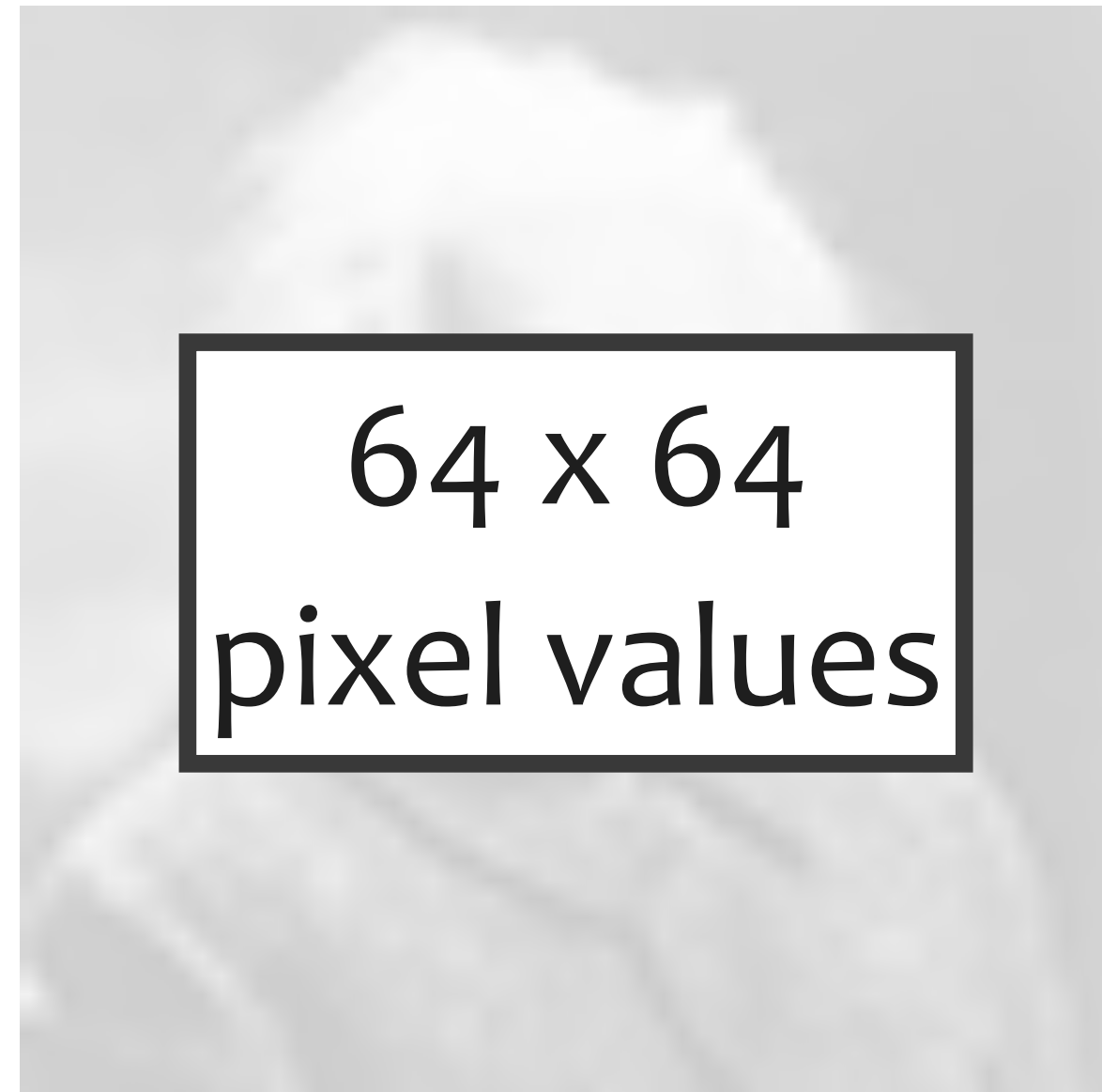


Image Upsampling

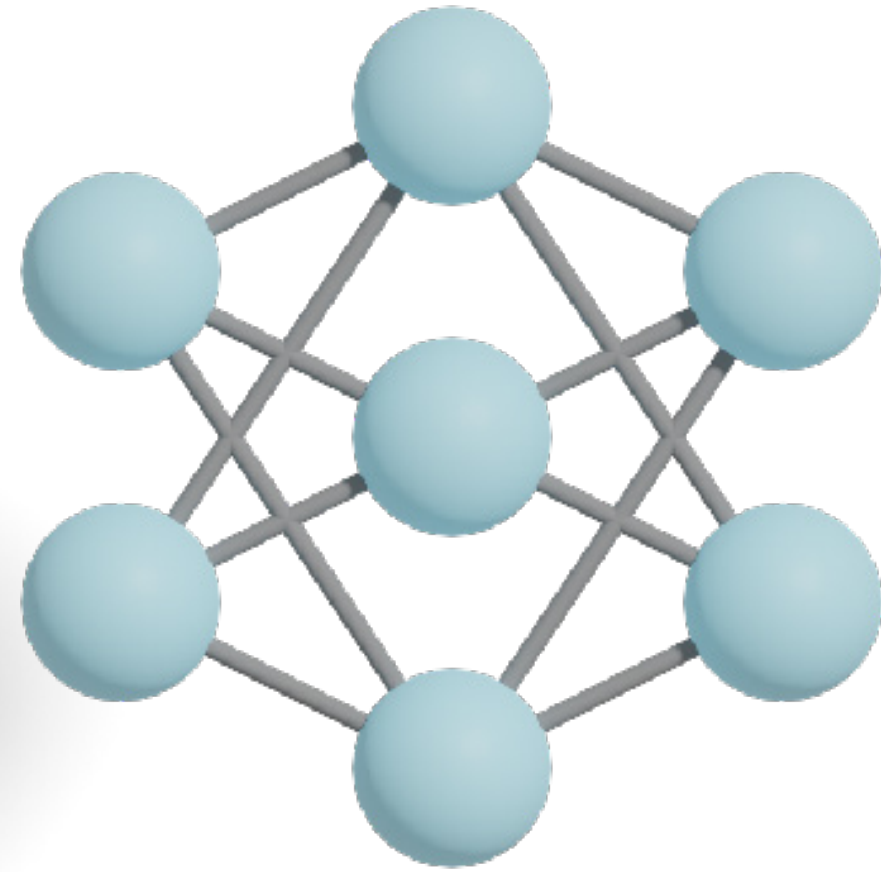
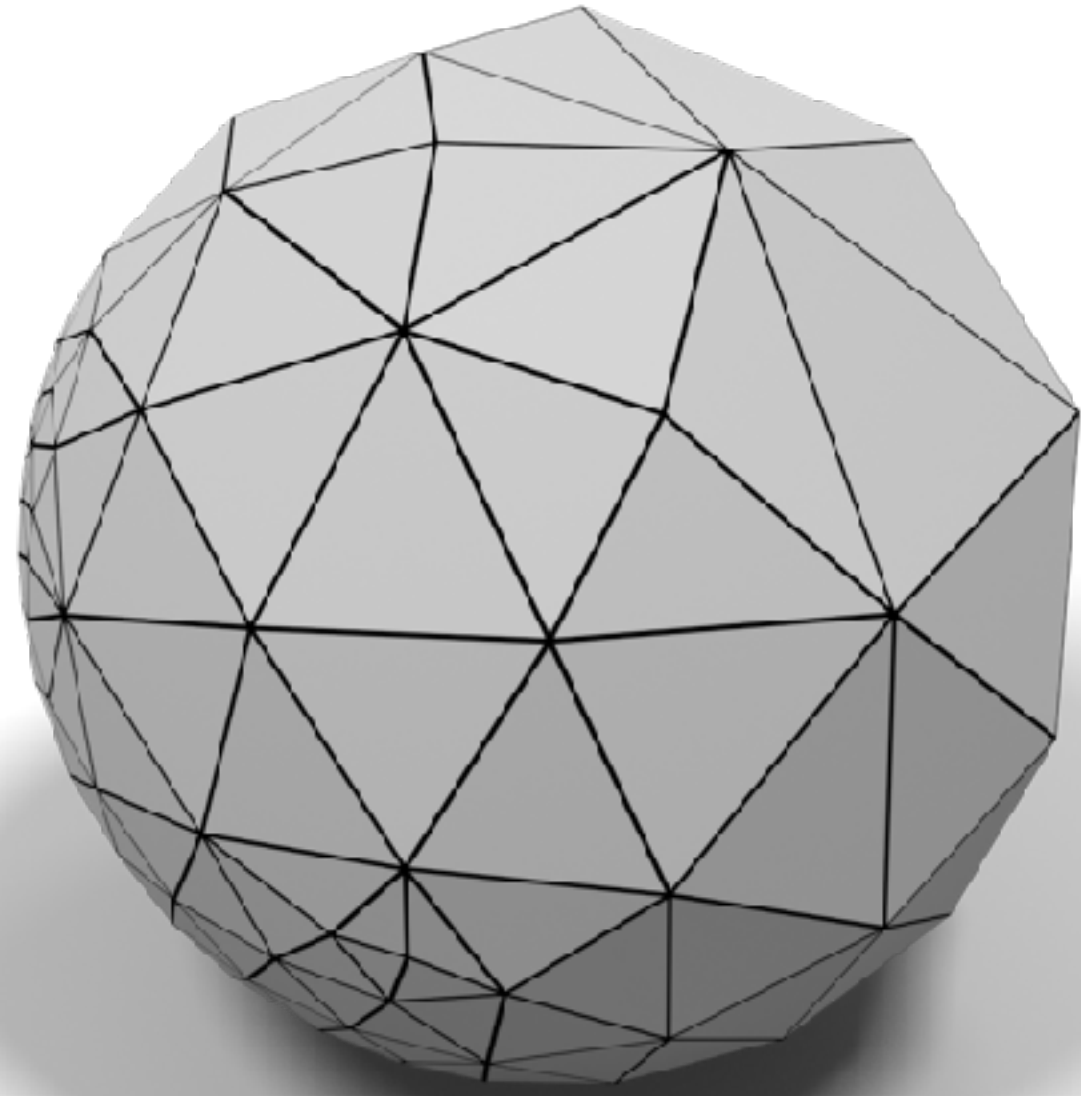


- assume image size 64
- assume grid structure
- assume top-left to bottom-right
- assume upright position

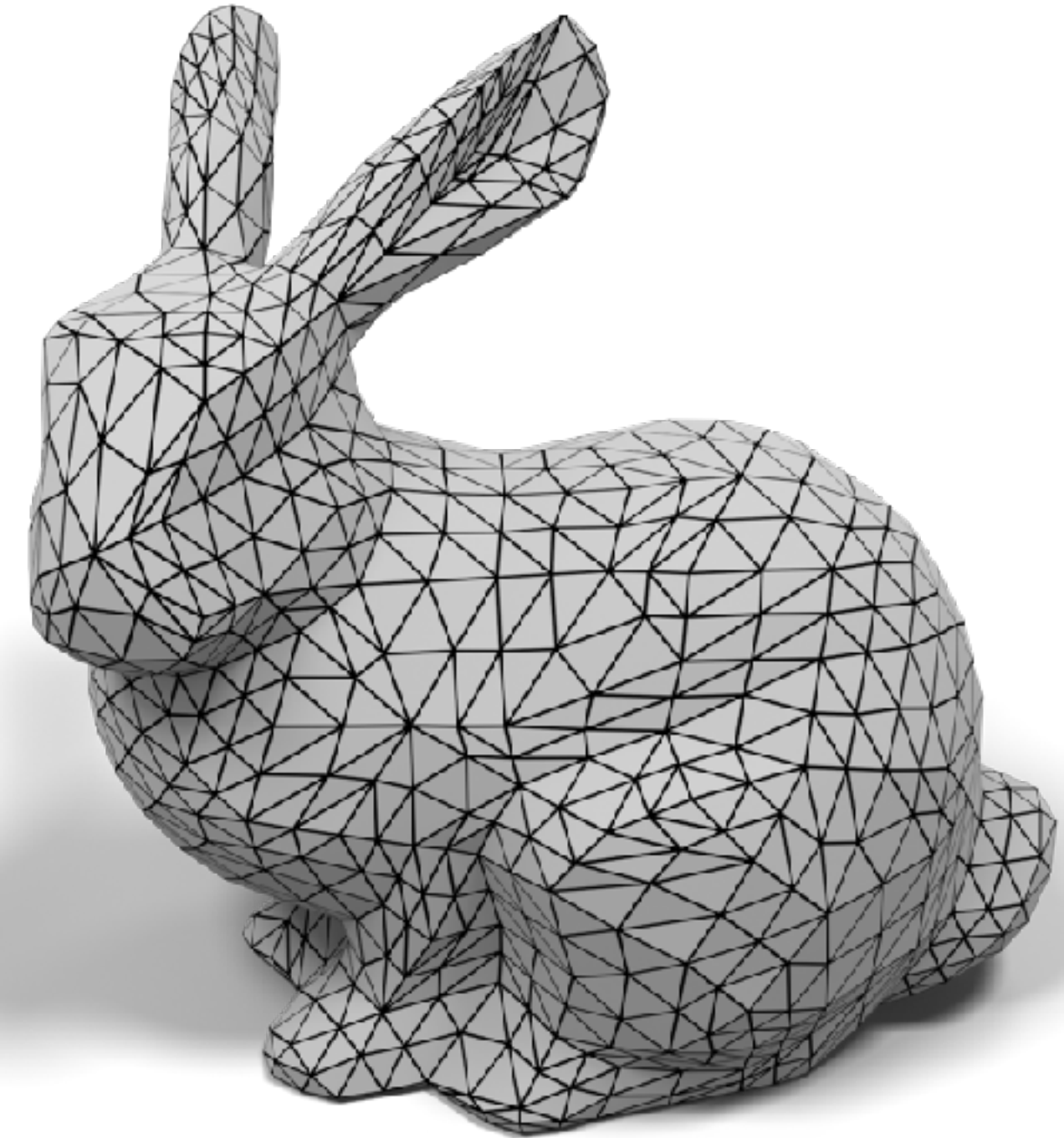


- assume image size 128
- assume grid structure
- assume top-left to bottom-right
- assume upright position

Draw inspiration from images

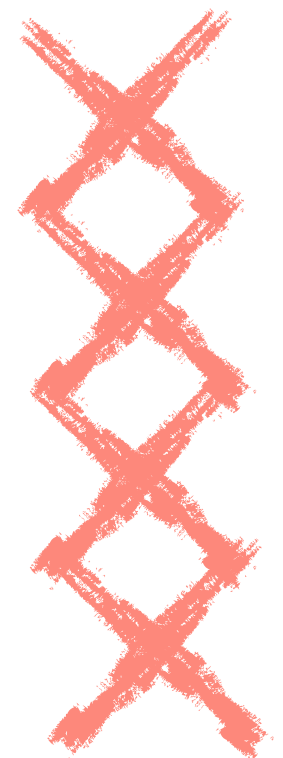
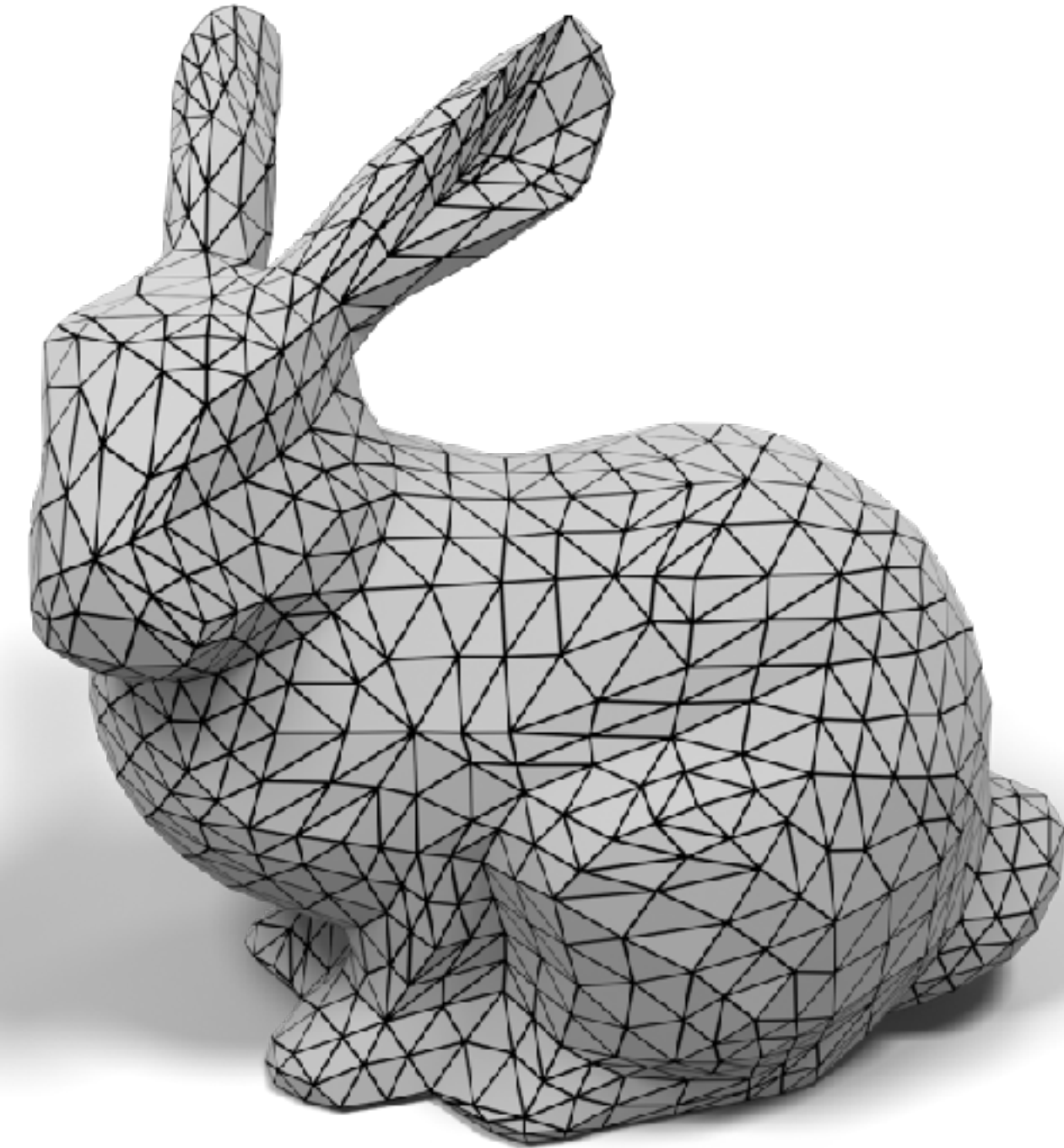
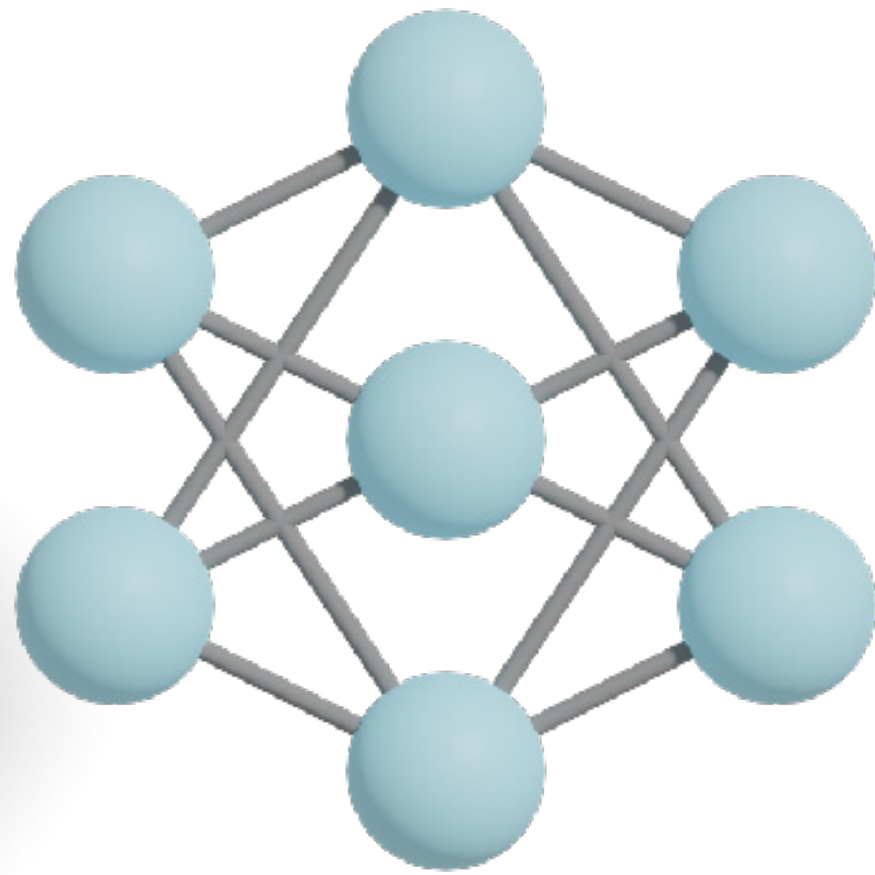
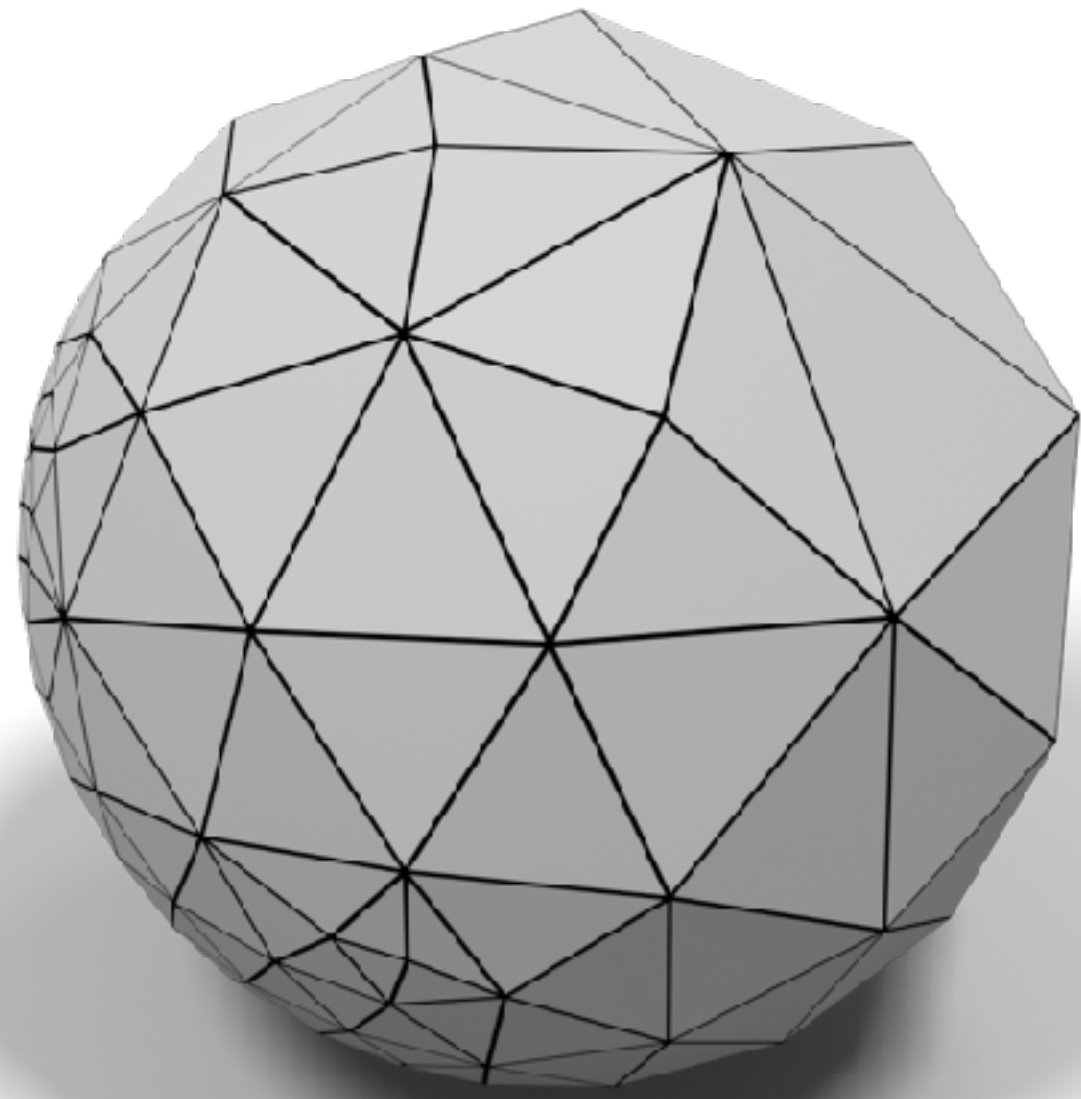


- assume image size 64
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- assume upright position

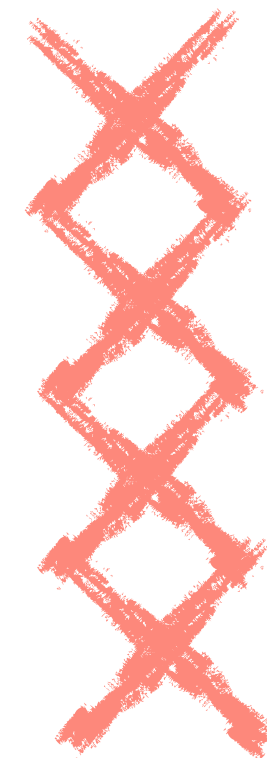


- assume image size 128
- assume grid structure
- assume top-left to bottom-right
- assume upright position

Draw inspiration from images

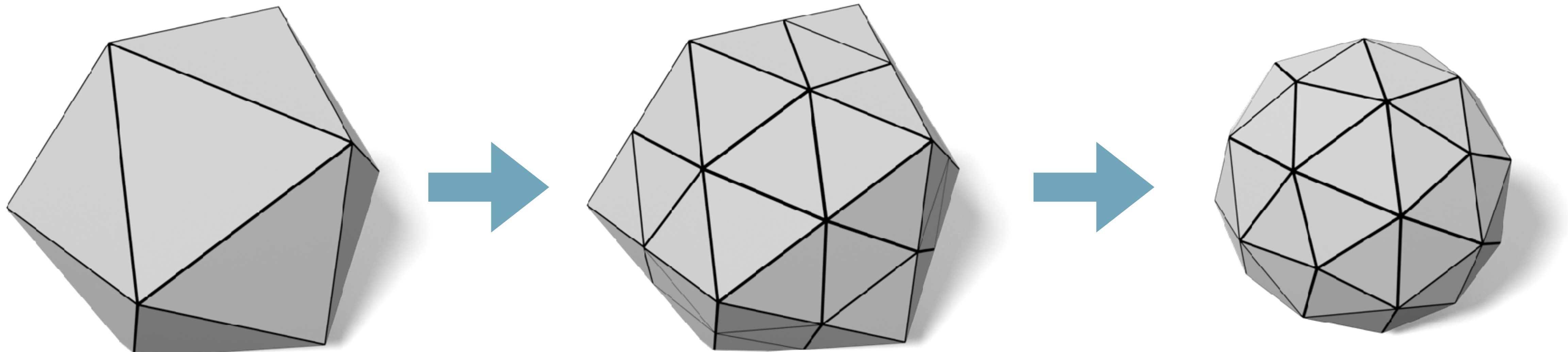
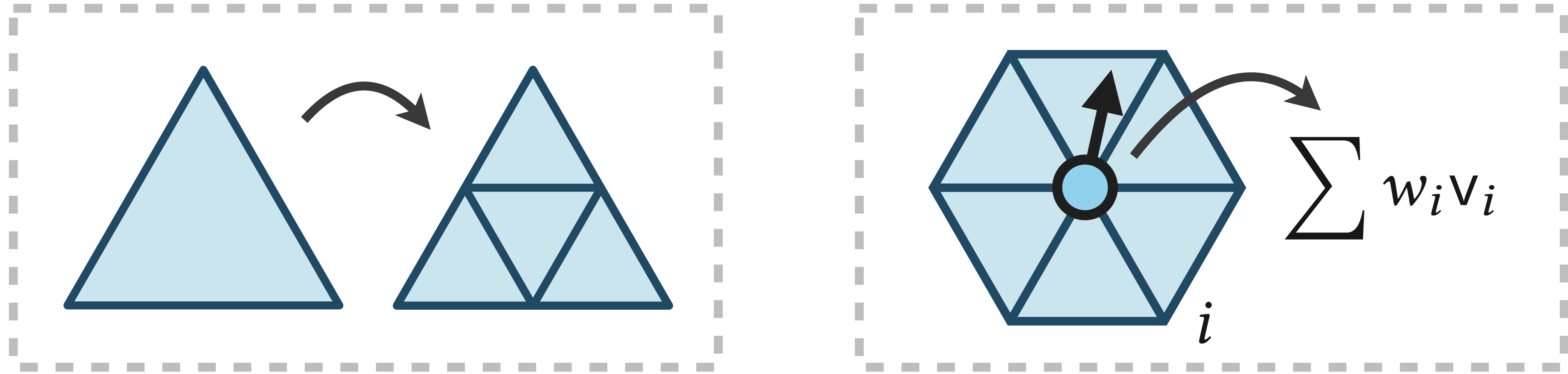


- assume 269 vertices
- assume a specific connectivity
- assume a specific ordering
- assume a specific orientation

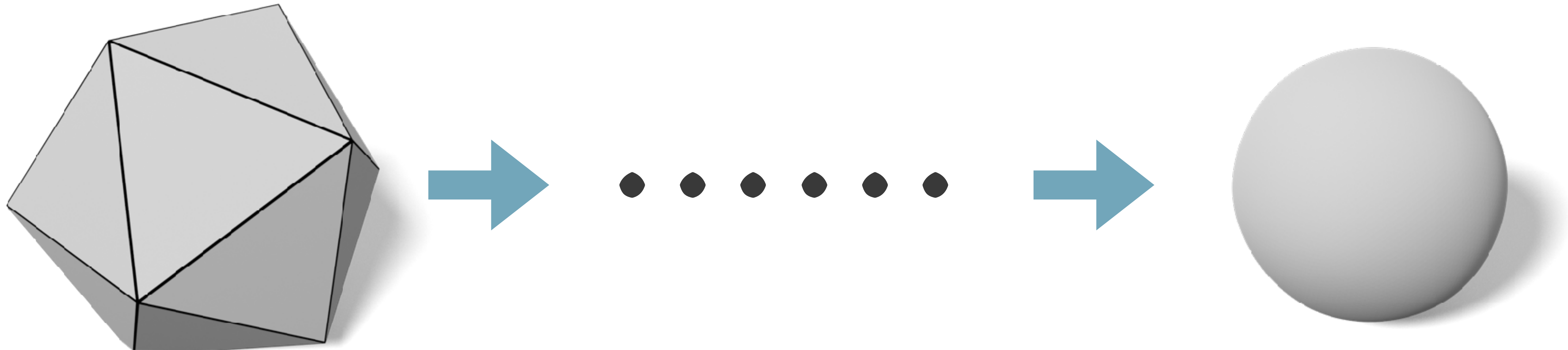
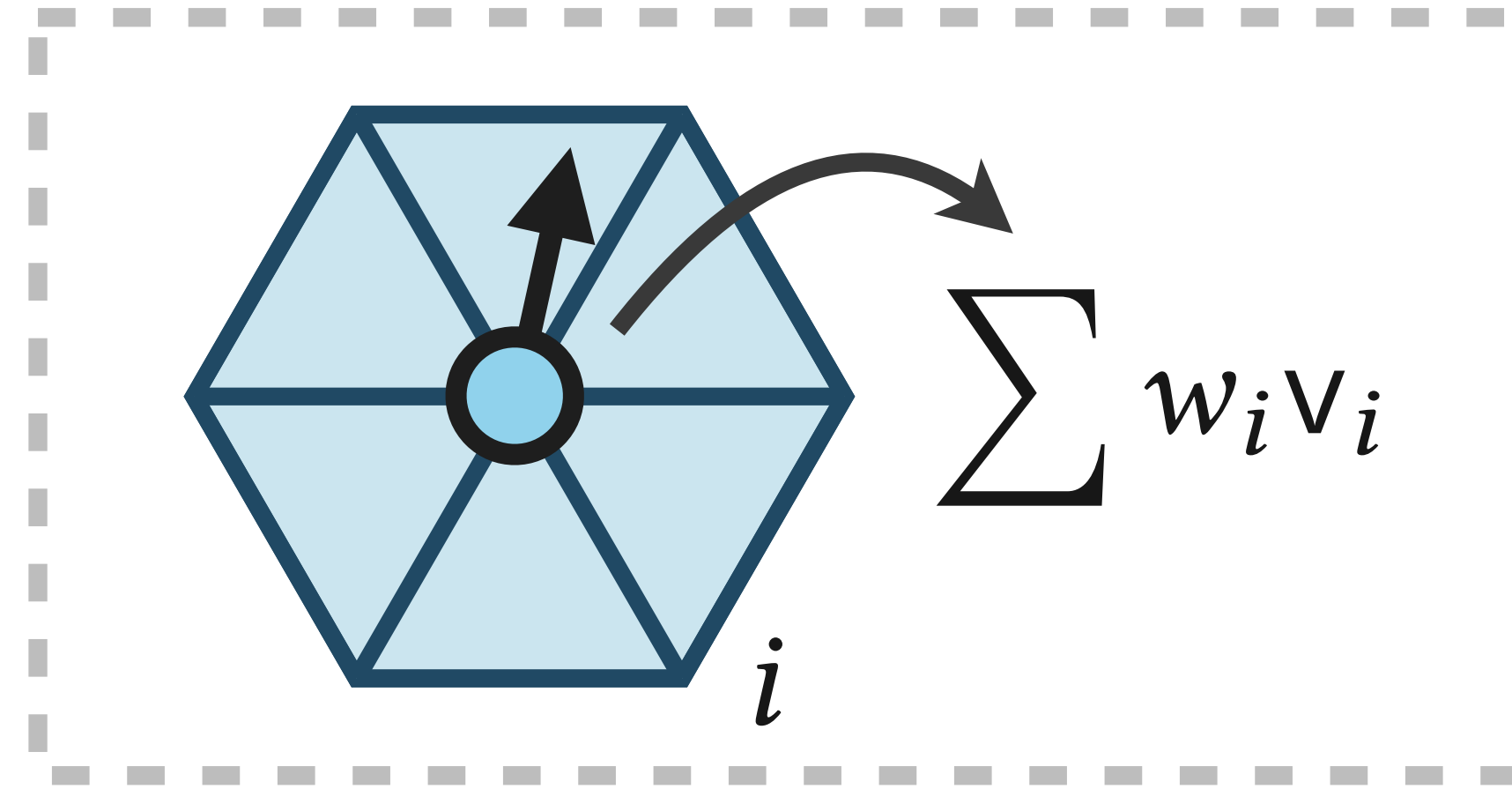
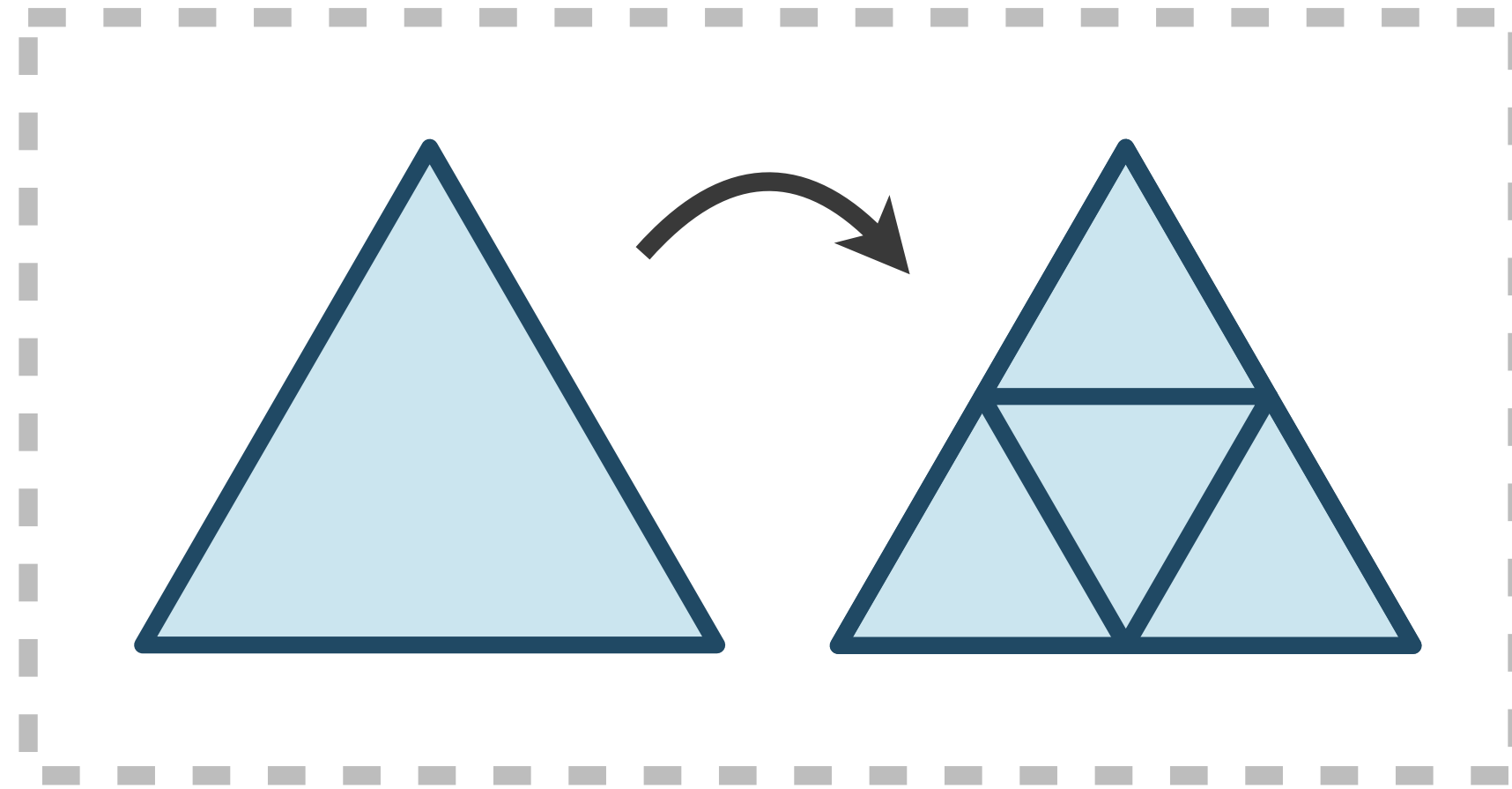


- assume 1070 vertices
- assume a specific connectivity
- assume a specific ordering
- assume a specific orientation

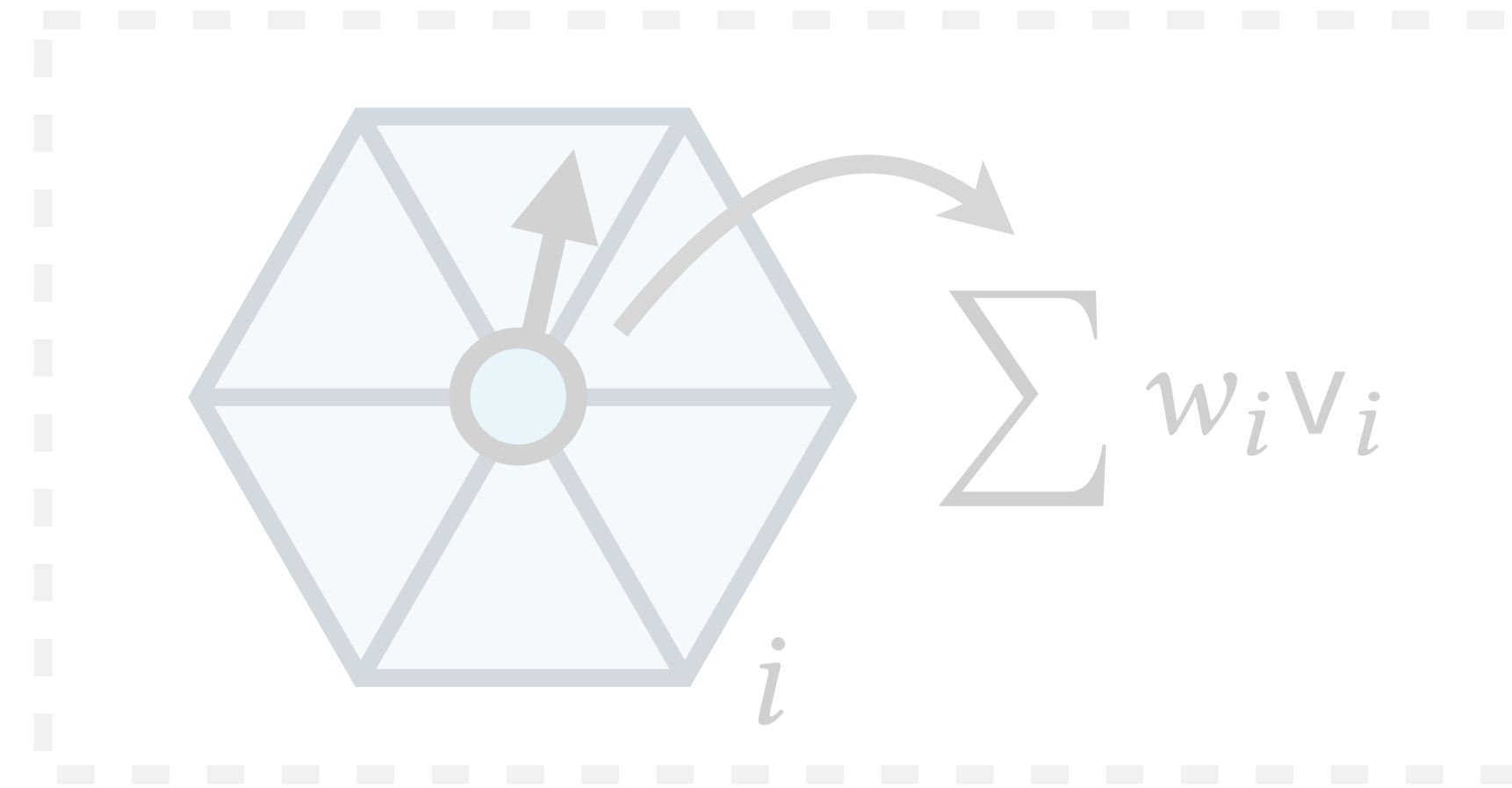
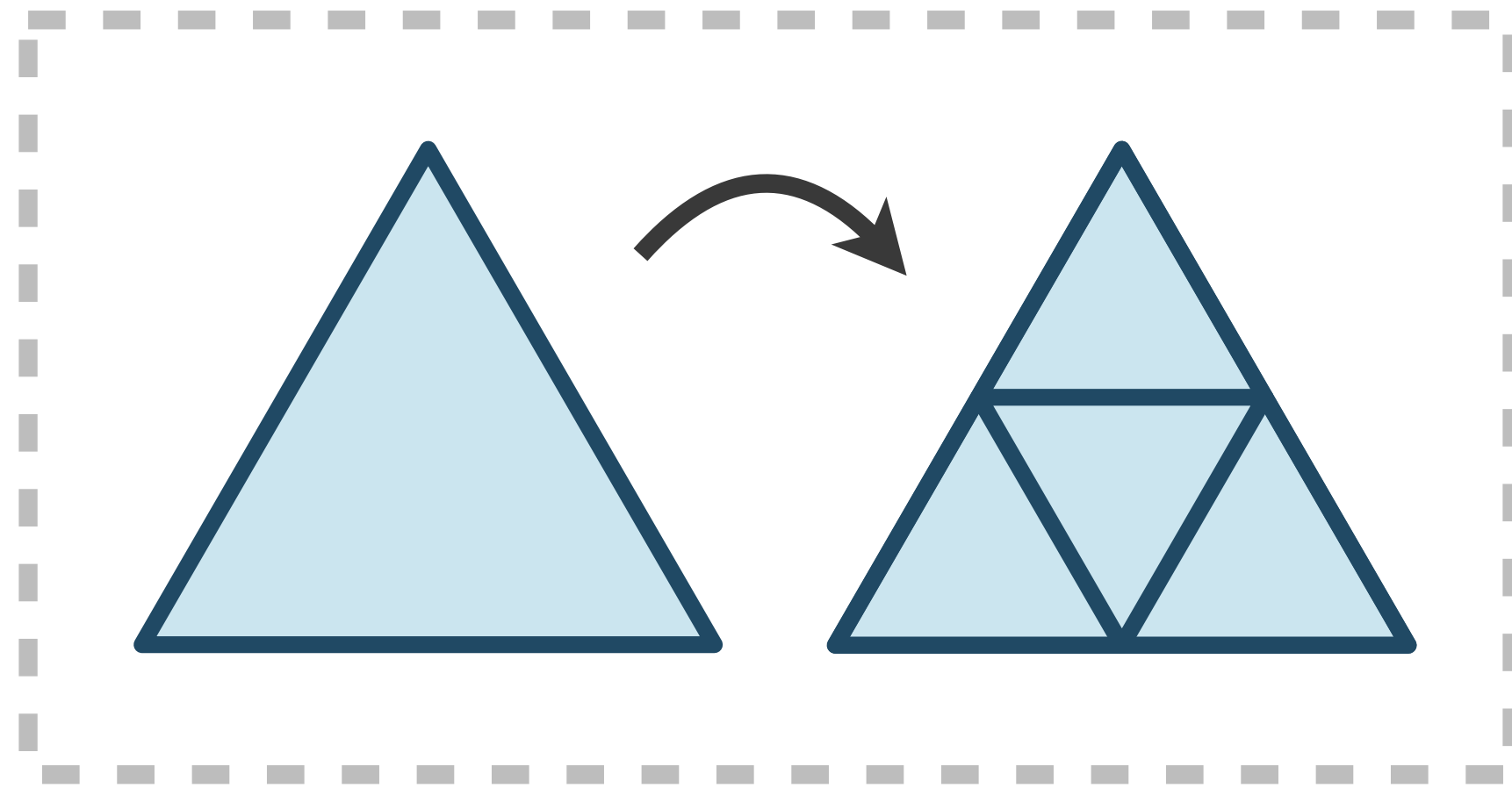
Classic Subdivision



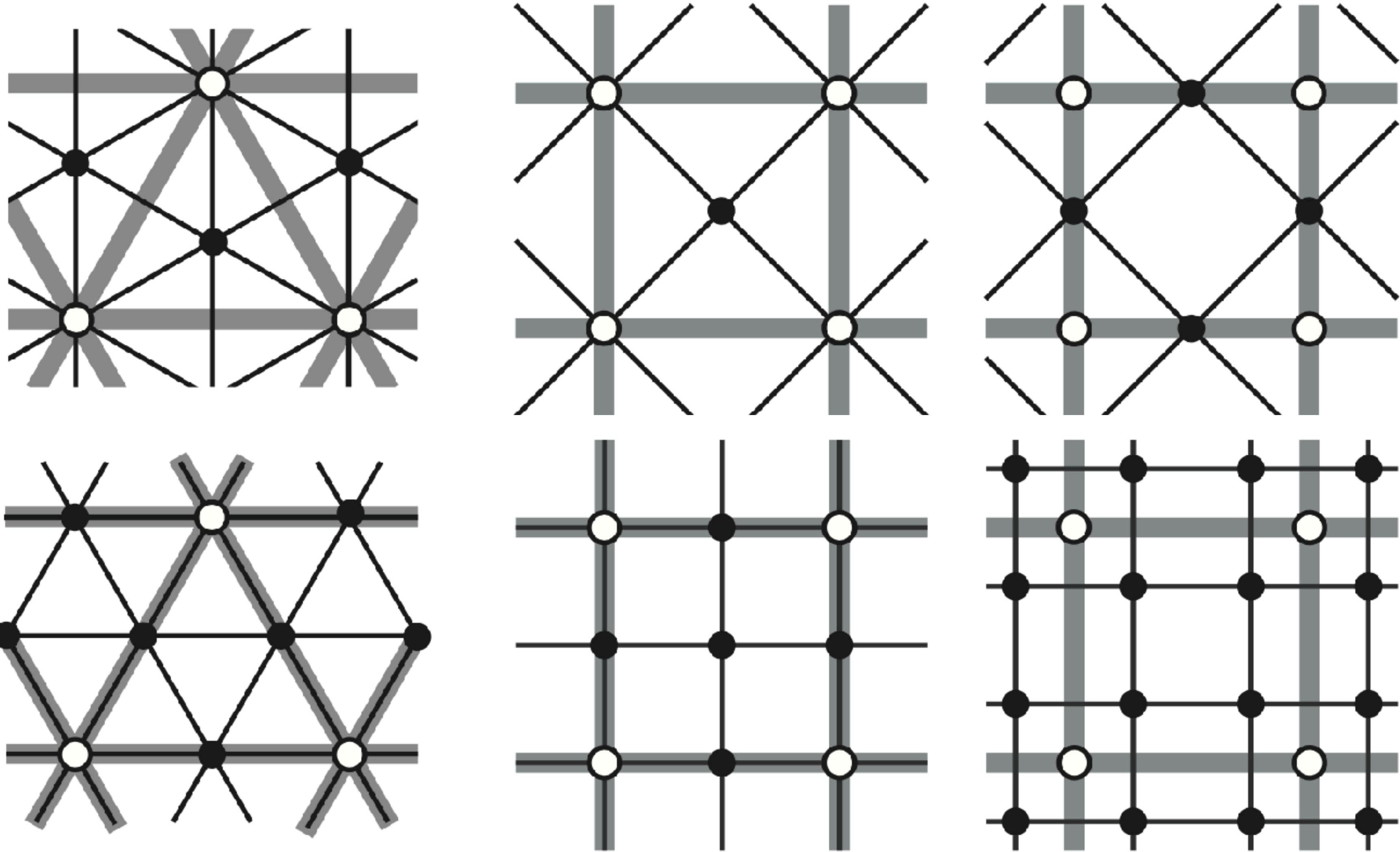
Classic Subdivision



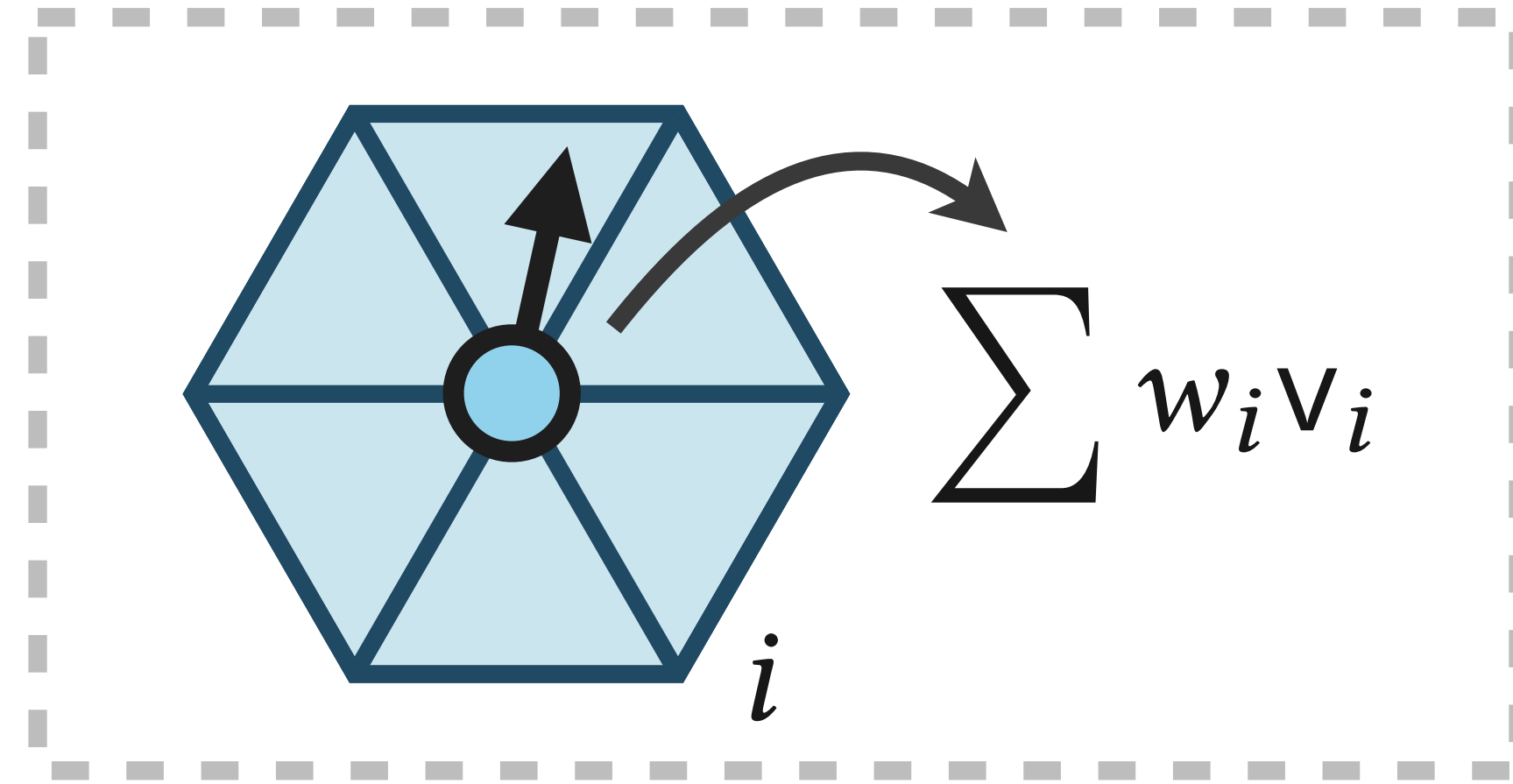
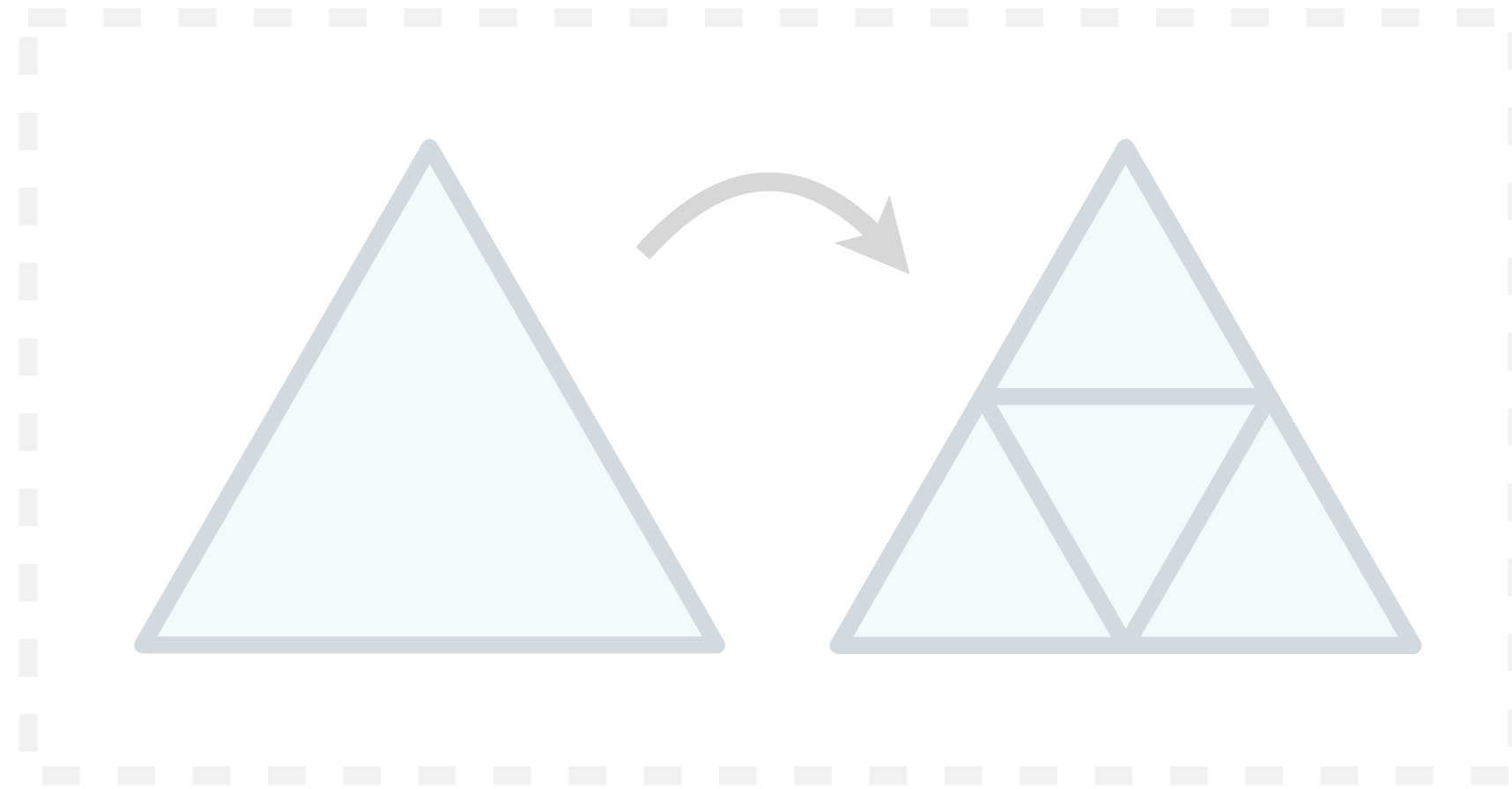
Where we should put the network?



Discrete Variables

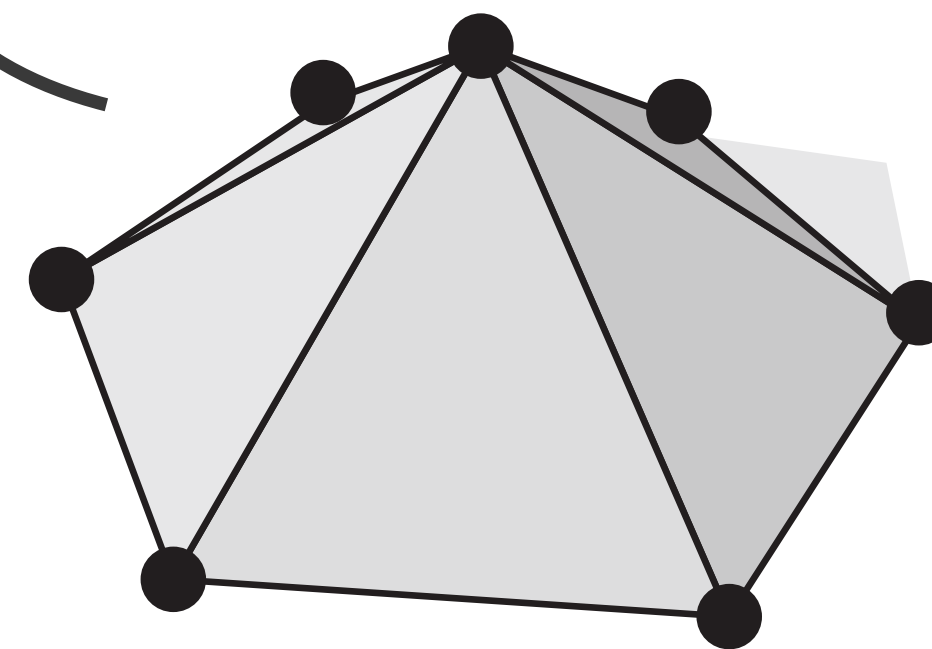
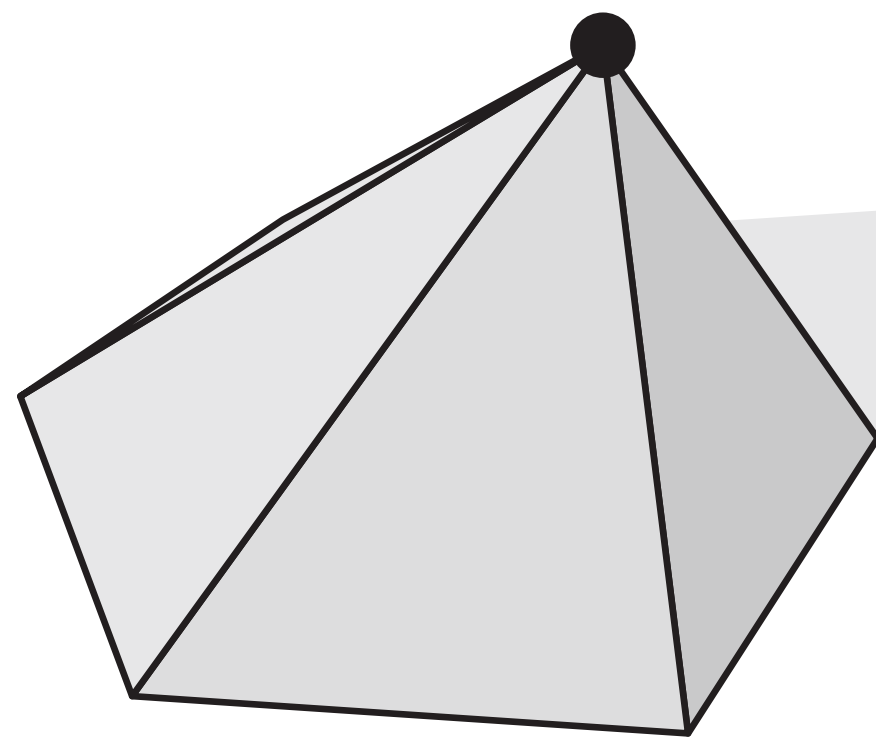


Where we should put the network?



From features to locations

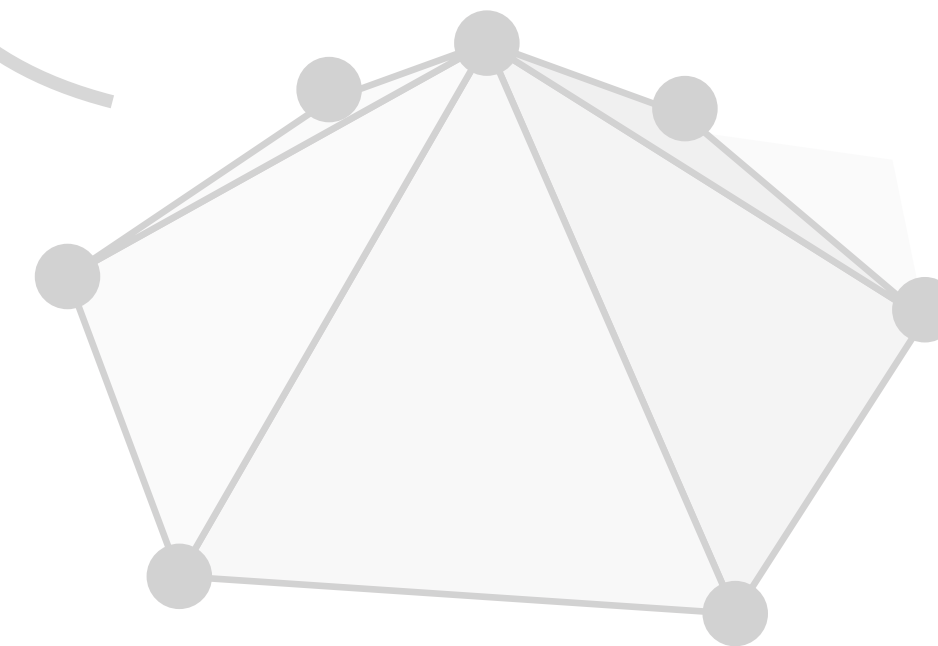
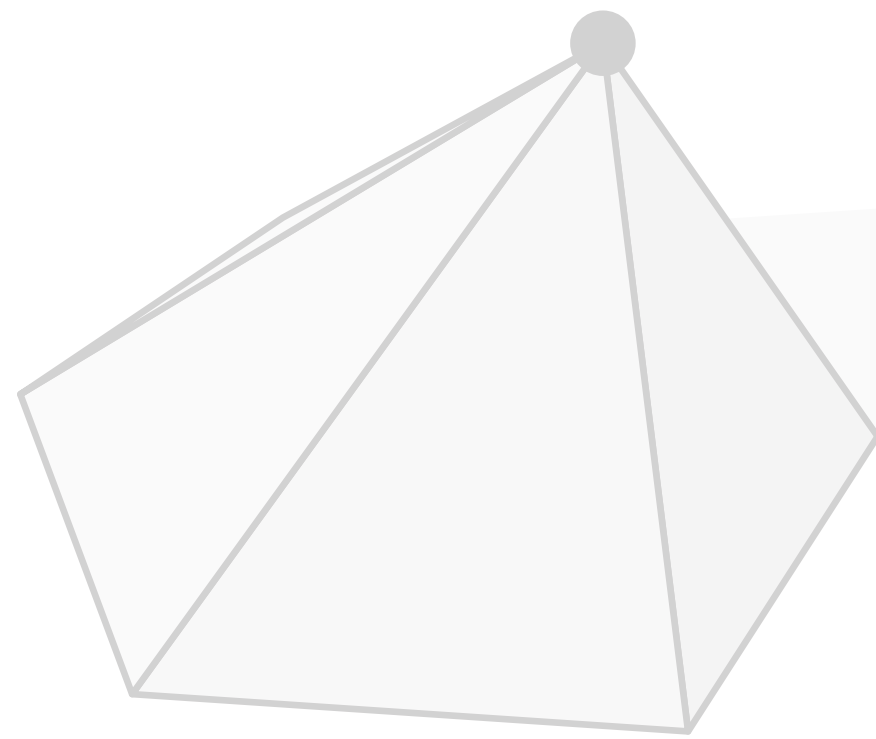
$$y = f_{\theta}(x)$$



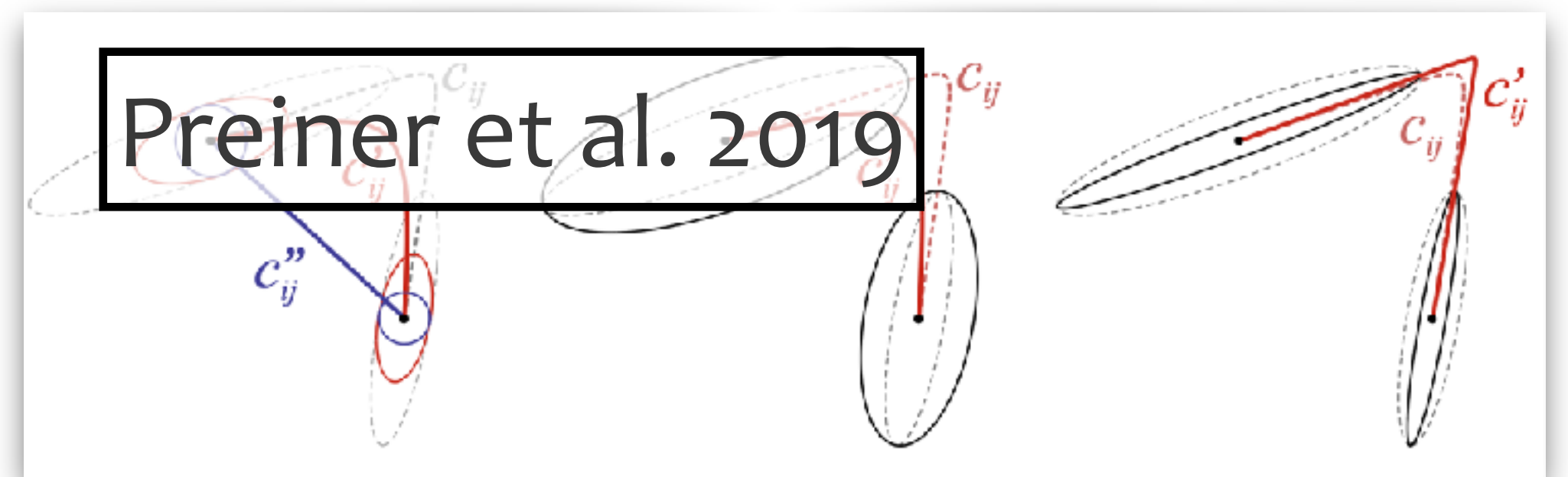
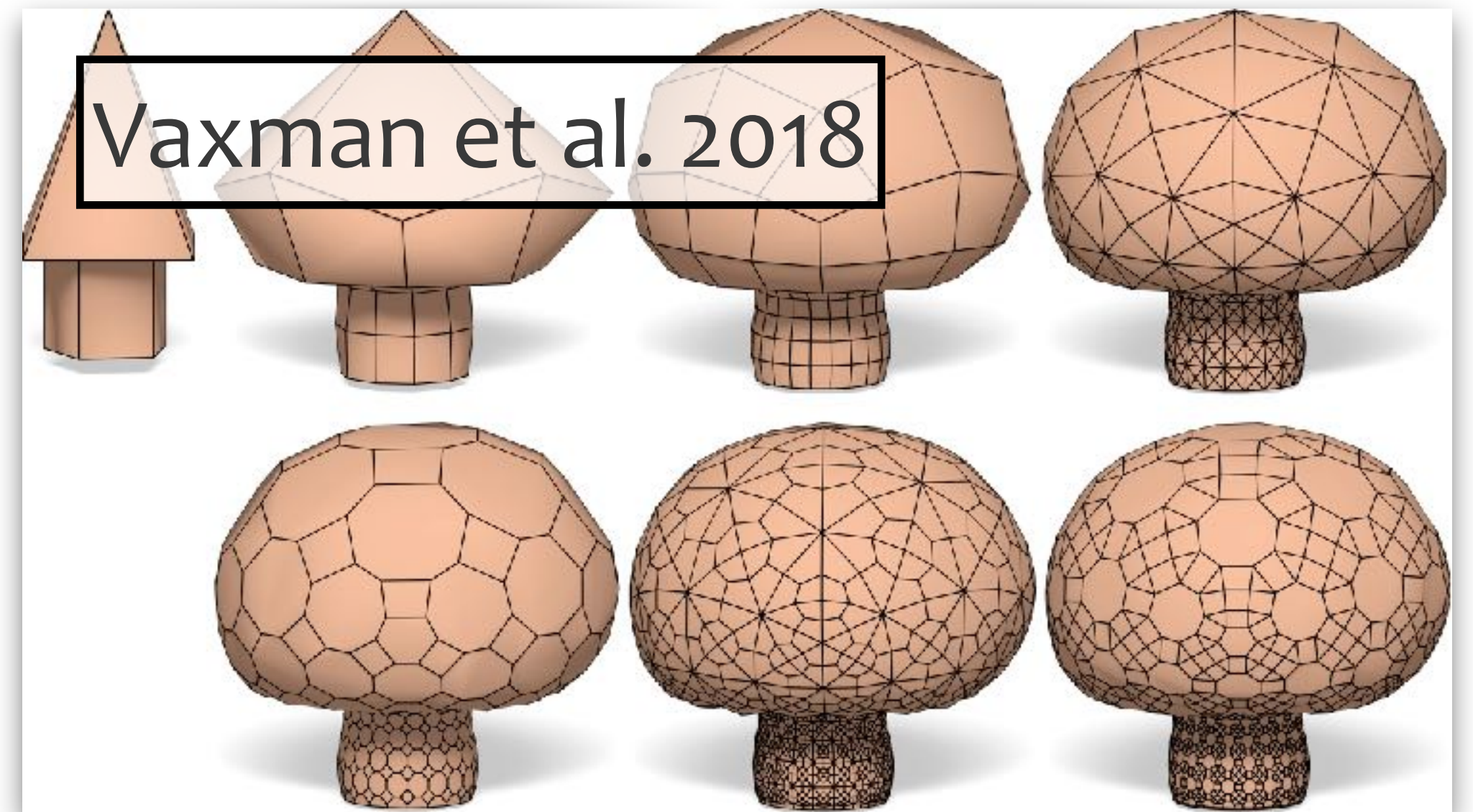
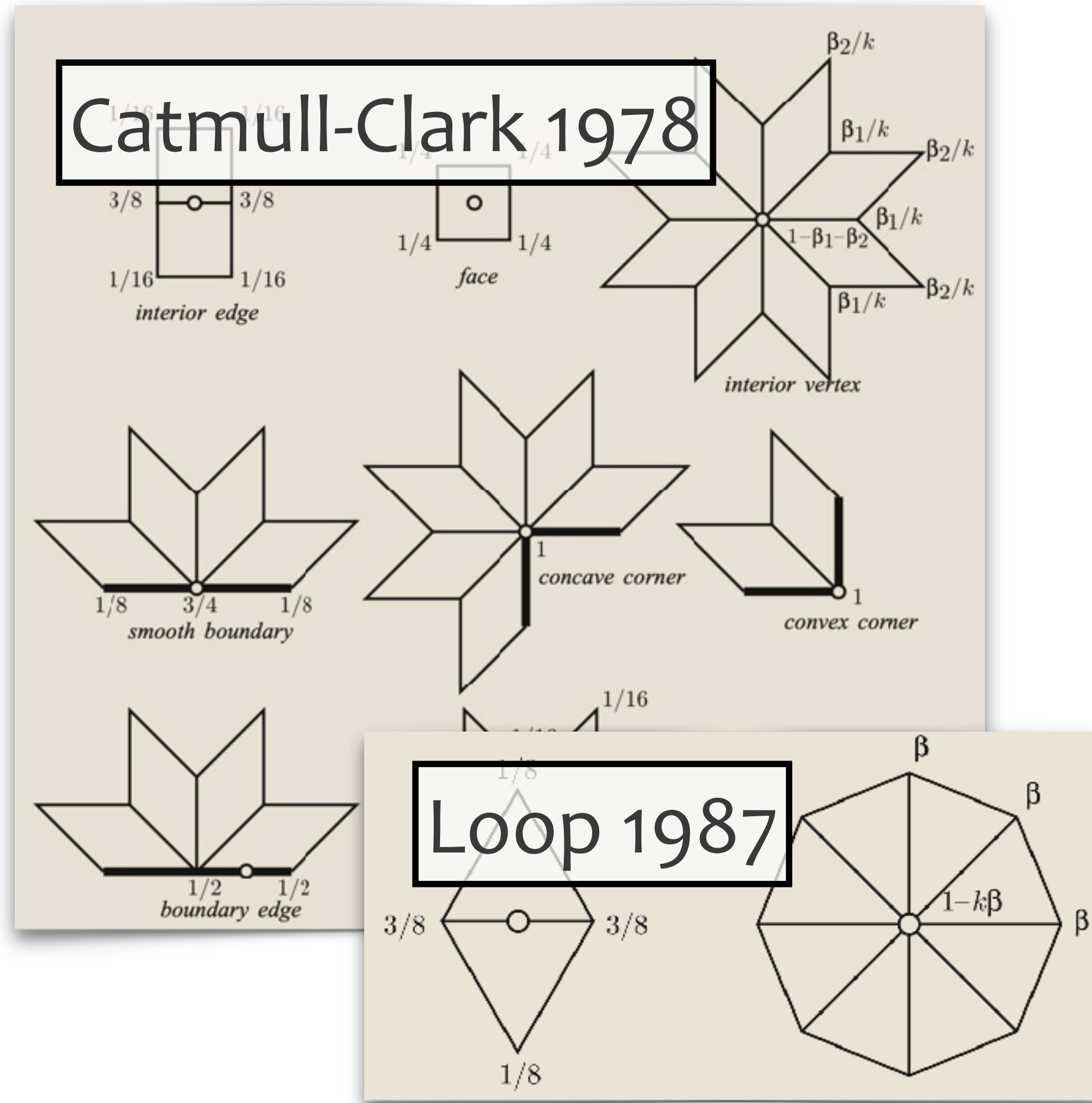
From features to locations

difficult to define

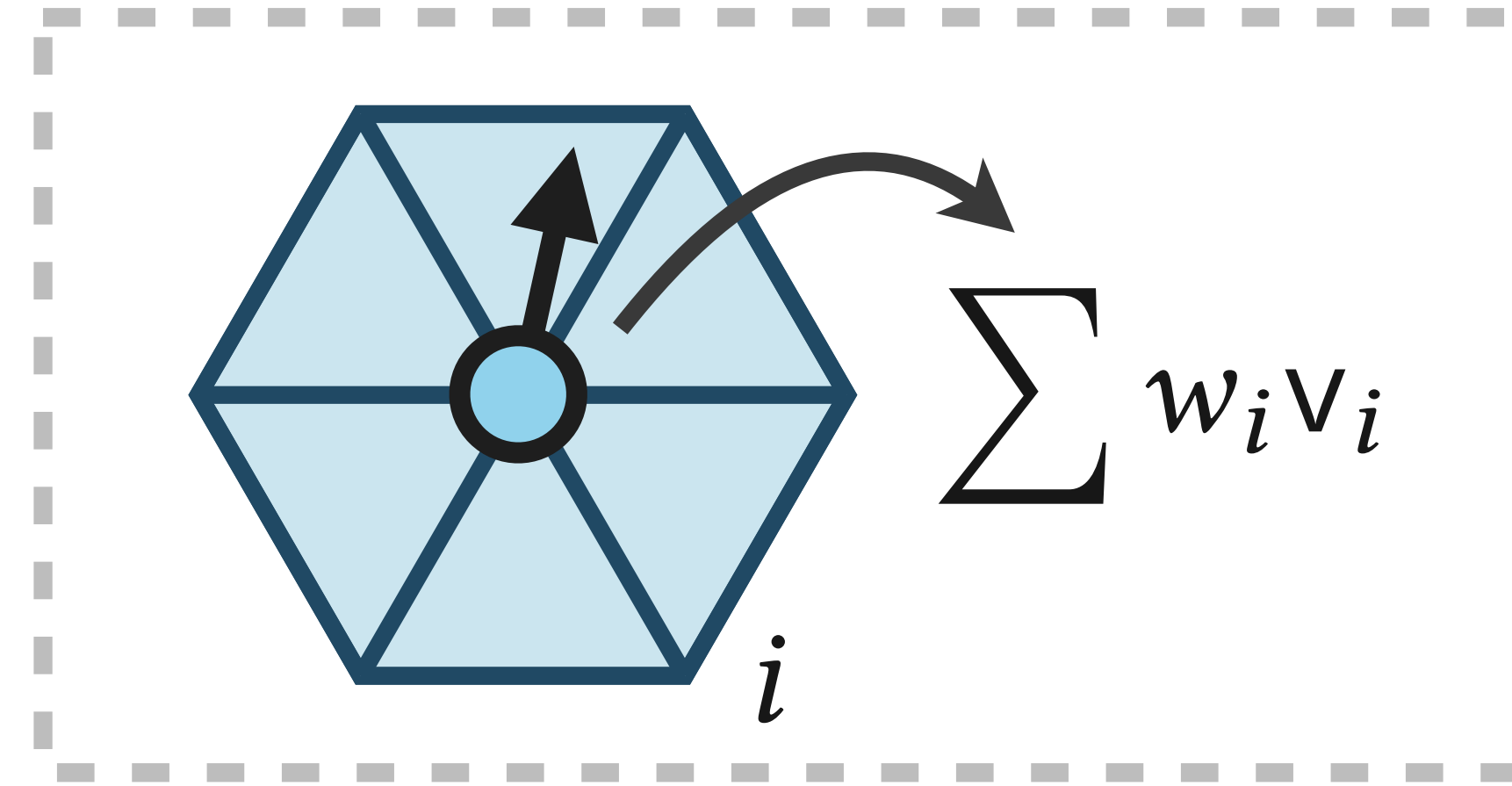
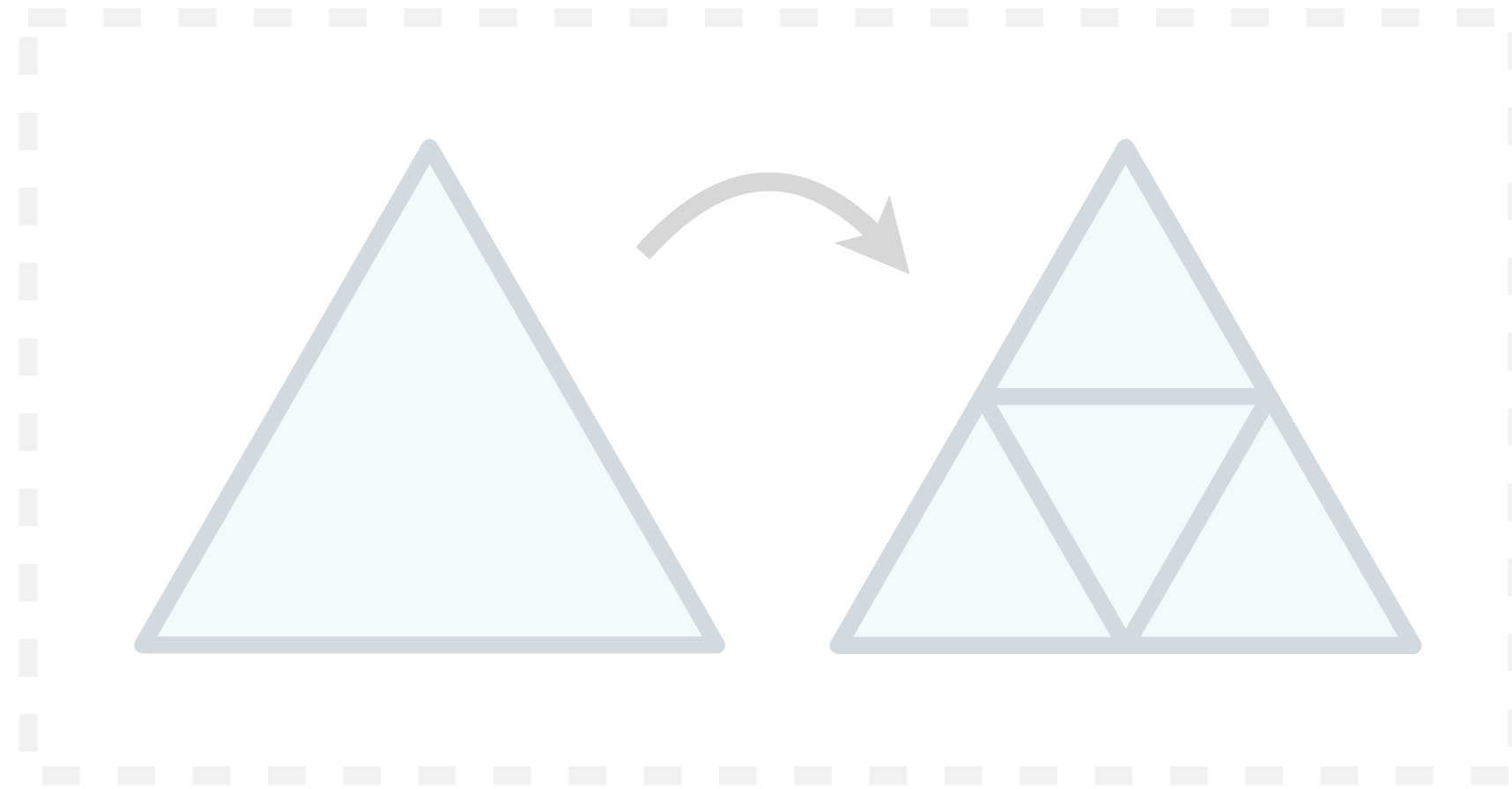
$$y = f_{\theta}(x)$$



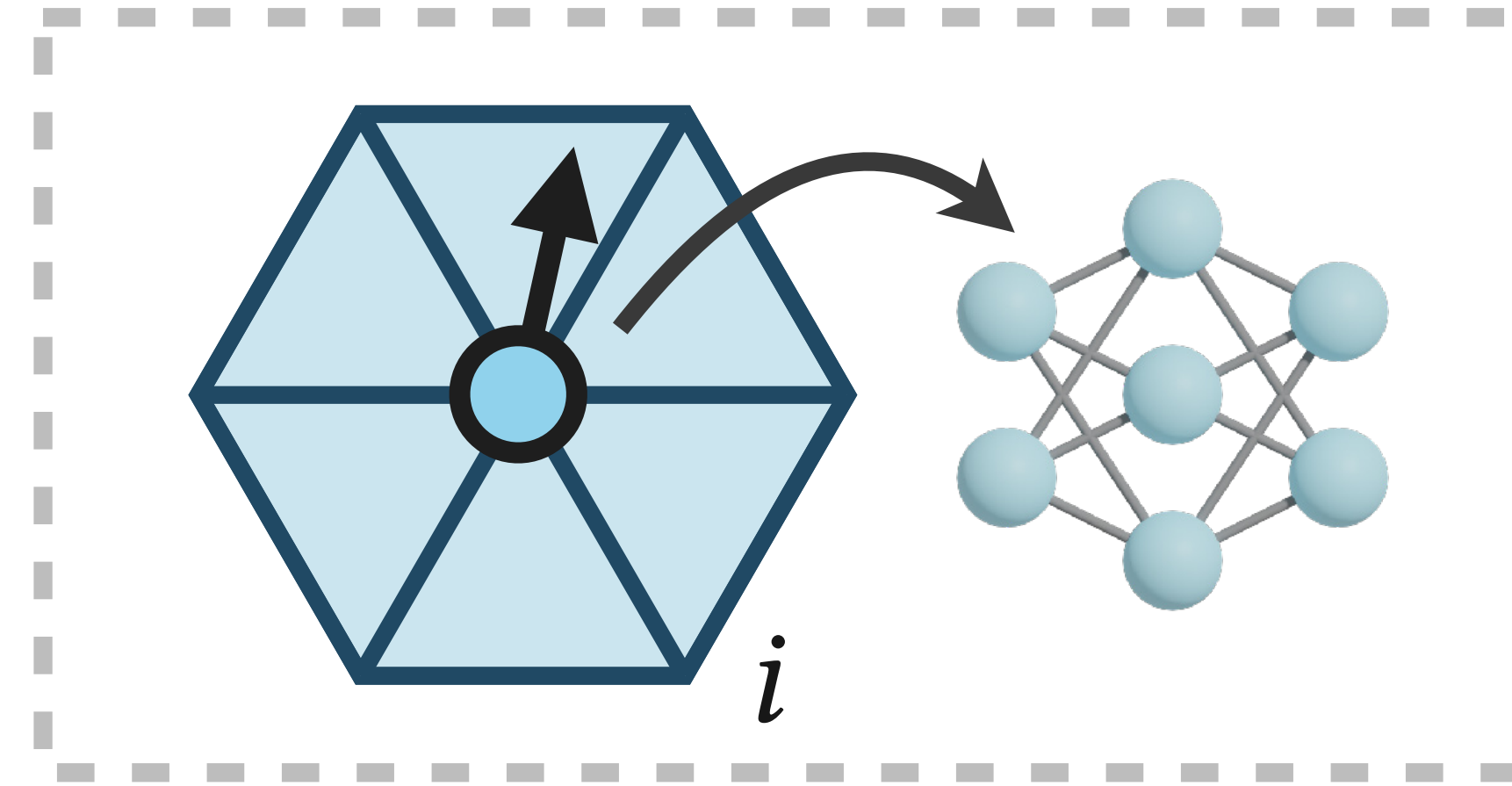
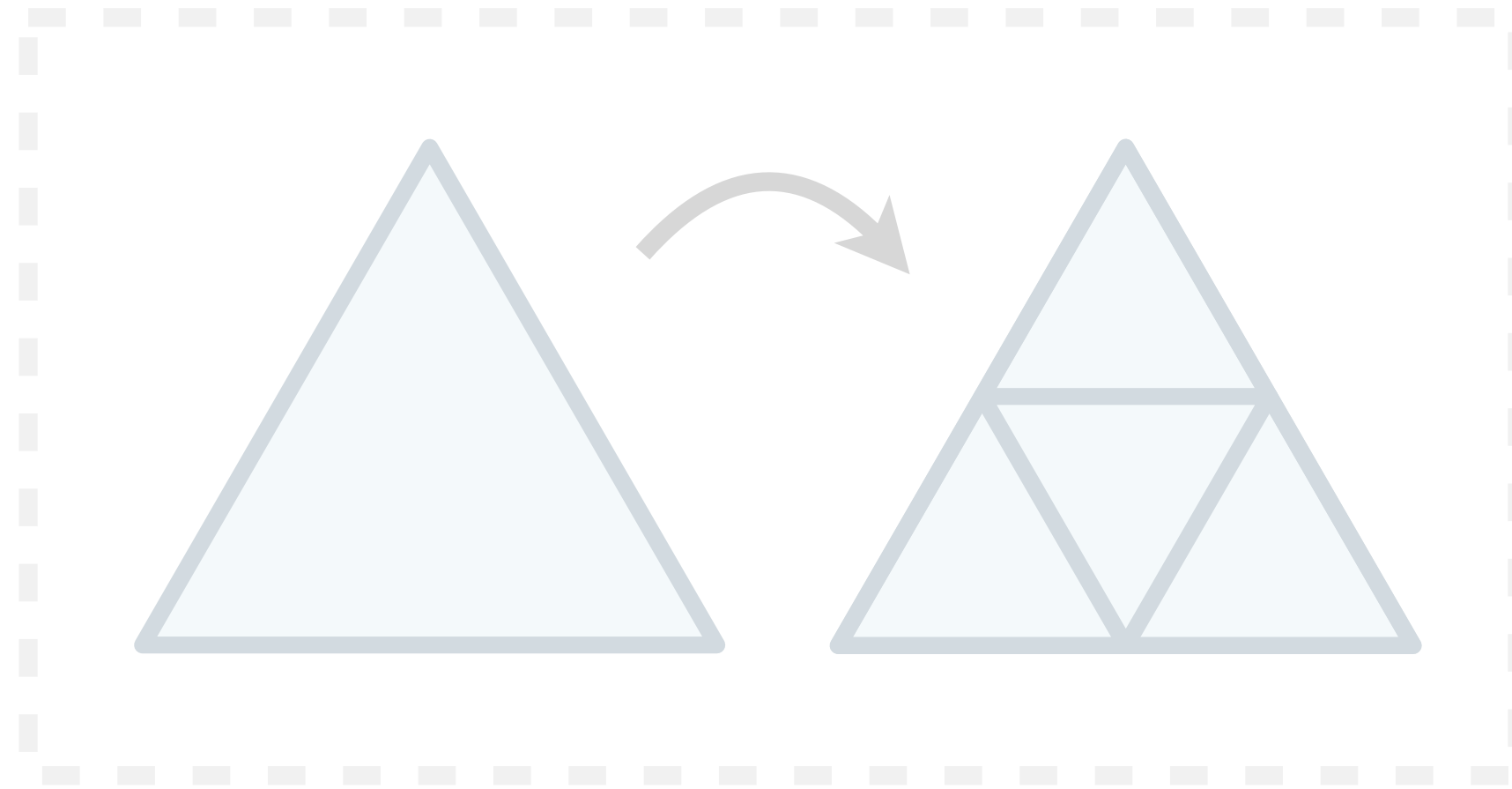
Still an ongoing research



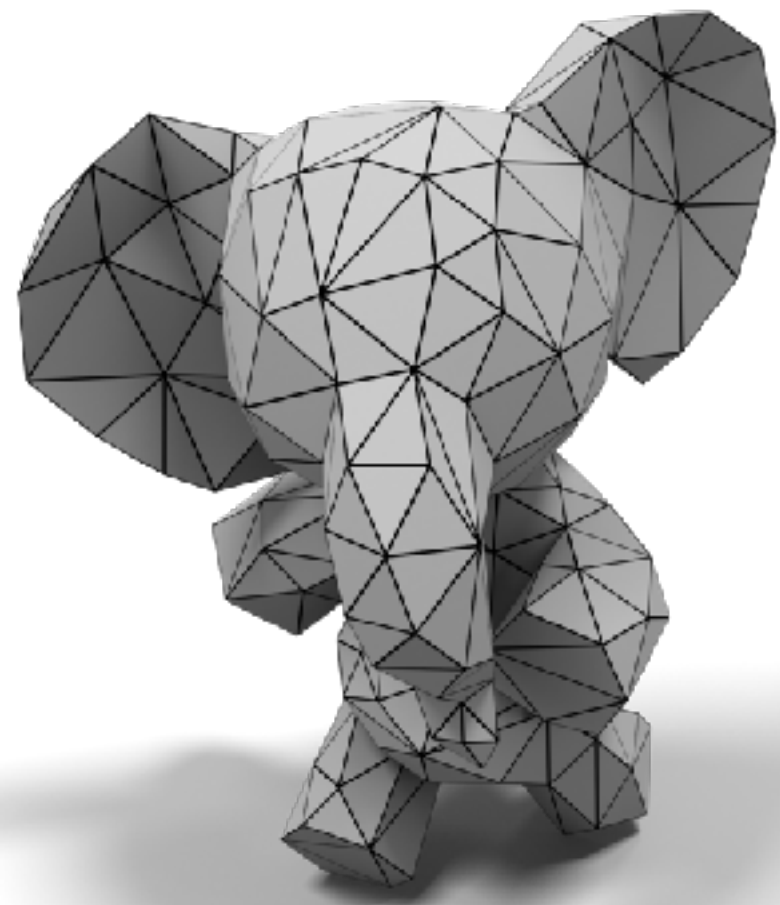
Where we should put the network?



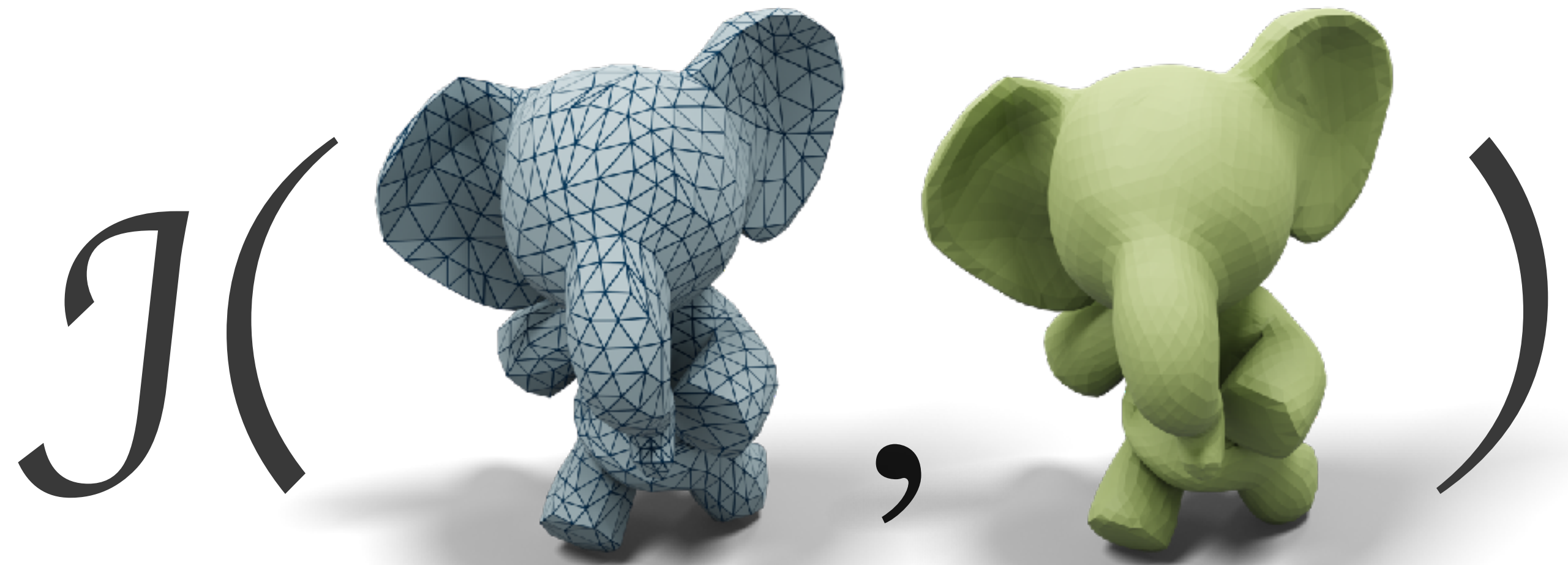
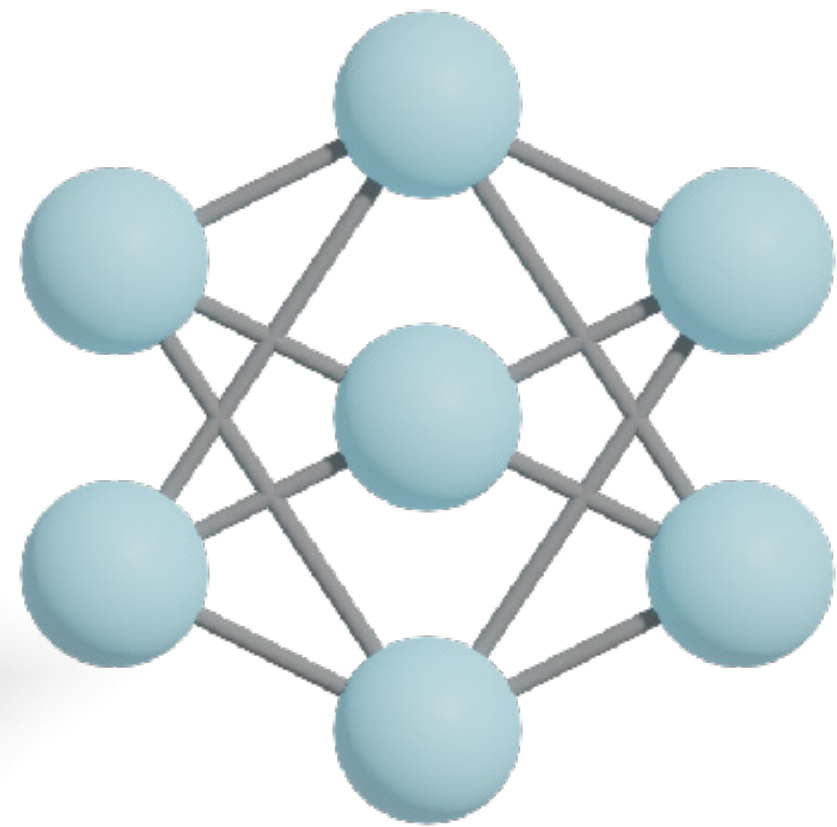
Where we should put the network?



Neural Subdivision Training



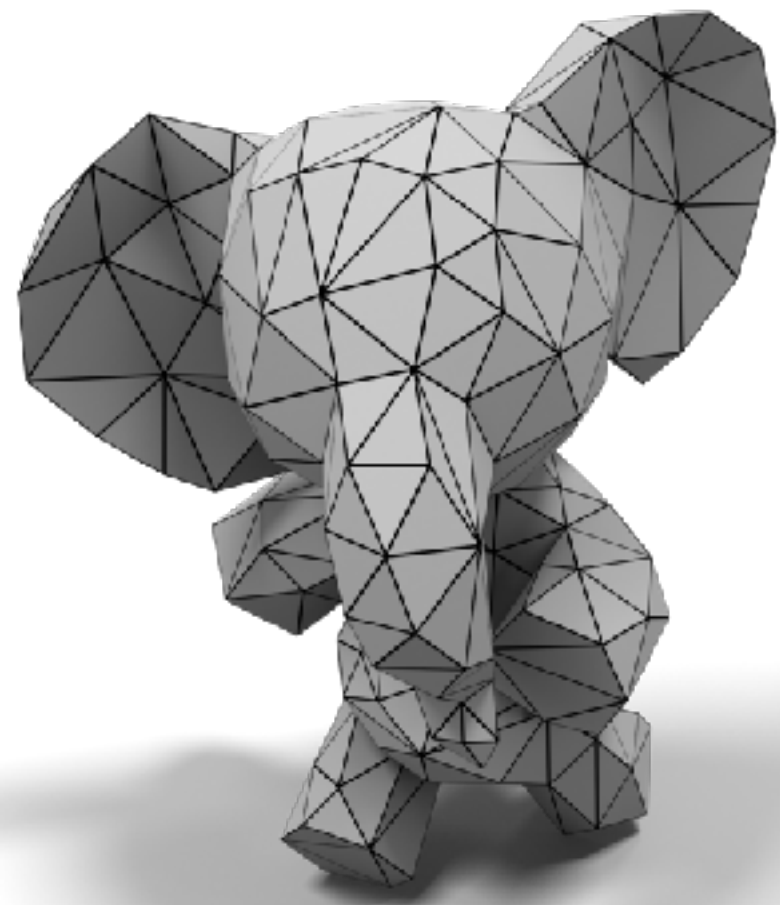
input



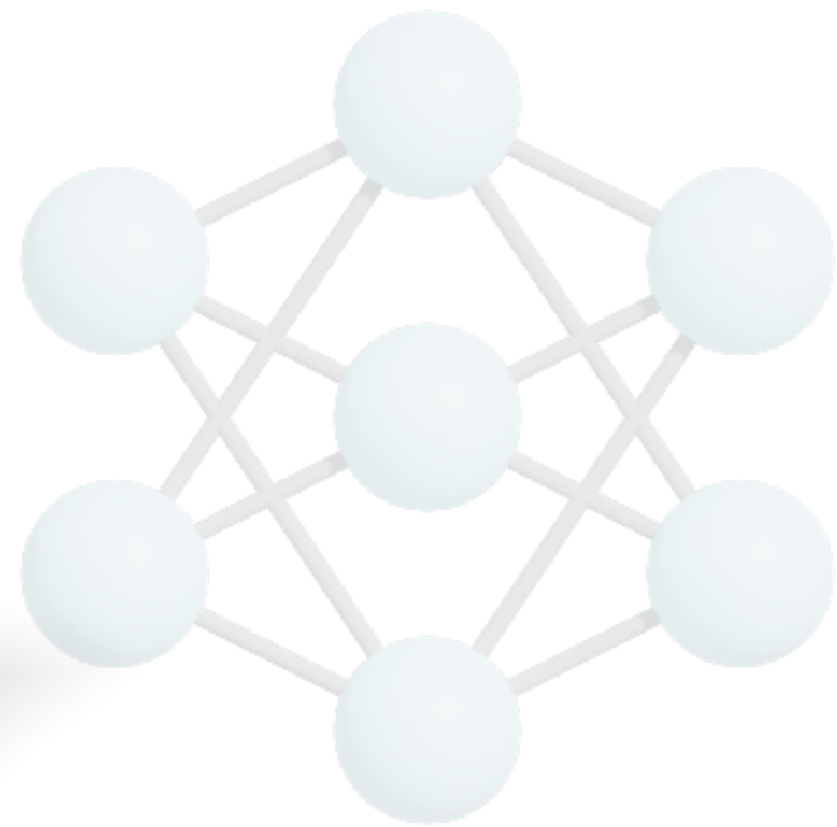
output

ground truth

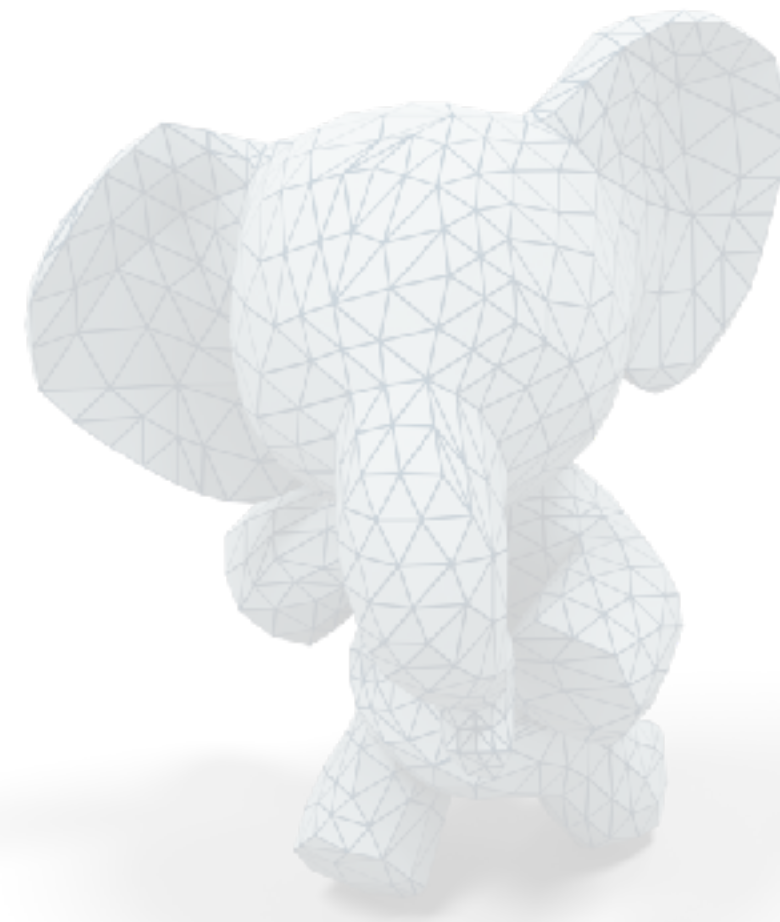
Neural Subdivision Training



input



\mathcal{J}

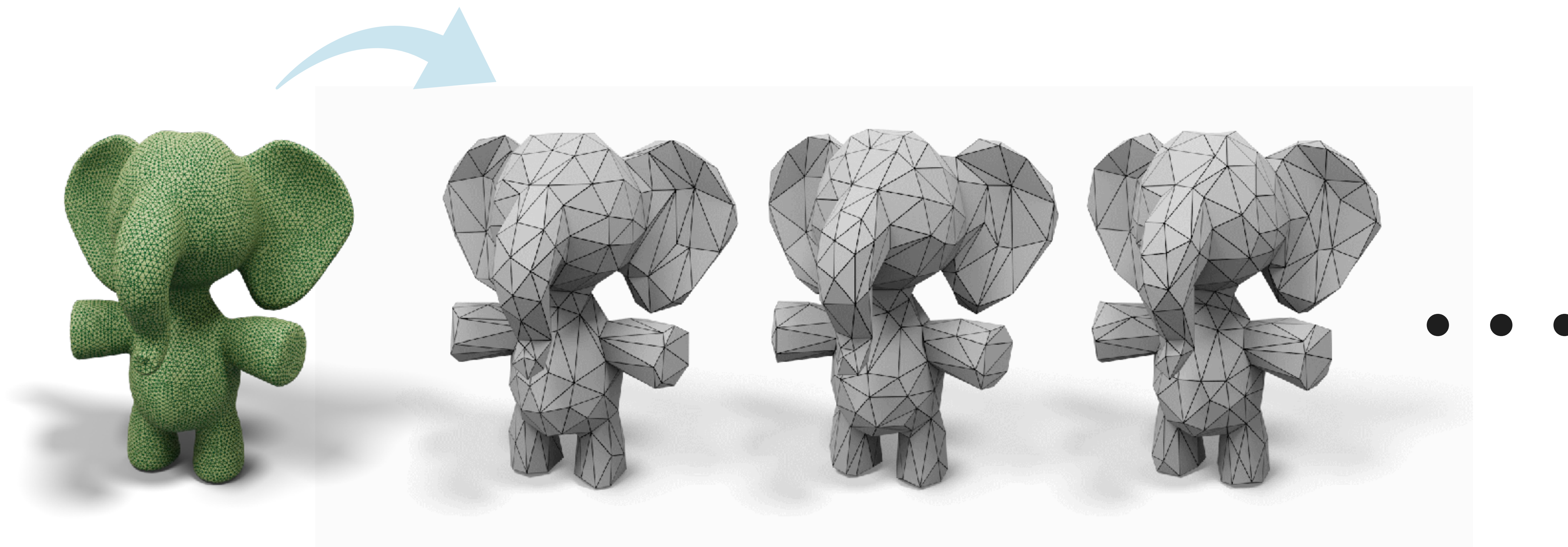


output



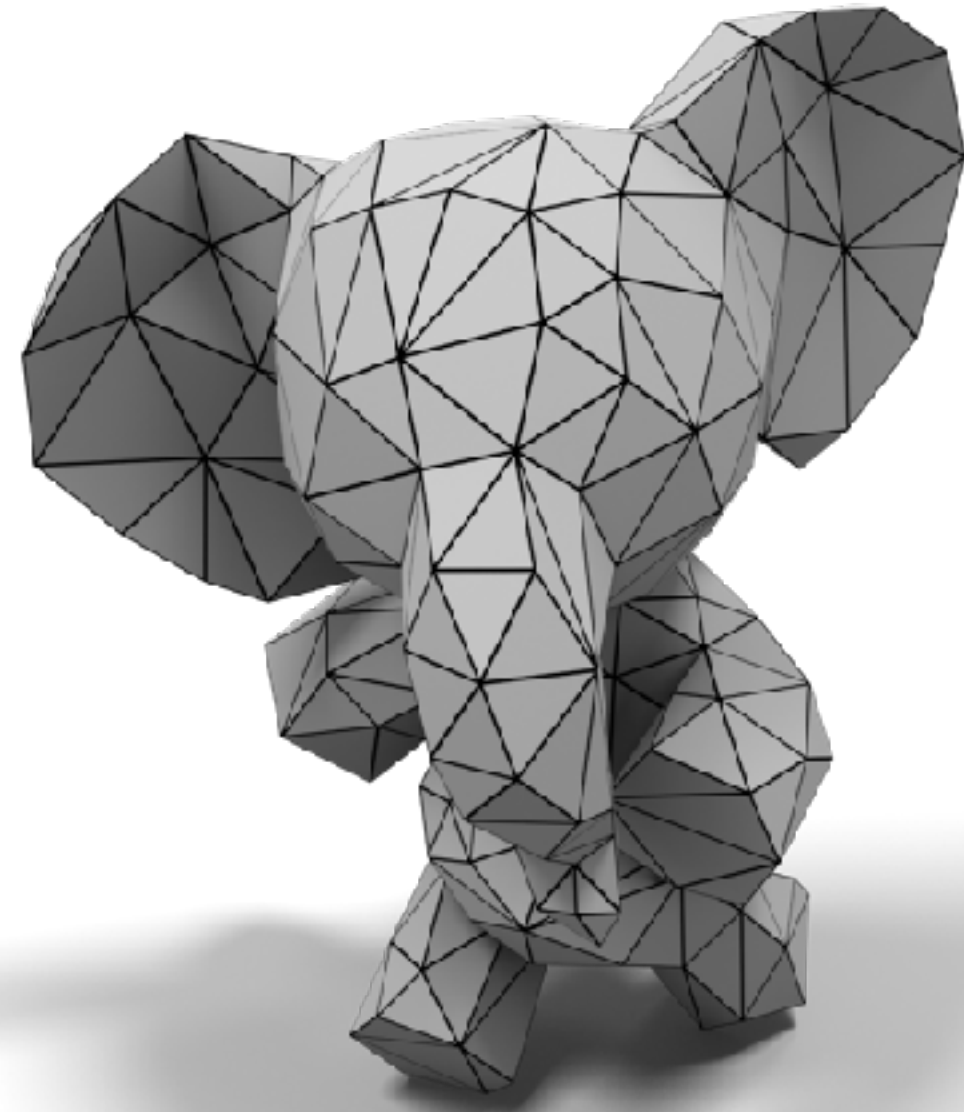
ground truth

Training Data

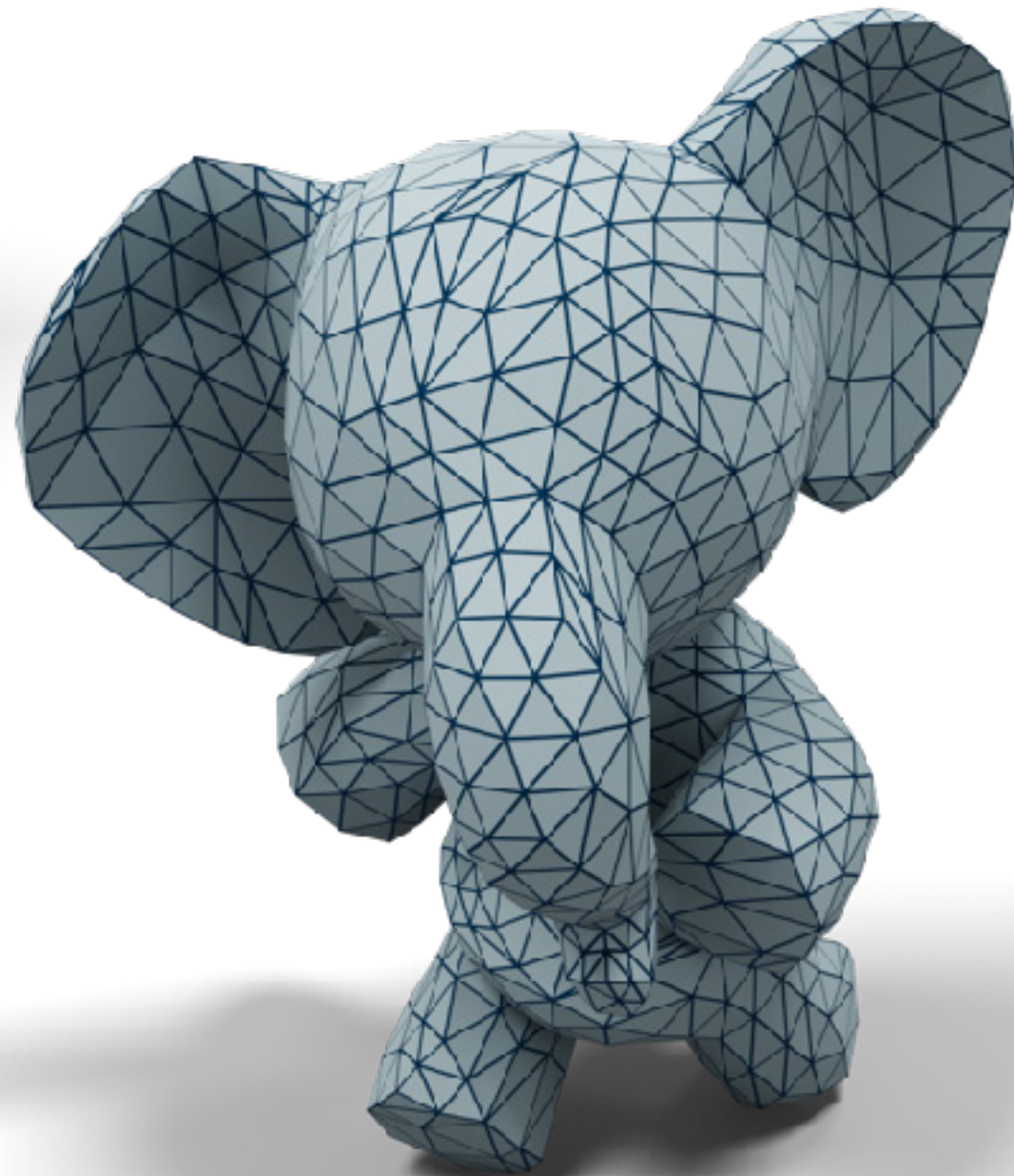


Neural Subdivision Training

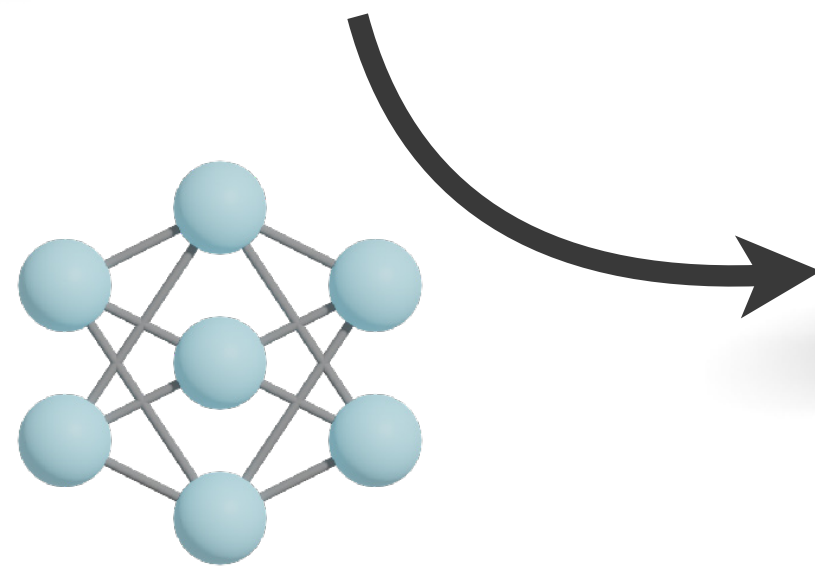
input



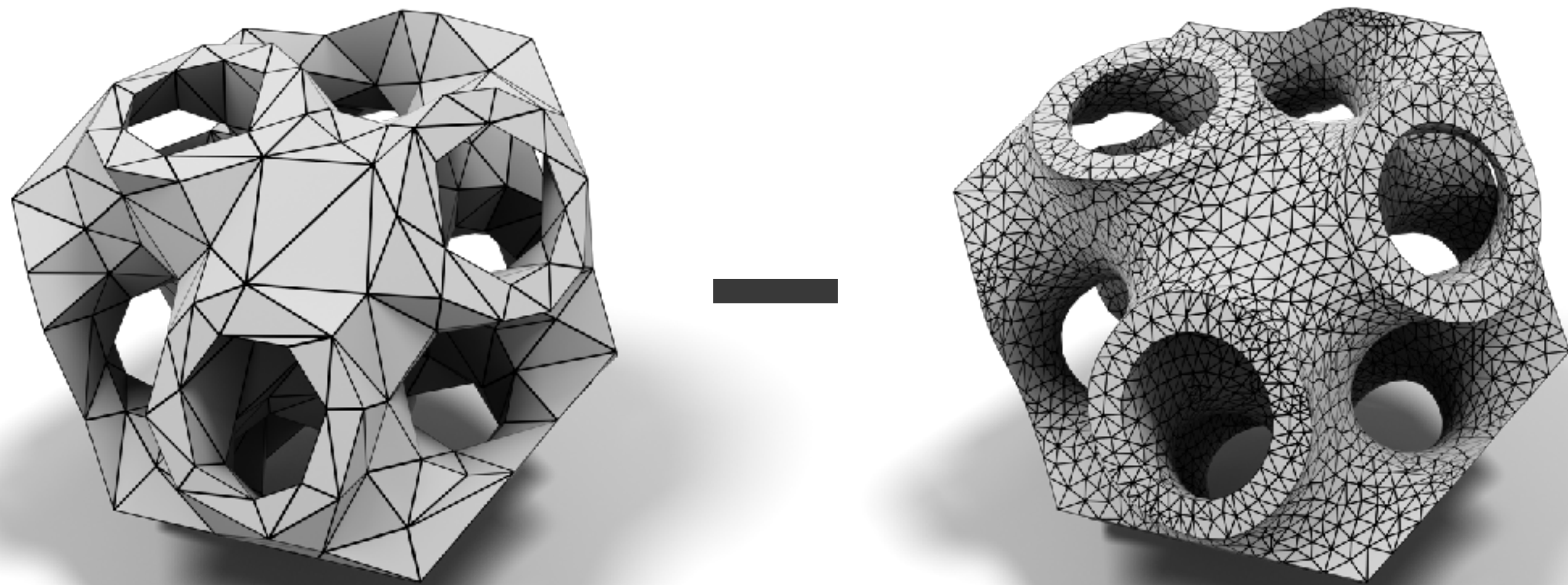
output



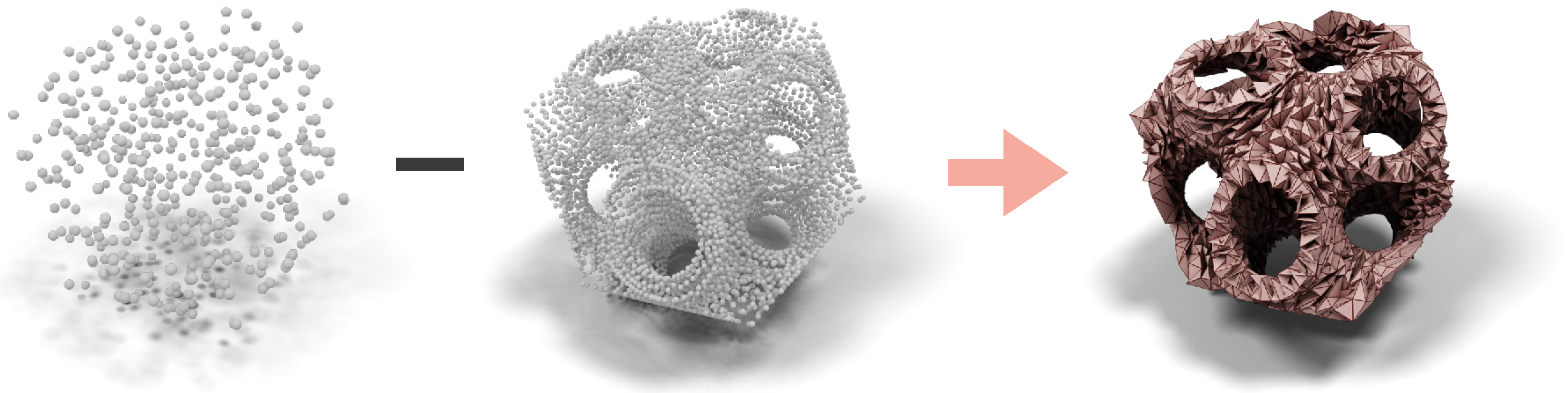
ground truth



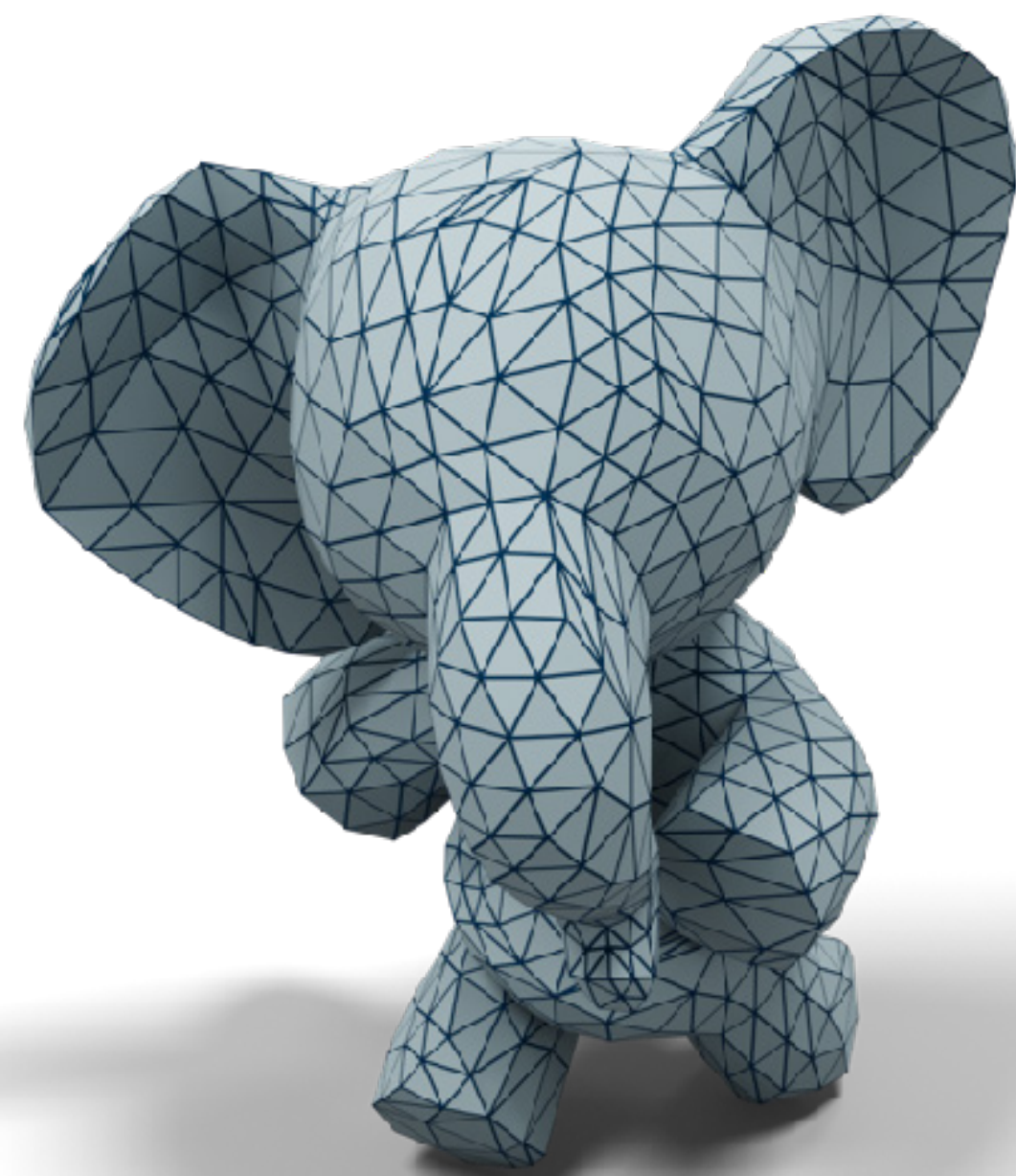
Chamfer Distance



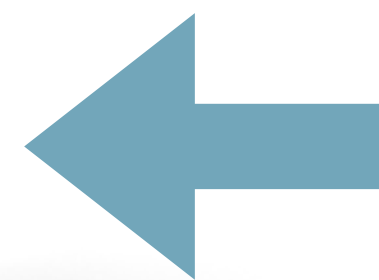
Chamfer Distance



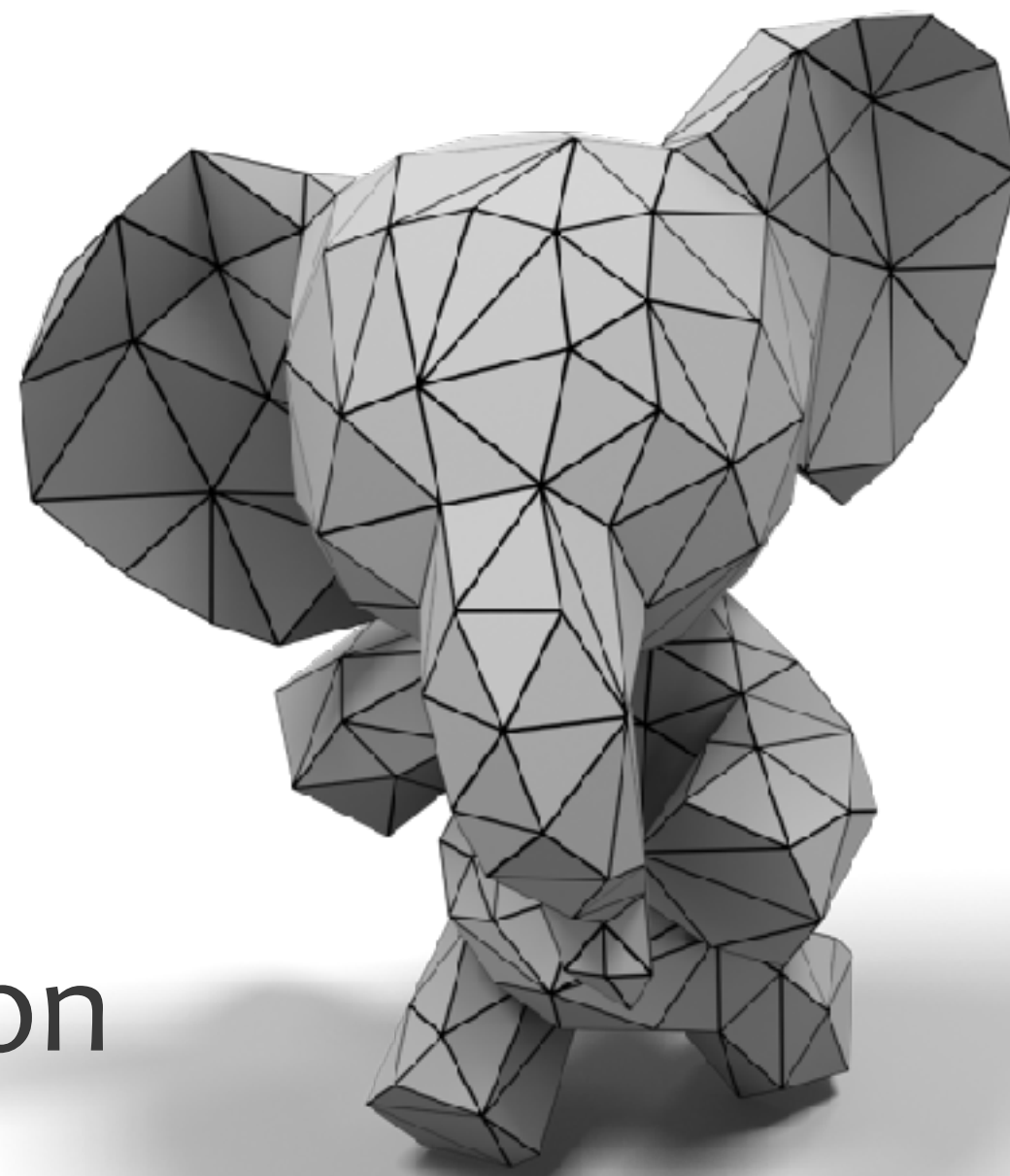
Leverage the Structure



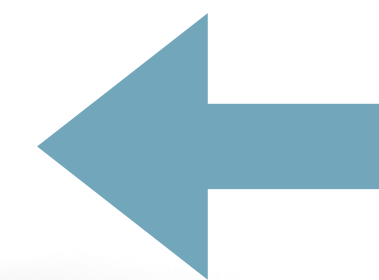
output



subdivision



input



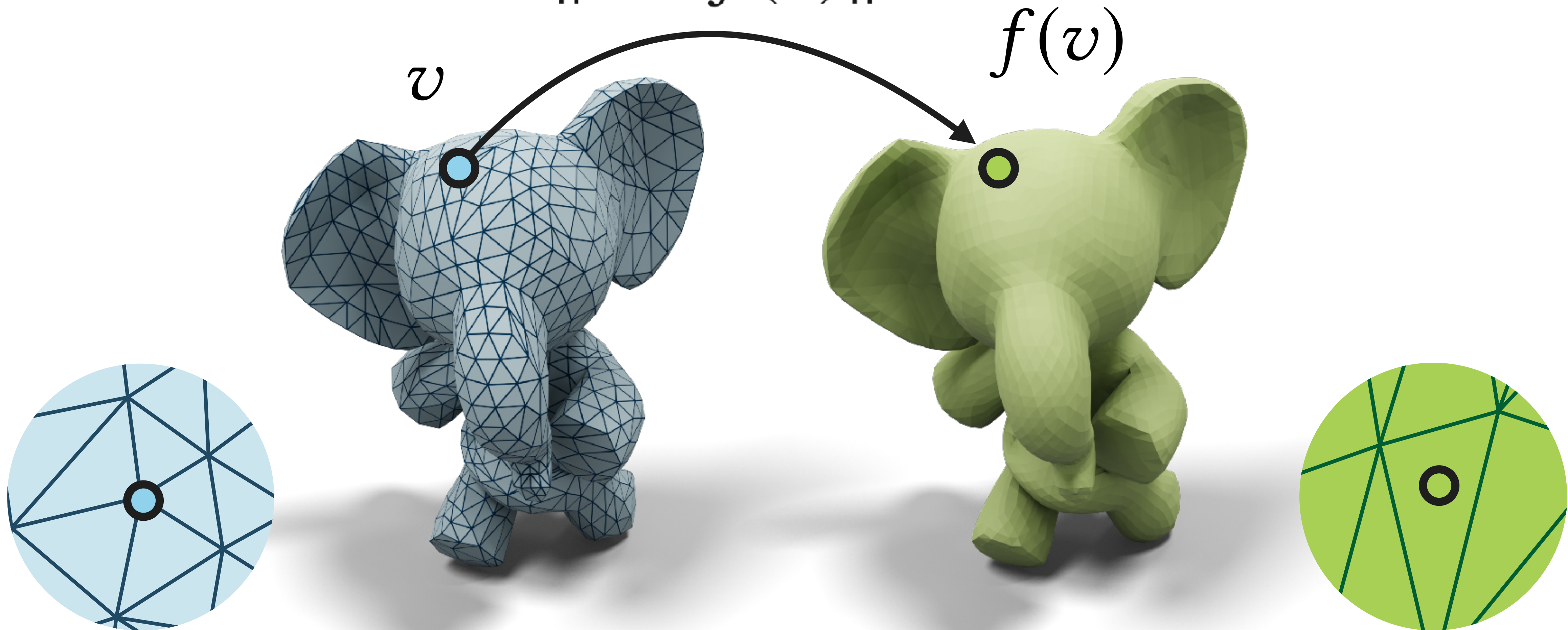
decimation



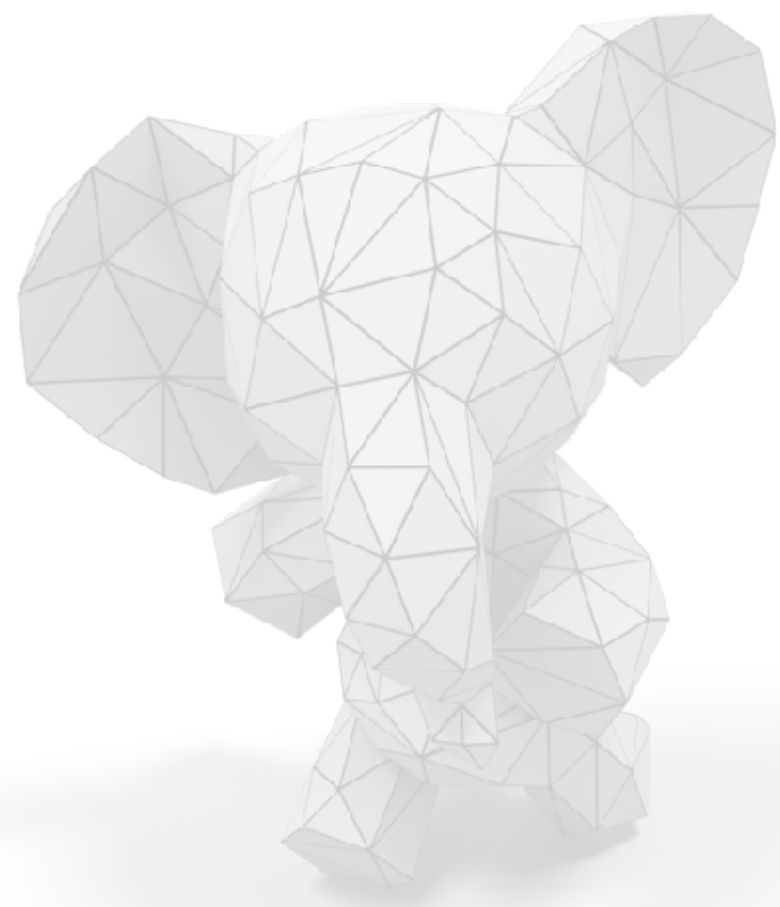
ground truth

Bijective Mapping

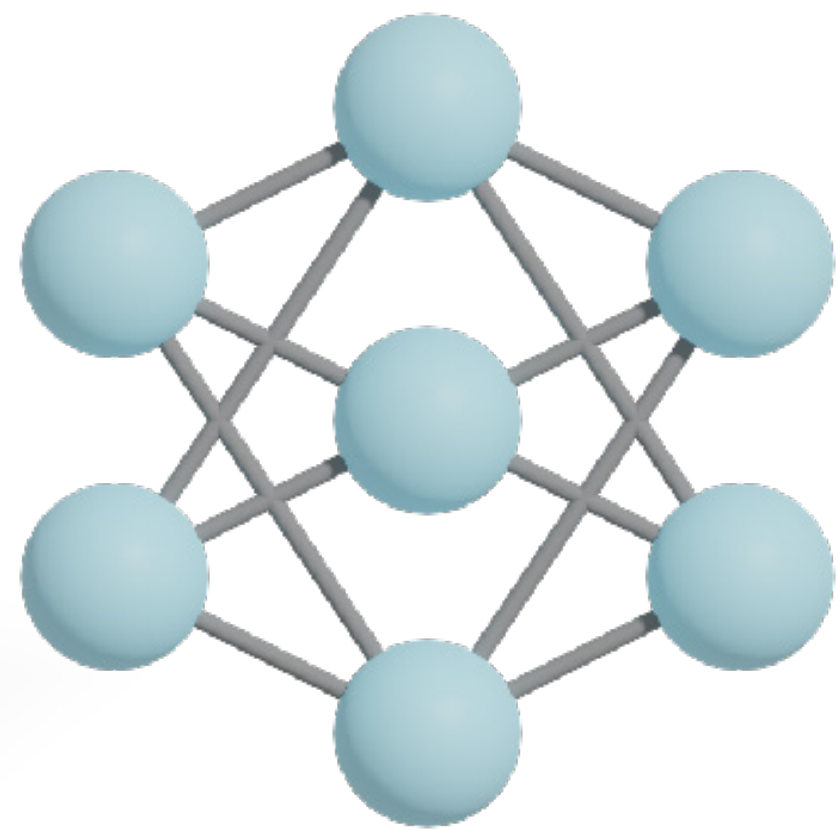
$$\|v - f(v)\|^2$$



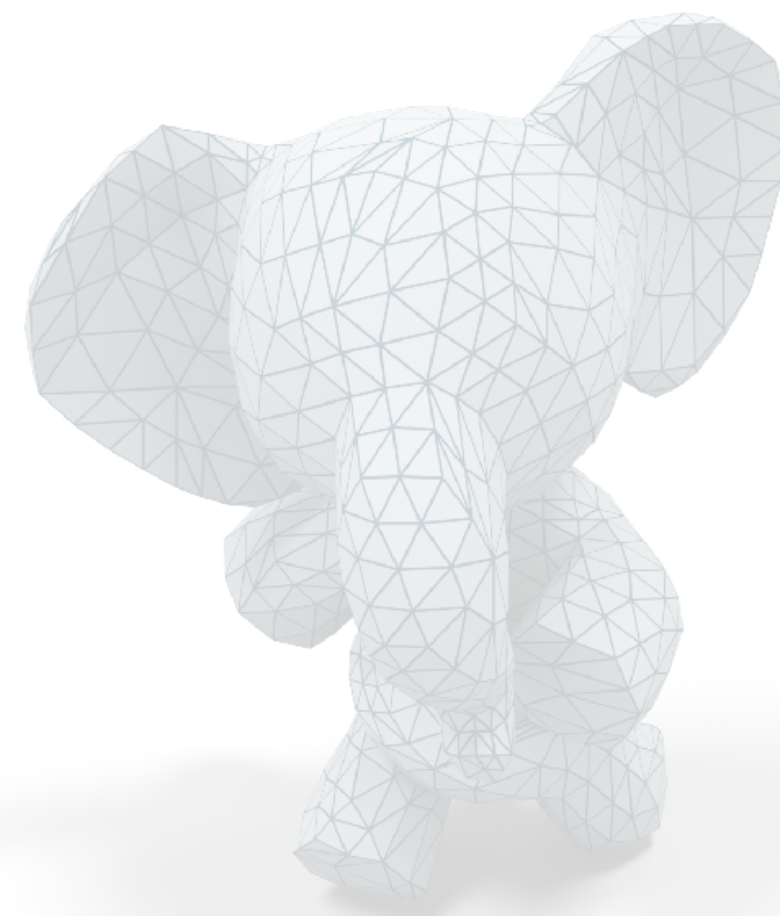
Neural Subdivision Training



input



\mathcal{J} (



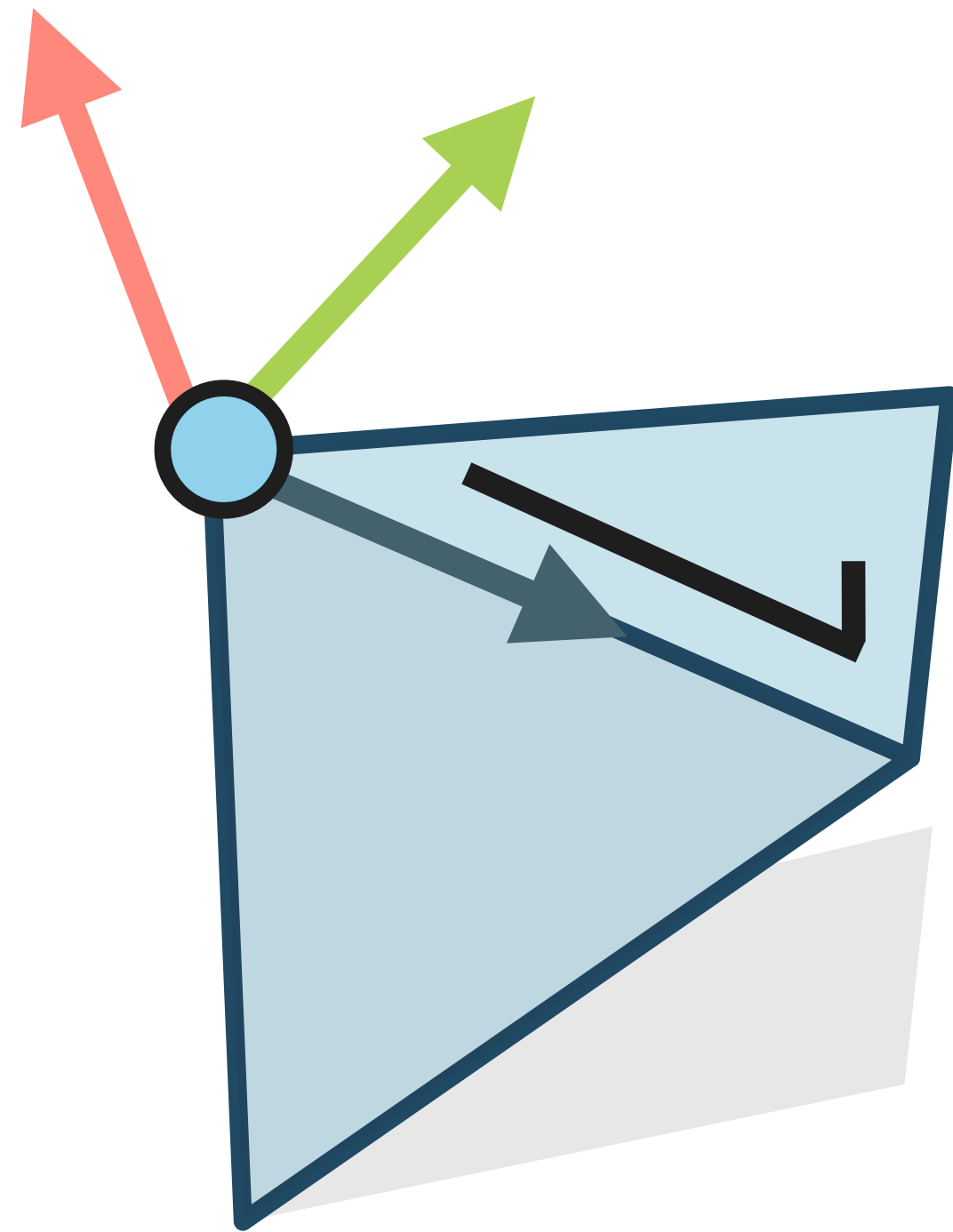
output



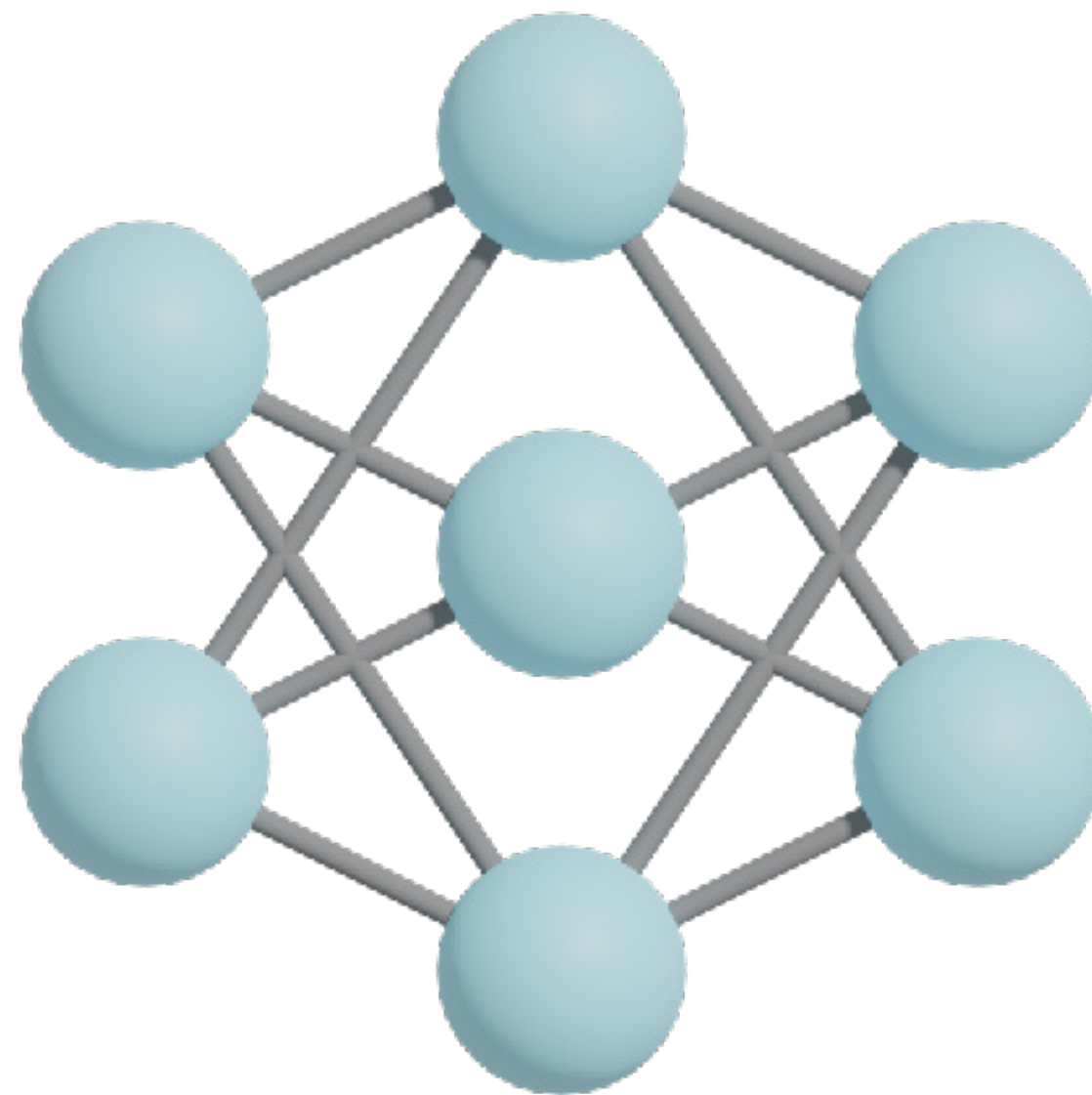
ground truth

,)

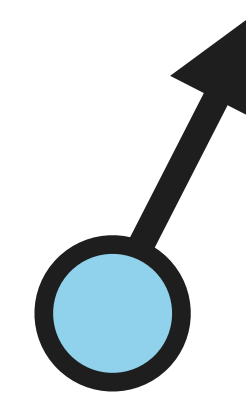
Subdivision Network



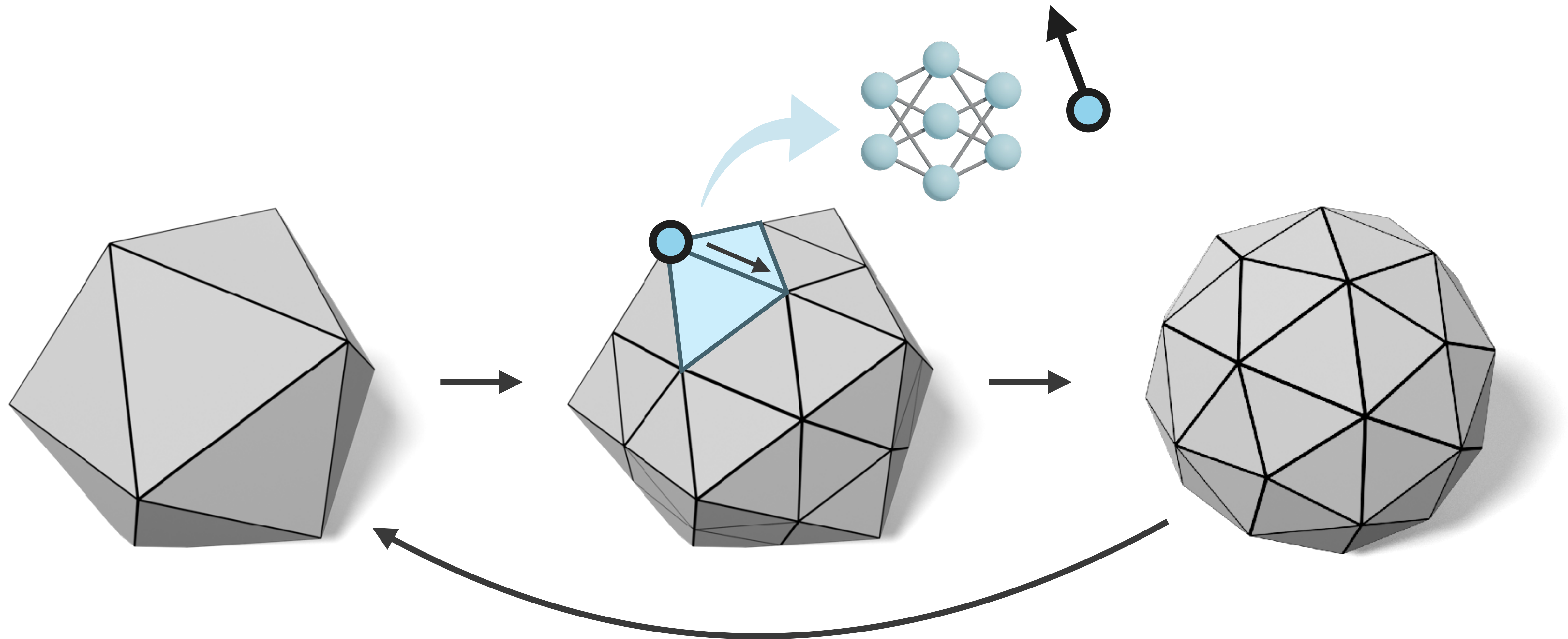
half-flap



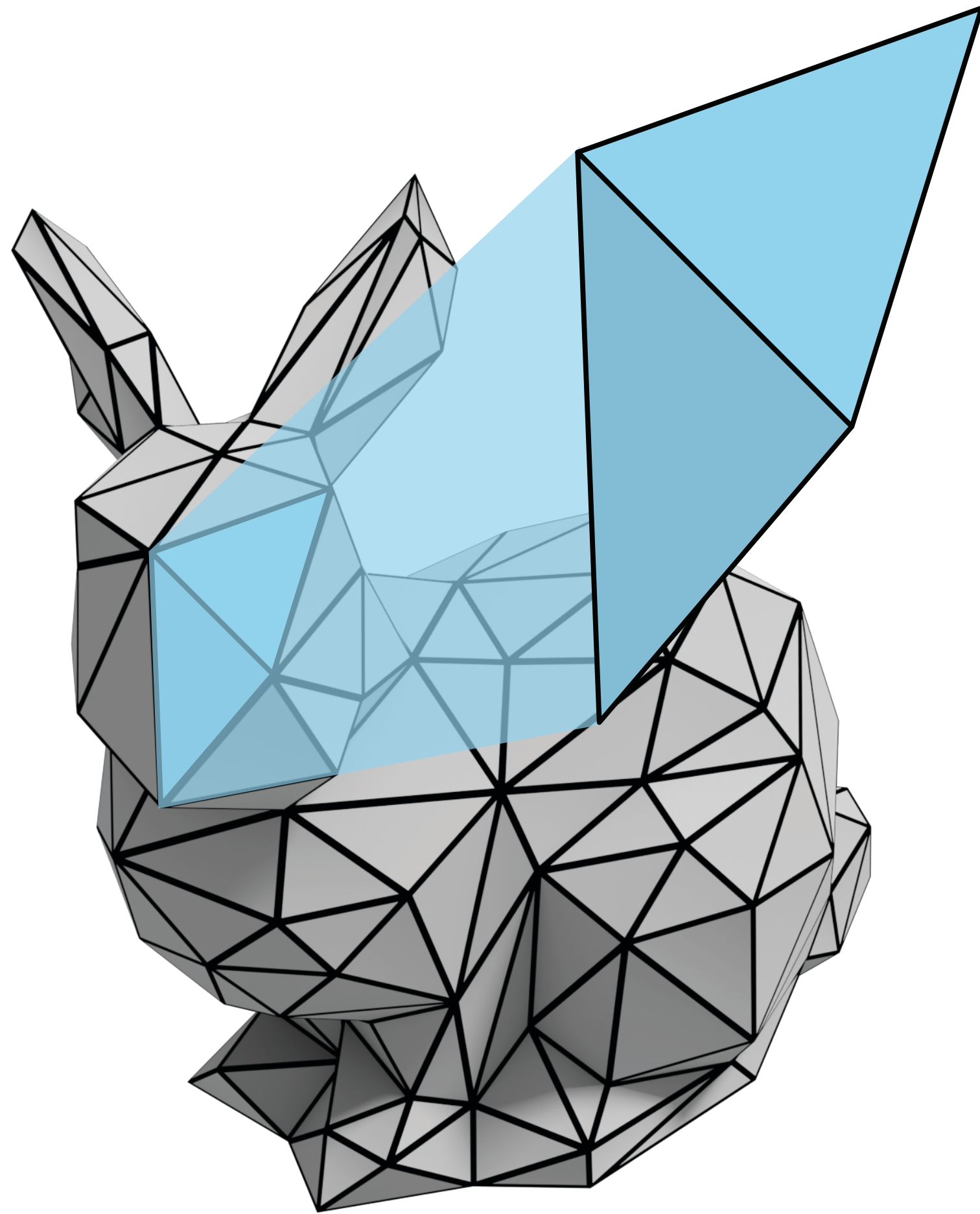
displacement



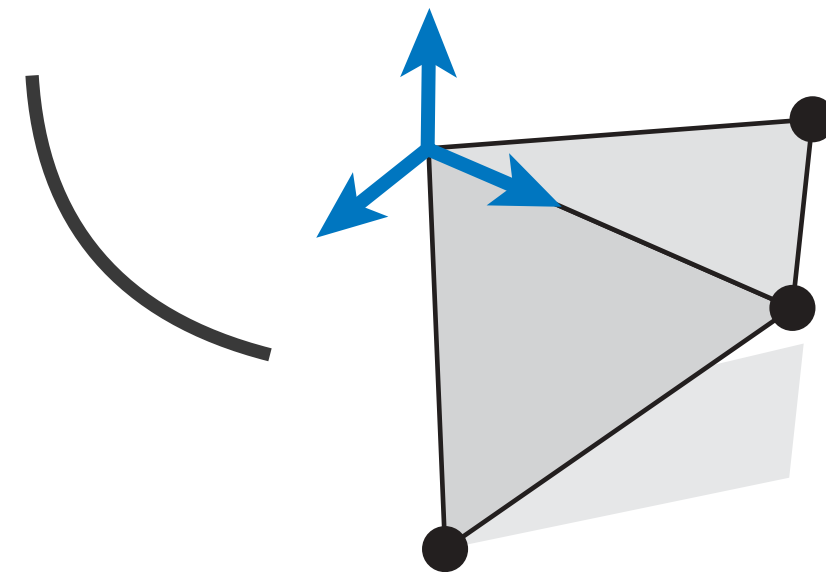
Subdivision Network



Key Takeaways



- ~~assume 1070 vertices~~
- ~~assume a specific connectivity~~
- ~~assume a specific ordering~~
- ~~assume a specific orientation~~



Alleviate limitations

quality

expensive training

generalization

large training data

push the limits

new possibilities

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single shape
training

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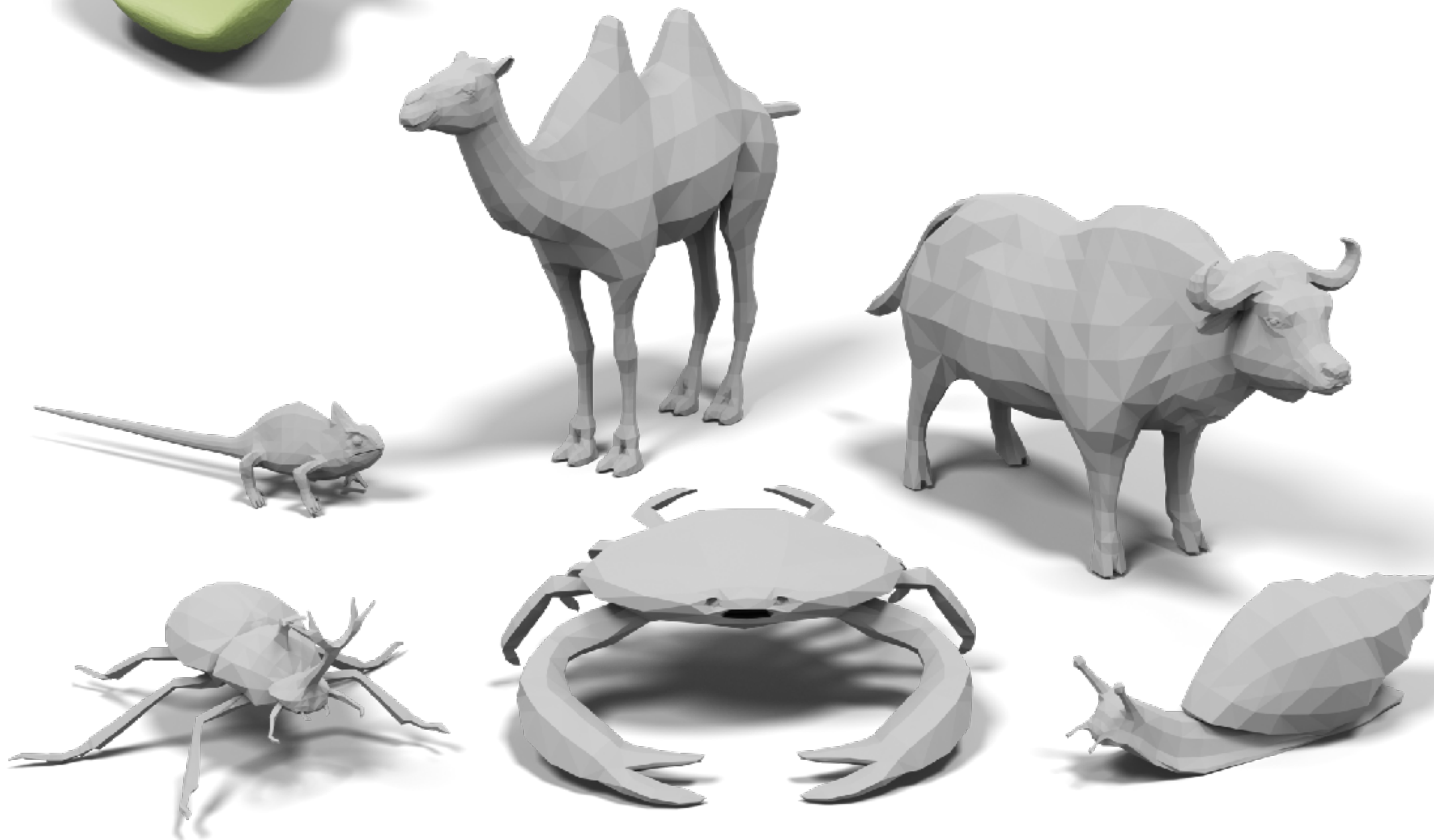
large training data

push the limits

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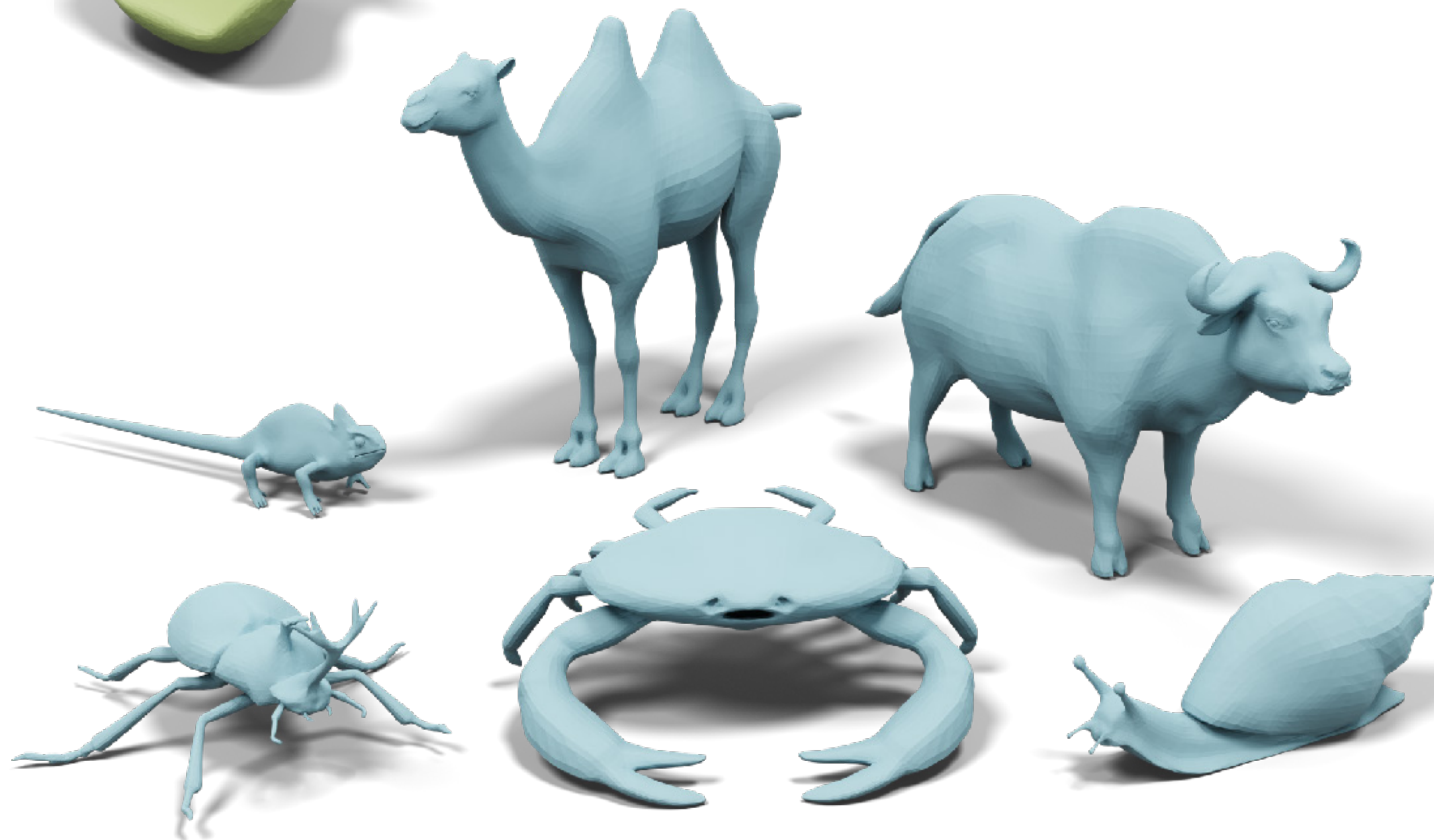
large training data

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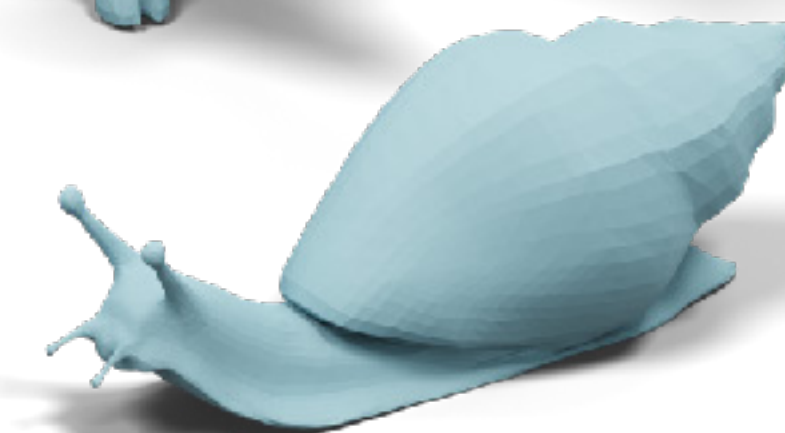
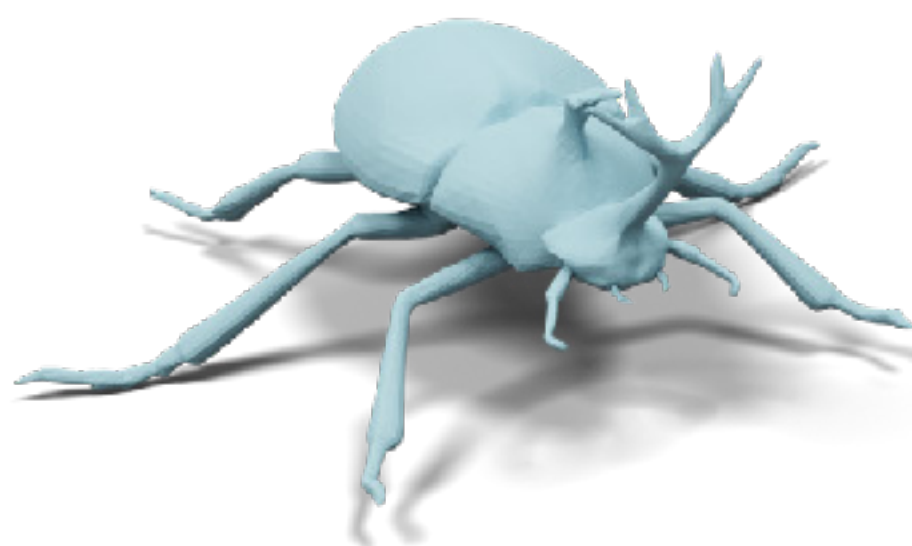
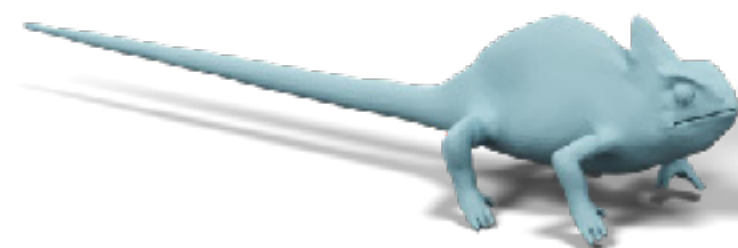
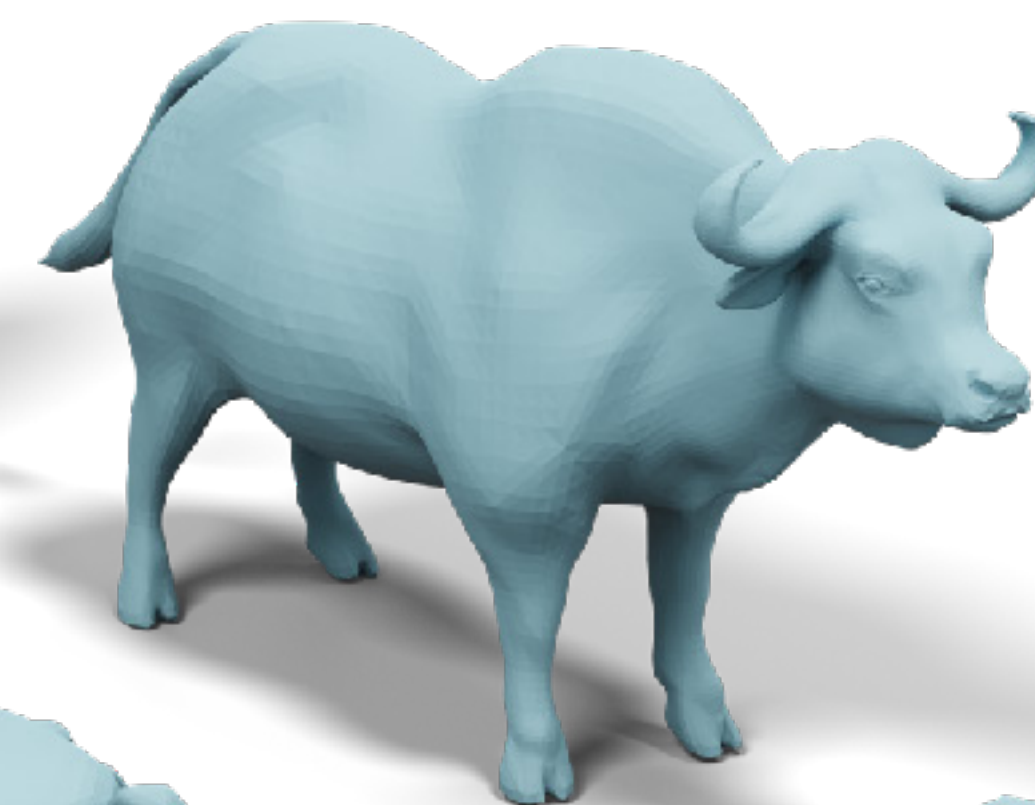
large training data

push the limits

new possibilities

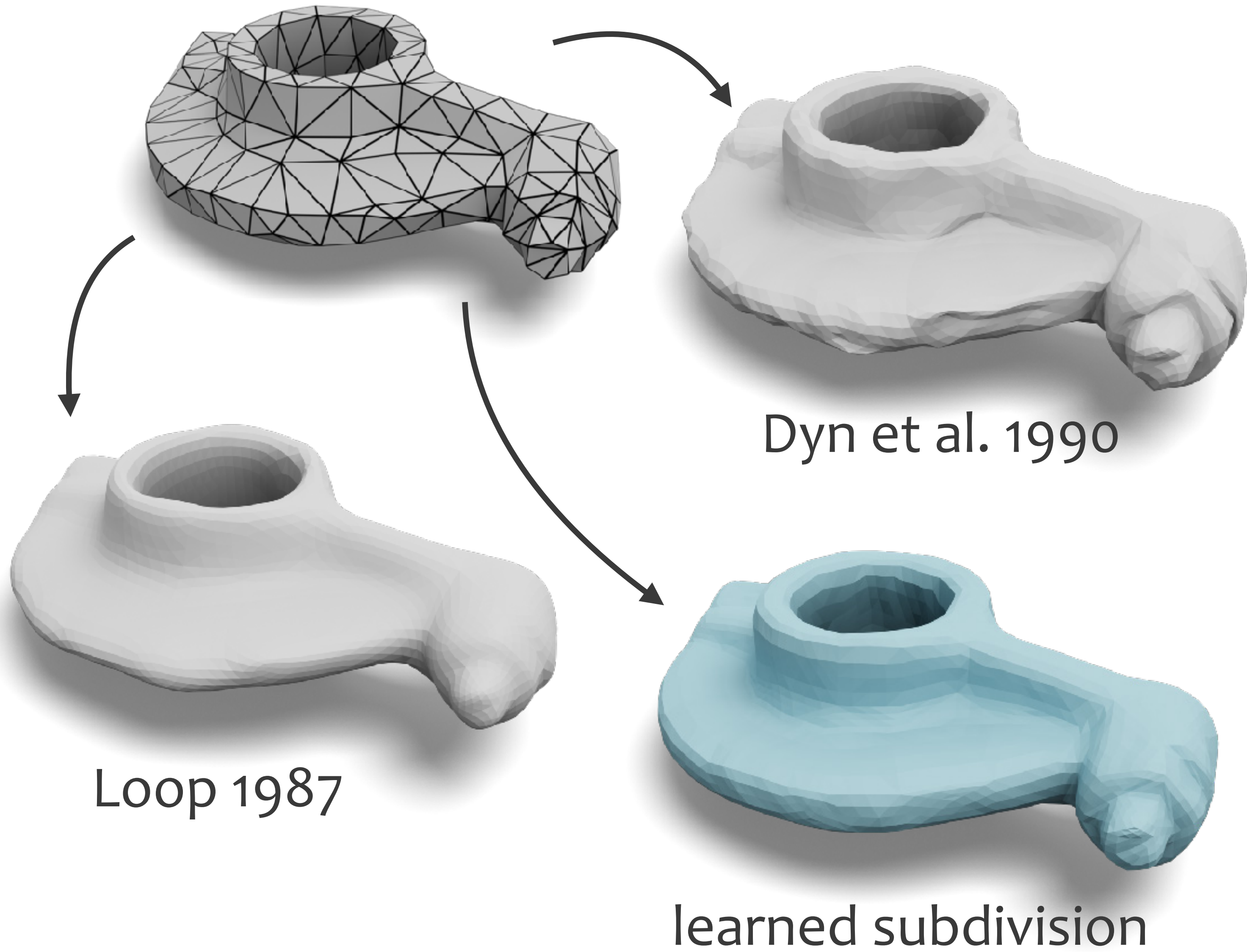


single shape
training



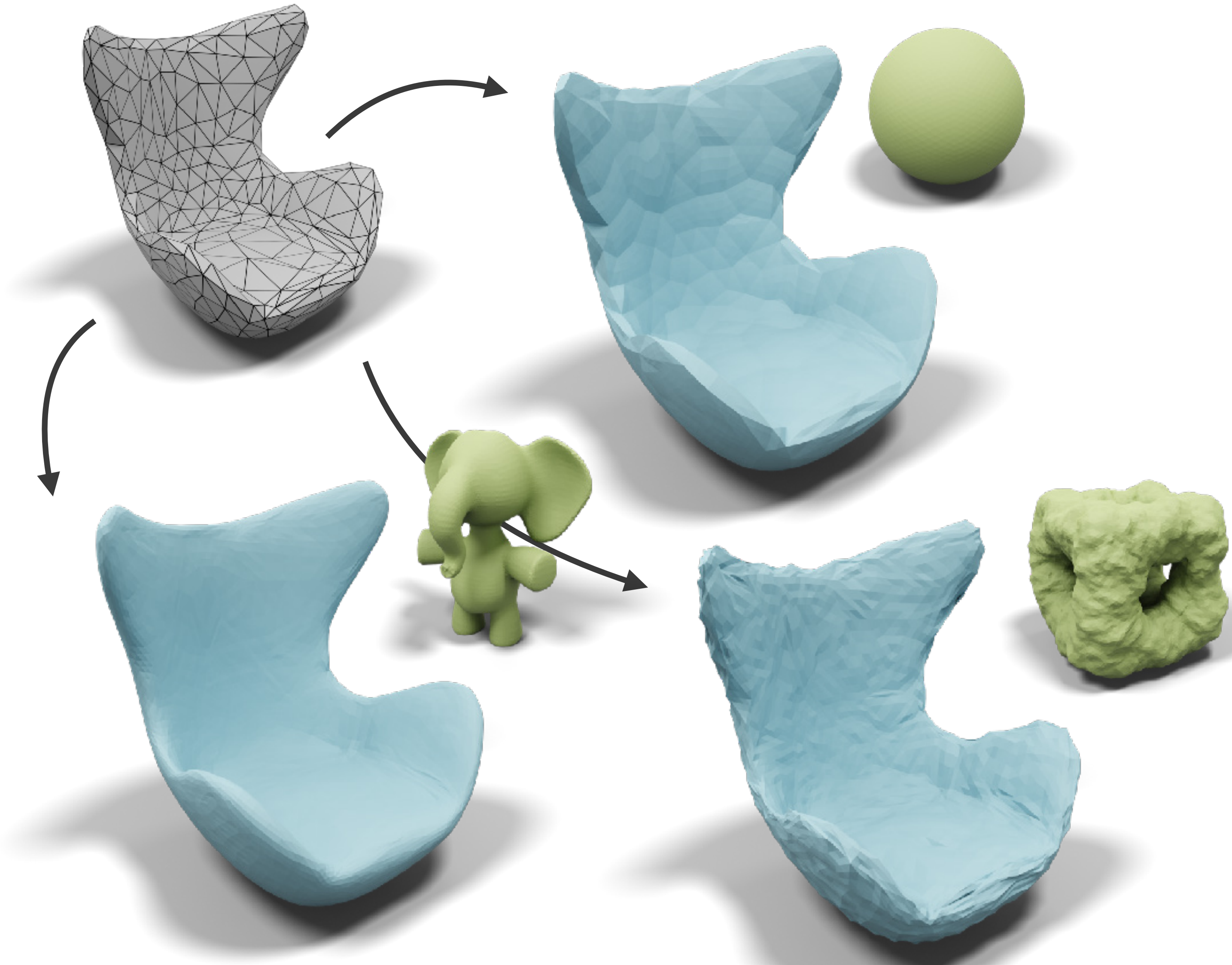
Enjoy Advantages

- quality
- expensive training
- generalization
- large training data
- push the limits
- new possibilities

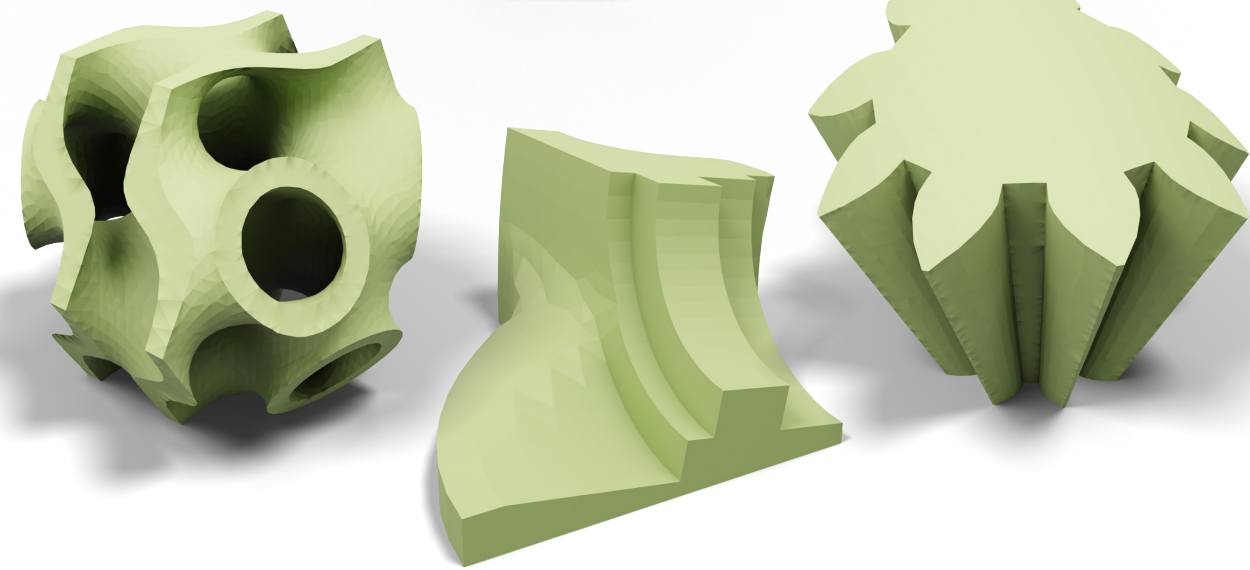


Enjoy Advantages

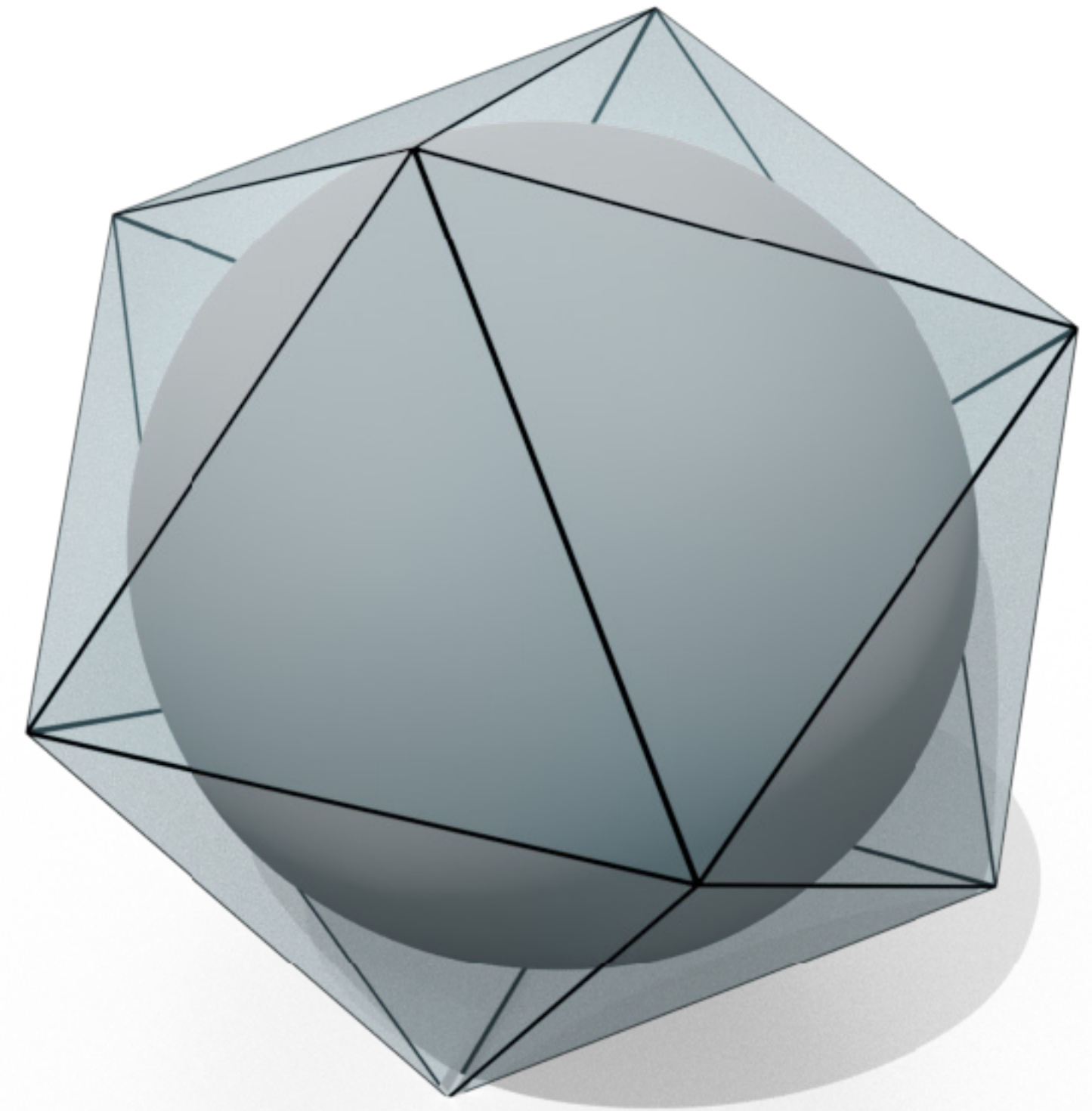
- quality
- expensive training
- generalization
- large training data
- push the limits
- new possibilities



Ongoing Research

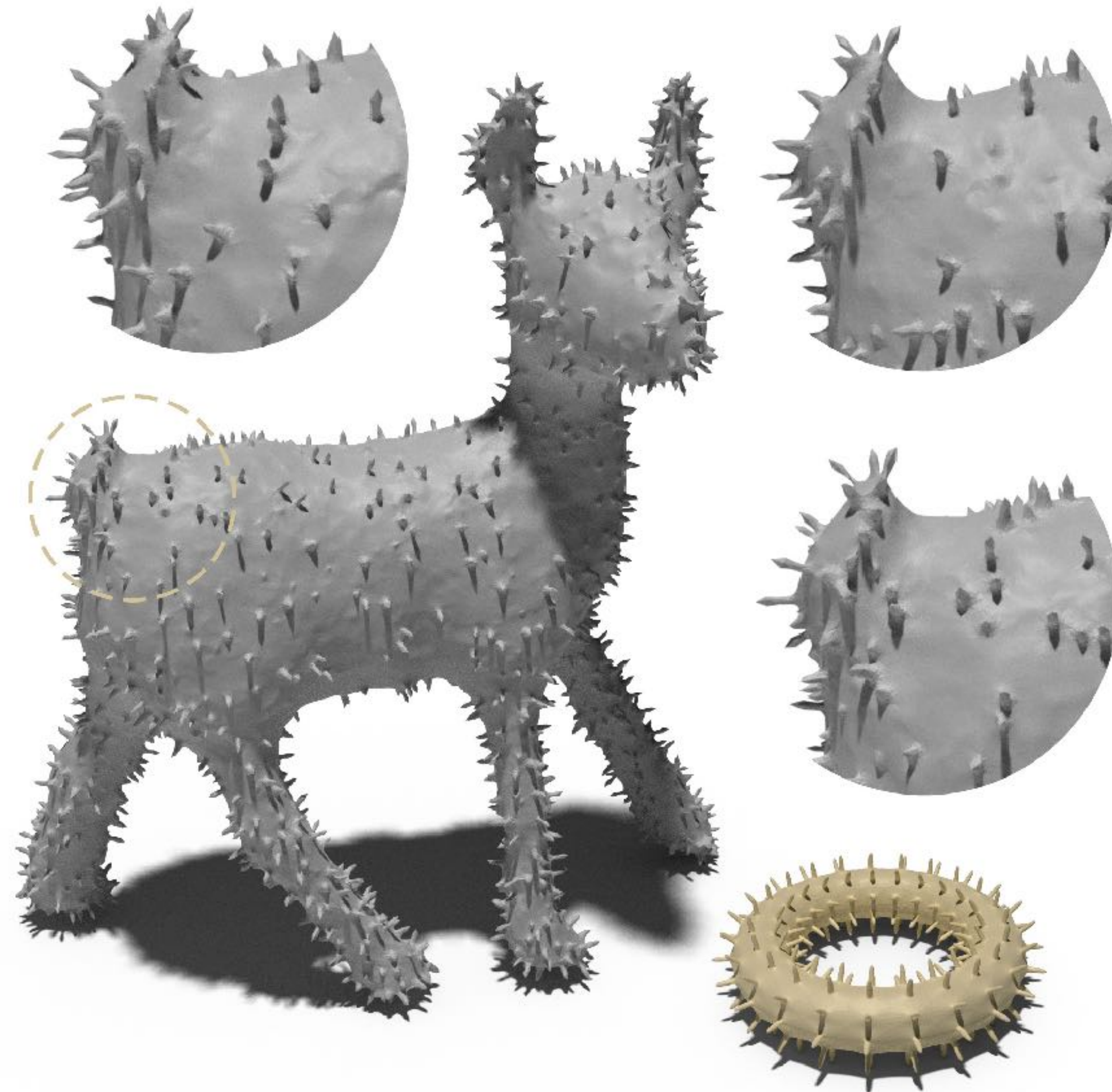


black-box

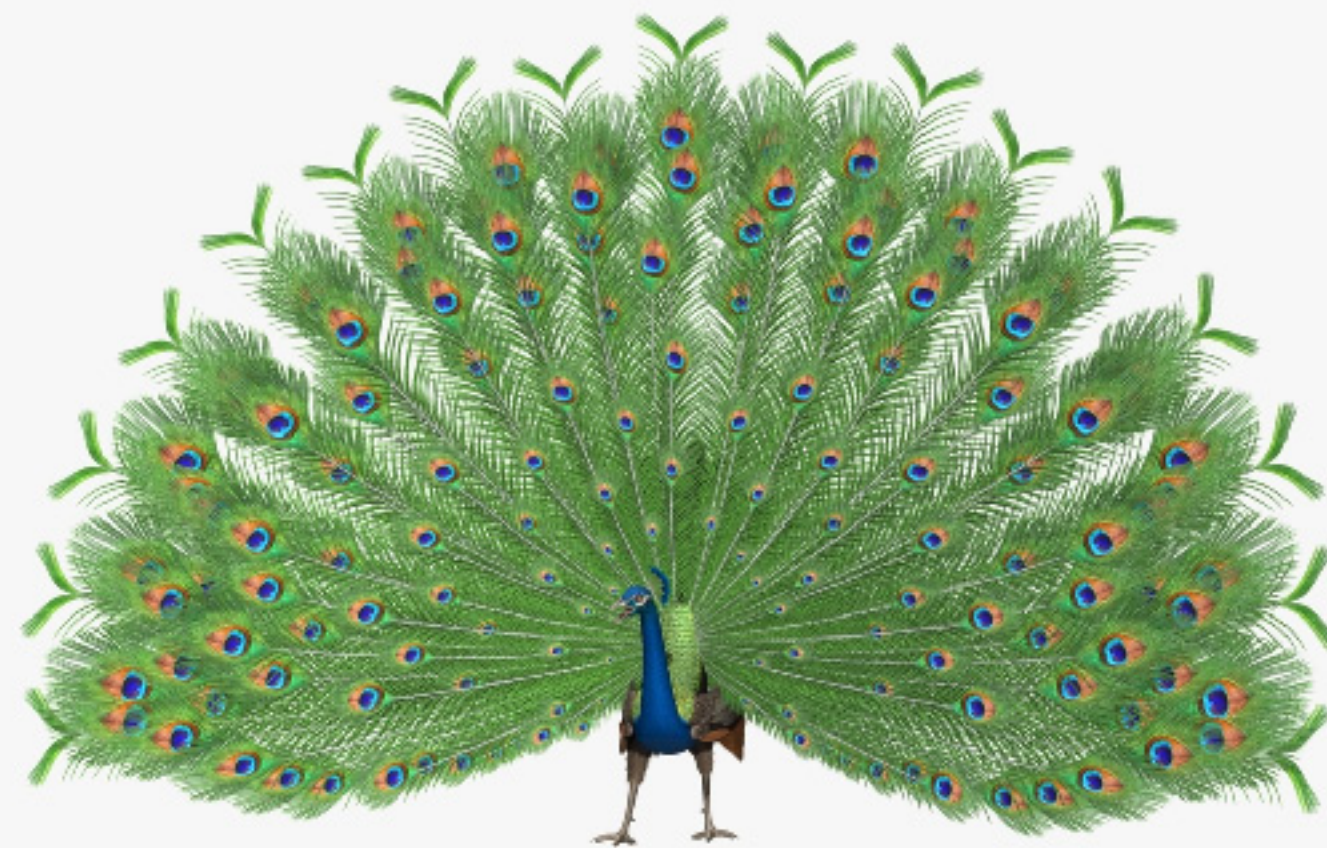
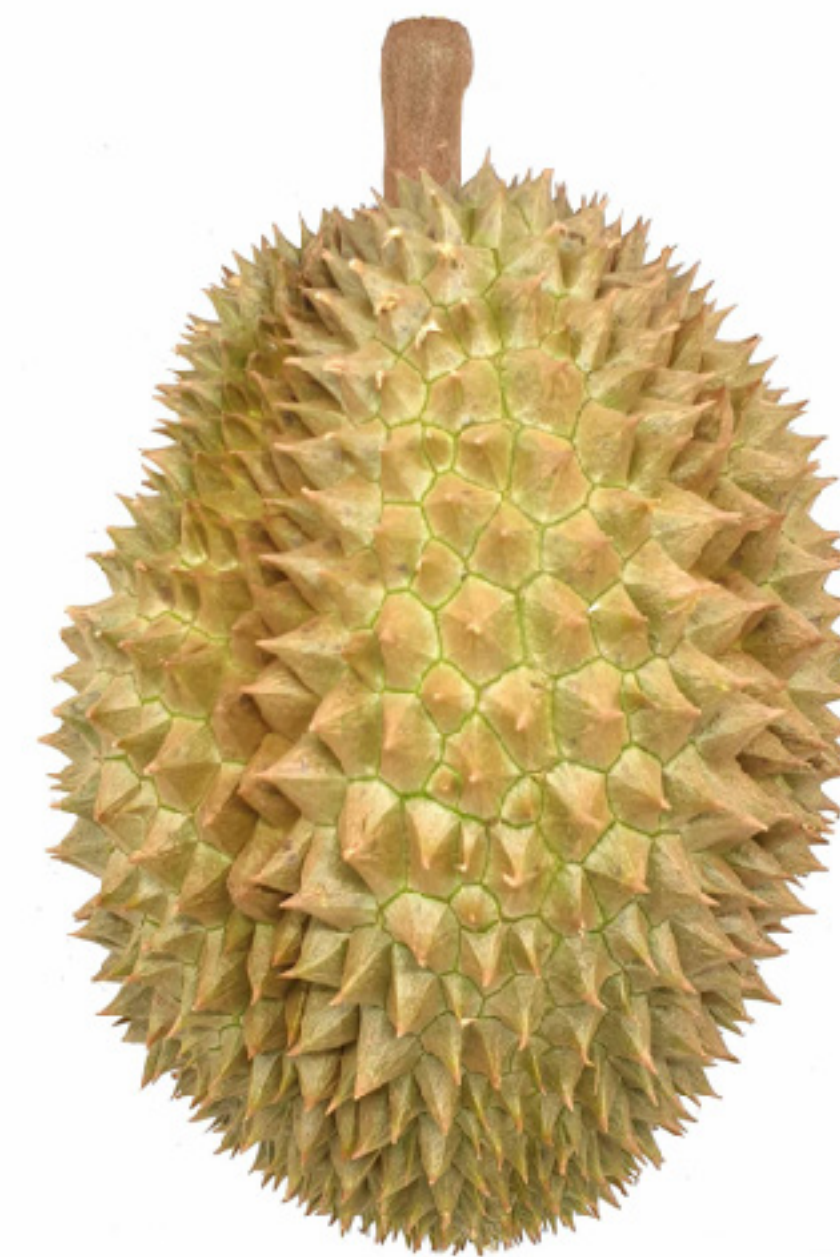


convergence

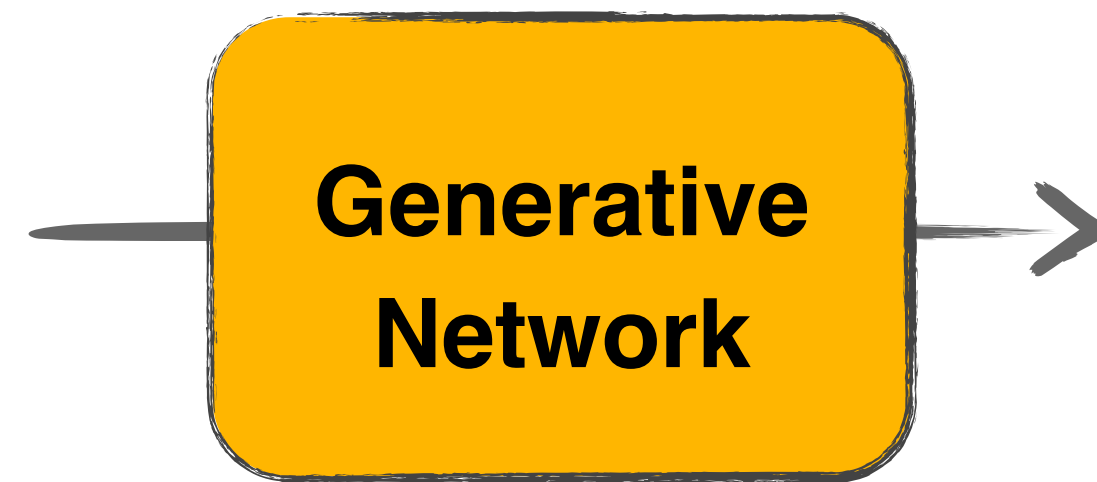
Deep Geometric Texture Synthesis



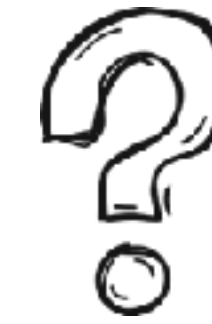
Geometric Textures



Objective: Generative Texture Model



External Dataset



Difficult to obtain collections with same geometric textures

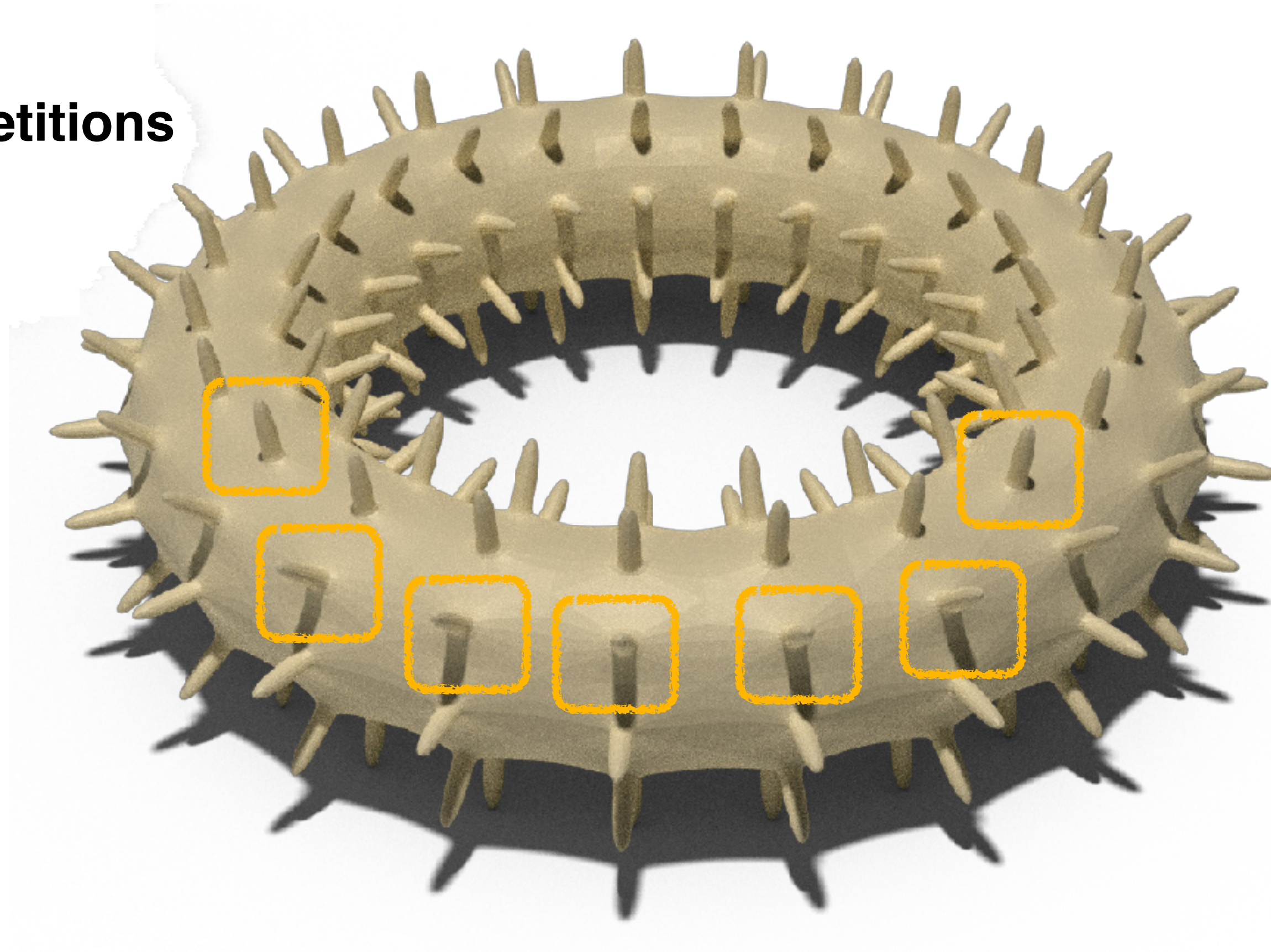
Inconsistencies make learning difficult



Learn from a Single Shape

Patches are training data

Textures contain self-repetitions

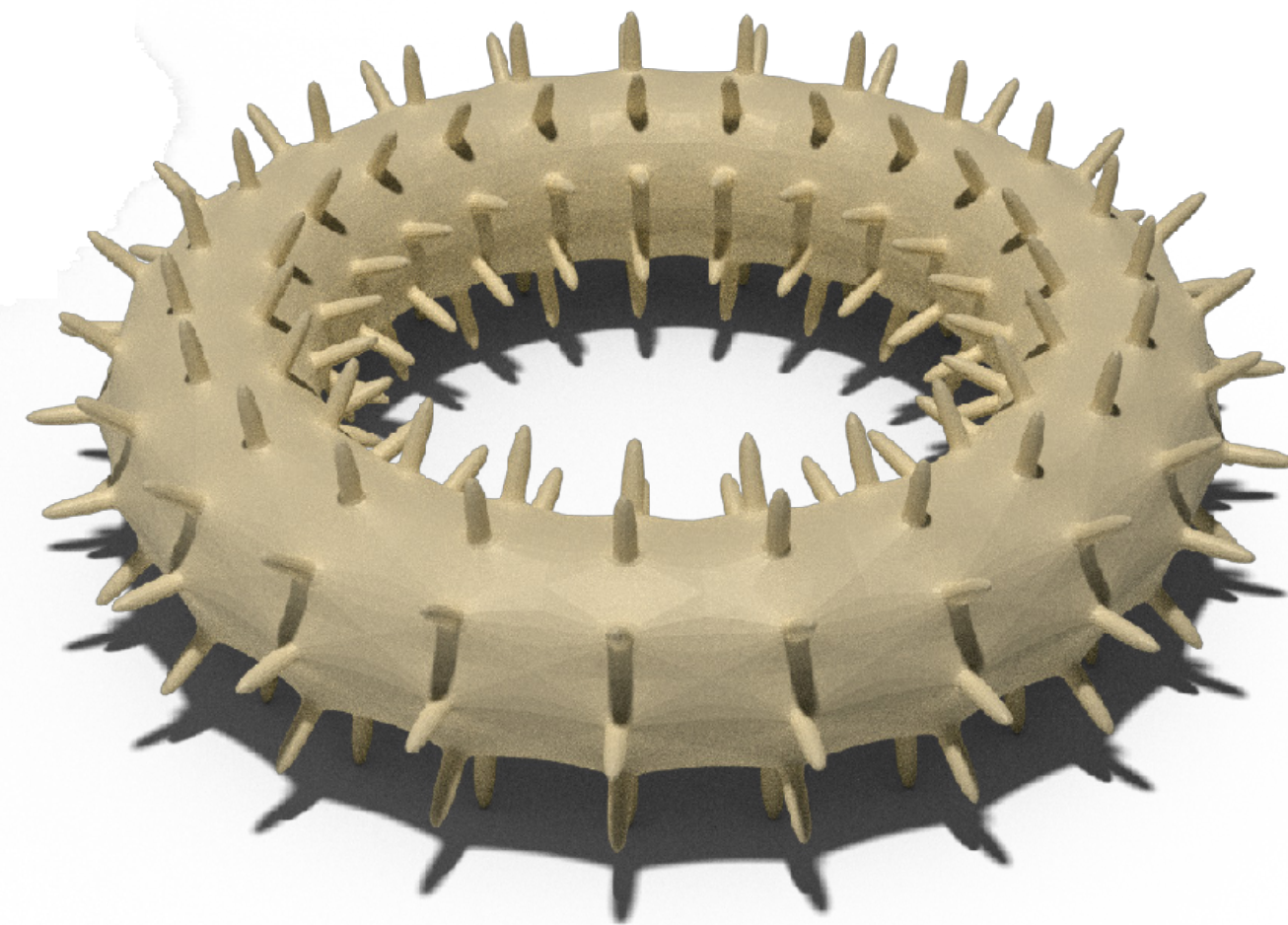


Learn from a Single Shape

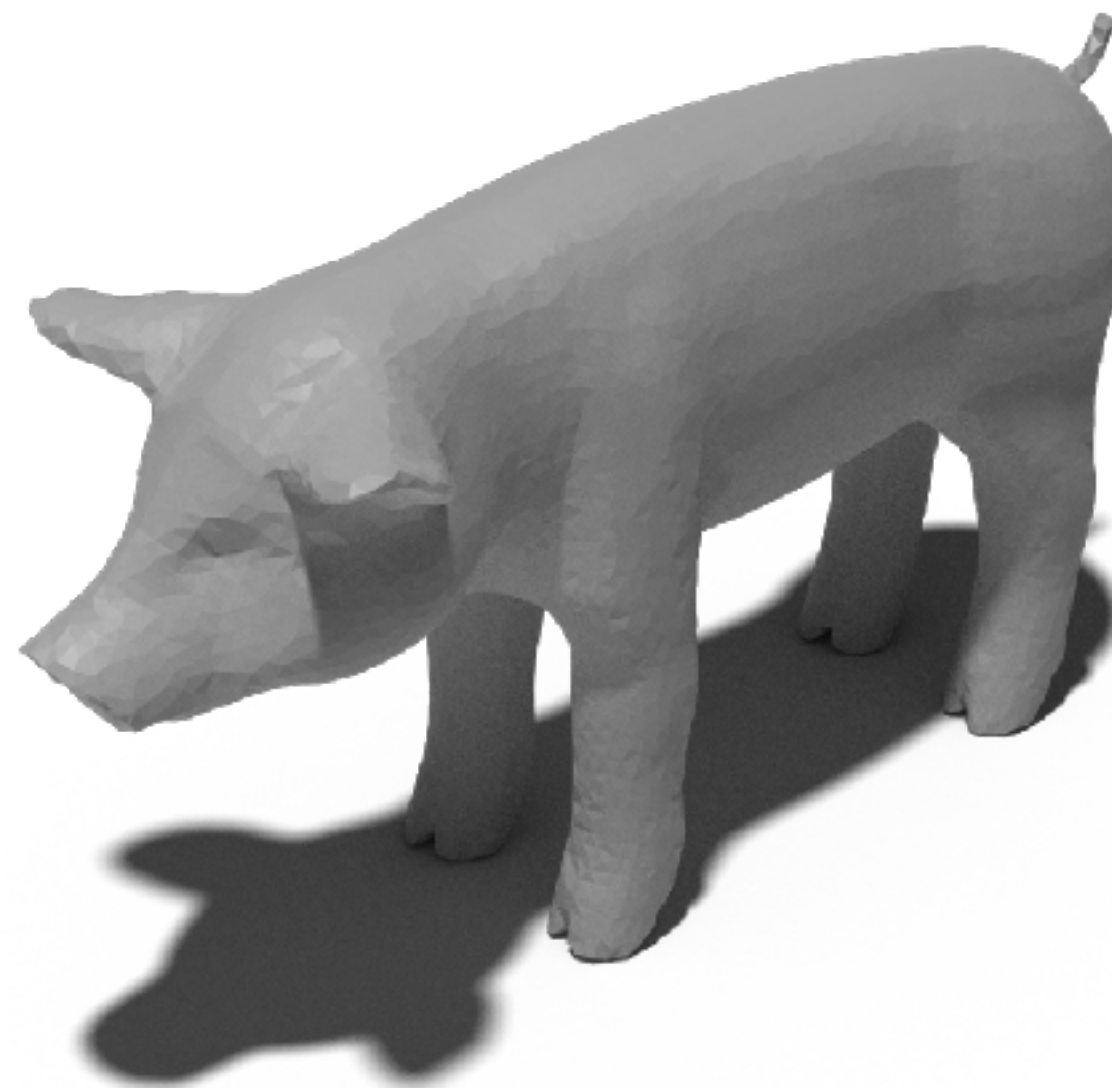
Patches are training data

Textures contain self-repetitions

Local patches are similar for different shapes!



Exemplar

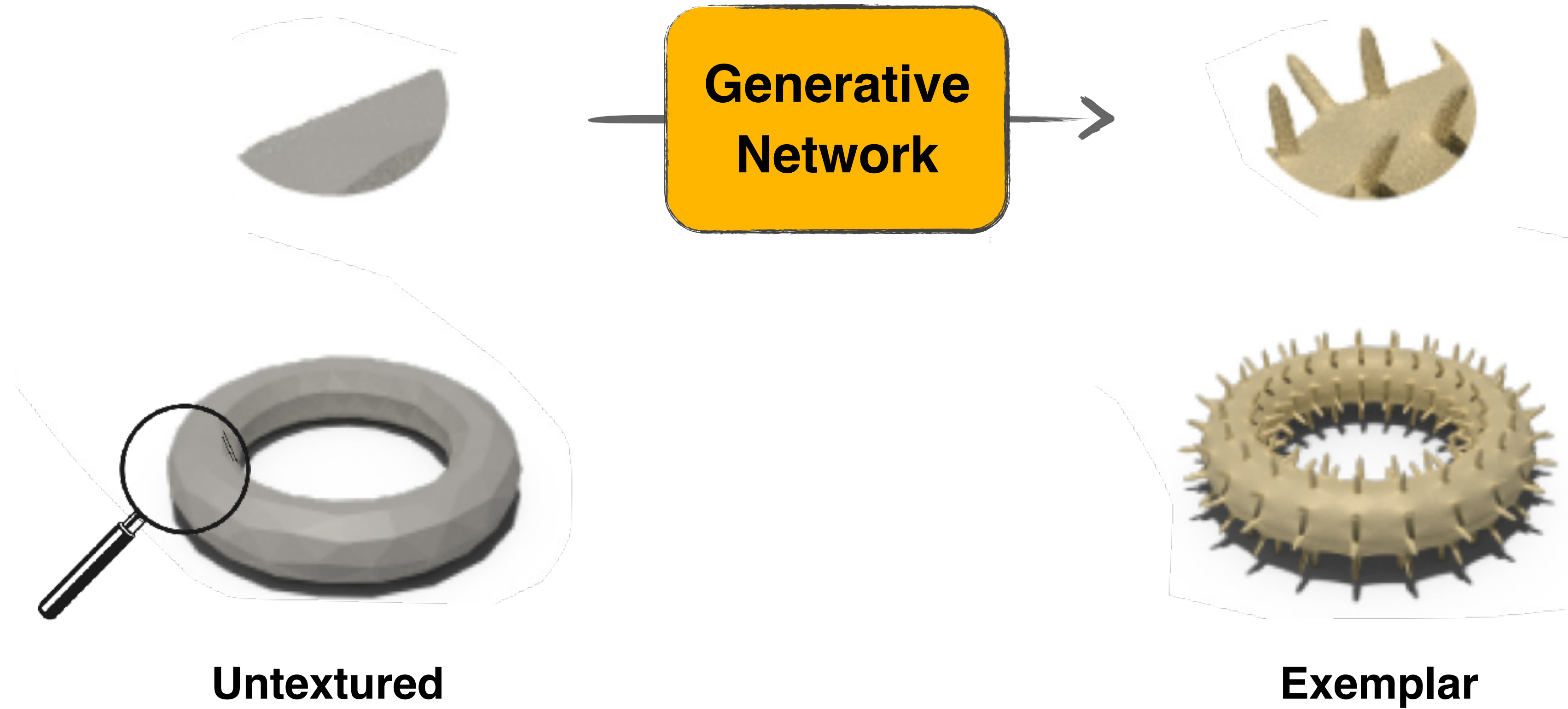


New Object

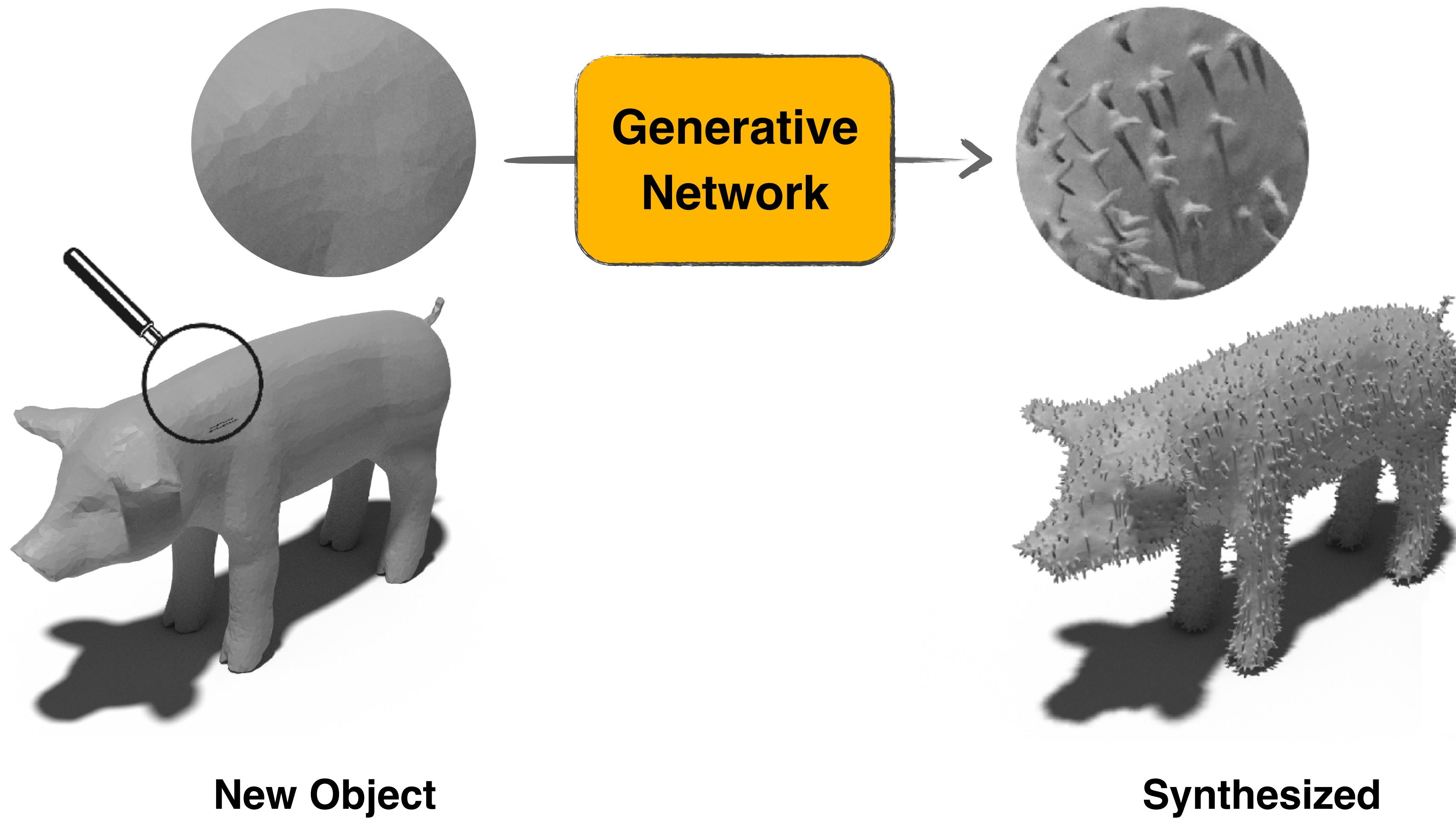


**Synthesized
Textures**

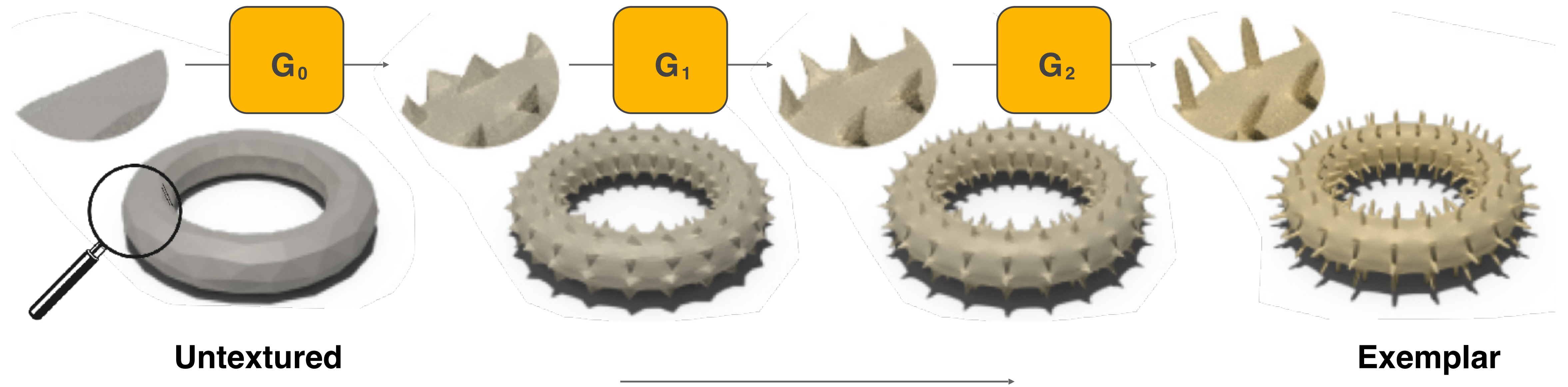
Train on local patches



Generalization from local patches

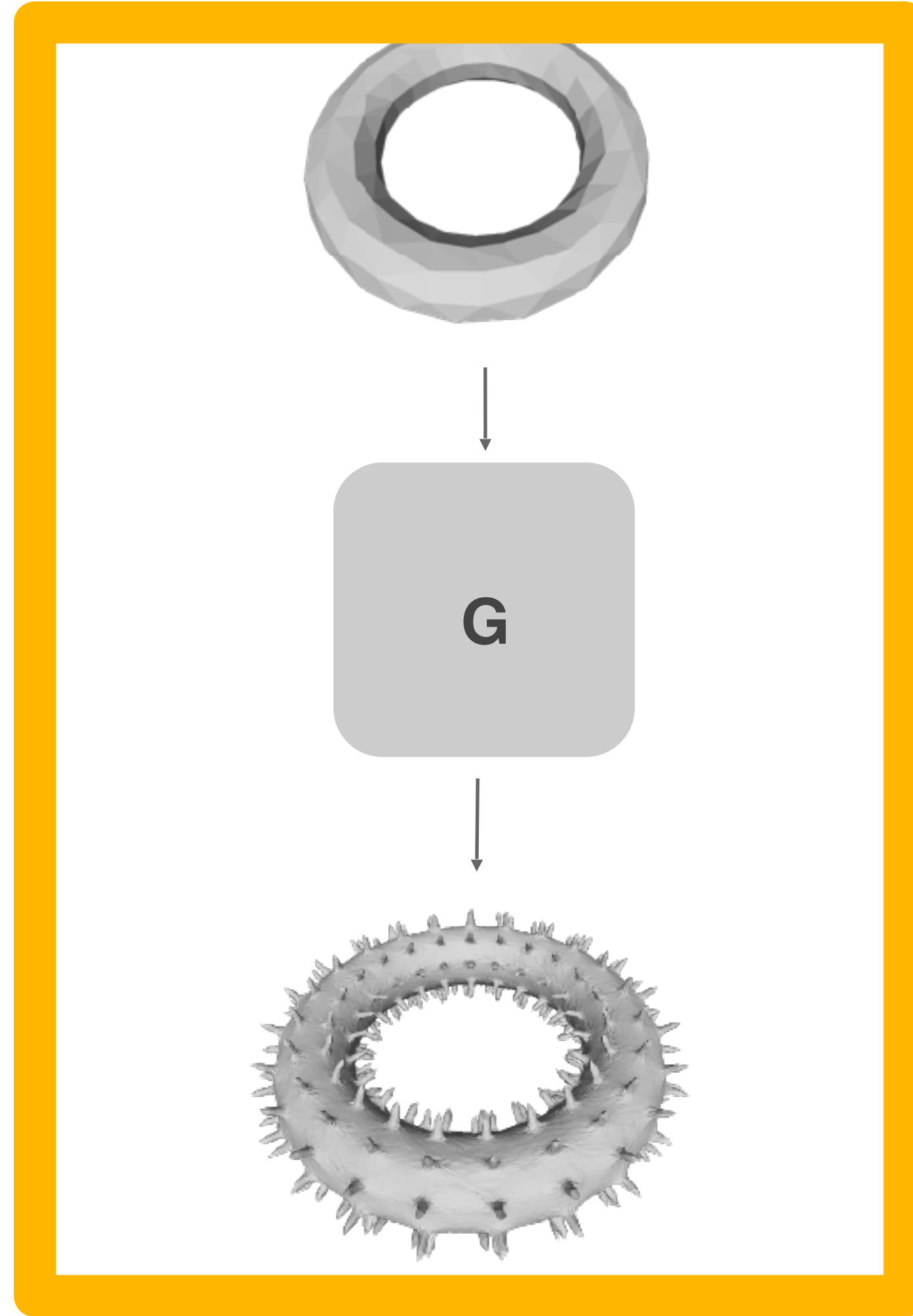


Progressive Texture Synthesis





Multi-Scale Training Inputs

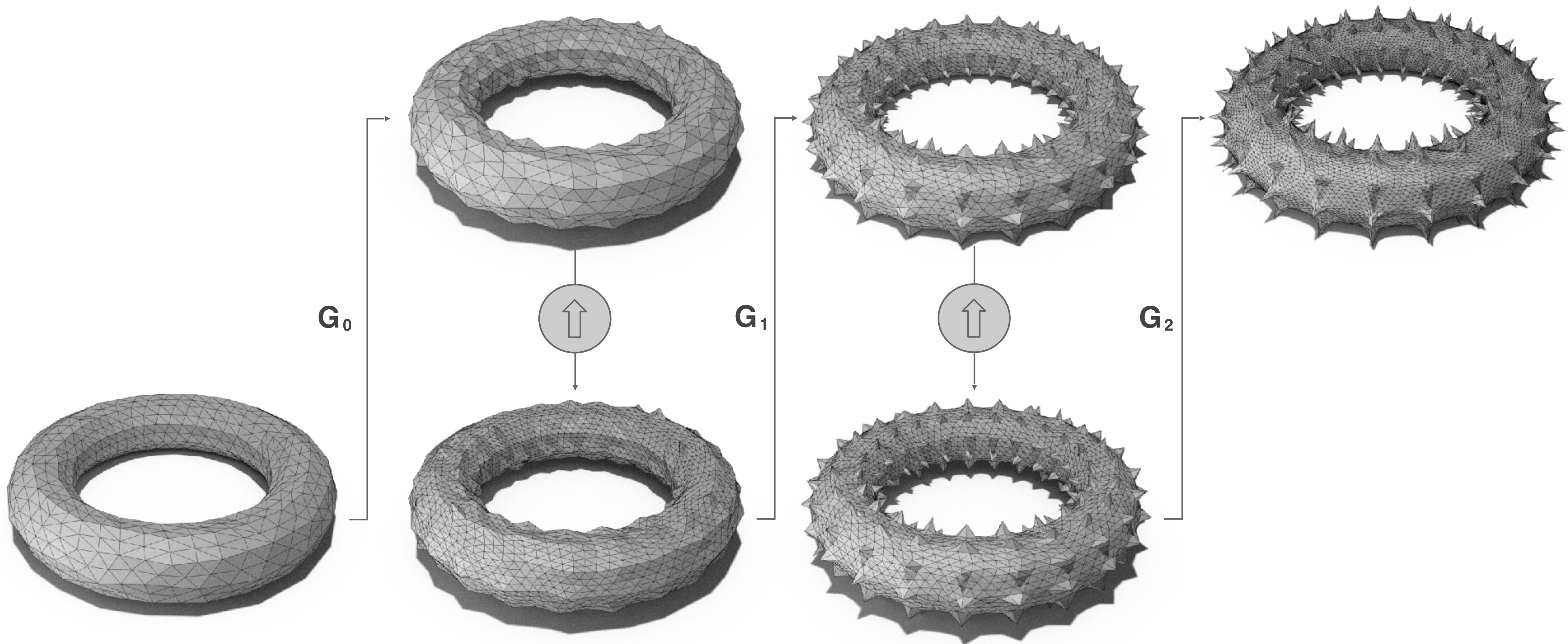


Progressive Training

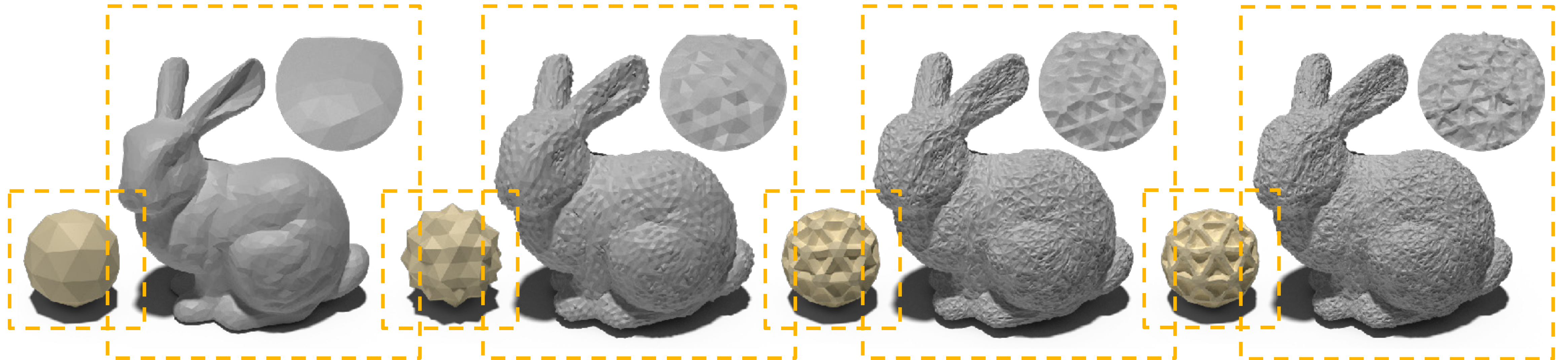


Inference

Progressive Texture Synthesis

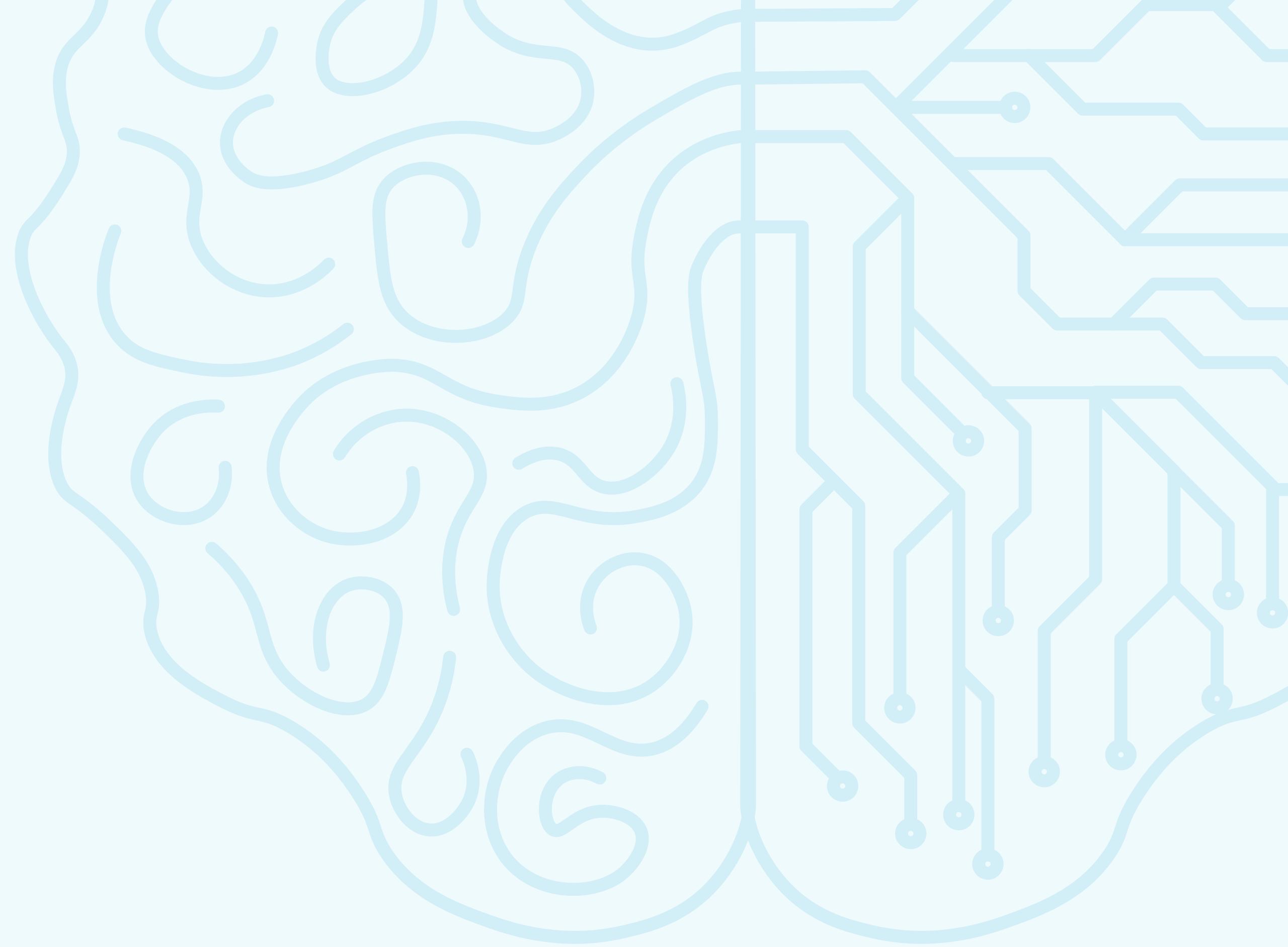


Multi-Scale Textures



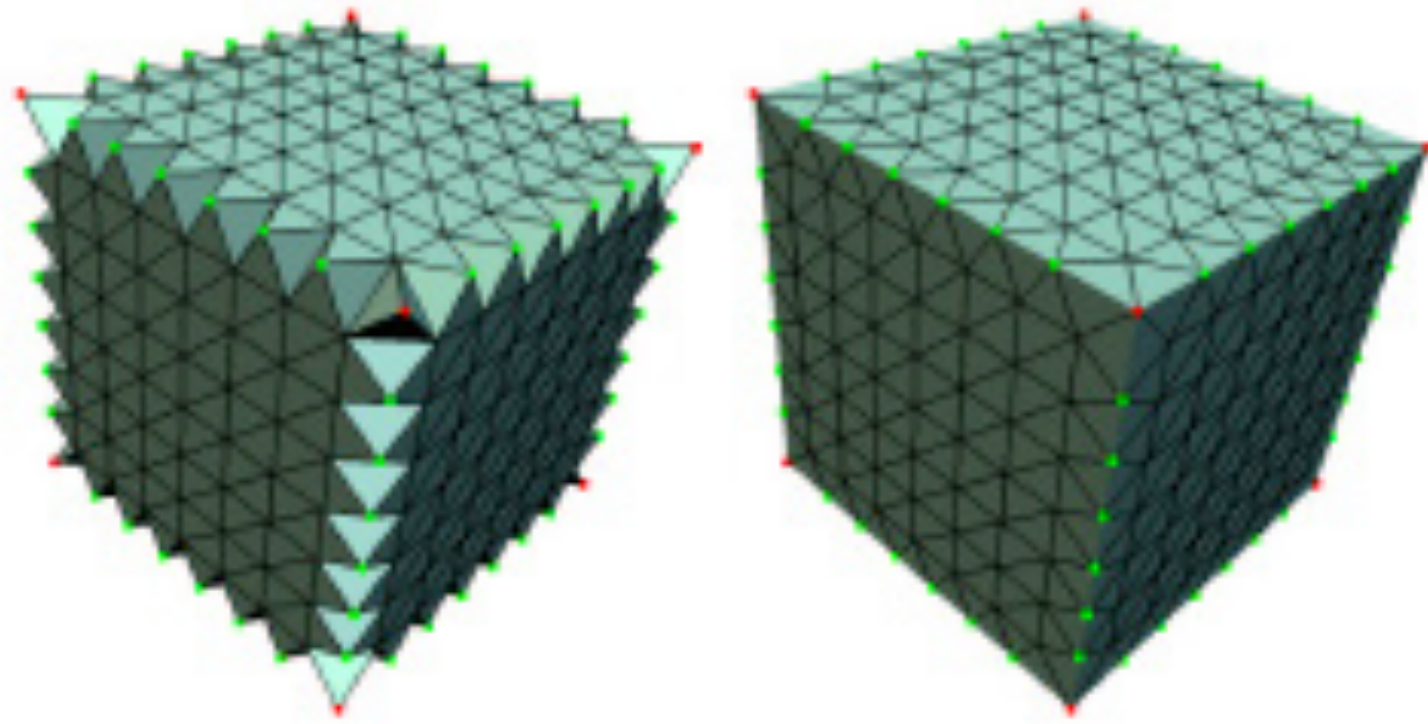
Texture Interpolation



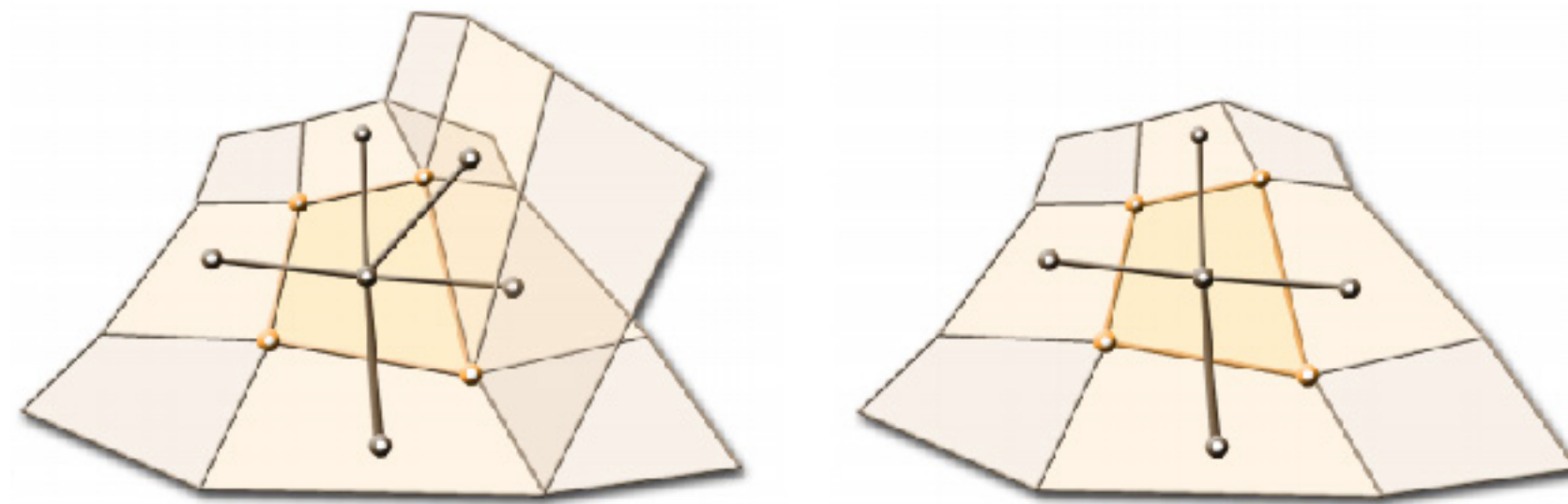


SUMMARY

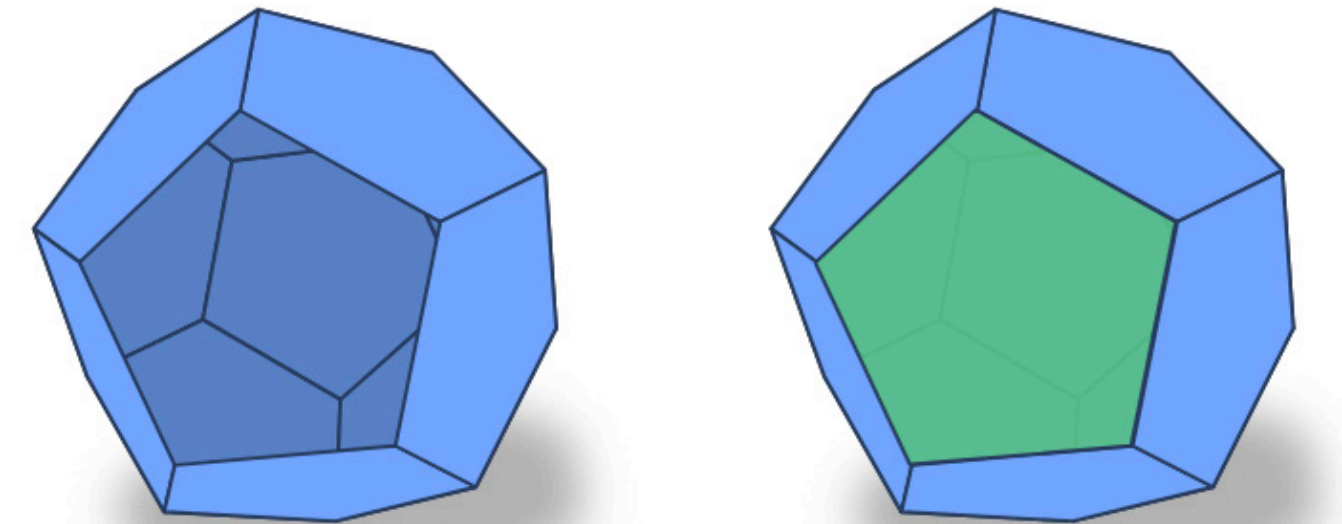
Connectivity based Mesh Learning



sharp features



fix non-manifold

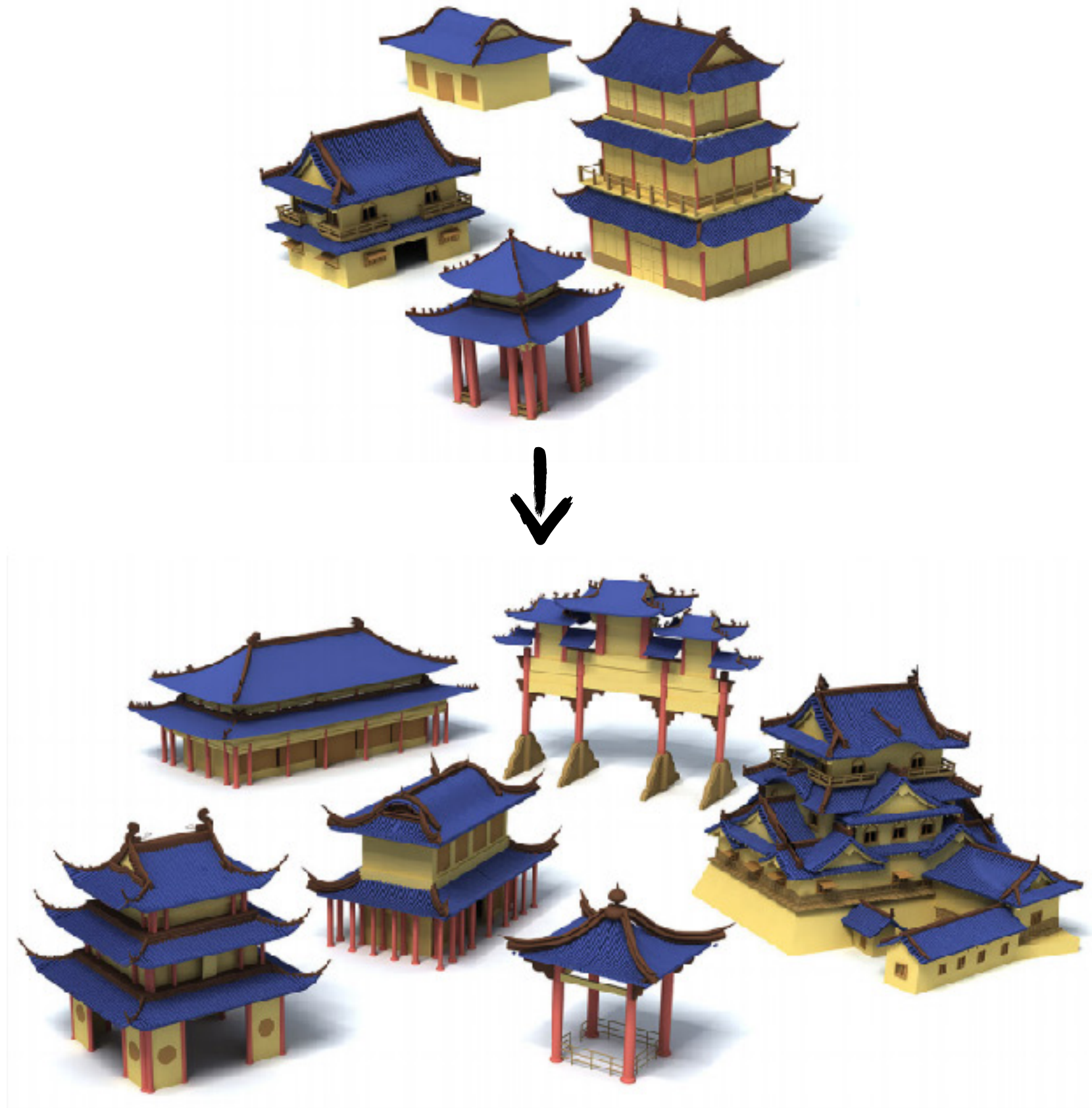
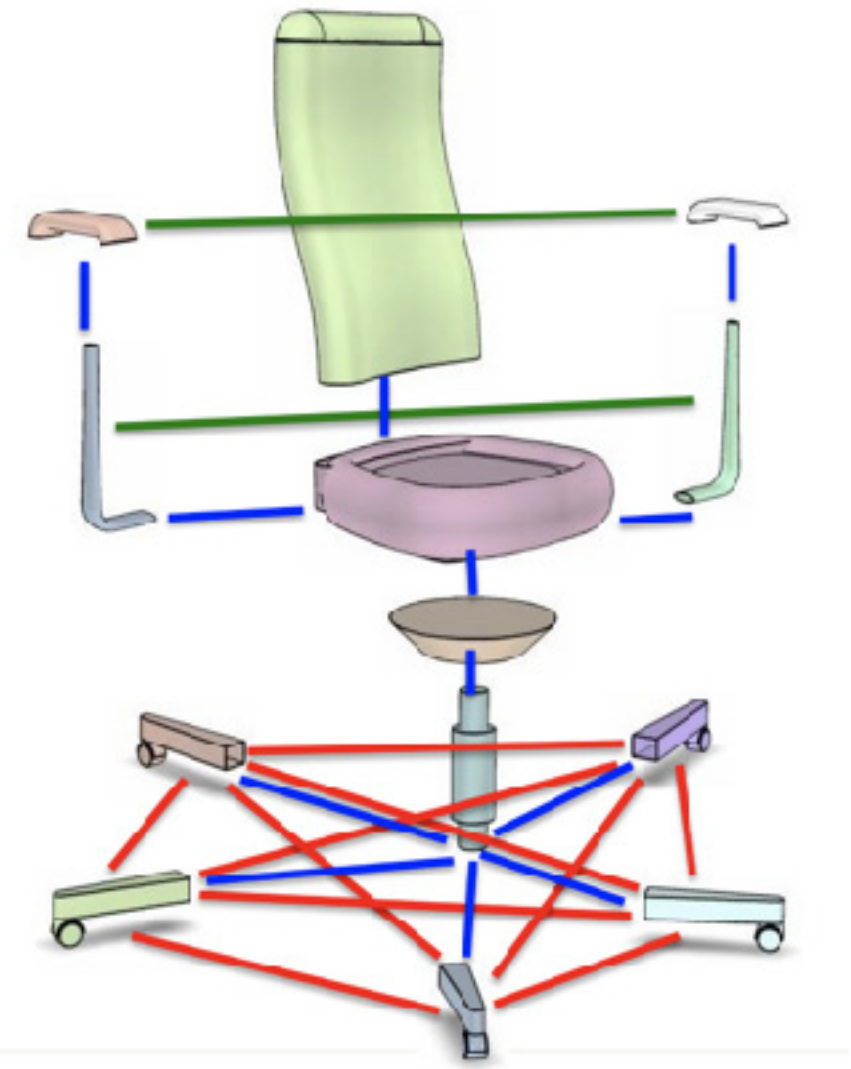


hole filling

Mesh Generative Models



structural learning



structural shape synthesis



mesh boolean

Shape Perception



input

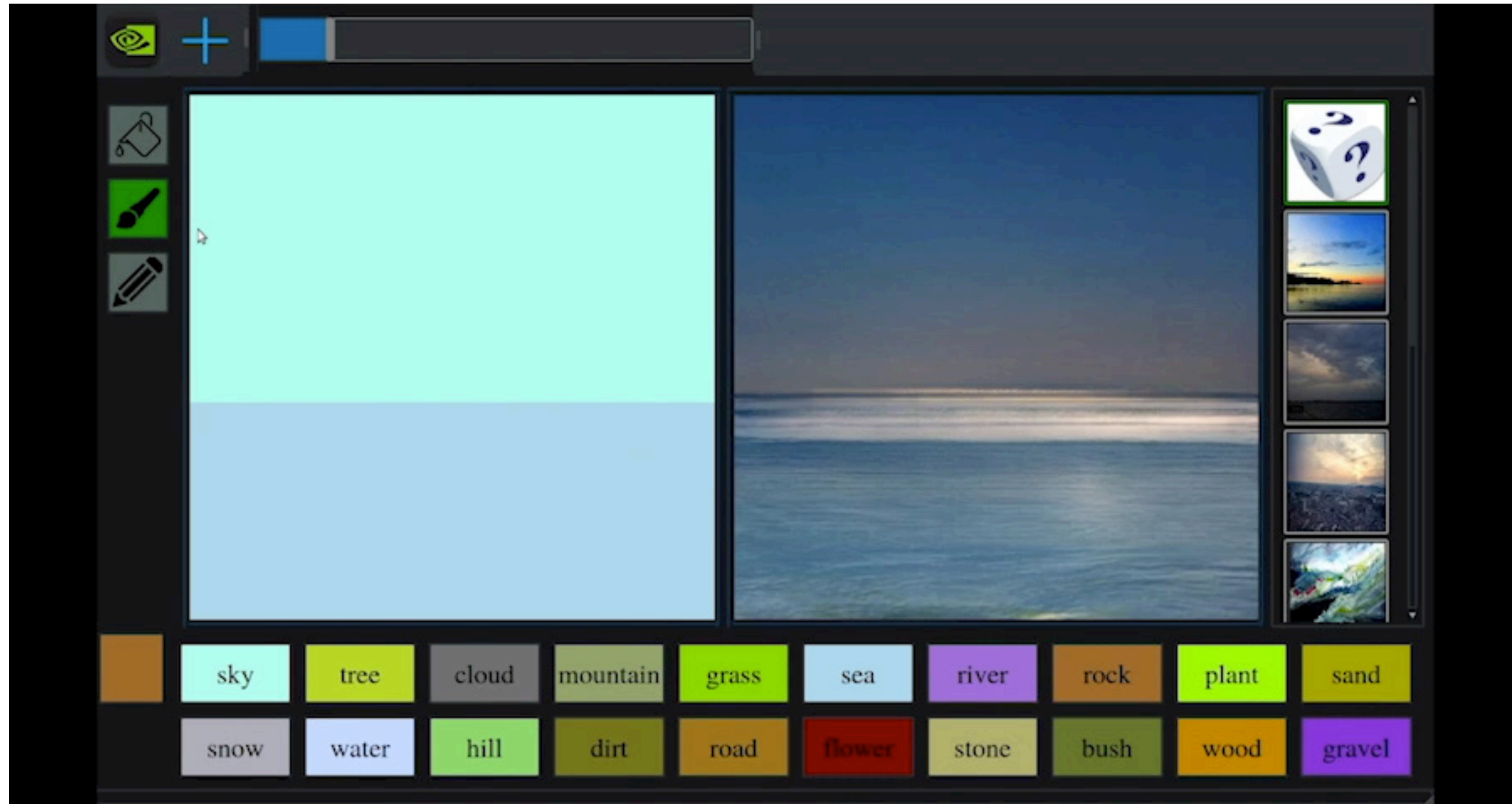


style



output

Futuristic 3D Modeling Tools



Draw Inspiration from Classic Methods

